

## PROPERTIES OF GASES

### Equation of State

For a perfect gas:  $pv = RT$

where  $p$  is pressure,  $\text{N/m}^2$ , Pa, or kPa

$v$  is specific volume,  $\text{m}^3/\text{kg}$

$T$  is absolute temperature,  $^\circ\text{K}$

$R$  is the gas constant,  $\text{J/kgK}$  or  $\text{kJ/kgK}$  and  $R = \mathcal{R}/M$

where  $\mathcal{R}$  is the Universal Gas Constant =  $8.3144 \text{ kJ/kmole K}$

$M$  is the molecular weight, e.g. for air  $M_{\text{air}} = 28.96 \text{ kg/kmol}$ ,  $R_{\text{air}} = 0.2871 \text{ kJ/kgK}$ .

### Other Properties

At moderate temperatures and pressures the properties internal energy and enthalpy are assumed to be independent of pressure.

$u = u(T, M)$  or for a particular gas  $u = u(T)$

and  $h = h(T, M)$  or  $h = h(T)$

specific heats:

$c_v = du/dT$ ,  $c_p = dh/dT$ , and  $c_p / c_v = \gamma$

since  $h = u + pv = u + RT$ , then  $dh/dT = du/dT + R$ . Thus  $c_p = c_v + R$  and

$c_p - c_v = R$ , or  $R = c_p(\gamma - 1) / \gamma$ .

### Second Law

$Tds = dh - v dp$

$\therefore ds = dh/T - v dp/T = dh/T - R dp/p$

for an isentropic process  $ds = 0$

$\therefore dh/T = R dp/p$ .

This expression may be integrated to give

$$\int_{T_1}^{T_2} c_p \frac{dT}{T} = R \ln \frac{p_2}{p_1}$$

For the special case where the specific heats remain constant this equation may be written as:

$$\frac{T_{2s}}{T_1} = \left( \frac{p_2}{p_1} \right)^{\frac{R}{c_p}} = \left( \frac{p_2}{p_1} \right)^{\frac{\gamma-1}{\gamma}}$$