

2.008

Process Control

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Outline

1. Optimization
2. Statistical Process Control
3. In-Process Control

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What is quality?

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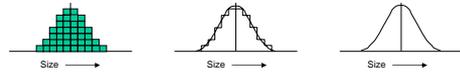
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Variation: Common and Special Causes

Pieces vary from each other:



But they form a pattern that, if stable, is called a distribution:

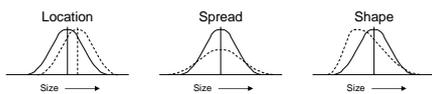


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Common and Special Causes (cont'd)

Distributions can differ in...



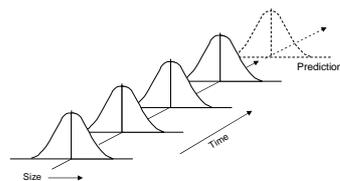
...or any combination of these

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Common and Special Causes (cont'd)

If only common causes of variation are present, the output of a process forms a distribution that is stable over time and is predictable:

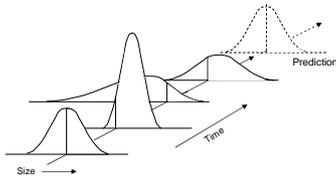


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Common and Special Causes (cont'd)

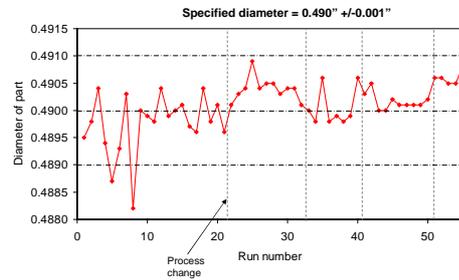
If special causes of variation are present, the process output is not stable over time and is not predictable:



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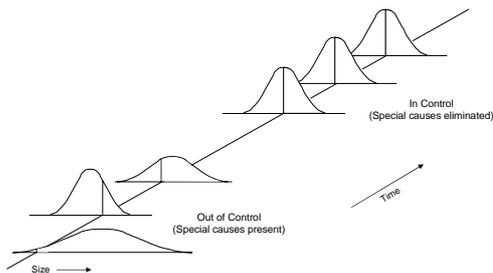
Variation: Run Chart



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Statistical Process Control

1. Detect disturbances (special causes)
2. Take corrective actions

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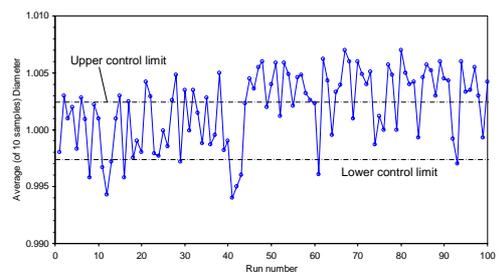
Central Limit Theorem

- A large number of independent events have a continuous probability density function that is normal in shape.
- Averaging more samples increases the precision of the estimate of the average.

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Shewhart Control Chart

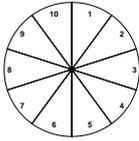


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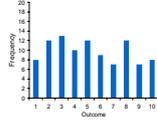
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Sampling and Histogram Creation

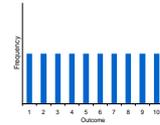
Wheel of Fortune: Equal probability of outcome 1-10, $P=0.1$



Taking 100 random samples, the resulting histogram would look like this



Taking ∞ random samples, the resulting histogram would look like this

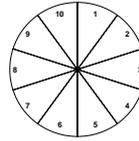


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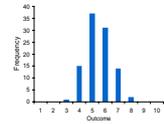
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Sampling and Histogram Creation (cont'd)

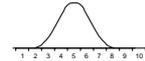
Wheel of Fortune: Equal probability of outcome 1-10, $P=0.1$



Take 10 random samples, calculate their average, and repeat 100 times, the resulting histogram would resemble



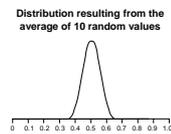
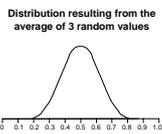
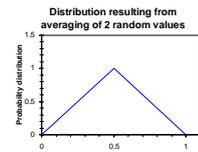
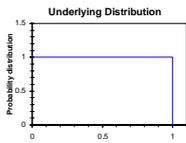
Take 10 random samples, calculate their average, and repeat ∞ times, the resulting histogram would approach the continuous distribution shown



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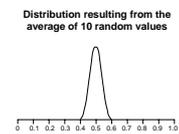
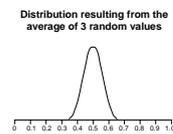
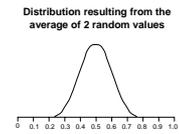
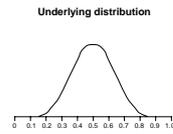
Uniform Distributions



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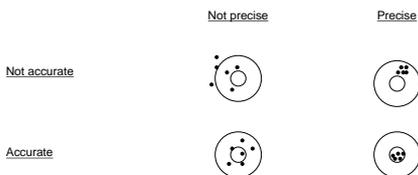
Normal Distribution



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Precision



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Shewhart Control Chart

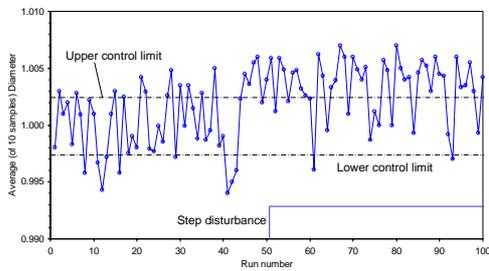
- Upper Control Limit (UCL), Lower Control Limit (LCL)
- Subgroup size ($5 < n < 20$)

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Shewhart Control Chart (cont'd)

Control chart based on 100 samples

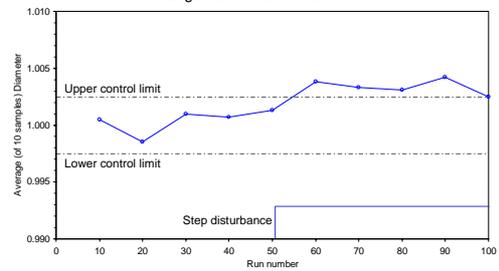


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Shewhart Control Chart (cont'd)

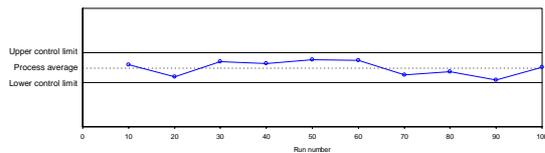
Control chart based on average of 10 samples, note the step change that occurs at run 51



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Control Charts



- Collection:**
 - Gather data and plot on chart.
- Control:**
 - Calculate control limits from process data, using simple formulae.
 - Identify special causes of variation; take local actions to correct.
- Capability:**
 - Quantify common cause variation; take action on the system.

These three phases are repeated for continuing process improvement.

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Setting the Limits

Idea: Points outside the limits will signal that something is wrong—an assignable cause. We want limits set so that assignable causes are highlighted, but few random causes are highlighted accidentally.

Convention for Control Charts:

- Upper control limit (UCL) = $\bar{x} + 3\sigma_{sg}$
 - Lower control limit (LCL) = $\bar{x} - 3\sigma_{sg}$
- (Where σ_{sg} represents the standard deviation of a subgroup of samples)

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Setting the Limits (cont'd)

Convention for Control Charts (cont'd):

$$\sigma_{\text{sub group}} = \sigma_{sg} \neq \sigma_{\text{process}}$$

$$\sigma_{\text{subgroup}} = \sigma_{\text{process}} / \sqrt{n}$$

$$UCL = \bar{x} + 3\sigma_{\text{process}} / \sqrt{n}$$

$$LCL = \bar{x} - 3\sigma_{\text{process}} / \sqrt{n}$$

As n increases, the UCL and LCL move closer to the center line, making the control chart more sensitive to shifts in the mean.

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Benefits of Control Charts

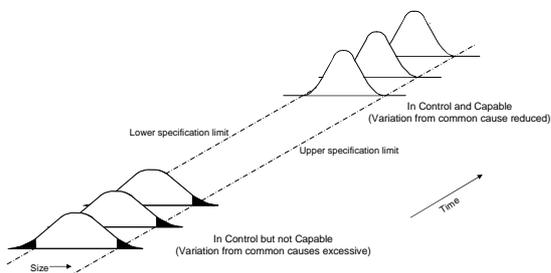
Properly used, control charts can:

- Be used by operators for ongoing control of a process
- Help the process perform consistently, predictably, for quality and cost
- Allow the process to achieve:
 - Higher quality
 - Lower unit cost
 - Higher effective capacity
- Provide a common language for discussing process performance
- Distinguish special from common causes of variation; as a guide to local or management action

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Process Capability



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Process Capability Index

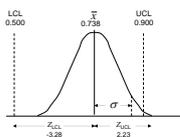
1. $C_p = \text{Range}/6\sigma$
2. C_{pk}

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Process Capability

- Take an example with:
Mean = .738
Standard deviation, $\sigma = .0725$
UCL = 0.900
LCL = 0.500



- Normalizing the specifications:

$$Z_{UCL} = \frac{UCL - \bar{x}}{\sigma} = \frac{0.900 - 0.738}{0.0725} = 2.23$$

$$Z_{LCL} = \frac{LCL - \bar{x}}{\sigma} = \frac{0.500 - 0.738}{0.0725} = -3.28$$

$$Z_{MIN} = 2.23 \text{ (on an absolute basis)}$$

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Process Capability (cont'd)

- Using the tables of areas under the Normal Curve, the proportions out of specification would be:

$$P_{UCL} = 0.0129$$

$$P_{LCL} = 0.0005$$

$$P_{total} = 0.0134$$

- The Capability Index would be:

$$C_{PK} = Z_{min}/3 = 2.23 / 3 = 0.74$$

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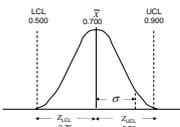
Process Capability (cont'd)

- If this process could be adjusted toward the center of the specification, the proportion of parts falling beyond either or both specification limits might be reduced, even with no change in Standard deviation.
- For example, if we confirmed with control charts a new mean = 0.700, then:

$$Z_{UCL} = \frac{UCL - \bar{x}_{new}}{\sigma} = \frac{0.900 - 0.700}{0.0725} = 2.76$$

$$Z_{LCL} = \frac{LCL - \bar{x}_{new}}{\sigma} = \frac{0.500 - 0.700}{0.0725} = -2.76$$

$$Z_{min} = 2.76$$



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Process Capability (cont'd)

- The proportions out of specification would be:

$$P_{UCL} = 0.0029$$

$$P_{LCL} = 0.0029$$

$$P_{total} = 0.0058$$

- The Capability Index would be:

$$C_{PK} = Z_{min}/3 = 2.76 / 3 = 0.92$$

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Improving Process Capability

- To improve the chronic performance of the process, concentrate on the common causes that affect all periods. These will usually require management action on the system to correct.
- Chart and analyze the revised process:
 - Confirm the effectiveness of the system by continued monitoring of the Control Chart