

## Part I Problems

**Problem 1:** For each spring-mass system, find whether pure resonance occurs, without actually calculating the solution.

a)  $2x'' + 10x = F(t)$ ;  $F(t) = 1$  on  $(0,1)$ ,  $F(t)$  is odd, and of period 2;

b)  $x'' + 4\pi^2x = F(t)$ ;  $F(t) = 2t$  on  $(0,1)$ ,  $F(t)$  is odd, and of period 2;

c)  $x'' + 9x = F(t)$ ;  $F(t) = 1$  on  $(0, \pi)$ ,  $F(t)$  is odd, and of period  $2\pi$

**Problem 2:** Find a periodic solution as a Fourier series to  $x'' + 3x = F(t)$ , where  $F(t) = 2t$  on  $(0, \pi)$ ,  $F(t)$  is odd, and has period  $2\pi$ .

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