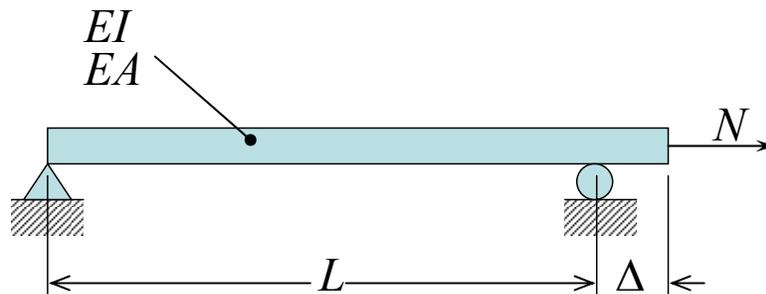


Lecture 6

Moderately Large Deflection Theory of Beams

Problem 6-1:

Part A: The department of Highways and Public Works of the state of California is in the process of improving the design of bridge overpasses to meet earthquake safety criteria. As a highly paid consultant to the project, you were asked to evaluate its soundness. You rush back to your lecture notes, and you model the overpass as a simply supported beam of span L with an overhang $\Delta = 0.01L$. Assume that the distributed load is a sinusoidal function.



- a) Calculate the maximum allowable midspan deflection $(w_o)_{critical}$ under which the beam will slide off its support.

Part B: Assume that the above design with an external axial force $N=0$ and $\Delta=0.01L$ has a safety factor of one. The design of earthquake resistant structures requires a safety factor of five, meaning that $(w_o)_{critical}$ must be increased by a factor of five without the bridge collapsing. Two possible design modifications were proposed. In the first one, the overhang is simply increased to Δ_{new} . In the second design, a tensile force N is applied to the bridge to increase its transverse stiffness and thus reduce the central deflection and the resulting motion of the support.

- b) For the first proposed modification, what length Δ_{new} of the overhang will meet the requirement of a safety factor of five? Give your result in terms of the original Δ and other parameters if needed.
- c) For the second design, what is the magnitude of the dimensionless tensile force N/EA that will give a safety factor equal to five?
- d) Which design is better? Can you think of a third alternative design solution?

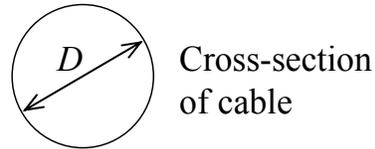
Problem 6-2:

A long span aerial tramway steel cable of length $L=1\text{km}$ is loaded by a hurricane wind with intensity $q(x)$ sinusoidally distributed between the end stations. The cable deflects by $w_0=5\text{m}$.

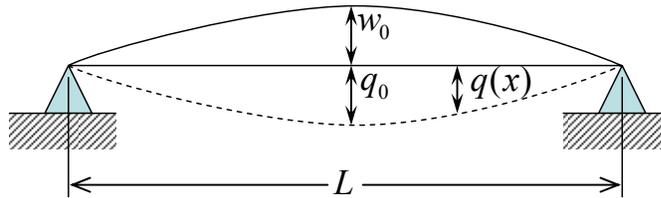
$$E = 2.1 \times 10^5 \text{ MPa}$$

$$\sigma_y = 300 \text{ MPa}$$

$$D = 60 \text{ mm}$$



$$q(x) = q_0 \sin\left(\frac{\pi x}{L}\right)$$



- Calculate the resulting load intensity q_0
- Calculate the tension in the cable N .
- Calculate the tensile stress.
- Compare (c) with the yield stress, and determine the safety factor.

Problem 6-3:

Plot the dimensionless deflections (w_0/L) versus the dimensionless line load for both bending and membrane (cable) solutions over a slender beam. At what dimensionless deflections will the bending and membrane solutions be equal, assuming a length to thickness ratio equal to 10?

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