

Topics: Continuous Charge Distributions

Related Reading:

Study Guide (Liao et al.): Sections 2.9-2.10; 2.13

Topic Introduction

Today we are focusing on understanding and calculating the electric field generated by a continuous distribution of charge. We will do problem solving #2, which highlights this concept and the associated calculations.

Charge Distributions

Electric fields “superimpose,” or add, just as gravitational fields do. Thus the field generated by a collection of charges is just the sum of the electric fields generated by each of the individual charges. If the charges are discrete, then the sum is just vector addition. If the charge distribution is continuous then the total electric field can be calculated by integrating the electric fields $d\mathbf{E}$ generated by each small chunk of charge dq in the distribution.

Charge Density

When describing the amount of charge in a continuous charge distribution we often speak of the *charge density*. This function tells how much charge occupies a small region of space at any point in space. Depending on how the charge is distributed, we will either consider the volume charge density $\rho = dq/dV$, the surface charge density $\sigma = dq/dA$, or the linear charge density $\lambda = dq/d\ell$, where V , A and ℓ stand for volume, area and length respectively.

Important Equations

Electric field from continuous charge distribution:

(NOTE: for point charge-like dq)

$$\vec{\mathbf{E}} = \frac{1}{4\pi\epsilon_0} \int \frac{dq}{r^2} \hat{\mathbf{r}}$$

Charge Densities:

$$dq = \begin{cases} \rho dV & \text{for a volume distribution} \\ \sigma dA & \text{for a surface (area) distribution} \\ \lambda d\ell & \text{for a linear distribution} \end{cases}$$