

## 22.251 Systems Analysis of the Nuclear Fuel Cycle

Fall 2009

### Lab #4 Solution

(a)

Data required for solution:

$$\text{Cell power} = 104.5 \text{ W/cc} * \text{Cell Volume} = 104.5 * 6.3504 = 663.62 \text{ W}$$

$$k\text{-inf} = 1.3827 \pm 0.0012$$

$$\text{weight loss to fission} = 0.56184$$

$$\text{neutron yield per fission} = \frac{k}{w_f} = \frac{1.3827}{0.56184} \approx 2.46$$

To obtain real reaction rates, Flux Multiplication Factor (FMF) is needed

$$FMF [FSN / \text{sec}] = \frac{P [J / \text{sec}] \times v [FN / \text{fiss}]}{k [FN / FSN] \times E_f [J / \text{fiss}]} \approx \frac{663.62 \times 2.46}{1.3827 \times 200 \times 1.602 \times 10^{-13}} = 3.686 \times 10^{13} [FSN / \text{sec}]$$

Real reaction rates are calculated from the tallied reaction rates as:

$$RR \left[ \frac{\text{reactions}}{\text{sec}} \right] = rr \left[ \frac{\text{barn}}{FSN \times \text{cm}^2} \right] \times FMF \left[ \frac{FSN}{\text{sec}} \right] \times V_{\text{cell}} [\text{cm}^3] \times N_{\text{nuclide}} \left[ \frac{\#}{\text{cm} \times \text{barn}} \right]$$

Table 1. Summary of the reaction rate [# / sec] calculation results for UO<sub>2</sub> and NU fuel

		UO <sub>2</sub>	UN
(n,γ) in U-238	Thermal	1.66E+12	1.46E+12
	Epithermal	8.35E+12	1.10E+13
	Total	1.00E+13	1.24E+13
(n,f) in U-235	Thermal	1.54E+13	1.33E+13
	Epithermal	4.21E+12	5.78E+12
	Total	1.96E+13	1.91E+13

Table 2. Spectral indices

	UO <sub>2</sub>	UN
$C^*$	0.512	0.651
$\delta_{25}$	0.274	0.435
$\rho_{28}$	5.019	7.529

(b)

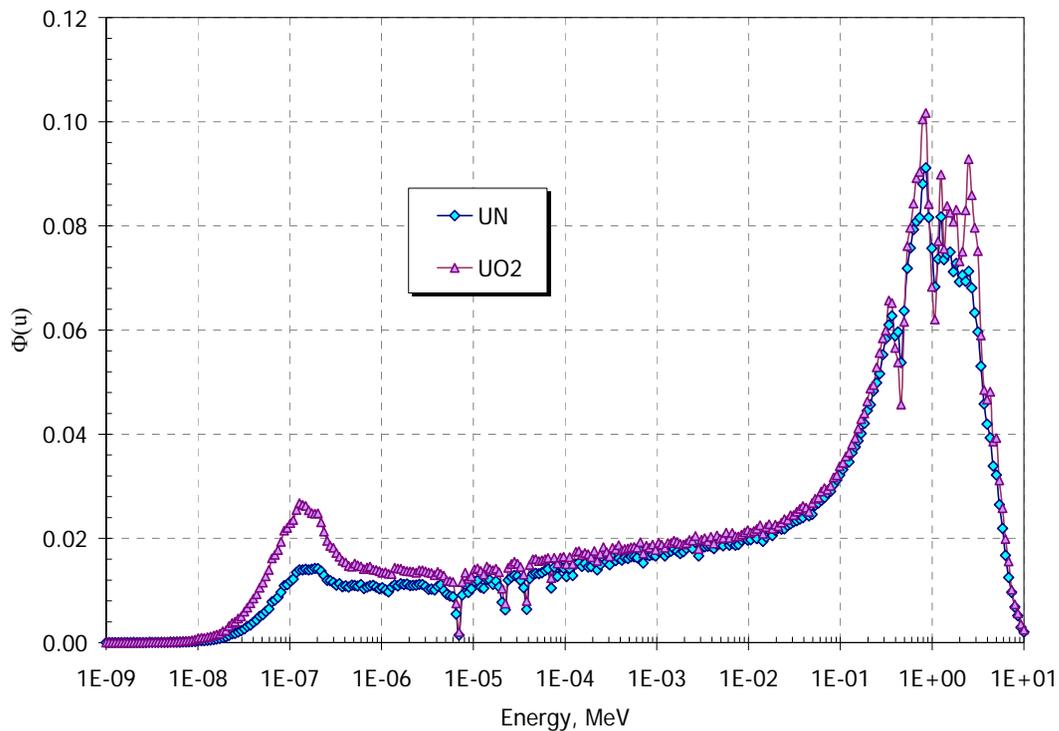
Table 3. Flux ratios for the UO<sub>2</sub> and UN fuel

	UO <sub>2</sub>	UN
$\varphi_2$	0.743	0.420
$\varphi_1$	6.167	5.596
$\varphi_2/\varphi_1$	0.120	0.075

With increasing H/HM, spectrum softens due to better moderation.

Higher enrichment hardens the spectrum because of the higher absorption of thermal neutrons by U-235 as it is primarily thermal absorber.

(c)



High density of nitride fuel effectively reduces H/HM and thus hardens the neutron spectrum (see above figure). Criticality is also reduced ( $k = 1.2366 \pm 0.0011$ ) due to the lower H/HM and somewhat high neutron absorption by N-14. The reduction in thermal flux component can also be observed from Tables 3 and 4.

(d)

Table 4. Flux ratios in the fuel and moderator

	UO <sub>2</sub>		UN	
	Fuel	Water	Fuel	Water
$\phi_2$	0.743	0.853	0.420	0.511
$\phi_1$	6.167	6.071	5.596	5.527
$\phi_2/\phi_1$	0.120	0.140	0.075	0.092

Fast neutrons are produced in the fuel and eliminated mainly in water as they slow down. Thermal neutrons are born in water and absorbed mainly in the fuel. Therefore, fraction of thermal neutrons is larger in water than in the fuel.

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