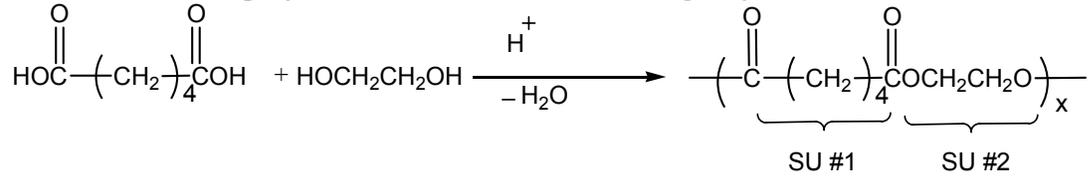


3.034 Practice Set A Solutions

We know that the polymer was made in the following way:

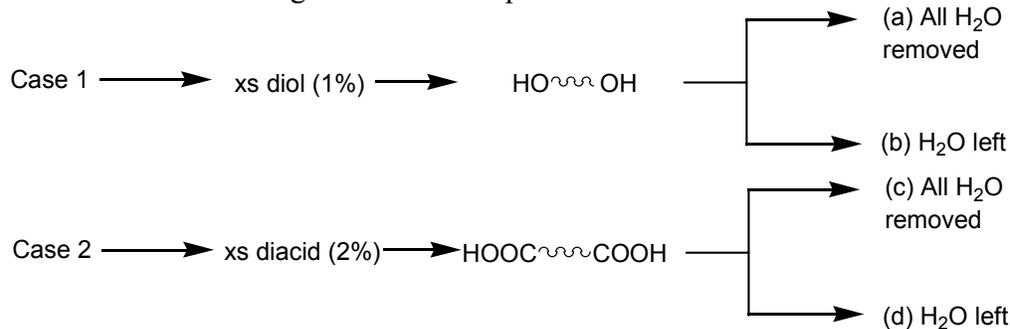


$$\bar{M}_n \approx 8300 \text{ g/mol}$$

$$\text{We know that } \bar{M}_n = \bar{D}_{\text{pn}} \cdot M_o, M_o = (M_{\text{SU\#1}} + M_{\text{SU\#2}})/2 = 86 \text{ g/mol}$$

Note M_o is not the repeat unit molecular weight and M_o is based on the molecular weight of the structural units not the original monomers.

We are asked to distinguish between 4 possibilities.



Let us first consider Case 1.

(a) 1% xs diol, all H₂O removed

$$\bar{D}_{\text{pn}} = (1+r)/(1+r-2pr) \quad \text{where } r = [\text{COOH}]_o/[\text{OH}]_o, \text{ remember } r \text{ is always less than one, and } p \text{ is the extent of rxn of COOH groups and varies from } 0 \rightarrow 1.$$

$$\text{If no H}_2\text{O, } p \rightarrow 1 \text{ and } \bar{D}_{\text{pn}} \text{ max} = (1+r)/(1-r)$$

Calculate r (on a 100 mol basis)

$$r = 100/101 \rightarrow r \approx 0.99 \quad (\text{watch significant figures!})$$

$$\text{Calculate } \bar{D}_{\text{pn}} = (1+r)/(1-r) = (1+0.99)/(1-0.99) = 199$$

$$\bar{M}_n = 86 \times \bar{D}_{\text{pn}} = 17,114 \text{ g/mol}$$

(b) 1% xs diol, [H₂O]/[OH]=0.05

Again $\bar{D}_{\text{pn}} = (1+r)/(1+r-2pr)$ where $r = [\text{COOH}]_o/[\text{OH}]_o$
 But here $p \neq 1 \rightarrow$ need to use equilibrium considerations to find p .

$$k_{eq} = 1.0 = \frac{[H_2O][-\text{COO}-]}{[OH][\text{COOH}]}$$

again p is the extent of rxn of COOH groups not OH groups

$$[-\text{COO}-] = p[\text{COOH}]_o$$

$$[\text{COOH}] = (1-p)[\text{COOH}]_o$$

$$[\text{OH}] = (1-p_B)[\text{OH}]_o = (1-pr)*[\text{COOH}]_o/r \quad p_B \rightarrow \text{the extent of rxn of OH groups, } p \neq p_B, \quad p_B = pr$$

Now we can go back to the k_{eq} expression.

$$k_{eq} = 1.0 = \frac{[H_2O][-\text{COO}-]}{[OH][\text{COOH}]} = \frac{P[\text{COOH}]_o x}{(1-P)[\text{COOH}]_o} \quad \text{where } x = \frac{[H_2O]}{[OH]}$$

$$\text{Solve for p: } p = 1/(1+x)$$

$$\text{When } x = 0.05, p = 0.95$$

$$\text{Calculate } \bar{D}_{pn} = (1+r)/(1+r-2pr) = 19 \quad \text{with } p=0.95 \text{ and } r=0.99$$

$$\bar{M}_n = 86 \times 19 = 1,640 \text{ g/mol}$$

Now let us consider Case 2

(c) 2% xs diacid, all H₂O removed

$$\bar{D}_{pn} = (1+r)/(1+r-2pr) \quad \text{again, } p \rightarrow 1 \text{ and } \bar{D}_{pn} = (1+r)/(1-r)$$

However, here $r = [\text{OH}]_o/[\text{COOH}]_o$, because the acid is in xs and $r \leq 1.0$!

We also need to redefine p,

p = the extent of rxn of OH groups and p varies from 0 → 1

$$\text{here } r = 100/102 \rightarrow r = 0.98$$

$$\text{Calculate } \bar{D}_{pn} = (1+r)/(1-r) = (1+0.98)/(1-0.98) = 99$$

$$\bar{M}_n = 86 \times 99 = 8,500 \text{ g/mol}$$

(d) 2% xs diacid, $[\text{H}_2\text{O}]/[\text{OH}]=0.05$

$$\text{Again } \bar{D}_{pn} = (1+r)/(1+r-2pr) \quad \text{where } r = [\text{OH}]_o/[\text{COOH}]_o$$

$p \neq 1 \rightarrow$ need to use equilibrium considerations to find p.

$$k_{eq} = 1.0 = \frac{[H_2O][-\text{COO}-]}{[OH][\text{COOH}]} \quad \text{remember: p is the extent of rxn of OH groups}$$

$$[-\text{COO}-] = p[\text{OH}]_o$$

$$[\text{OH}] = (1-p)[\text{OH}]_o$$

$$[\text{COOH}] = (1-p_B)[\text{COOH}]_o = (1-pr)*[\text{OH}]_o/r \quad p_B \rightarrow \text{the extent of rxn of COOH groups}$$

Substitute into the k_{eq} expression.

$$k_{eq} = 1.0 = \frac{p[OH]_o x}{(1 - pr)[OH]_o / r} \quad \text{where } x = \frac{[H_2O]}{[OH]}$$

Solve for p: $p = (1/r)/(1+x) \rightarrow p = 0.97$

Solve for $\bar{D}_{pn} = (1+r)/(1+r-2pr) \approx 26$

$$\bar{M}_n = 86 \times 26 = 2,260 \text{ g/mol}$$

The closest M_n is 2% diacid, all water removed.

Summary

	r=0.99, P=1	r=0.98, P=1	r=0.99, P=0.95	r=0.98, P=0.97
D_{pn}	199	99	19	26
M_n (g/mol)	17,144	8,500	1,640	2,260