

October 26, 2004 – mini-Quiz #6 – 8.03

Your name . . . . .

Mark your recitation: R01 – R02 – R03 – R04 – R05

In lectures, we discussed the following dispersion relation

$$\omega^2 = v^2 k^2 + \alpha k^4$$

1. (4 pts) What is the medium for which this relationship is a fairly good approximation?

A string in musical instruments.

2. (4 pts) What is the origin of the term  $\alpha k^4$ ?

The stiffness of the string is responsible for this term.

The restoring force due to the tension is approximately proportional to  $k^2$ , the restoring force due to stiffness is approximately proportional to  $k^4$ . We chose a specific example, and calculated the effect this has on the tenth harmonic of a piano string whose fundamental is about 80 Hz.

3. (2 pts) What are the SI units of  $\alpha$ ?

$\alpha k^4$  must have the same units as  $\omega^2$  which is  $sec^{-2}$ . Since  $k$  has units  $m^{-1}$ ,  $\alpha$  has units  $m^4/sec^2$ .