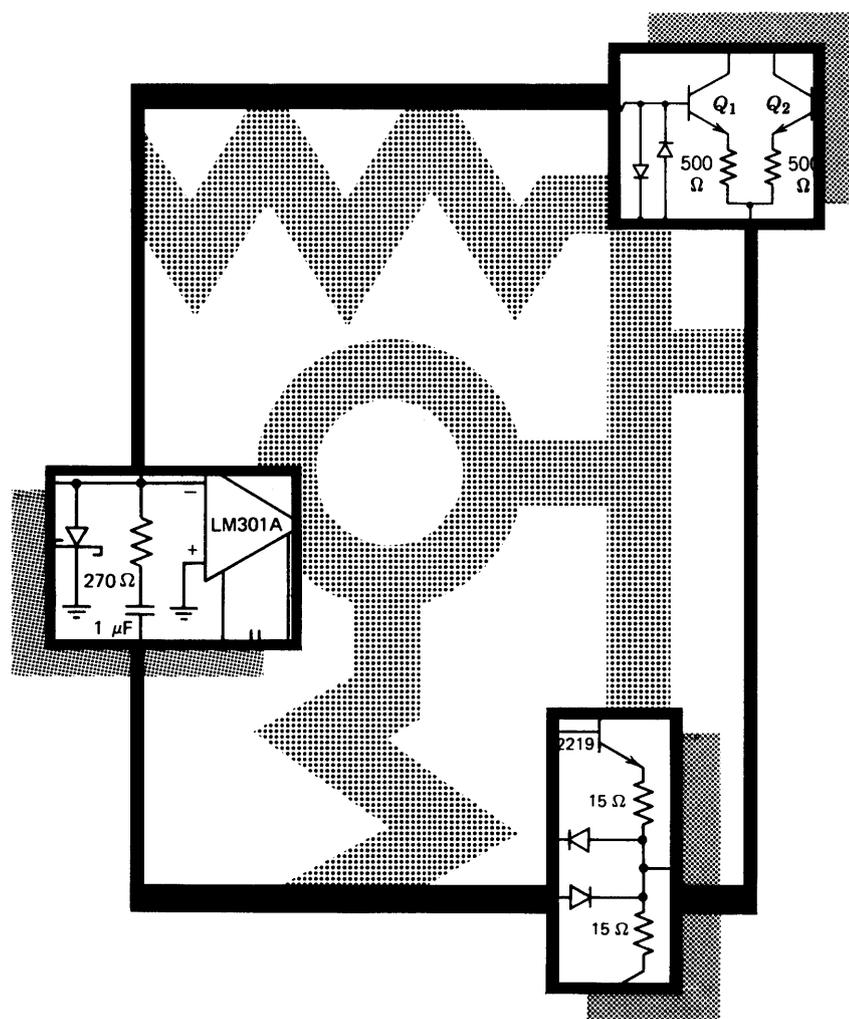


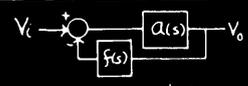
# Introduction to Systems with Dynamics

# 3



**Blackboard 3.1**

Dynamics - a First Look



Corner where  $\frac{a_0 f_0}{\tau_a \omega} = 1$

-LT =  $\frac{a_0 f_0}{\tau_a s + 1}$

$A(s) = \frac{a_0}{(\tau_a s + 1)(\tau_f s + 1)}$ ,  $f = f_0$

$A(s) \cong \frac{1}{f_0} \frac{1}{\frac{\tau_a \tau_f s^2}{a_0 f_0} + \frac{(\tau_a + \tau_f)}{a_0 f_0} s + 1}$

$A(s) = \frac{a_0}{\tau_a s + 1} \cdot \frac{1}{1 + \frac{a_0 f_0}{\tau_a s + 1}}$

$a = \frac{a_0}{\tau_a s + 1}$ ,  $f = f_0$ :

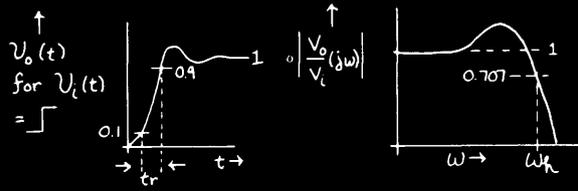
$A(s) = \frac{a_0}{\tau_a s + 1} \cdot \frac{1}{1 + \frac{a_0 f_0}{\tau_a s + 1}} = \frac{1}{f_0} \frac{1}{\frac{\tau_a s}{a_0 f_0} + \frac{\tau_a + \tau_f}{a_0 f_0} + 1}$

$\frac{1}{f_0} \frac{1}{\tau_a s + 1}$

$|A(j\omega)| = \frac{1}{f_0} \frac{1}{\sqrt{(1 - \frac{\omega^2}{\omega_n^2})^2 + \frac{4\zeta^2 \omega^2}{\omega_n^2}}}$

3-1

**Blackboard 3.2**

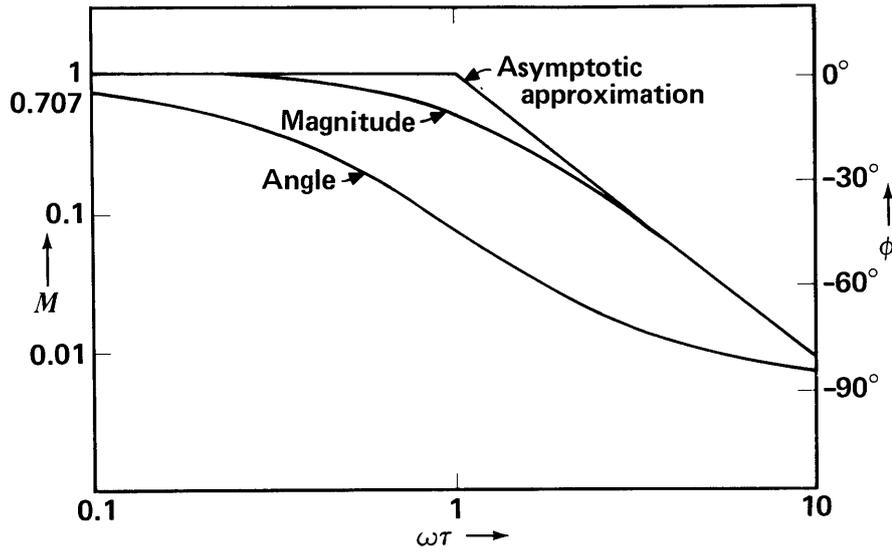


$t_r \omega_k = 2.2$

$t_r f_k = 0.35$

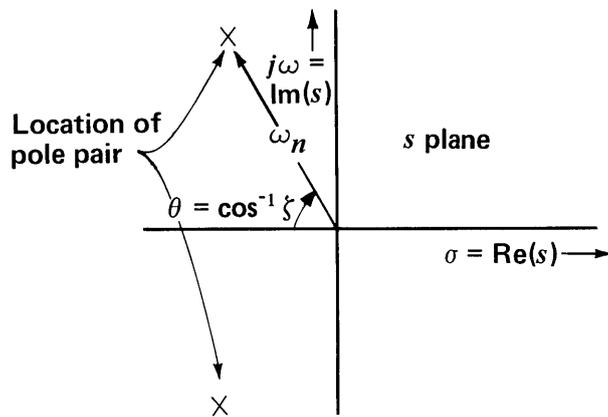
3-2

**Viewgraph 3.1**



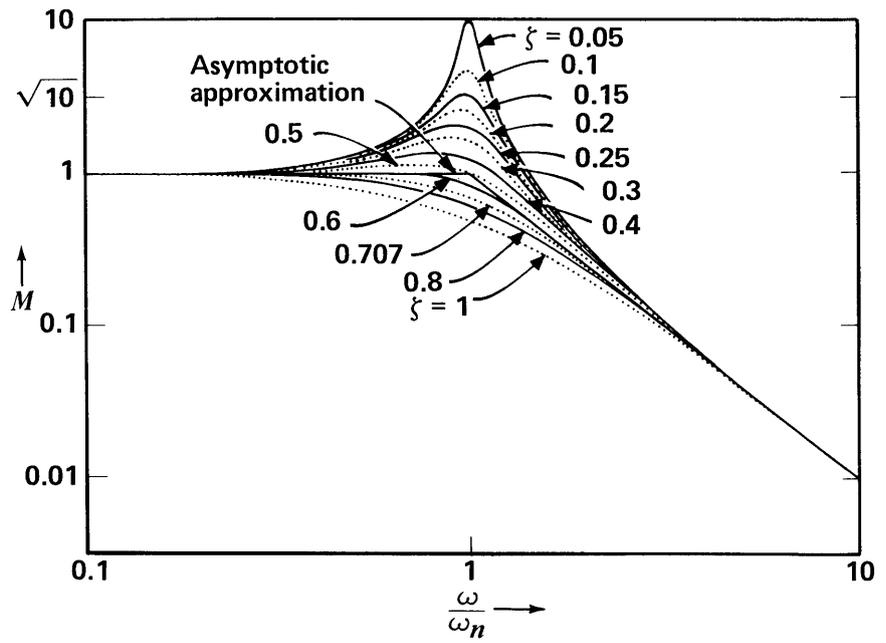
**Frequency response of first-order system.**

**Viewgraph 3.2**



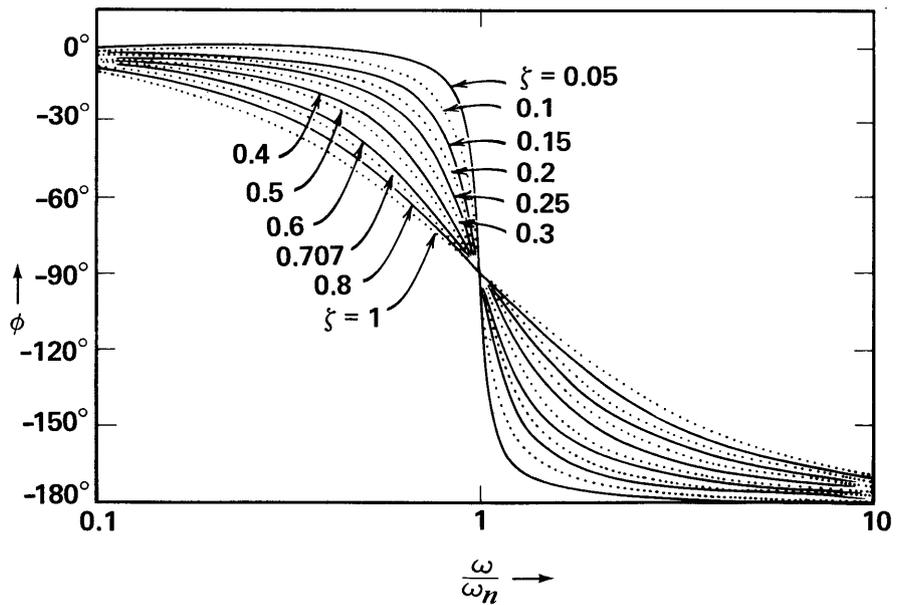
**$s$ -plane plot of complex pole pair**

**Viewgraph 3.3**

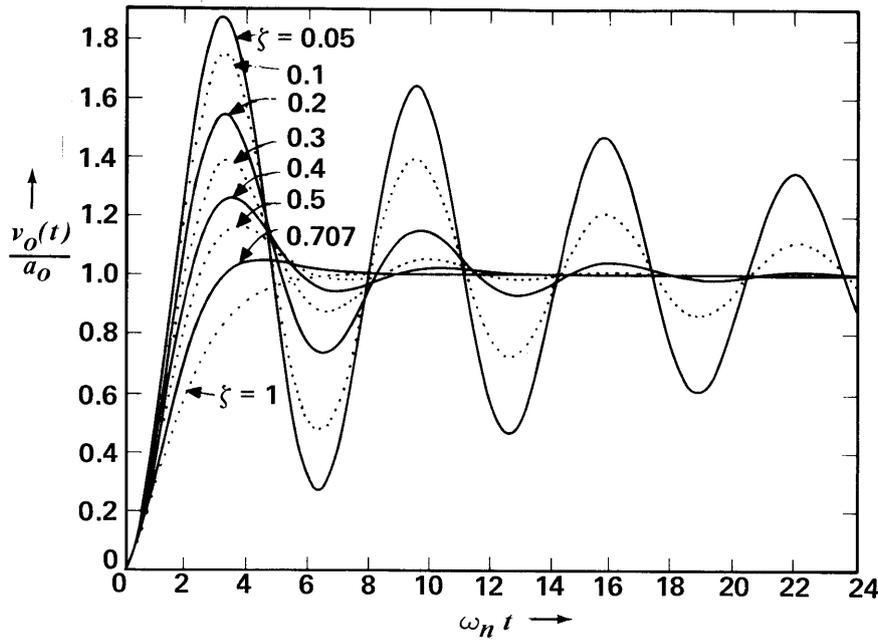


Frequency response of second-order system. (a) Magnitude

**Viewgraph 3.4**

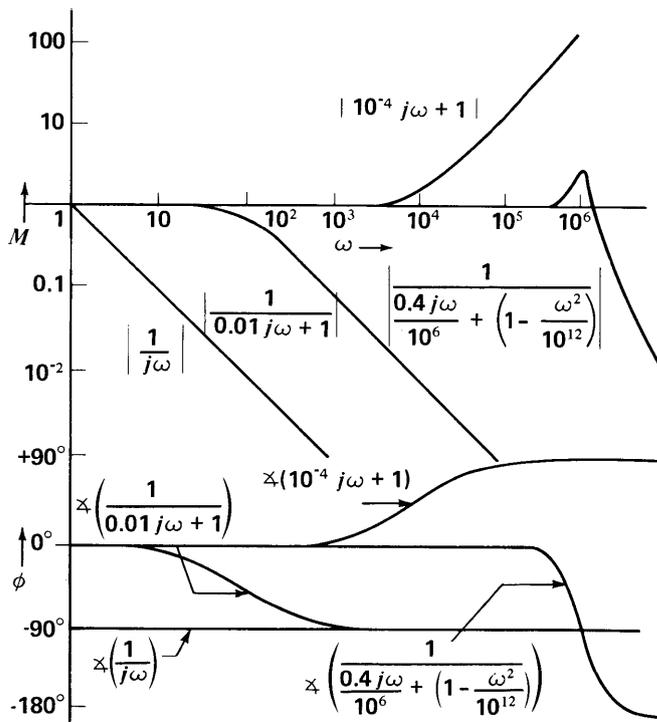


Frequency response of second-order system. (b) Angle.



Viewgraph 3.5

Step responses of second-order system.

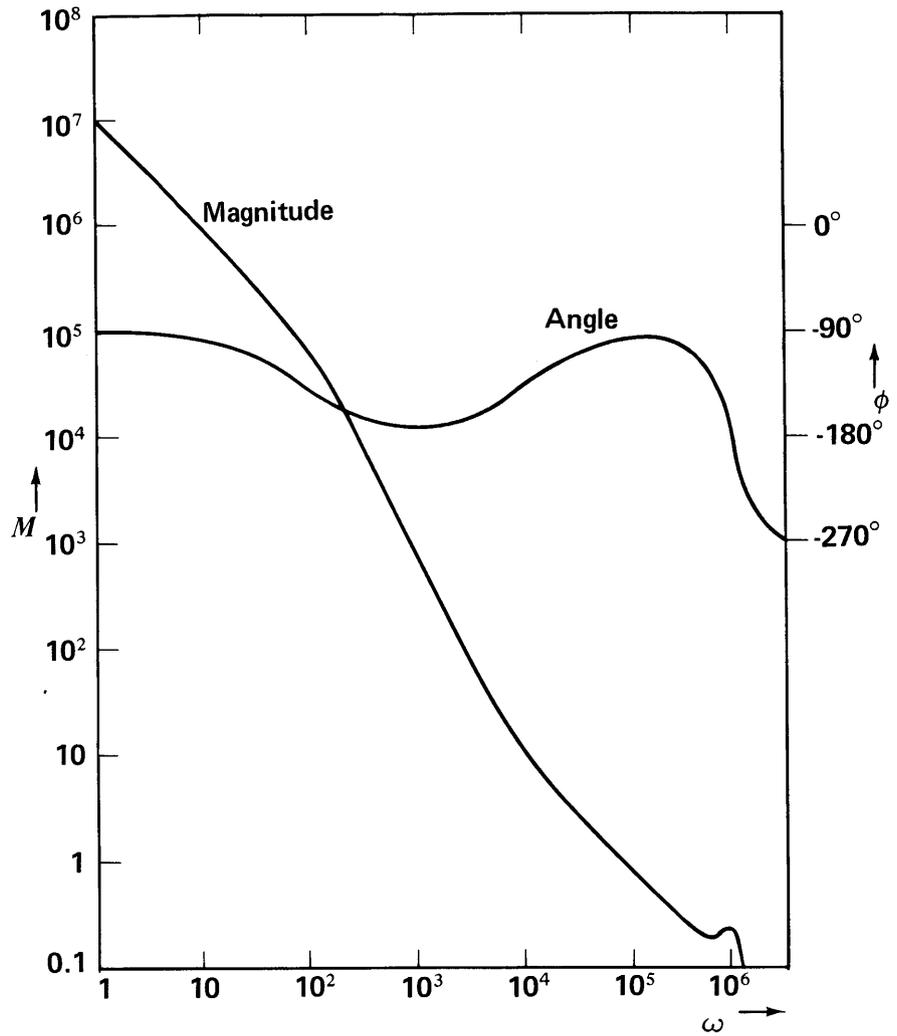


Viewgraph 3.6

(a) Individual factors

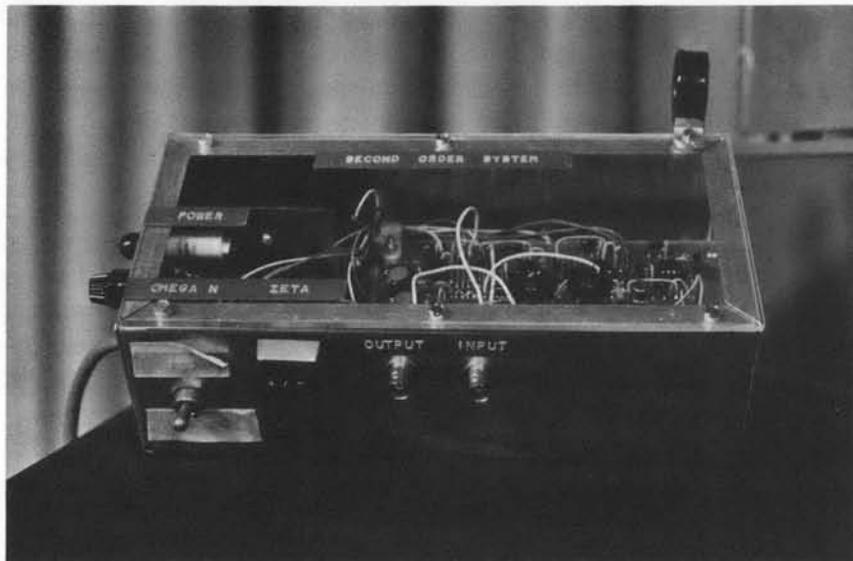
Bode plot of  $\frac{10^7 (10^{-4}s + 1)}{s(0.01s + 1)(s^2/10^{12} + 2(0.2)s/10^6 + 1)}$

Viewgraph 3.7

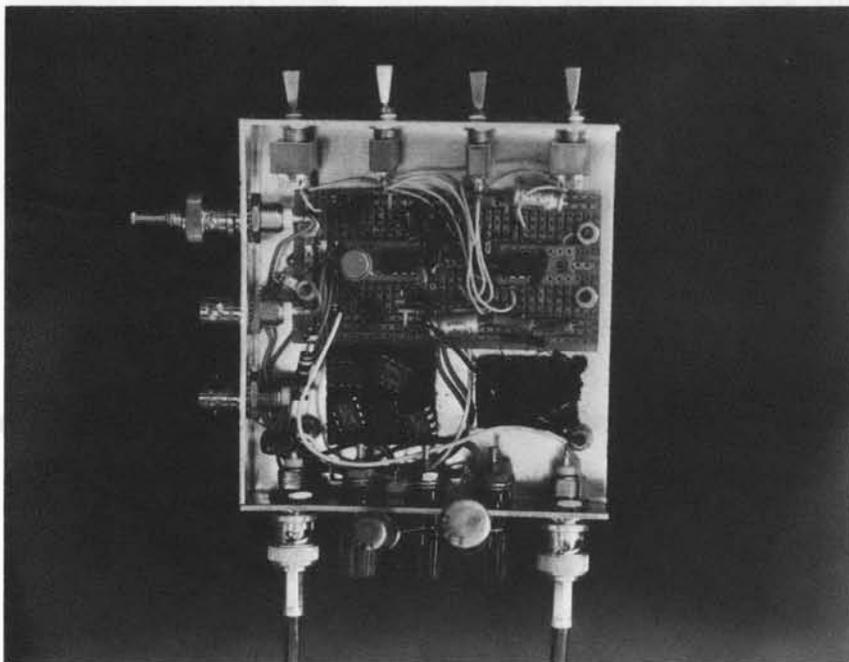


(b) Bode plot

Bode plot of 
$$\frac{10^7 (10^{-4} s + 1)}{s(0.01s + 1)(s^2/10^{12} + 2(0.2)s/10^6 + 1)}$$



**Demonstration Photograph 3.1**  
Second-order system



**Demonstration Photograph 3.2**  
Operational-amplifier for comparison  
with second-order response

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**Comments**

This lecture serves as an introduction to the dynamics of feedback systems. Aspects of this topic form the basis for more than half the material covered here. If the dynamics of systems could be adjusted at will, it would be possible to achieve arbitrarily high desensitivities and to modify electrical or mechanical impedances in any required way.

We will never solve for the exact closed-loop transient response of a high-order system, preferring instead to estimate important properties by considering lower-order systems that accurately approximate the actual behavior. A demonstration indicating a specific example of this type of approximation is included.

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**Additional Discussion**

I mention in the lecture that a factor of 0.707 corresponds to a  $-3$  dB change on a decibel scale. This reflects the convention usually used for feedback systems where gains (even dimensioned ones) are converted to dB as  $20 \log_{10}(\text{gain})$ .

Note that in viewgraphs 3.1, 3.3, 3.4, and 3.5, the horizontal axis is normalized so that the resultant curves can be easily scaled for any particular bandwidth system. Thus the horizontal axis in 3.1 is presented as a multiple of  $\frac{1}{\tau}$ , in 3.3 and 3.4 as a multiple of  $\omega_n$ , and in 3.5 as a multiple of  $\frac{1}{\omega_n}$ .

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**Reading**

Textbook: Sections 3.1, 3.3, 3.4, and 3.5. While we will not use the material in Section 3.2 directly, you may want to review it if you have not worked with Laplace transforms recently.

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**Problems**

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**Problem 3.1 (P3.1)**

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**Problem 3.2 (P3.2)**

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**Problem 3.3 (P3.5)**

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**Problem 3.4 (P3.7)**

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**Problem 3.5 (P3.8)**

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RES.6-010 Electronic Feedback Systems  
Spring 2013

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