

## Part I Problems and Solutions

**Problem 1:** Find  $\mathcal{L}(t^4 e^{\pi t})$

**Solution:**

$$\mathcal{L}(t^4) = \frac{24}{s^5} \rightarrow \mathcal{L}(t^4 e^{\pi t}) = \frac{24}{(s - \pi)^5}$$

**Problem 2:** Find  $\mathcal{L}^{-1}\left(\frac{3}{2s-4}\right)$

**Solution:**

$$\frac{3}{2s-4} = \frac{3}{2} \frac{1}{s-2} \xrightarrow{\mathcal{L}^{-1}} \frac{3}{2} e^{2t}$$

**Problem 3:** Find  $\mathcal{L}^{-1}\left(\frac{1}{s^2+4s+4}\right)$

**Solution:**

$$\frac{1}{s^2 + 4s + 4} = \frac{1}{(s + 2)^2} \xrightarrow{\mathcal{L}^{-1}} te^{-2t}$$

(since  $\mathcal{L}^{-1}\left(\frac{1}{s^2}\right) = t$ )

**Problem 4:** Find  $\mathcal{L}^{-1}\left(\frac{s+2}{s^2+4s+5}\right)$

**Solution:**

$$\frac{s+2}{s^2 + 4s + 5} = \frac{s+2}{(s+2)^2 + 1} \xrightarrow{\mathcal{L}^{-1}} e^{-2t} \cos t$$

(since  $\mathcal{L}^{-1}\left(\frac{s}{s^2+1}\right) = \cos t$ )

**Problem 5:** Find  $\mathcal{L}^{-1}\left(\frac{5s-6}{s^2-3s}\right)$

**Solution:**

$$\frac{5s-6}{s^2 - 3s} = \frac{2}{s} + \frac{3}{s-3} \xrightarrow{\mathcal{L}^{-1}} 2 + 3e^{3t}$$

**Problem 6:** Find  $\mathcal{L}^{-1}\left(\frac{5-2s}{s^2+7s+10}\right)$

**Solution:**

$$\frac{5-2s}{s^2 + 7s + 10} = \frac{5-2s}{(s+2)(s+5)} = \frac{3}{s+2} - \frac{5}{s+2} \xrightarrow{\mathcal{L}^{-1}} 3e^{-2t} - 5e^{-5t}$$

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18.03SC Differential Equations

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