

# 2.008 Design & Manufacturing II

Spring 2004

## Metal Cutting II

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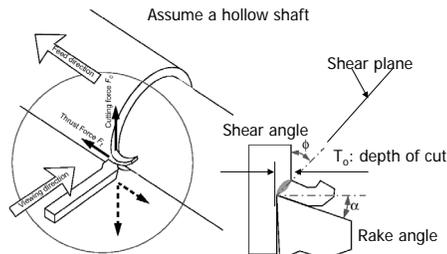
## Cutting processes

- Objectives
  - Product quality: surface, tolerance
  - Productivity: MRR↑, Tool wear↓
- Physics of cutting
  - Mechanics
  - Force, power
- Tool materials
- Design for manufacturing

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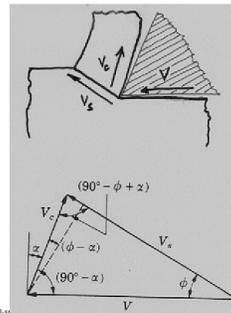
## Orthogonal cutting in a lathe



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## Velocity diagram in cutting zone



$$\frac{V}{\cos(\phi - \alpha)} = \frac{V_s}{\cos(\alpha)} = \frac{V_c}{\sin(\phi)}$$

$$\frac{V_c}{V} = \frac{t_o}{t_c} = r = \frac{\sin(\phi)}{\cos(\phi - \alpha)}$$

$$V_c = \frac{V \sin(\phi)}{\cos(\phi - \alpha)}$$

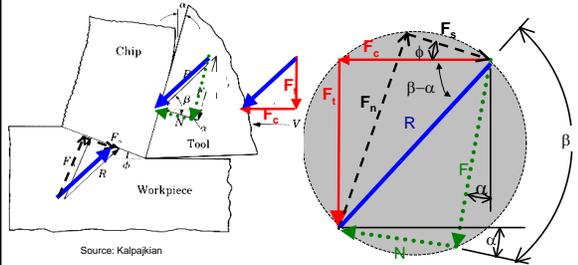
$$\frac{V_c}{V} = \frac{t_o}{t_c} = r = \frac{\sin(\phi)}{\cos(\phi - \alpha)}$$

Cutting ratio:  $r < 1$

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## E. Merchant's cutting diagram



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## FBD of Forces

$$\beta = \text{Friction Angle} \quad F = R \cdot \sin(\beta) \quad F_t = R \cdot \sin(\beta - \alpha)$$

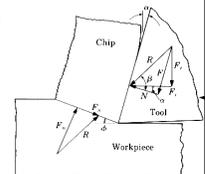
$$\mu = \tan(\beta) \quad N = R \cdot \cos(\beta) \quad F_c = R \cdot \cos(\beta - \alpha)$$

$$F_s = F_c \cdot \cos(\phi) - F_t \cdot \sin(\phi) = R \cos(\phi + \beta - \alpha)$$

$$F_n = F_c \cdot \sin(\phi) + F_t \cdot \cos(\phi)$$

$$\mu = \frac{F}{N} = \frac{F_t + F_c \cdot \tan(\alpha)}{F_c - F_t \cdot \tan(\alpha)}$$

Typically:  $0.5 < \mu < 2$



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## Analysis of shear strain

$\gamma = \frac{bc+cd}{ac} = \cot\phi + \tan(\phi-\alpha)$

- What does this mean:
  - Low shear angle = large shear strain
  - **Merchant's** assumption: Shear angle adjusts to minimize cutting force or max. shear stress
  - Can derive:
 
$$\phi = 45^\circ + \frac{\alpha}{2} - \frac{\beta}{2}$$

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## Shear Angle

$\phi = 45^\circ + \frac{\alpha}{2} - \frac{\beta}{2}$

Maximize shear stress  $\tau = \frac{F_s}{A_s} = \frac{F_s}{\frac{A}{\sin\phi}}$   
 $\frac{d\tau}{d\phi} = 0$

Minimize  $F_c$   
 $F_s = A_s \cdot \sigma_s$   
 $F_s = F_c \cdot \cos(\phi) - F_t \cdot \sin(\phi) = R \cos(\phi + \beta - \alpha)$   
 $F_c = R \cdot \cos(\beta - \alpha) \quad \frac{dF_c}{d\phi} = 0$

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## Power

Power input:  $F_c \cdot V \Rightarrow$  shearing + friction  
 MRR (Material Removal Rate) =  $w \cdot t_o \cdot V$

Power for shearing:  $F_s \cdot V_s$   
 Specific energy for shearing:  $u_s = \frac{F_s \cdot V_s}{w \cdot t_o \cdot V}$

Power dissipated via friction:  $F \cdot V_c$   
 Specific energy for friction:  $u_f = \frac{F \cdot V_c}{w \cdot t_o \cdot V}$  ← MRR

Total specific energy:  $u_s + u_f = \frac{F \cdot V_c}{w \cdot t_o \cdot V} + \frac{F_s \cdot V_s}{w \cdot t_o \cdot V}$   
 Experimental data

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## Cutting zone pictures

continuous    secondary shear    BUE  
 serrated    discontinuous

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## Chip breaker

Continuous chip: bad for automation

- Stop and go  
 - milling

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## Cutting zone distribution

Hardness    Temperature

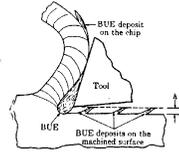
Mean temperature:  $CV^a b^b$   
 HSS:  $a=0.5, b=0.375$

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## Built up edge

- What is it?
- Why can it be a good thing?
- Why is it a bad thing?
  - Thin BUE
- How to avoid it...

- Increasing cutting speed
- Decreasing feed rate
- Increasing rake angle
- Reducing friction (by applying cutting fluid)

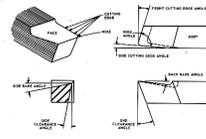


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## Tools

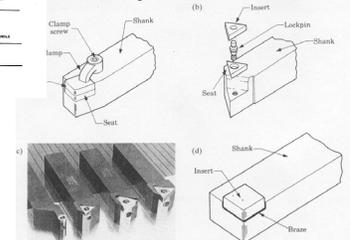
HSS (1-2 hours)



Inserts



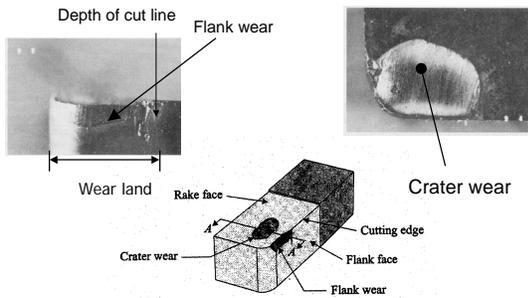
- High T
- High  $\sigma$
- Friction
- Sliding on cut surface



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## Tool wear up close



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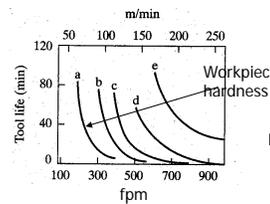
Source: Kalpakjian

## Taylor's tool wear relationship (flank wear)

F. W. Taylor, 1907

$$V \cdot T^n = C$$

T = time to failure (min)  
V = cutting velocity ( fpm )



$$V \cdot T^n \cdot d^x \cdot f^y = C$$

d = depth of cut

f = feed rate

$$\text{Ex. } T = C^7 \cdot V^{-7} \cdot d^{-1} \cdot f^{-4}$$

Optimum for max MRR?

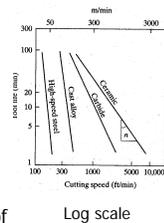
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Source: Kalpakjian

## Taylor's tool life curves (Experimental)

- Coefficient  $n$  varies from:
 

<u>Steels</u>	<u>Ceramics</u>
0.1	0.7
- As  $n$  increases, cutting speed can be increased with less wear.
- Given that,  $n=0.5$ ,  $C=400$ , if the  $V$  reduced 50%, calculate the increase of tool life?



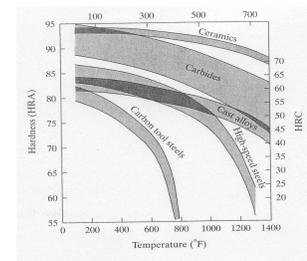
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Kalpakjian

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## What are good tool materials?

- Hardness
  - wear
  - temperature
- Toughness
  - fracture

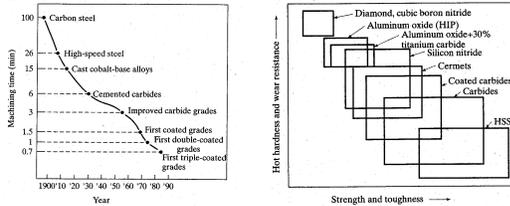


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Source: Kalpakjian

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## History of tool materials



Trade off: Hardness vs Toughness  
wear vs chipping

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Sandvik Coromant, Kalpakjian

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## HSS

- High-speed steel, early 1900
- Good wear resistance, fracture resistance, not so expensive
- Suitable for low K machines with vibration and chatter, why?
- M-series (Molybdenum)
  - Mb (about 10%), Cr, Vd, W, Co
  - Less expensive than T-series
  - Higher abrasion resistance
- T-series (Tungsten 12-18%)
- Most common tool material but not good hot hardness

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## Carbides

- Hot hardness, high modulus, thermal stability
- Inserts
- Tungsten Carbide (WC)
  - (WC + Co) particles (1-5  $\mu$ ) sintered
  - WC for strength, hardness, wear resistance
  - Co for toughness
- Titanium Carbide (TiC)
  - Higher wear resistance, less toughness
  - For hard materials
- Uncoated or coated for high-speed machining
  - TiN, TiC, TiCN, Al<sub>2</sub>O<sub>3</sub>
  - Diamond like coating
  - CrC, ZrN, HfN

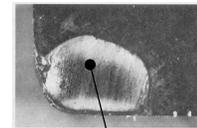


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## Crater wear

- Diffusion is dominant for crater wear
- A strong function of temperature
- Chemical affinity between tool and workpiece
- Coating?



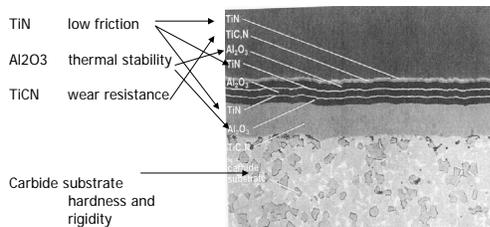
Crater wear

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## Multi-phase coating

Custom designed coating for heavy duty, high speed, interrupted, etc.



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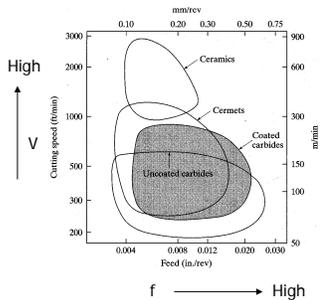
## Ceramics and CBN

- Aluminum oxide, hardness, high abrasion resistance, hot hardness, low BUE
- Lacking toughness (add ZrO<sub>2</sub>, TiC), thermal shock
- Cold pressed and hot sintered
- Cermets (ceramic + metal)
  - Al<sub>2</sub>O<sub>3</sub> 70%, TiC 30%, brittleness, \$\$\$
- Cubic Boron Nitride (CBN)
  - 2<sup>nd</sup> hardest material
  - brittle
- Polycrystalline Diamond

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## Range of applications

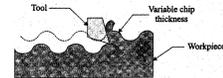


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## Chatter

- Severe vibration between tool and the workpiece, noisy.
- In general, self-excited vibration (regenerative)
- Acoustic detection or force measurements
- Cutting parameter control, active control



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## Turning parameters

- $MRR = \pi D_{avg} N \cdot d \cdot f$ 
  - $N$ : rotational speed (rpm),  $f$ : feed (in/rev),  $d$ : depth of cut (in)
  - $l$ : length of cut (in)
- Cutting time,  $t = l / fN$
- Torque =  $F_c (D_{avg}/2)$
- Power = Torque  $\cdot \omega$
- 1 hp = 396000 in.lbf/min = 550 ft.lbf/sec

### Example

- 6 inch long and 0.5 in diameter stainless steel is turned to 0.48 in diameter.  $N=400$  rpm, tool in traveling 8 in/min, specific energy = 4 w.s/mm<sup>2</sup> = 1.47 hp.min/in<sup>3</sup>
- Find cutting speed, MRR, cutting time, power, cutting force.

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## Sol.

- $D_{avg} = (0.5 + 0.48)/2 = 0.49$  in
- $V = \pi \cdot 0.49 \cdot 400 = 615$  in/min
- $d = (0.5 - 0.48)/2 = 0.01$  in
- $F = 8/400 = 0.02$  in/rev
- $MRR = V \cdot f \cdot d = 0.123$  in<sup>3</sup>/min
- Time to cut =  $6/8 = 0.75$  min

$$P = 1.47 \times 0.123 = 0.181 \text{ hp} = \text{Torque} \times \omega$$

$$1 \text{ hp} = 396000 \text{ in-lb/min}$$

$$T = P/\omega = F_c \cdot (D_{avg}/2)$$

$$\text{Then, } F_c = 118 \text{ lbs}$$

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## Drilling parameters

- MRR:  $MRR = \left( \frac{\pi D^2}{4} \right) f \cdot N$
- Power: specific energy  $\times$  MRR
- Torque: Power/ $\omega$
- A hole in a block of magnesium alloy, 10 mm drill bit, feed 0.2 mm/rev,  $N=800$  rpm
- Specific power 0.5 W.s/mm<sup>2</sup>
- MRR
- Torque

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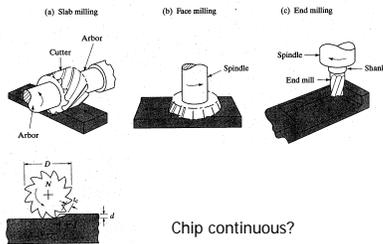
## Sol

- $MRR = \pi (10 \times 10 / 4) \cdot 0.2 \cdot 800 = 210$  mm<sup>3</sup>/s
- Power = 0.5 W.s/mm<sup>2</sup>  $\cdot$  210 mm<sup>3</sup>/s
  - = 105 W = 105 N.m/s
  - =  $T \cdot \omega$
  - =  $T \cdot 2\pi \cdot 800/60$
  - = 1.25 N.m

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## Milling



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## Milling parameters ( ' ' ' )

- Parameters:
  - Cutting speed,  $V = \pi DN$
  - $t_c$ ; chip depth of cut
  - $d$ ; depth of cut
  - $f$ ; feed per tooth
  - $v$ ; linear speed of the workpiece
  - $n$ ; number of teeth
  - $t$ ; cutting time,
  - $w$ ; width of cut
- Torque: Power/ $\omega$
- Power: sp. Energy x MRR

$$t_c = \frac{2fd}{D} \leftarrow \text{approximation}$$

$$f = \frac{v}{Nn}$$

$$t = \frac{l + l_c}{v}$$

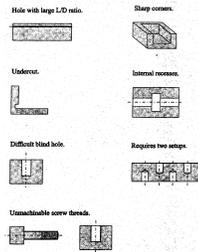
$$\text{MRR} = \frac{hwd}{t} = wdv$$

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## DFM for machining

- Geometric compatibility
- Dimensional compatibility
  - Availability of tools
  - Drill dimensions, aspect ratio
- Constraints
  - Process physics
  - Deep pocket
  - Machining on inclined faces
- Set up and fixturing
  - Tolerancing is \$\$\$
  - Minimize setups



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