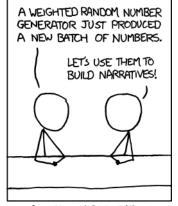
Welcome to 18.05 Jeremy Orloff and Jonathan Bloom Introduction to Probability and Statistics Spring 2014



ALL SPORTS COMMENTARY

Courtesy of xkcd. CC-BY-NC. http://xkcd.com/904/

MITx/18.05x

You should have received this information in an email. If you did not see us after class.

- We'll use the MITx platform:
- If you registered you should be able to see the class.
- We're working on giving pre-registered students access.
- Site will have all reading materials and problem sets
- Copies of the slides with solutions to all problems discussed in class will be posted after each class

Active Learning

Read the 'Calendar and Information' section on our MITx site.

Before class

- Reading and reading questions.
- Reading questions count toward grade.
- Lecture will assume you've done the reading.

In class:

- Combination of lecture and problem solving
- We won't assume you've completely mastered the reading.
 - Will assume a level of familiarity.
 - ▶ Use the discussion boards on the MITx/18.05x site.
 - Bring questions to class.

Class

Read the 'Calendar and Information' section on our MITx/18.05x site.

Class Time

- TR: Lecture/clicker questions/board questions
 Participation on clicker questions counts towards your grade
 No computer use in class on TR.
- F: Studio bring your laptop

In-class Groups

- Groups of 3.
- You will be able to choose your own group.
- If you need to find a group or your group needs a third person let us know and we'll help.

R: for computation, simulation and visualization

- will teach you everything you need
- no hardcore programming.

Problem Sets

- Usually due on Mondays
- Turn in by 4:30 PM
- You'll be able to check your numerical answers to problems on the MITx/18.05x site before the due date.
- Problem sets will be graded on your explanation of your answer.

Clickers and R

Clickers

- Buy a TurningTechnology clicker at MIT coop.
- \bullet Follow the instructions for registering it to this class in the 'Calendar and Information' section of MITx/18.05x

R

- Free open source package.
- Very easy to use and install.
- Instructions and a link for this are on MITx/18.05x.

Calendar, Information, Policies and Goals

Everything we just went over and more is in the Calendar and Information section of MIT x/18.05x

For Next Time

- Familiarize yourself with the MITx/18.05x site
- Get and register clicker
- Install R and R Studio

- Read class 1 notes (summary of what we'll do today)
- Go through the class 2 sequence and answer the reading questions

Probability vs. Statistics

Different subjects: both about random processes

Probability

- Logically self-contained
- A few rules for computing probabilities
- One correct answer

Statistics

- Messier and more of an art
- Get experimental data and try to draw probabilistic conclusions
- No single correct answer

Counting: Motivating Examples

What is the probability of getting exactly 1 heads in 3 tosses of a fair coin?

Poker Hands

Deck of 52 cards

- 13 ranks: 2, 3, ..., 9, 10, J, Q, K, A
- 4 suits: $\heartsuit, \spadesuit, \diamondsuit, \clubsuit$,

Poker hands

- Consists of 5 cards
- A one-pair hand consists of two cards having one rank and the remaining three cards having three other rank
- Example: $\{2\heartsuit, 2\spadesuit, 5\heartsuit, 8\clubsuit, K\diamondsuit\}$

The probability of a one-pair hand is:

- 1) less than 5%
- 2) between 5% and 10%
- 3) between 10% and 20%
- 4) between 20% and 40%
- 5) greater than 40%

Sets in Words

Old New England rule: don't eat clams (or any shellfish) in months without an 'r' in their name.

- S = all months
- L = the month has 31 days
- R = the month has an 'r' in its name

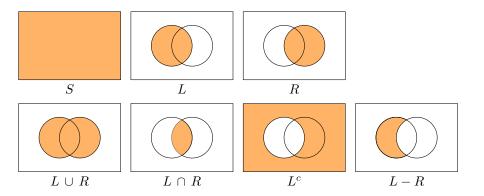
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S = {\text{Jan, Feb, Mar, Apr, May, Jun, Jul, Aug, Sep, Oct, Nov, Dec}}
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$$L = \{ Jan, Mar, May, Jul, Aug, Oct, Dec \}$$

$$R = \{ Jan, Feb, Mar, Apr, Sep, Oct, Nov, Dec \}$$

 $L \cap R = \{\text{Jan, Mar, Oct, Dec}\} = \text{months with 31 days and an 'r'}$

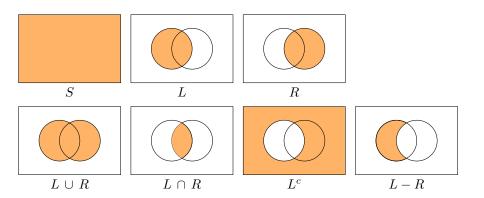
Visualize Set Operations with Venn Diagrams



Product of Sets

$$S \times T = \{(s,t)\}$$

Inclusion-Exclusion Principle



Board Question

A band consists of singers and guitar players.

- 7 people sing
- 4 play guitar
- 2 do both

How many people are in the band?

Rule of Product

3 shirts, 4 pants = 12 outfits

(More powerful than it seems.)

Concept Question: DNA

DNA is made of sequences of nucleotides: A, C, G, T.

How many DNA sequences of length 3 are there?

(i) 12 (ii) 24 (iii) 64 (iv) 81

Concept Question: DNA

DNA is made of sequences of nucleotides: A, C, G, T.

How many DNA sequences of length 3 are there?

(i) 12 (ii) 24 (iii) 64 (iv) 81

How many DNA sequences of length 3 are there with no repeats?

(i) 12 (ii) 24 (iii) 64 (iv) 81

Board Question 1

There are 5 Competitors in 100m final.

How many ways can gold silver and bronze be awarded?

Photograph of Usain Bolt running a race removed due to copyright restrictions.

Board Question 2

I won't wear green and red together; I think black or denim goes with anything; I won't wear crimson period. Here is my wardrobe.

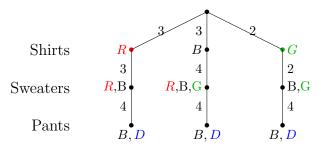
Shirts: 3B, 3R, 2G; sweaters 1B, 2R, 1G; pants 2D,2B.



How many different outfits can I wear?

Solution

<u>answer:</u> Suppose we choose shirts first. Depending on whether we choose red compatible or green compatible shirts there are different numbers of sweaters we can choose next. So we split the problem up before using the rule of product. A multiplication tree is the easiest way to present the answer.



Multiplying down the paths of the tree:

Number of outfits =
$$(3 \times 3 \times 4) + (3 \times 4 \times 4) + (2 \times 2 \times 4) = 100$$

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Permutations

Lining things up. How many ways can you do it?

'abc' and 'cab' are different permutations of {a, b, c}

Permutations of k from a set of n

Give all permutations of 3 things out of $\{a, b, c, d\}$

Permutations of k from a set of n

Give all permutations of 3 things out of $\{a, b, c, d\}$

abc abd acb acd adb adc bac bad bca bcd bda bdc cab cad cba cbd cda cdb dab dac dba dbc dca dcb

Would you want to do this for 7 from a set of 10?

Combinations

Choosing subsets – order doesn't matter.

How many ways can you do it?

Combinations of k from a set of n

Give all combinations of 3 things out of $\{a, b, c, d\}$

Answer: $\{a,b,c\}, \{a,b,d\}, \{a,c,d\}, \{b,c,d\}$

Permutations and Combinations

abc acb bac bca cab cba
$$\{a,b,c\}$$

abd adb bad bda dab dba $\{a,b,d\}$
acd adc cad cda dac dca $\{a,c,d\}$
bcd bdc cbd cdb dbc dcb $\{b,c,d\}$
Permutations: Combinations: ${}_{4}P_{3}$ ${}_{3}^{4} = {}_{4}C_{3}$

$$\binom{4}{3} =_4 C_3 = \frac{{}_4P_3}{3!}$$

Board Question

- a) Count the number of ways to get exactly 3 heads in 10 flips of a coin.
- b) For a fair coin, what is the probability of exactly 3 heads in 10 flips?

MIT OpenCourseWare http://ocw.mit.edu

18.05 Introduction to Probability and Statistics

Spring 2014

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