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THE CLIMATE MACHINE V:
INTEGRATED ASSESSMENT I
Sensitivity Studies and
Uncertainty Analysis using the
Integrated Global System Model

R. PRINN, April 14, 2008

1. Structural & Parametric Uncertainty
2. Sensitivity Analysis
3. Uncertainty Analysis: IGSM 1
4. Uncertainty Analysis: IGSM 2.2
5. Communicating Uncertainty

TWO TYPES OF UNCERTAINTY

STRUCTURAL UNCERTAINTY

PARAMETRIC UNCERTAINTY

TWO TYPES OF ANALYSIS

SENSITIVITY

UNCERTAINTY

▪ SENSITIVITY ANALYSIS

$$\Rightarrow dY = \sum_i \frac{\partial Y}{\partial x_i} dx_i$$

$$\Rightarrow (dY)^2 = \sum_i \left(\frac{\partial Y}{\partial x_i} dx_i \right)^2 + \sum_{j \neq k} \frac{\partial Y}{\partial x_j} dx_j \frac{\partial Y}{\partial x_k} dx_k$$

$$= \sum_i \left(\frac{\partial Y}{\partial x_i} dx_i \right)^2 \text{ if errors due to } x_j \leftarrow$$

uncorrelated with errors due to x_k and errors have zero mean

▪ UNCERTAINTY ANALYSIS

$$\Rightarrow CDF(Y) = P[Y' \leq Y]$$

$$\Rightarrow PDF(Y) = \frac{dCDF(Y)}{dY}$$

e.g., Normal (Gaussian)

$$PDF(Y) = \frac{1}{\sqrt{2\pi}\sigma} \exp\left(-\frac{(Y-\mu)^2}{2\sigma^2}\right) \leftarrow$$

$$\mu = \int Y' PDF(Y') dY' \text{ (first moment = mean or expected value)} \leftarrow$$

$$\sigma^2 = \int (Y' - \mu)^2 PDF(Y') dY' \text{ (second moment = variance = [std. dev.]^2)} \leftarrow$$

Sensitivity Analysis using the MIT INTEGRATED GLOBAL SYSTEM MODEL VERSION 1

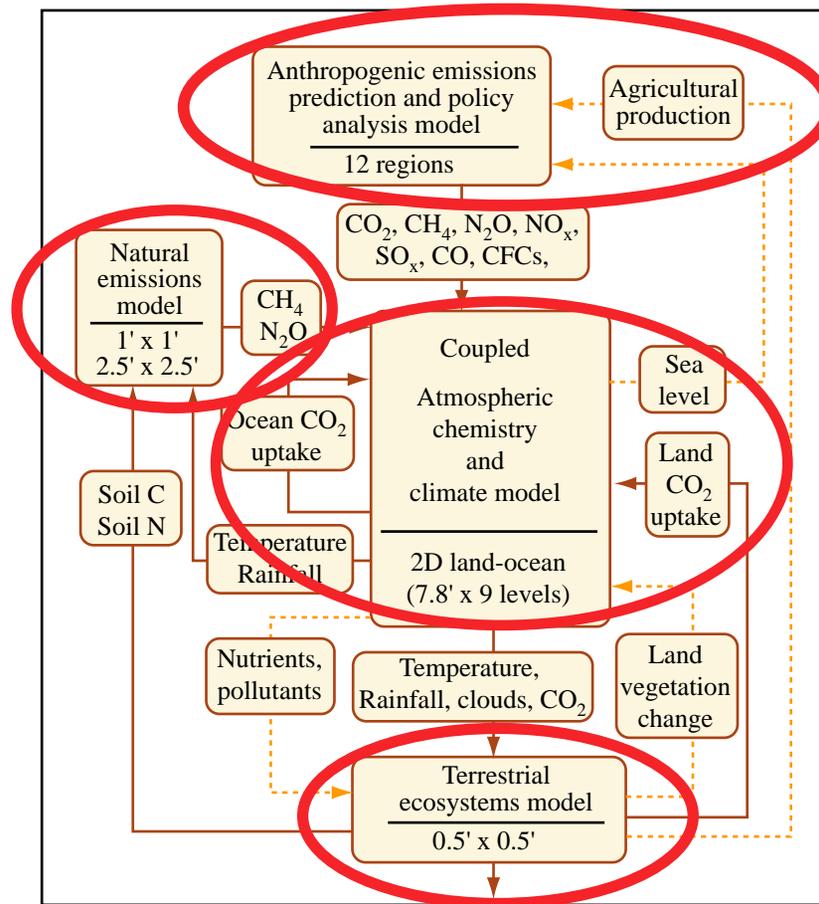


Figure by MIT OpenCourseWare.

SENSITIVITY ANALYSIS: *Defining the uncertain parameters*

Image removed due to copyright restrictions. See Table IV in:

Prinn, R., et al. "Integrated Global System Model for Climate Policy Assessment: Feedbacks and Sensitivity Studies." *Climatic Change* 41, no. 3/4 (1999): 469-546.

Schematic illustrating the seven runs performed for the Sensitivity Analysis of the IGSM 1. Open ellipses denote points in sequence where output is available, with the letters in the ellipse denoting the identifying symbol for the output.

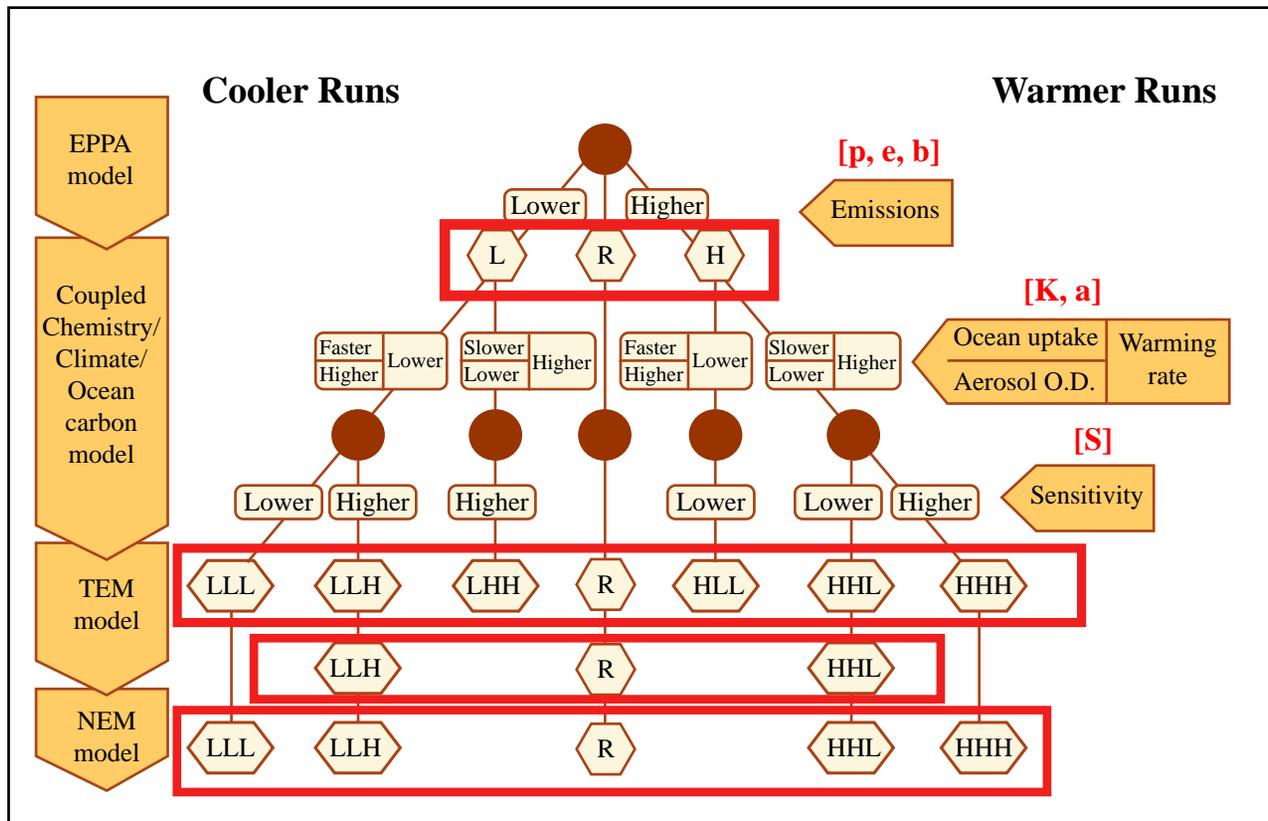


Figure by MIT OpenCourseWare.

Sensitivity of Temperature Change from 1990 to 2100 to assumed: Emissions (p, e, b); Ocean Heat & Carbon Uptake and Aerosol Forcing (K, a); & Climate Sensitivity (s)

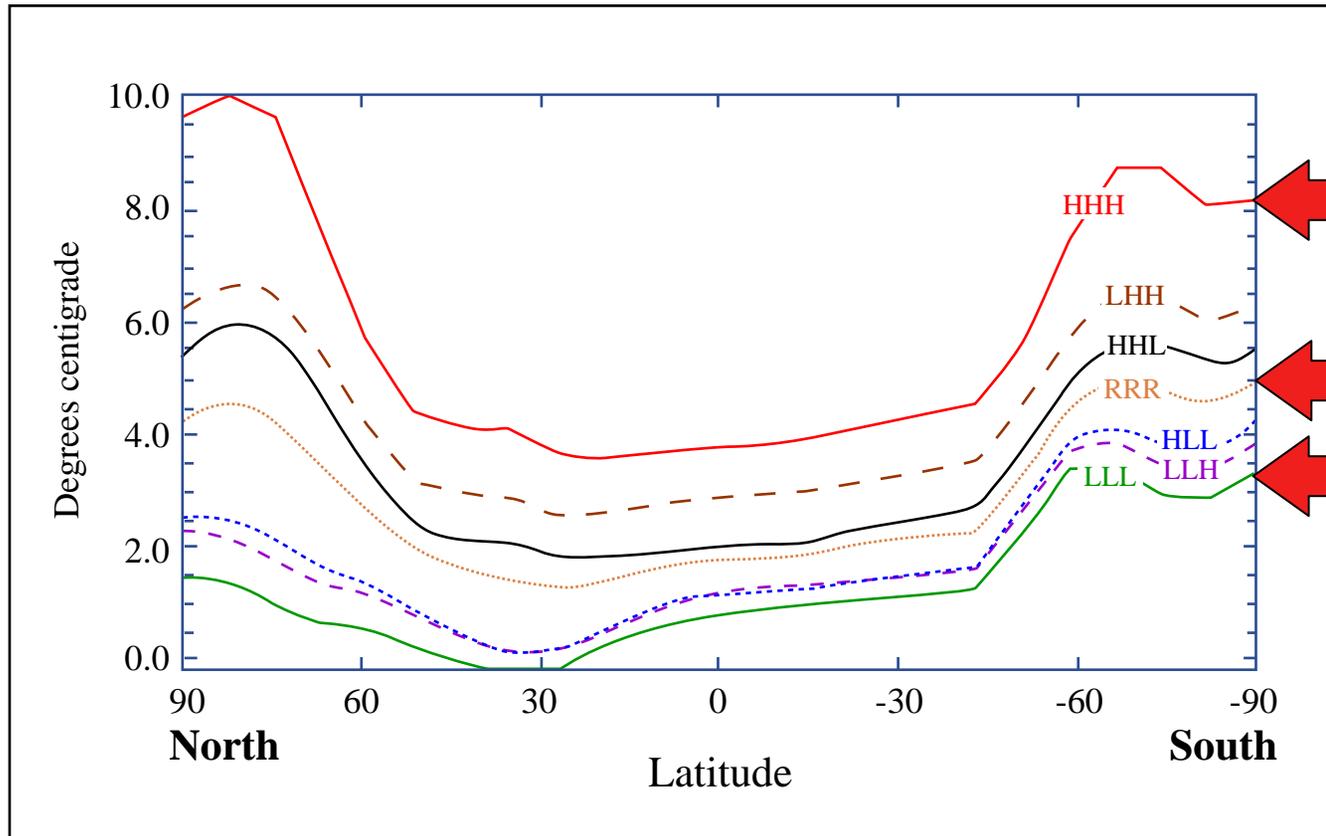


Figure by MIT OpenCourseWare.

Uncertainty Analysis using the MIT INTEGRATED GLOBAL SYSTEM MODEL VERSION 1

**THE MAJOR CLIMATE
FORECAST MODEL
UNCERTAINTIES INVOLVE
CLOUDS, OCEAN MIXING
& AEROSOL FORCING.**

**THESE UNCERTAINTIES ARE
CONSTRAINED BY
OBSERVATIONS**

**ADDED TO THESE
ARE SUBSTANTIAL
UNCERTAINTIES
IN EMISSION
FORECASTING**

*TO ESTIMATE THE PDFs
OF VARIOUS MEASURES
OF CLIMATE CHANGE,
WE USE VERY LARGE
ENSEMBLES OF IGSM
RUNS ,EACH WITH
RANDOMLY CHOSEN
EQUAL PROBABILITY
CHOICES FOR THE
UNCERTAIN MODEL
PARAMETERS.*

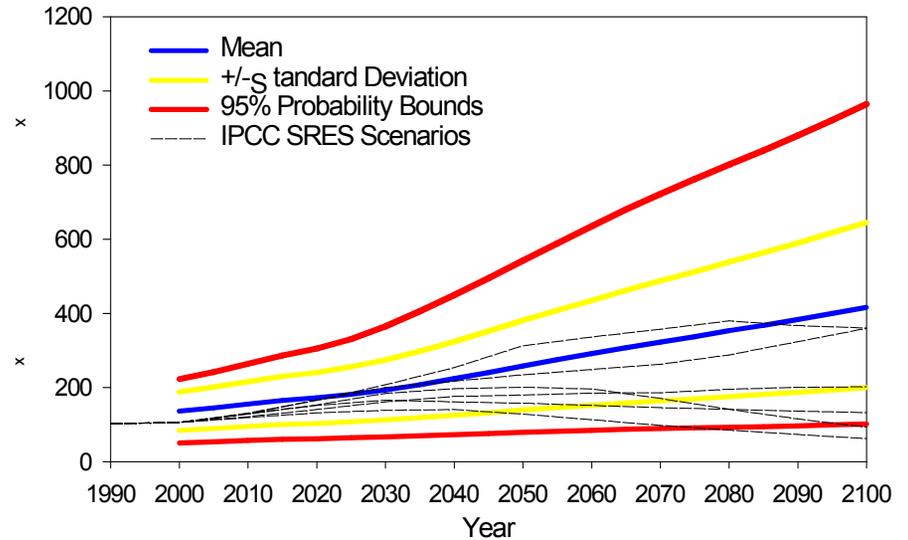
Uncertainty Analysis Method

- 250 runs of the MIT IGSM with Latin hypercube sampling of uncertain model parameters
- No explicit policy and stringent policy (at or below 550ppm CO₂ equivalent) cases
- Policy should lower probability of damaging outcomes

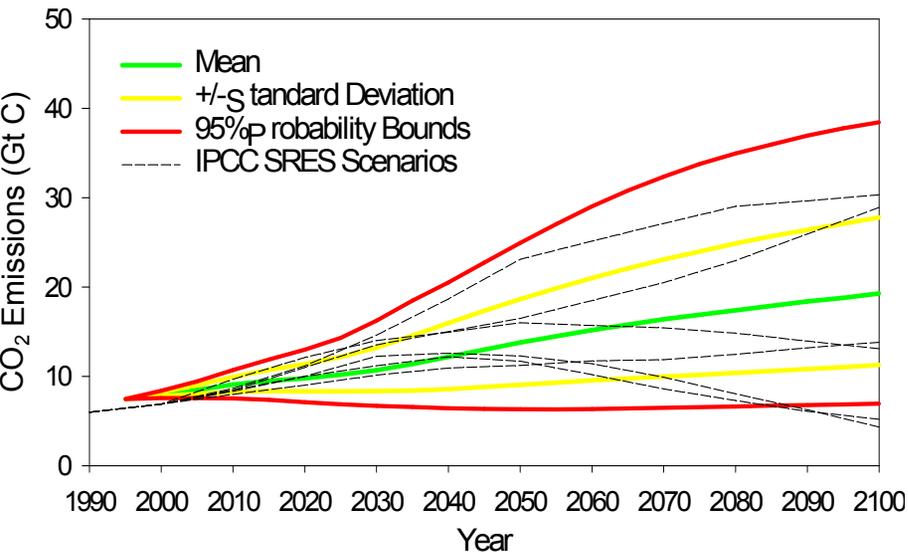
**TO ADDRESS
UNCERTAINTY
MIT CLIMATE MODEL
HAS FLEXIBLE
SENSITIVITY,
OCEAN MIXING
& AEROSOL
FORCING WHOSE
UNCERTAINTIES
ARE CONSTRAINED
BY OBSERVATIONS**

Images removed due to copyright restrictions. See Figure 4 in:
Forest, Chris, et al. "Quantifying Uncertainties in Climate System
Properties with the Use of Recent Climate Observations."
Science 295 (2002): 113-117.

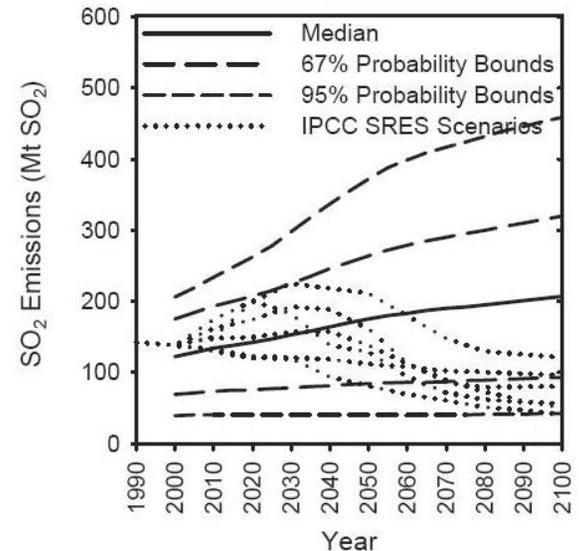
**PROBABILITY RANGES
FOR NO-POLICY CASE
OF EMISSIONS OF
SELECTED CLIMATE-
FORCING &
POLLUTING GASES
(EPPA cf. SRES)**



Global CO₂ Emissions (PgC/yr)



Global NO_x Emissions (Tg/yr)

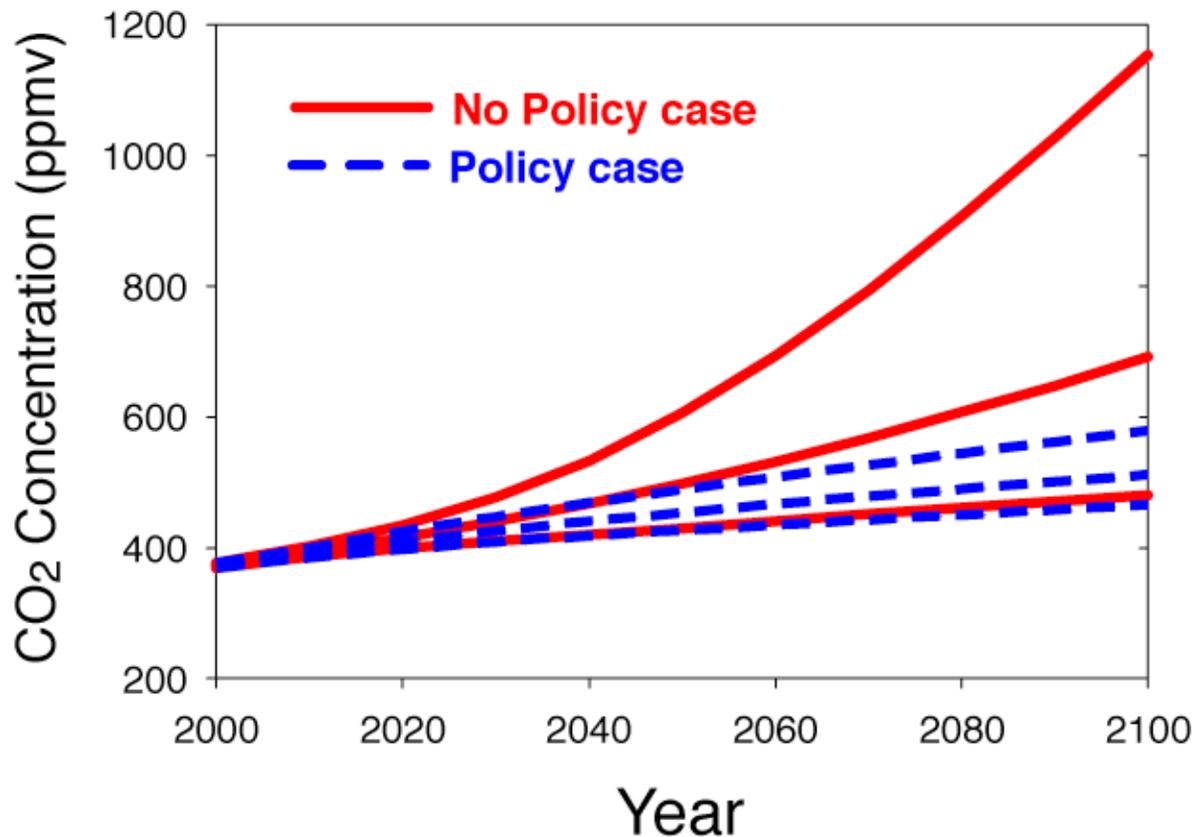


Global SO₂ Emissions (Tg/yr)

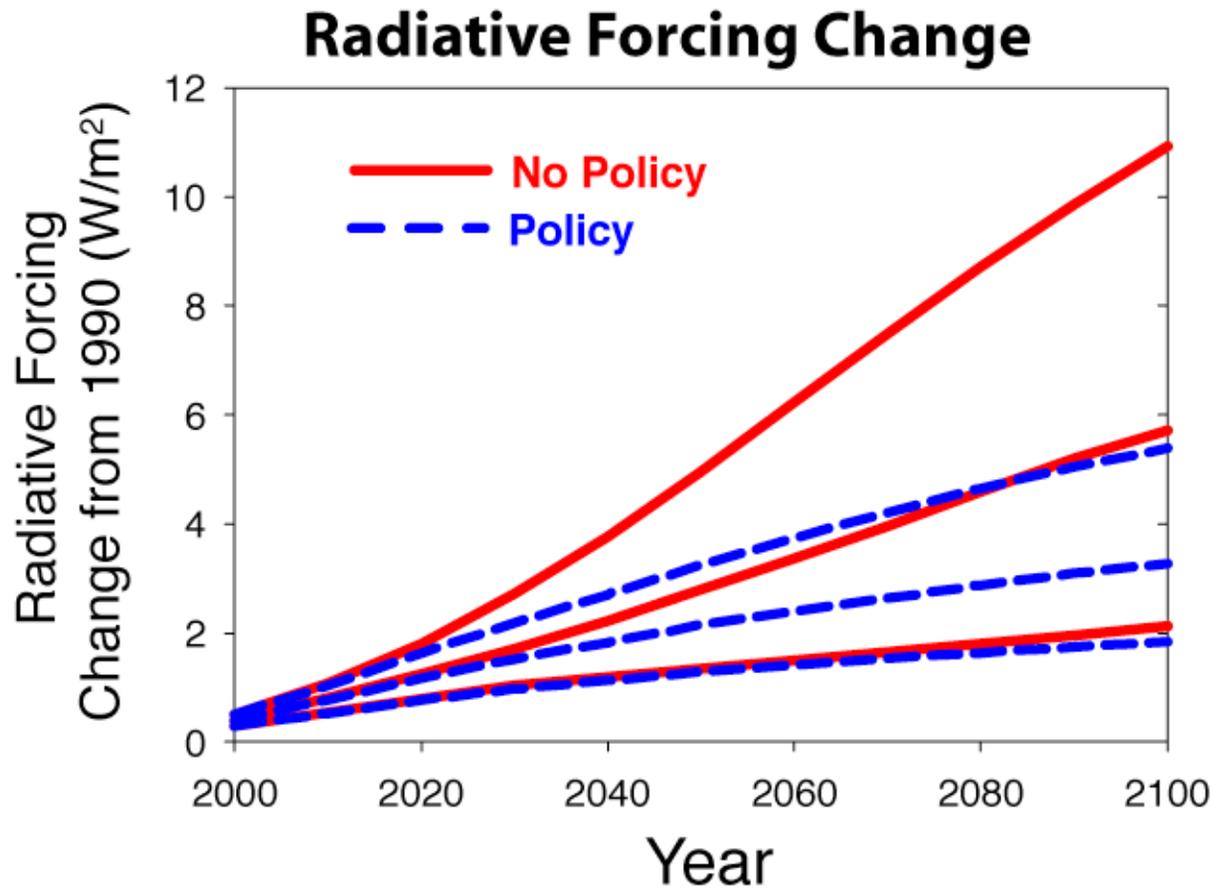
Ref: Webster et al, Atmos. Environ., 2002

Courtesy Elsevier, Inc., <http://www.sciencedirect.com>.
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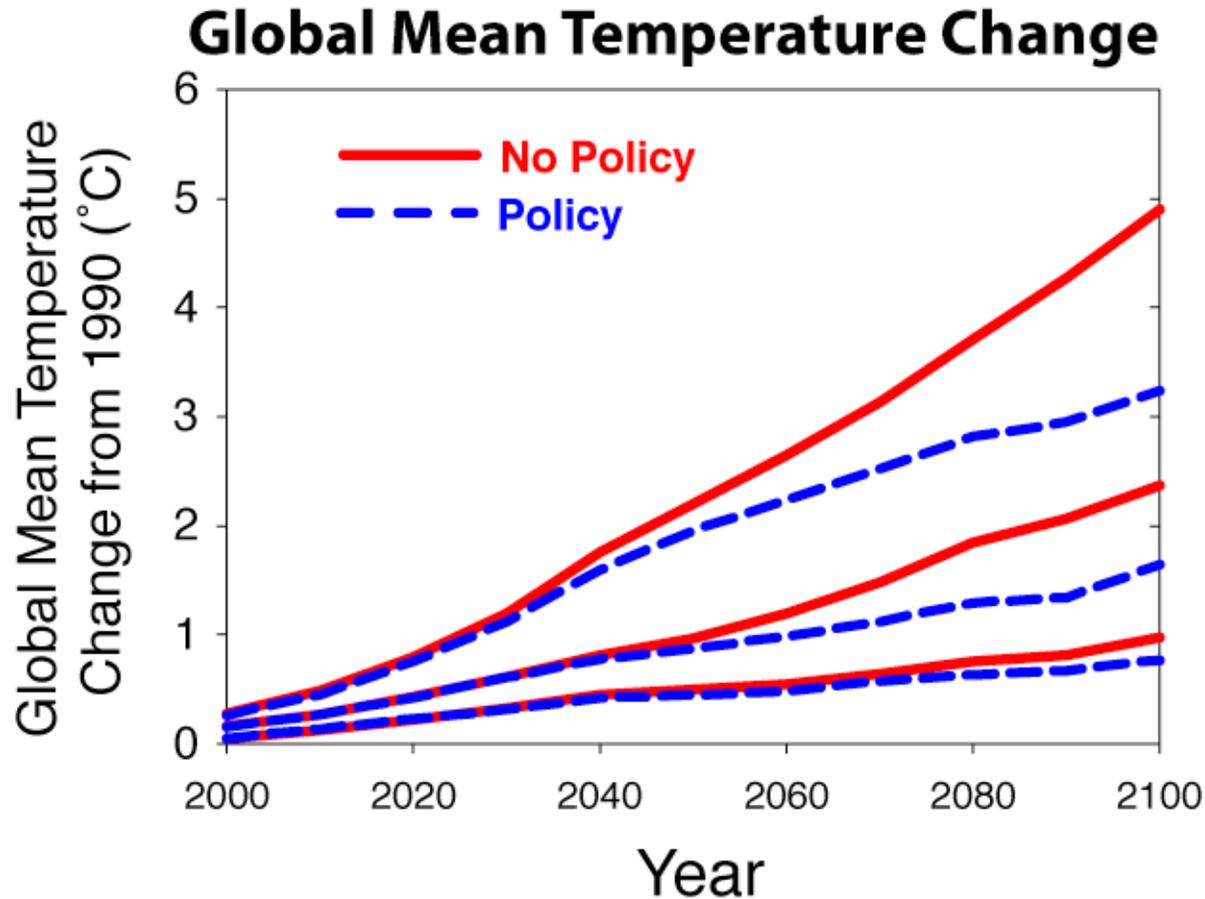
CO₂ Concentration Change



Projected changes in atmospheric CO₂ concentrations relative to 1990. Solid lines show the lower 95%, median, and upper 95% in the absence of greenhouse gas restrictions, and dashed lines show the lower 95%, median, and upper 95% under a policy that approximately stabilizes CO₂ concentrations at 550 ppm.



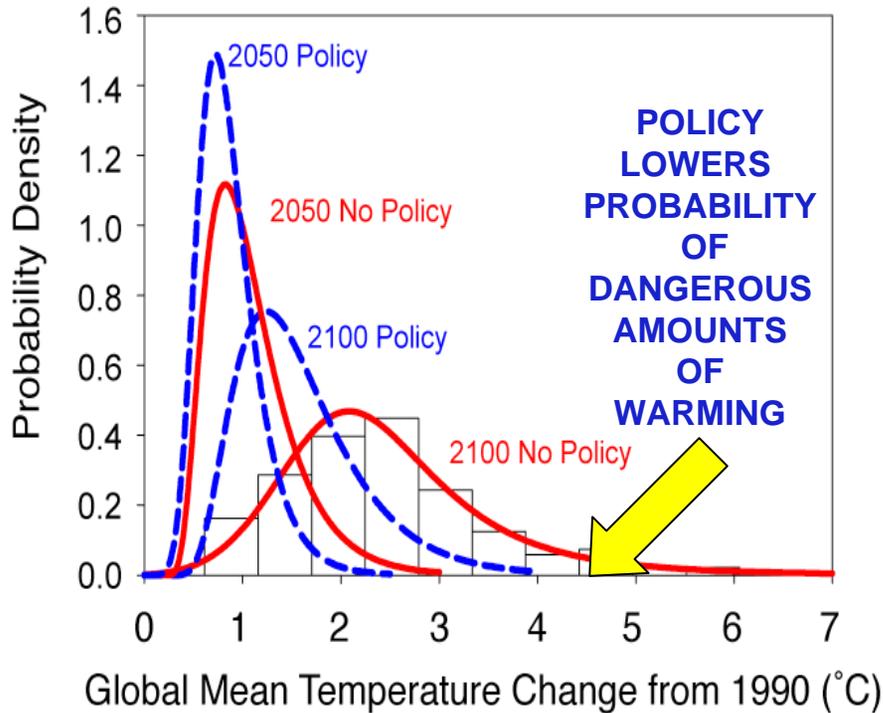
Projected changes in radiative forcing relative to 1990 due to all greenhouse gases. Solid lines show the lower 95%, median, and upper 95% in the absence of greenhouse gas restrictions, and dashed lines show the lower 95%, median, and upper 95% under a policy that approximately stabilizes CO₂ concentrations at 550 ppm.



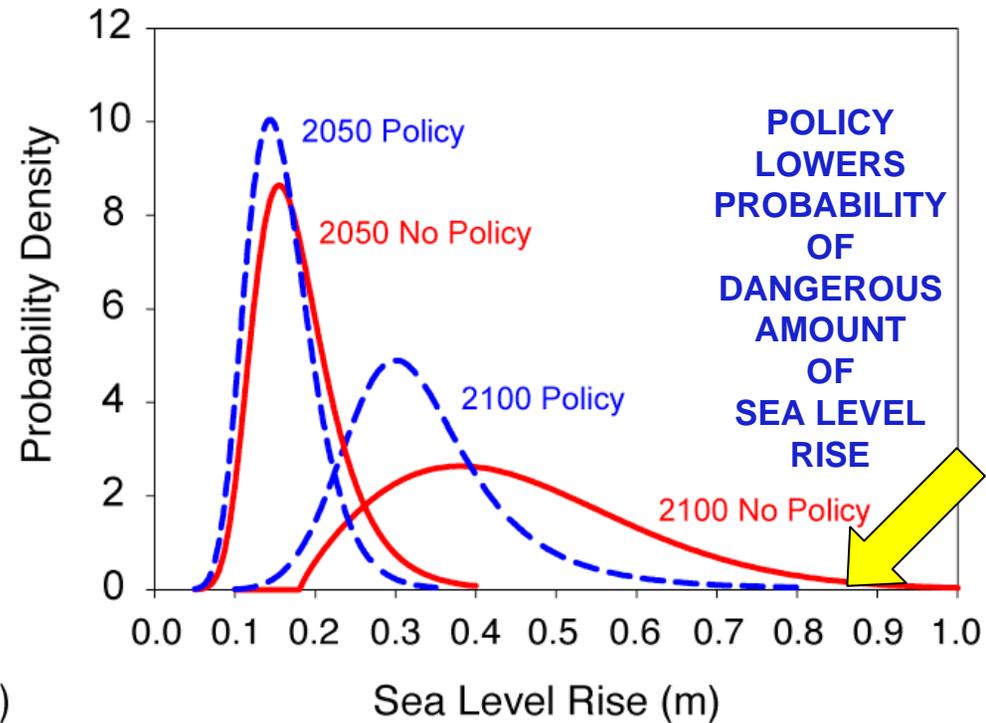
Projected changes in global mean surface temperature relative to 1990. Solid lines show the lower 95%, median, and upper 95% in the absence of greenhouse gas restrictions, and dashed lines show the lower 95%, median, and upper 95% under a policy that approximately stabilizes CO₂ concentrations at 550 ppm.

FULL PDF'S OF KEY MEASURES OF CLIMATE CHANGE
for 1990-2100, WITH & WITHOUT the (550 ppm) POLICY

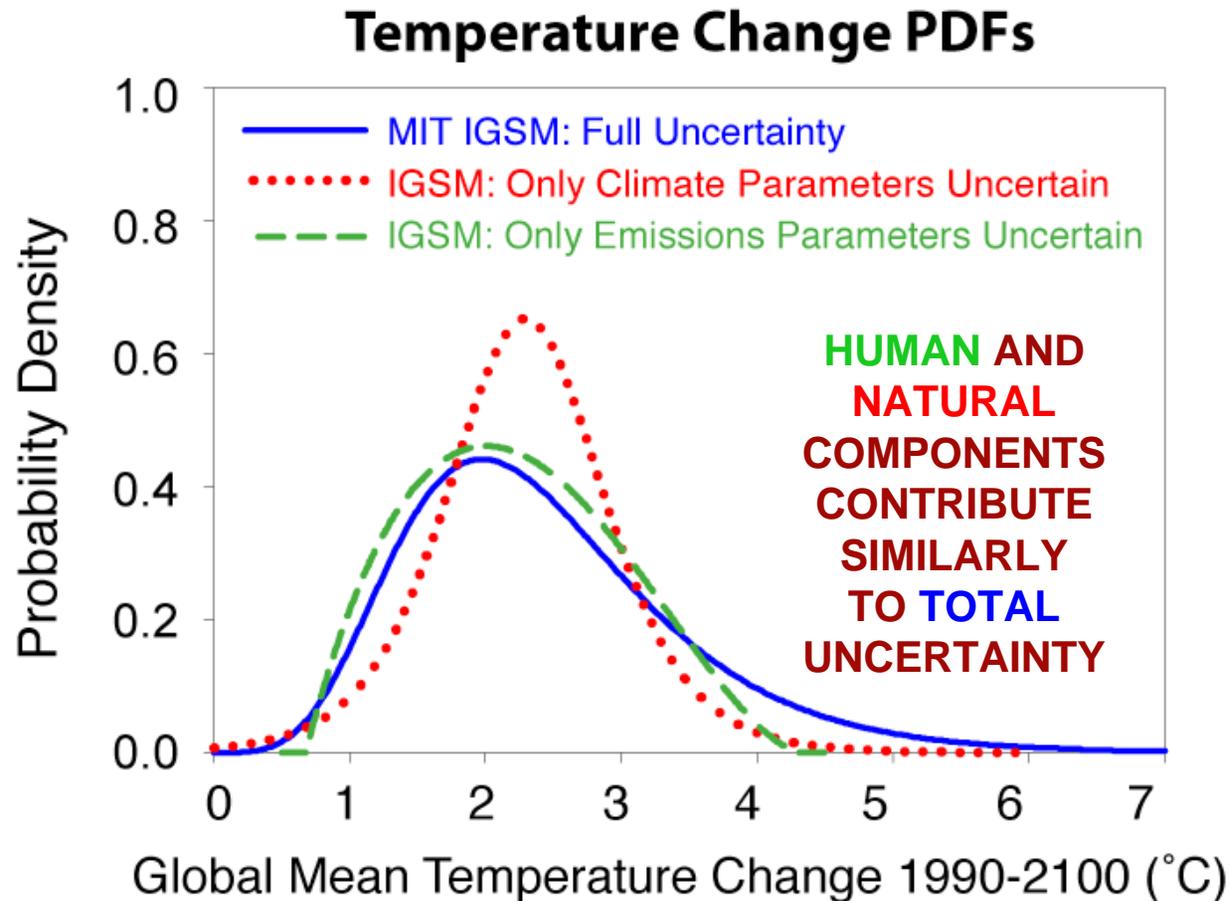
Temperature Change PDFs



Sea Level Rise PDFs

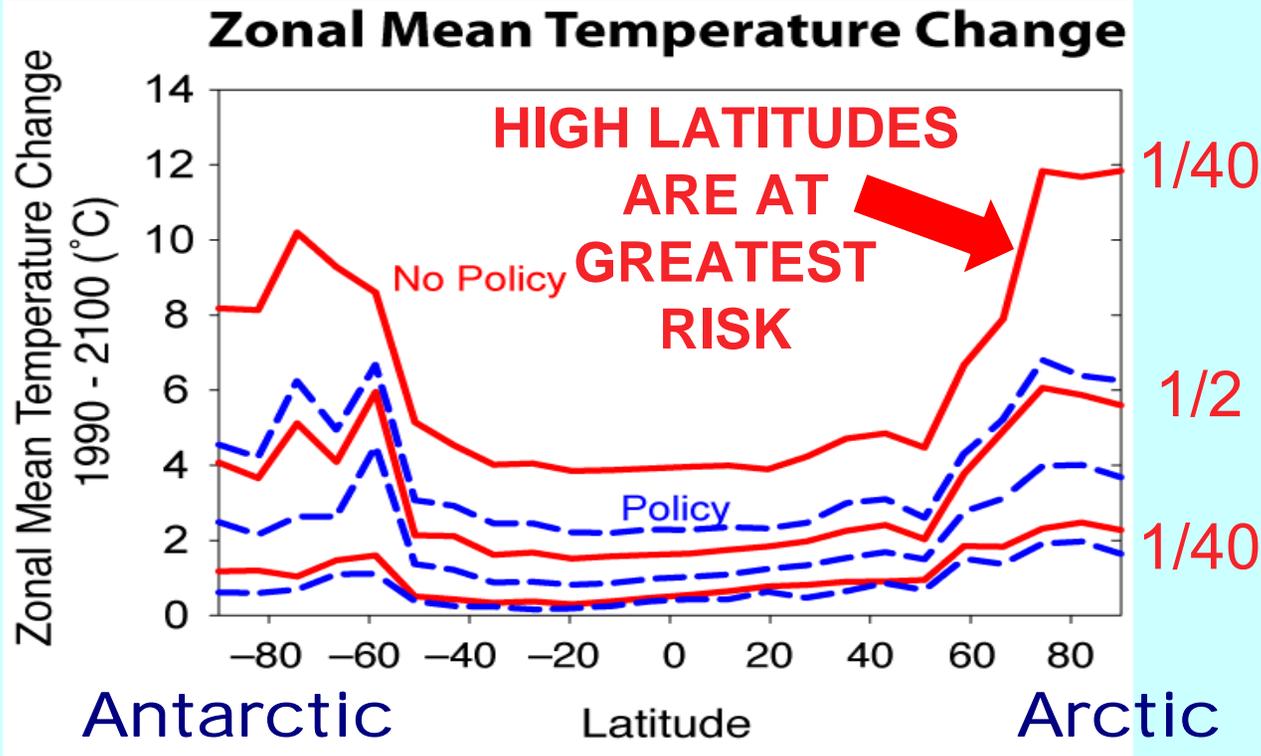


INFLUENCE OF EMISSIONS VS. CLIMATE ON THE PDF'S



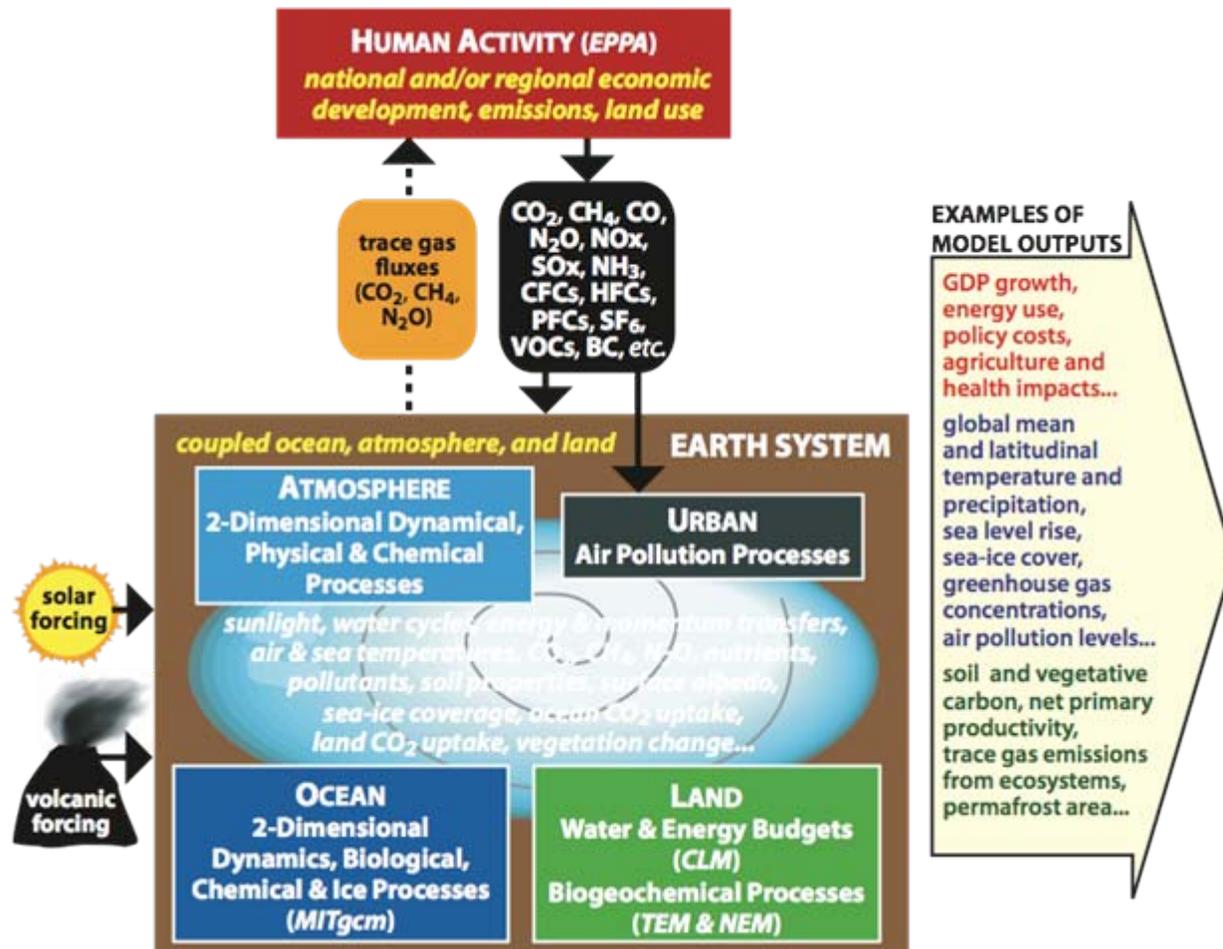
Probability distributions of global mean surface temperature change from 1990 to 2100 from all uncertain parameters (solid blue), only climate model parameters uncertain and emissions fixed (dotted red), and only emissions uncertain with climate model parameters fixed (dashed green).

WHAT IS THE PROBABILITY OF VARIOUS AMOUNTS OF CLIMATE CHANGE BY LATITUDE for 1990-2100, WITH & WITHOUT A (550 ppm CO₂-equivalent) POLICY?



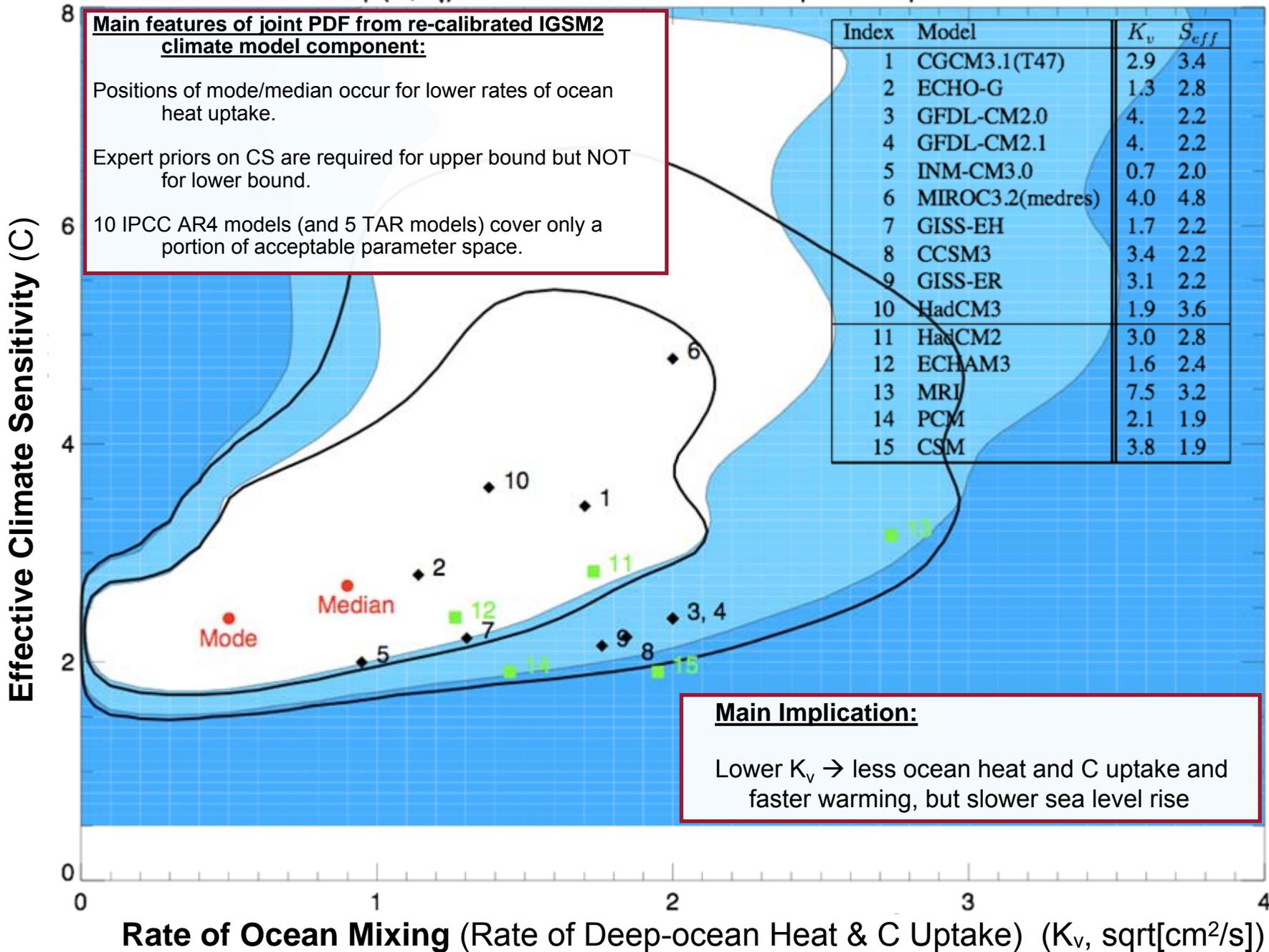
Projected change in surface warming by latitude band between 1990 and 2100. The median value, and lower 95% and upper 95% bounds are shown. Solid lines show distributions resulting from no emissions restrictions and dashed lines are distributions under the sample policy.

Uncertainty Analysis of MIT IGSM 2.2 under No Policy and Stabilization Scenarios

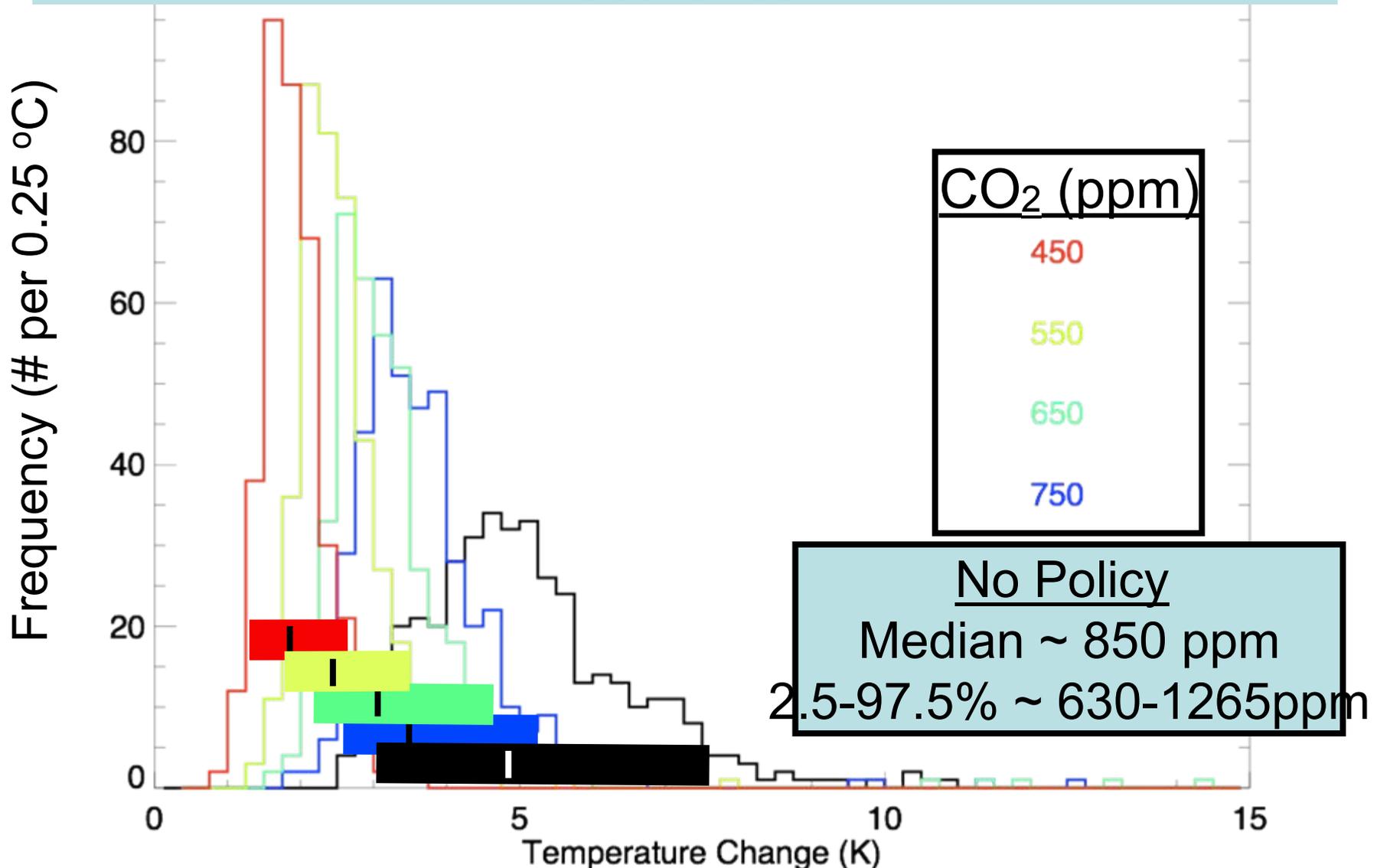


Methodology

- Estimate probability distributions for input parameters controlling the emissions and climate projections-system models
 - (1) Emissions Uncertainties
 - (2) Climate System Response Uncertainties:
 - Climate Sensitivity
 - Rate of Heat uptake by Deep Ocean
 - Radiative Forcing Strength of Aerosols
 - (3) Greenhouse Gas Cycle Uncertainties:
 - CO₂ Fertilization Effect on Ecosystem Sink
 - Rate of Carbon Uptake by Deep-Ocean
 - Trends in Rainfall Frequency on CH₄ + N₂O
- Generate 400 member ensembles to represent Monte Carlo sample
- Simulate Reference (i.e., No Policy) and Four Stabilization Scenarios (450, 550, 650, and 750 ppm)



Frequency Distributions for Temperature Change from 2000 to 2100 under No Policy and 4 CCSP Stabilization Scenarios



COMMUNICATING UNCERTAINTY AND RISK

Risks of Global Mean Temperature Increase Since Preindustrial

	$\Delta T > 2^{\circ}\text{C}$	$\Delta T > 4^{\circ}\text{C}$	$\Delta T > 6^{\circ}\text{C}$
No Policy	400 in 400	4 in 5	1 in 3
Stabilize at 750	400 in 400	3 in 5	1 in 50
Stabilize at 650	98 in 100	1 in 5	1 in 200
Stabilize at 550	97 in 100	1 in 20	<1 in 400
Stabilize at 450	70 in 100	<1 in 400	<1 in 400

COMMUNICATING UNCERTAINTY AND RISK

Risks of Ocean Impacts

	Sea Level Rise > 0.3m	Sea Level Rise > 0.6m
No Policy	19 in 20	8 in 50
Stabilize at 750	17 in 20	2 in 50
Stabilize at 650	15 in 20	1 in 50
Stabilize at 550	11 in 20	<1 in 400
Stabilize at 450	5 in 20	< 1 in 400

Why is the Reference distribution shifted To higher temperatures?

- Radiative Forcing Increases?
 - Emissions (higher lower bound)
 - Reduced Ocean Carbon Uptake
 - Additional forcing such as Black Carbon & Tropospheric Ozone (additional forcing included but still calibrated by net aerosols in 1990s)
- Climate Model Response?
 - Climate Model Parameters show higher response
- Learning?
 - Distributions better defined
 - Distributions shifted higher

Conclusions regarding odds of Future Climate Change from latest Analysis

- $\Delta T > 2^{\circ}\text{K}$ above pre-industrial
 - virtually certain under No Policy scenario
 - reduced to 7 in 10 chance with 450 ppm stabilization
- $\Delta\text{SeaLevel} > 0.3$ meters above pre-industrial
 - 19 chances in 20 under No Policy scenario
 - reduced to 1 in 4 chance with 450 ppm stabilization

Concluding Remarks

As with all investigations of complex and only partially understood systems the probability results must be treated with appropriate caution:

- ❑ Current knowledge of stability of great ice sheets, stability of thermo-haline circulation, ecosystem dynamics, climate-severe storm connections, future technological innovation, human population dynamics, political change, etc., is limited.
- ❑ Therefore, “surprises” not currently evident from model studies including uncertainty studies may occur.