

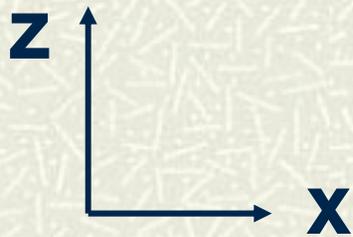
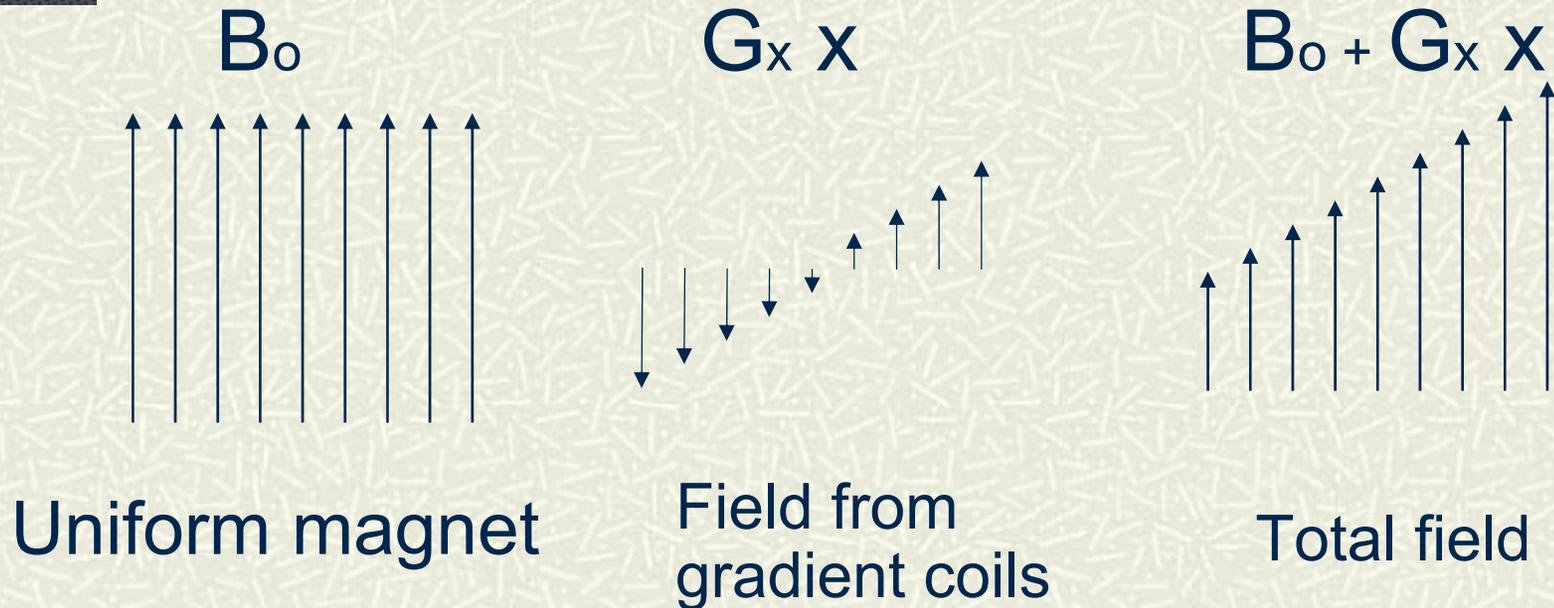
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HST.583 Functional Magnetic Resonance Imaging: Data Acquisition and Analysis  
Fall 2008

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- 1) MR image encoding for fMRI
- 2) BOLD Contrast

# Magnetic field gradient: the key to image encoding



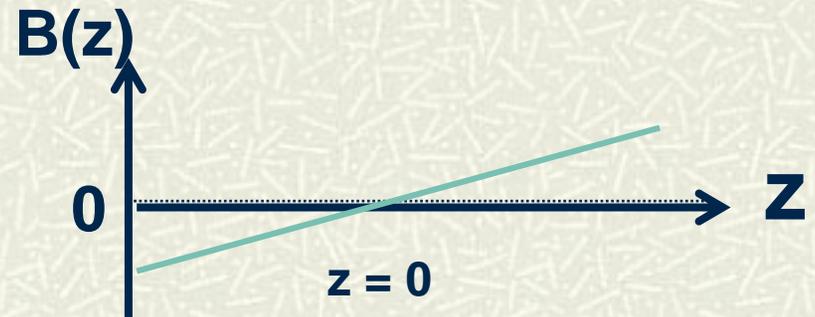
$$G_x = \partial B_z / \partial x$$

# Gradient field for MR encoding

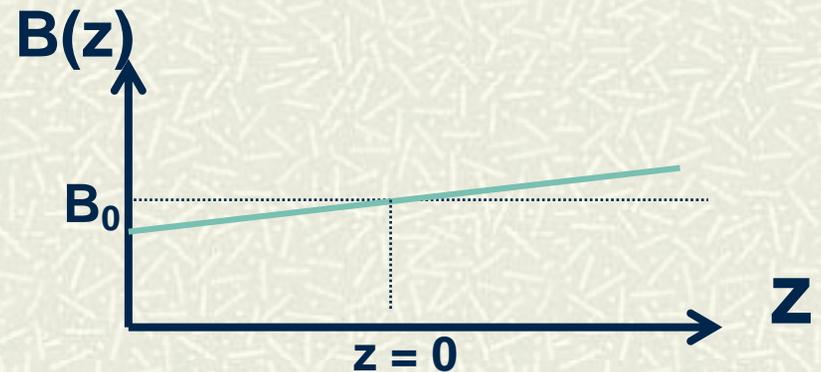
The magnet's field is homogeneous.



A gradient coil is a spool of wire designed to provide a linear “trim” field.



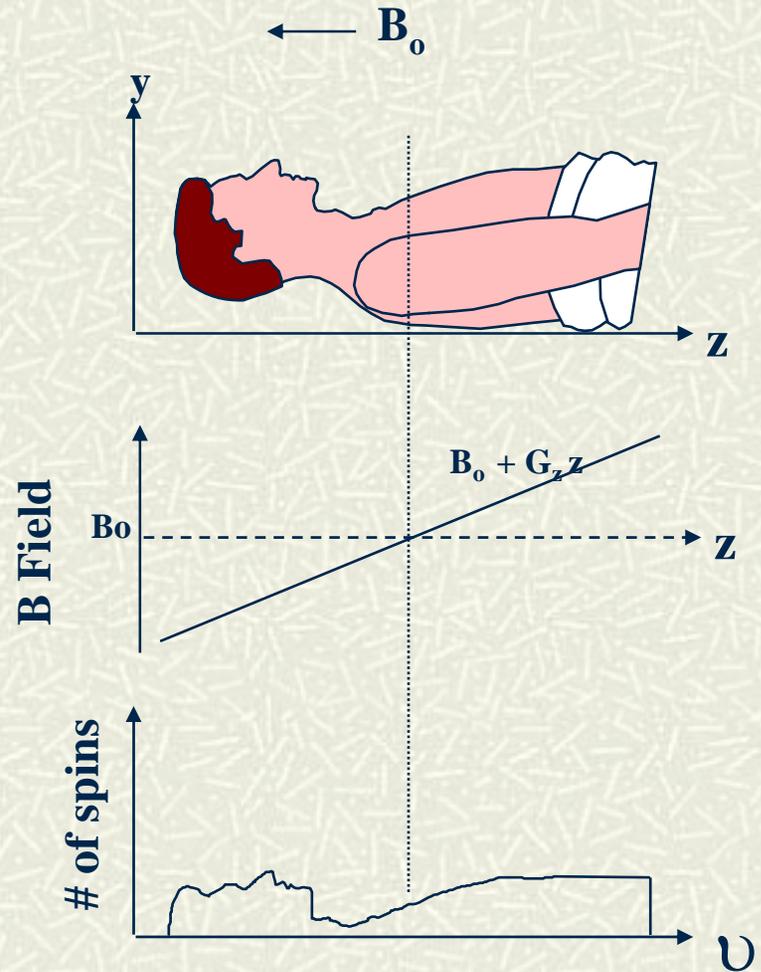
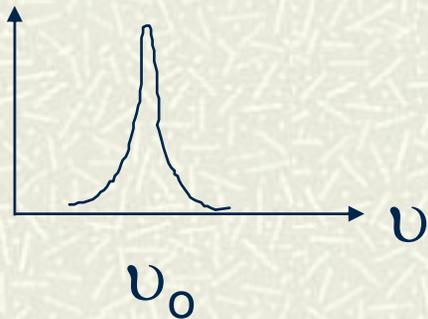
Gradient coil in magnet



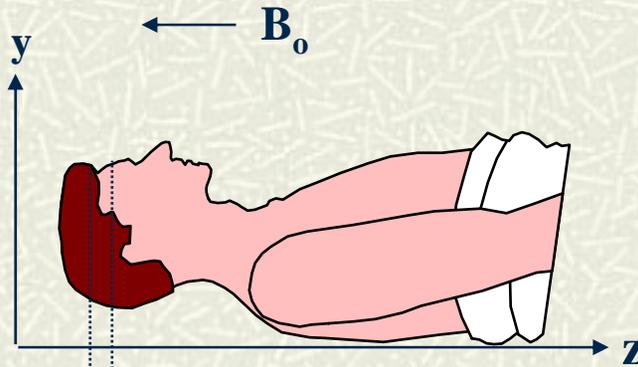
# A gradient causes a spread of frequencies

MR frequency of the protons in a given location is proportional to the local applied field.

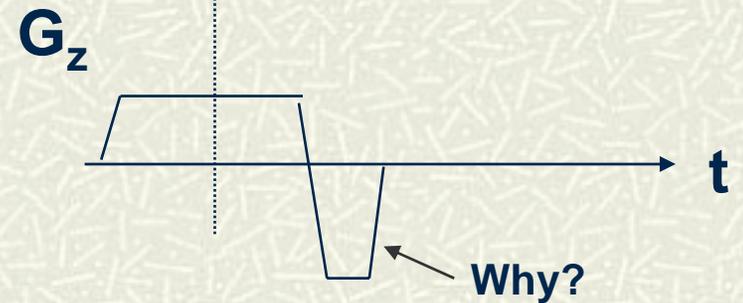
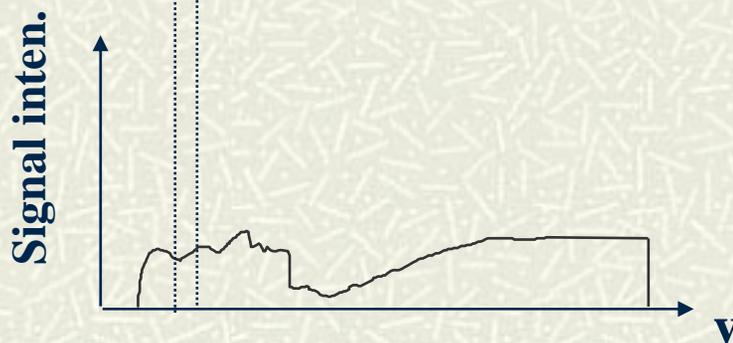
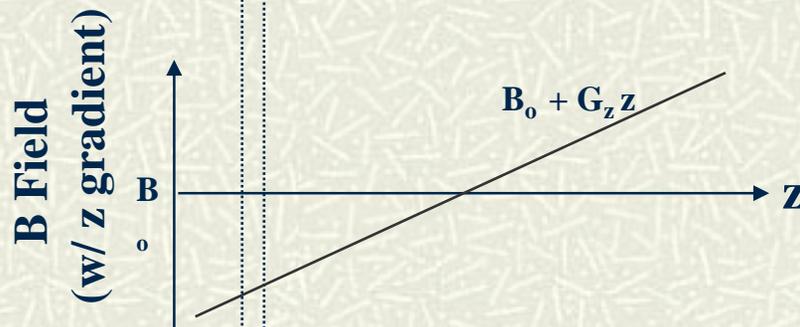
$$\nu = \gamma \mathbf{B}_{\text{TOT}} = \gamma (\mathbf{B}_0 + \mathbf{G}_z z)$$



# Step one: excite a slice



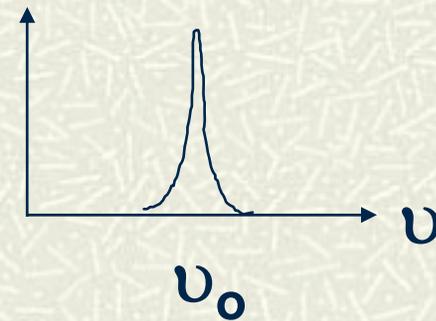
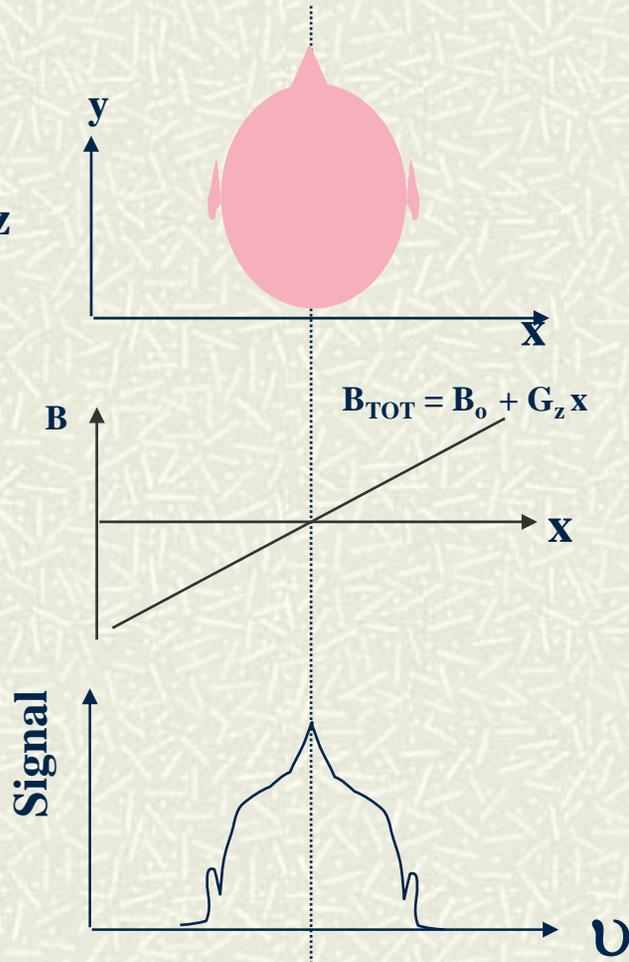
While the gradient is on, excite only band of frequencies.



# Step two: encode spatial info. in-plane

“Frequency encoding”

$B_0$  along z



with gradient

without gradient

# 'Pulse sequence' so far

RF



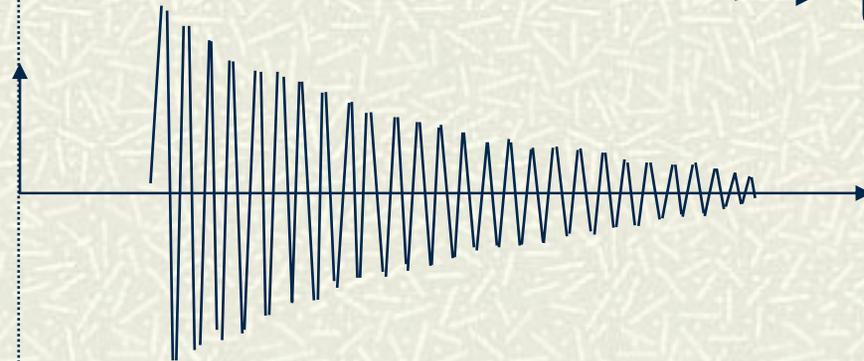
"slice select"



"freq. encode"  
(read-out)



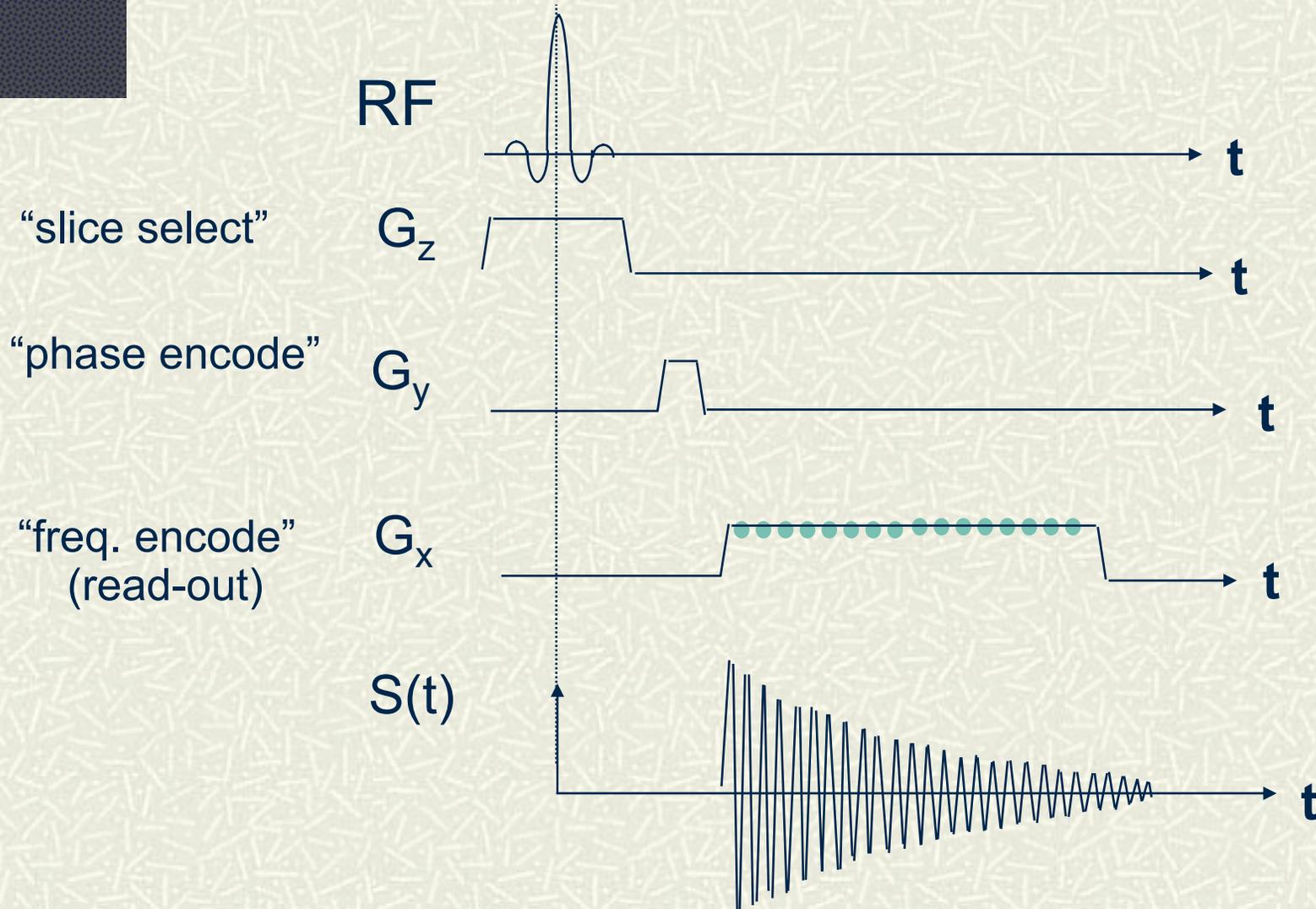
$S(t)$



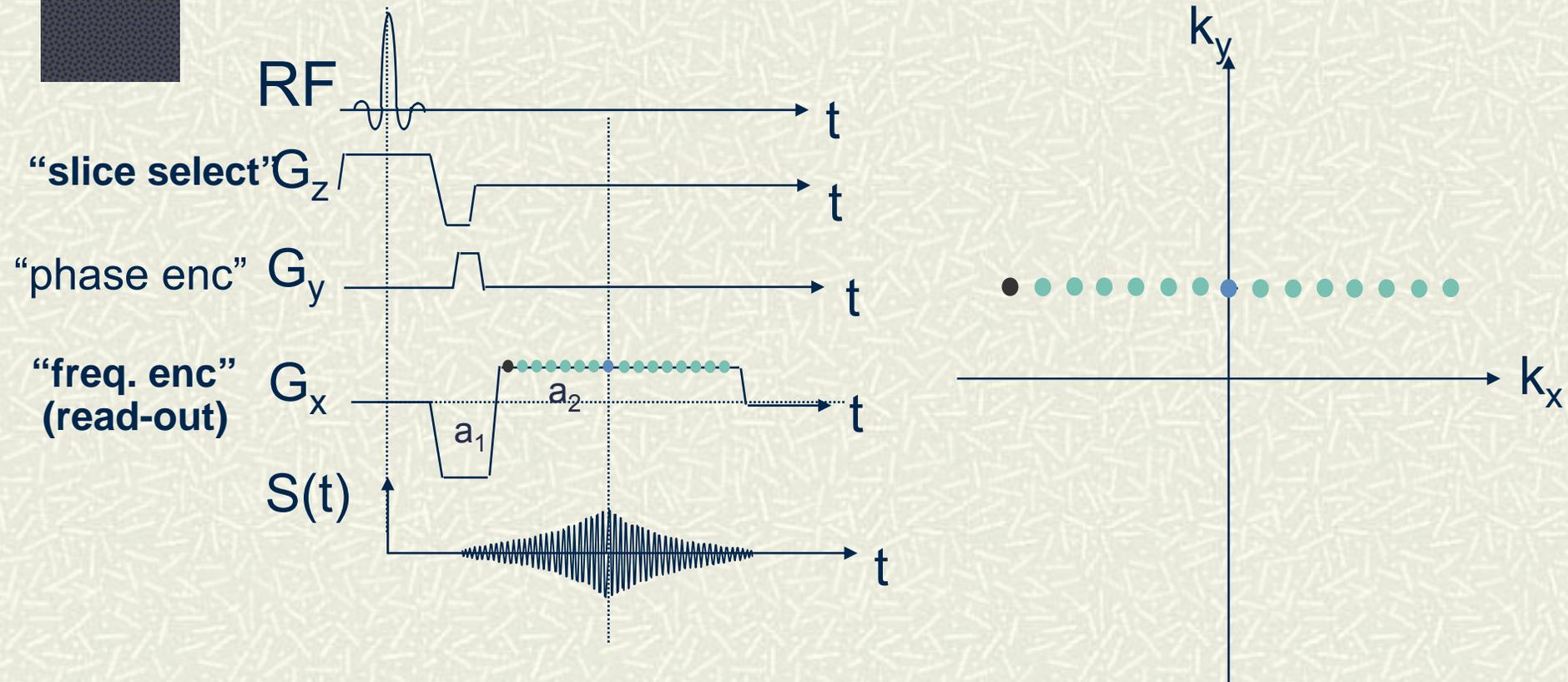
Sample points



# “Phase encoding”



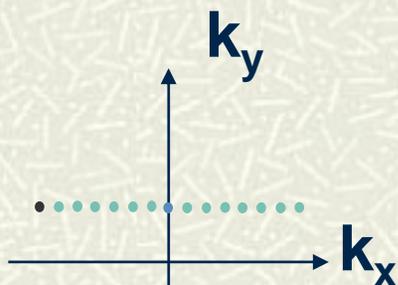
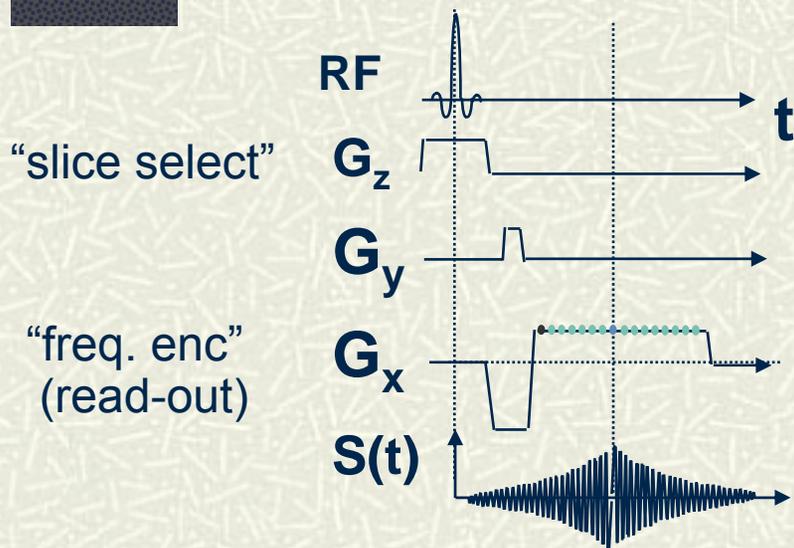
# “Spin-warp” encoding



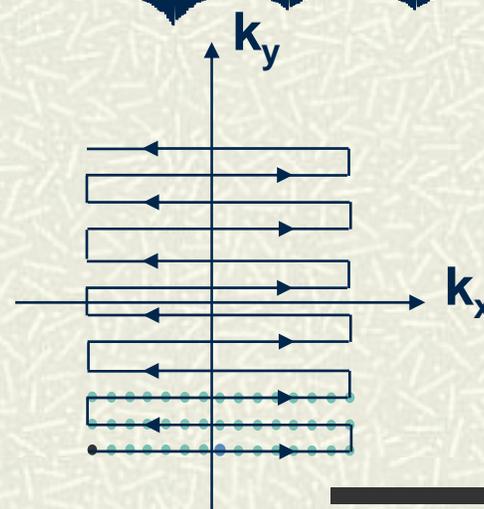
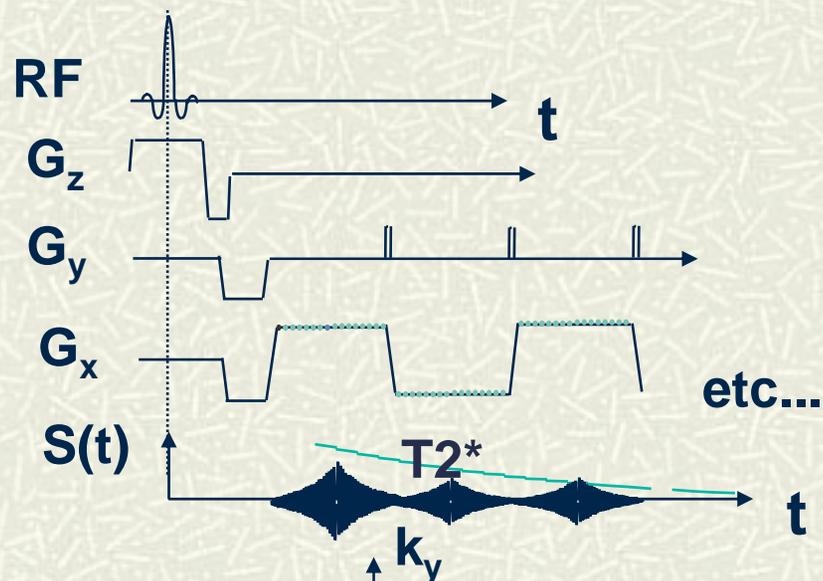
one excitation, one line of kspace...

# What's the difference?

## conventional MRI



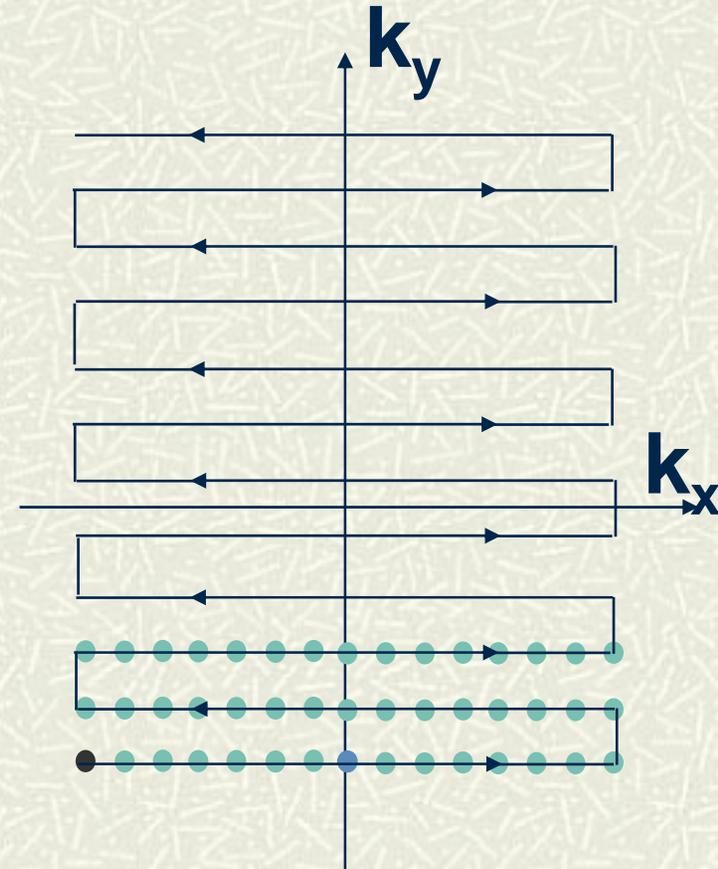
## “fast” imaging



# “Echo-planar” encoding

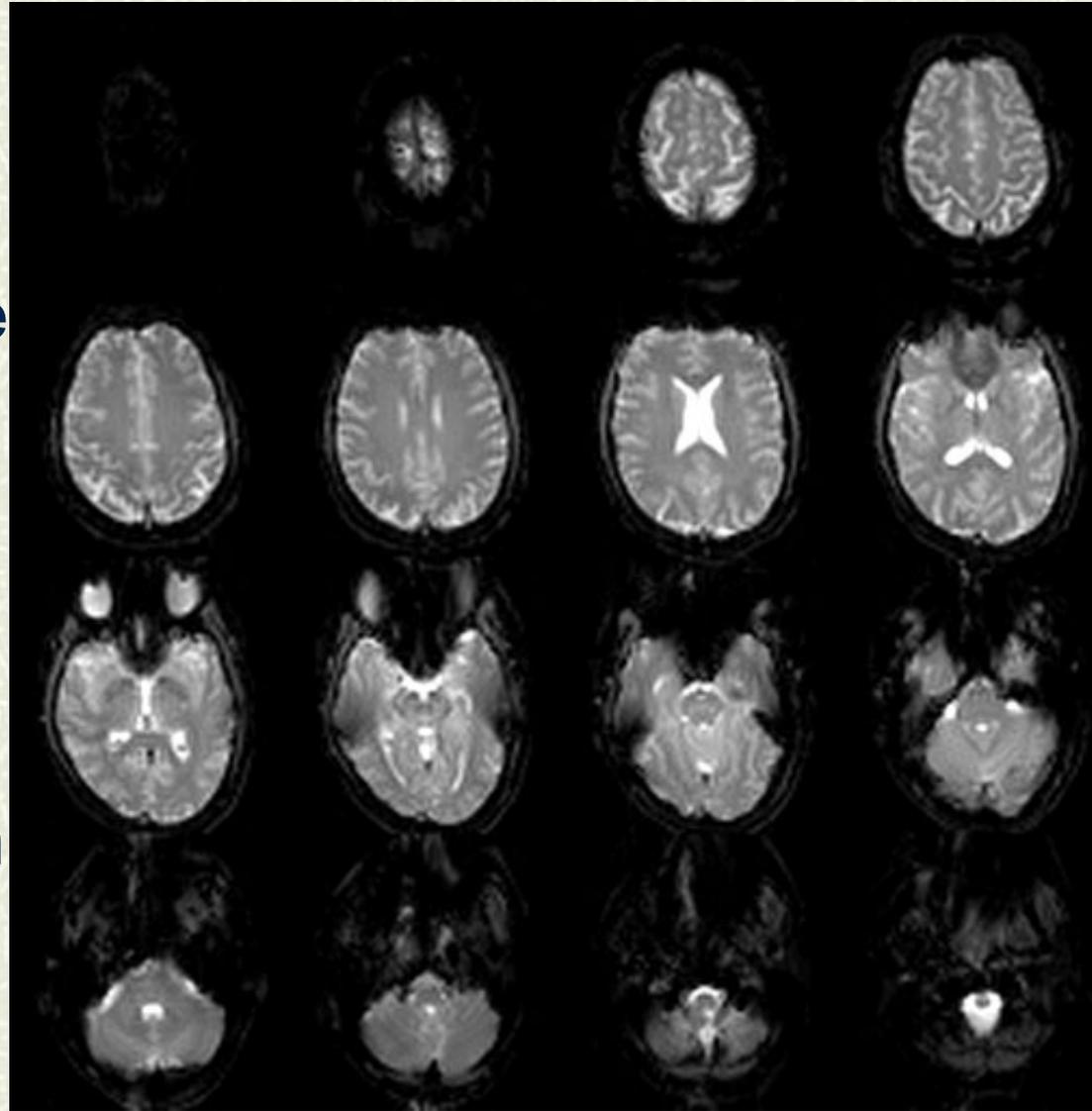
## Observations:

- Adjacent points along  $k_x$  are taken with short  $\Delta t$  ( $= 5 \text{ us}$ ). (high bandwidth)
- Adjacent points along  $k_y$  are taken with long  $\Delta t$  ( $= 500\text{us}$ ). (low bandwidth)
- A given line is read quickly, but the total encode time is longer than conventional Imaging.
- Adjacent lines are traversed in opposite directions.

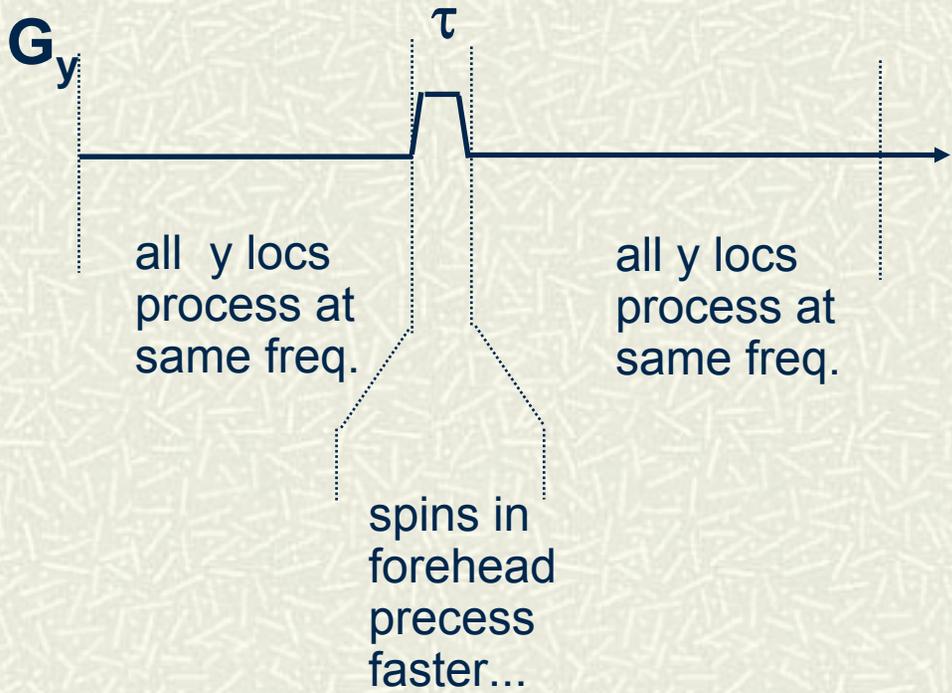
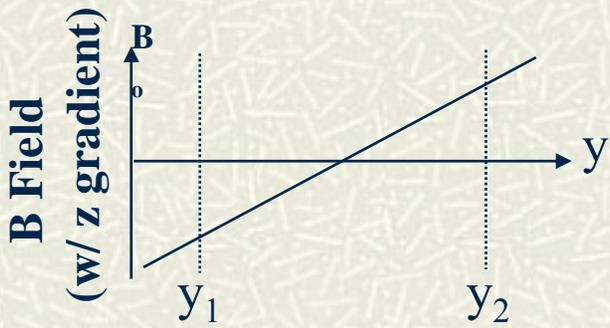
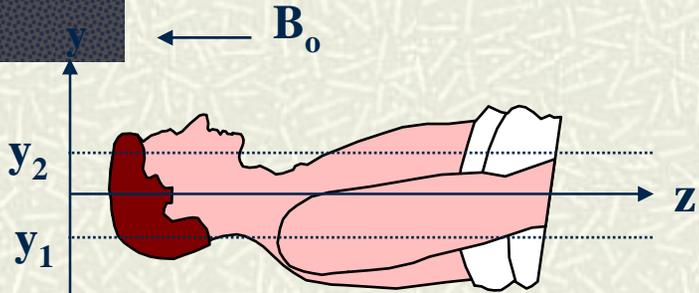


# Drawbacks of Single Shot Imaging

- Require high gradient performance to eliminate susceptibility induced distortions.
- Susceptibility in the head is worse at 3T than 1.5T.



# How does blipping on a grad. encode spatial info?

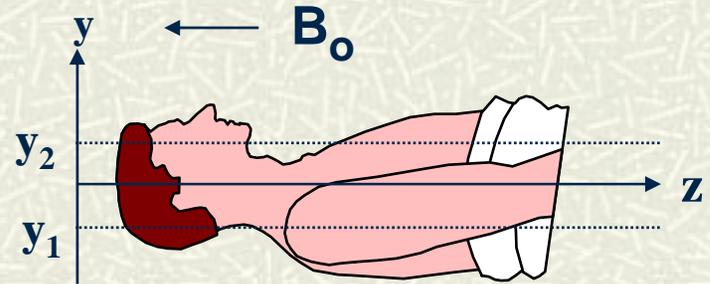


$$\nu(y) = \gamma \mathbf{B}_{TOT} = \gamma (\mathbf{B}_0 + \Delta y \mathbf{G}_y)$$

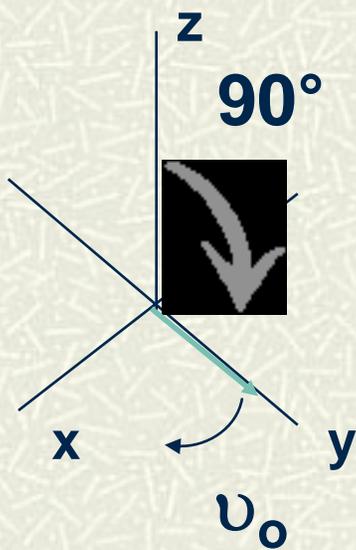
$$\Delta\theta(y) = \Delta\nu(y) t = \gamma \Delta y (\mathbf{G}_y t)$$

# How does blipping on a grad. encode spatial info?

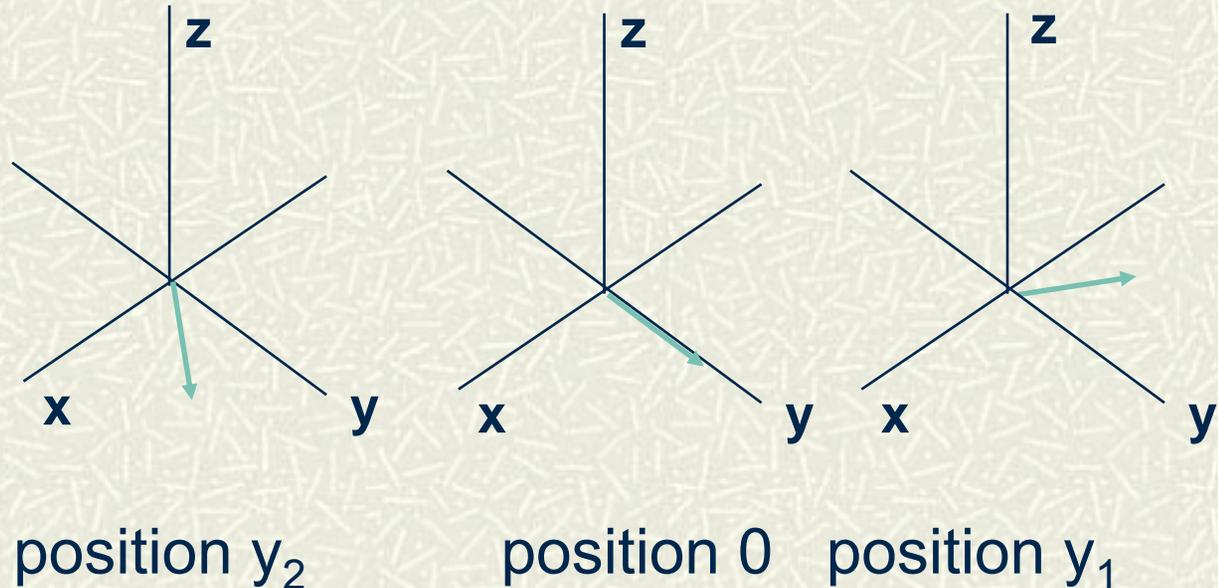
$$\theta(y) = v(y) \tau = \gamma G_y \Delta y \tau$$



after RF



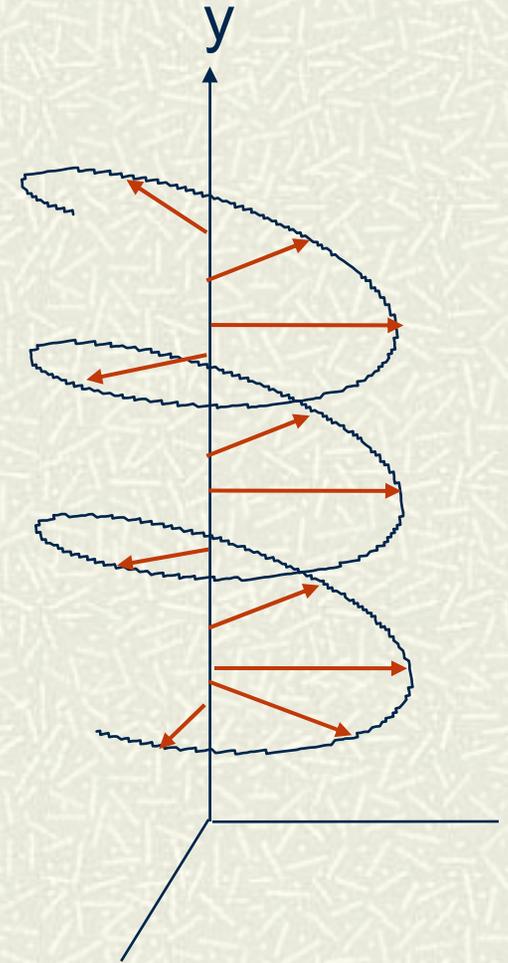
After the blipped y gradient...



# How does blipping on a grad. encode spatial info?

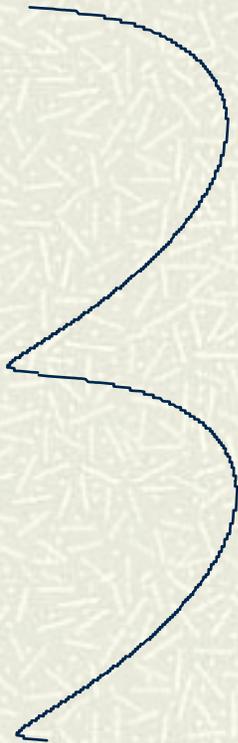
The magnetization in the  $xy$  plane is wound into a **helix** directed along  $y$  axis.

Phases are 'locked in' once the blip is over.

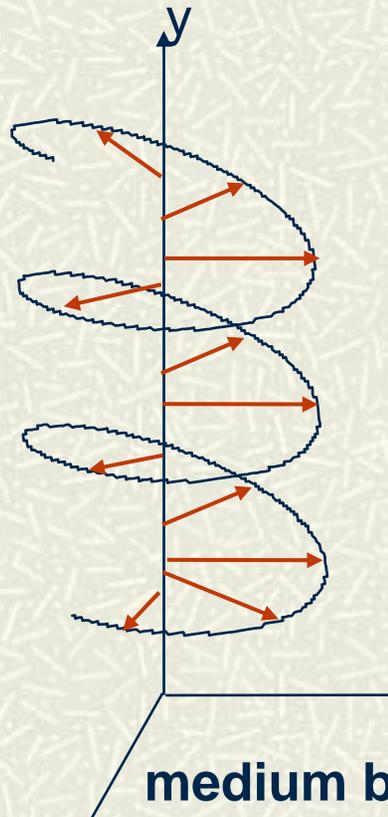


# Big gradient blip area means tighter helix

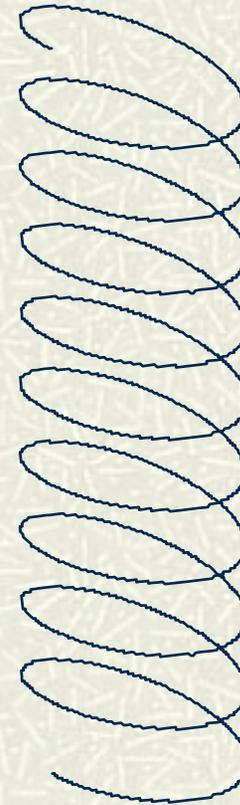
$$\begin{aligned}\theta(y) &= v(y) \tau \\ &= \gamma G_y \Delta y \tau \\ &= \gamma \Delta y (G_y \tau)\end{aligned}$$



**small blip**

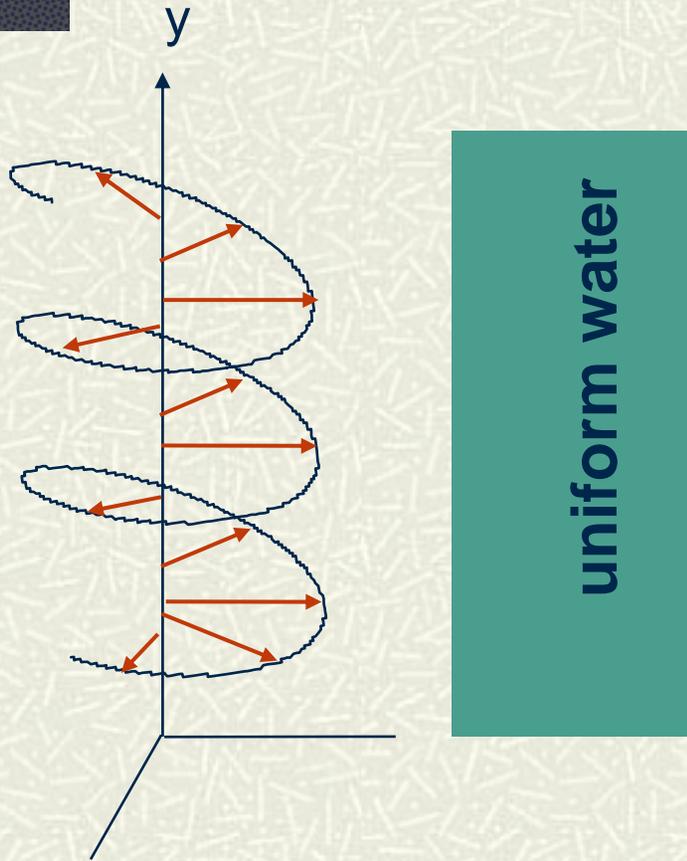


**medium blip**

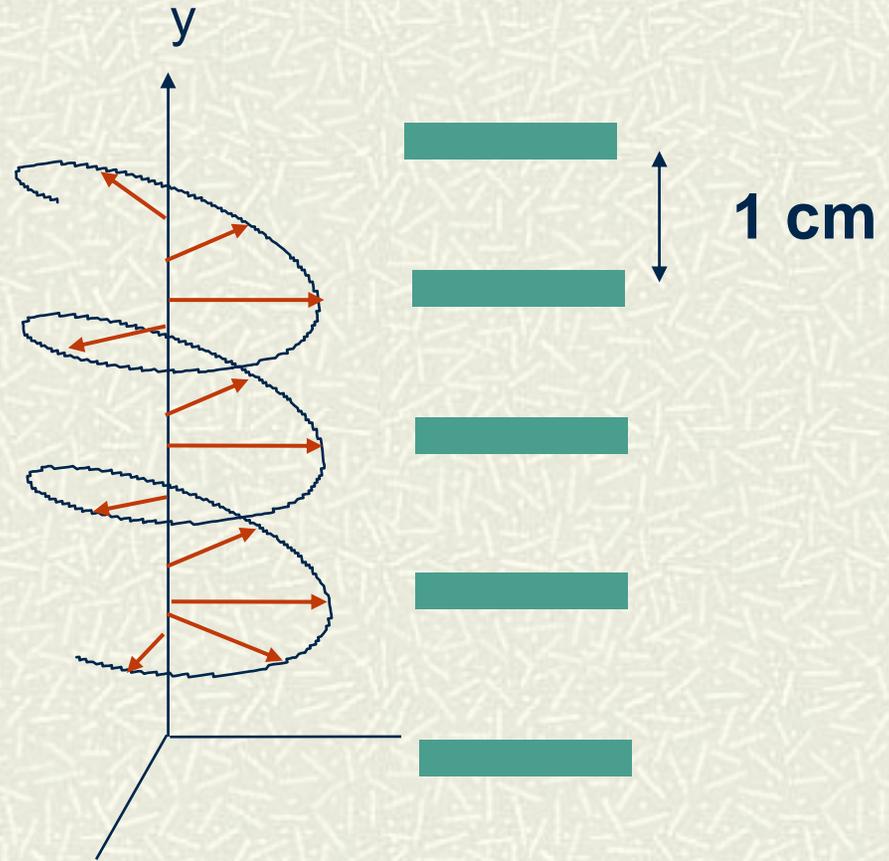


**large blip**

# Signal after the blip: Consider 2 samples:

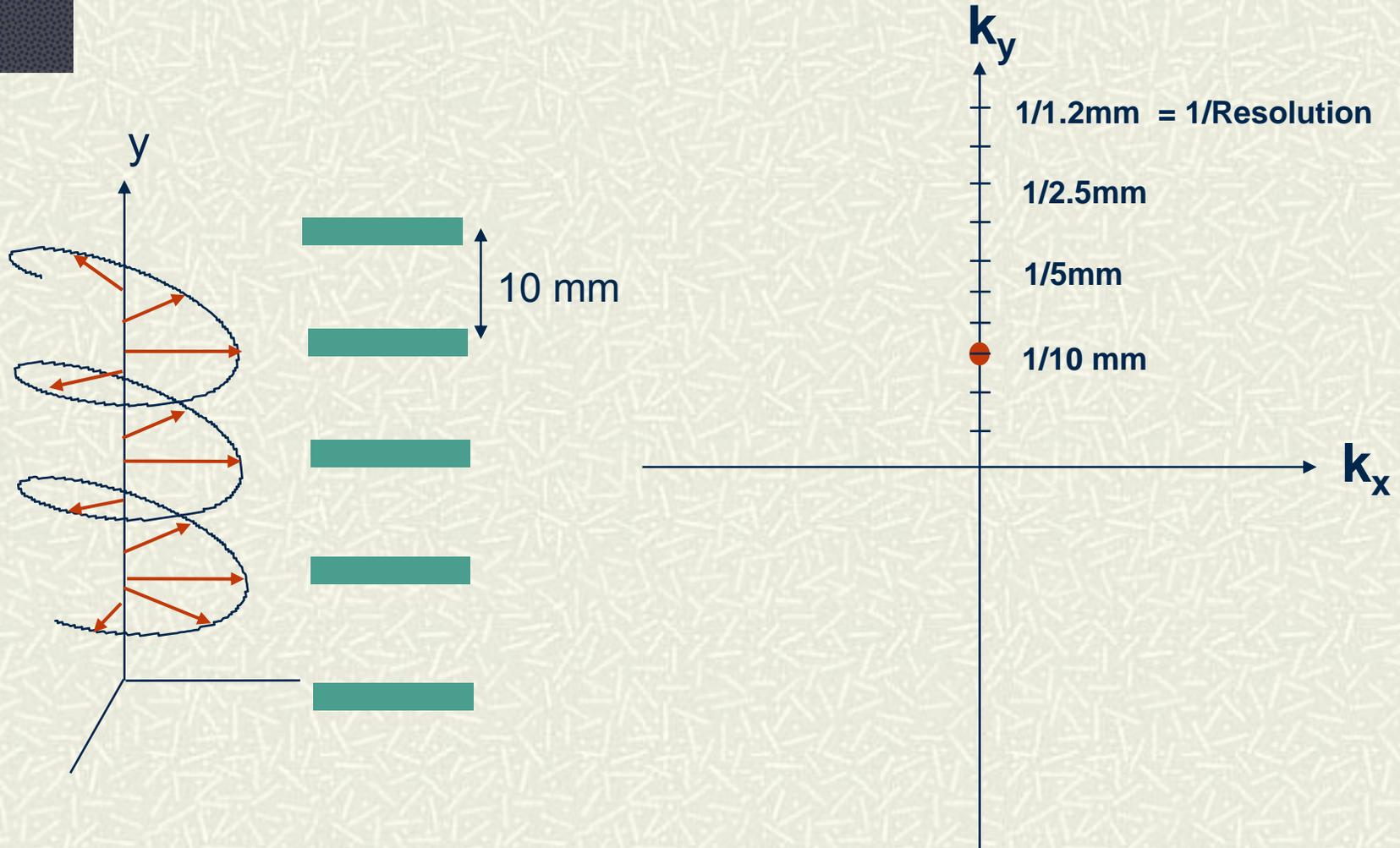


**no signal observed**

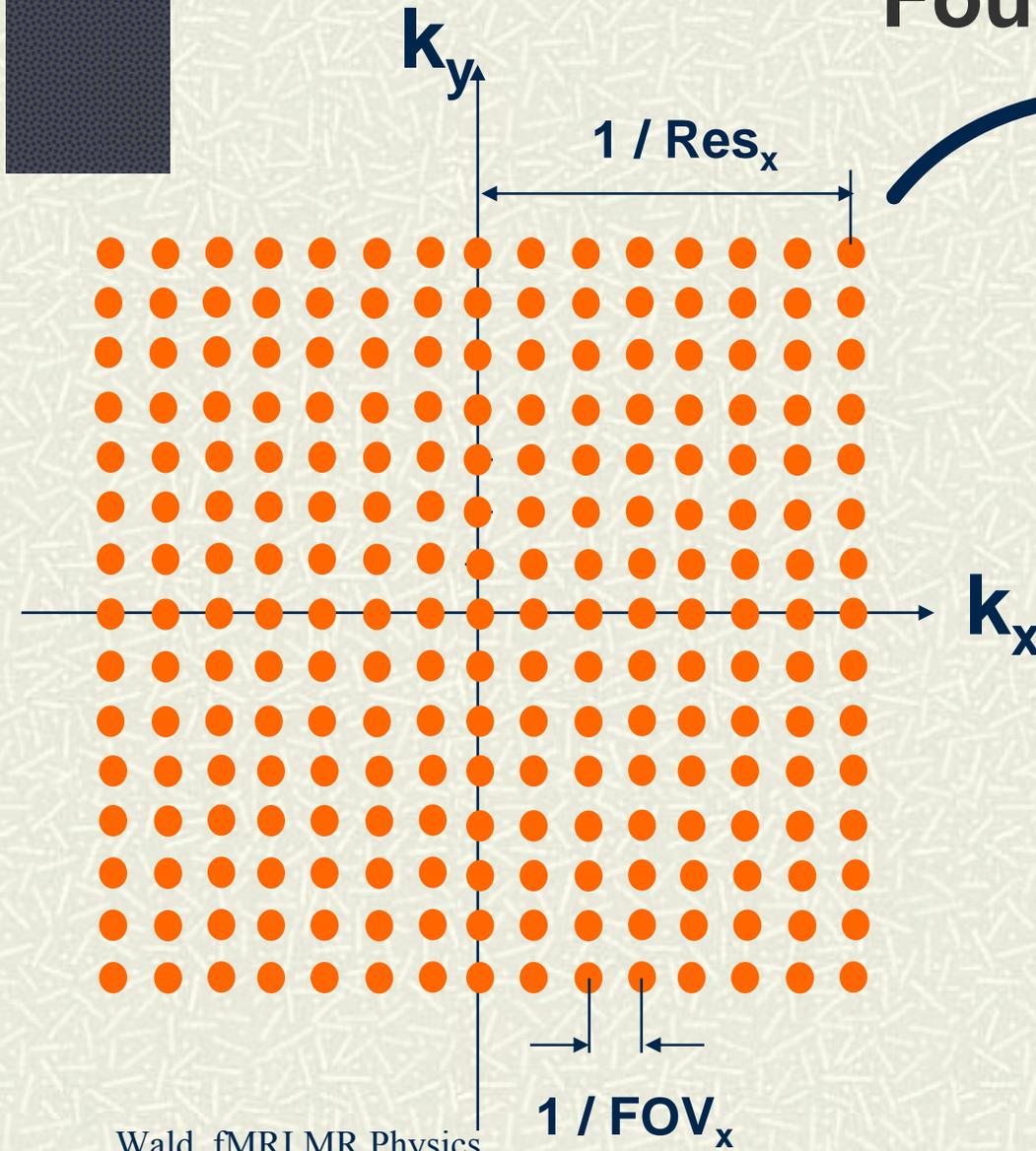


**signal is as big as if no gradient**

# You've measured: intensity at a spatial frequency...

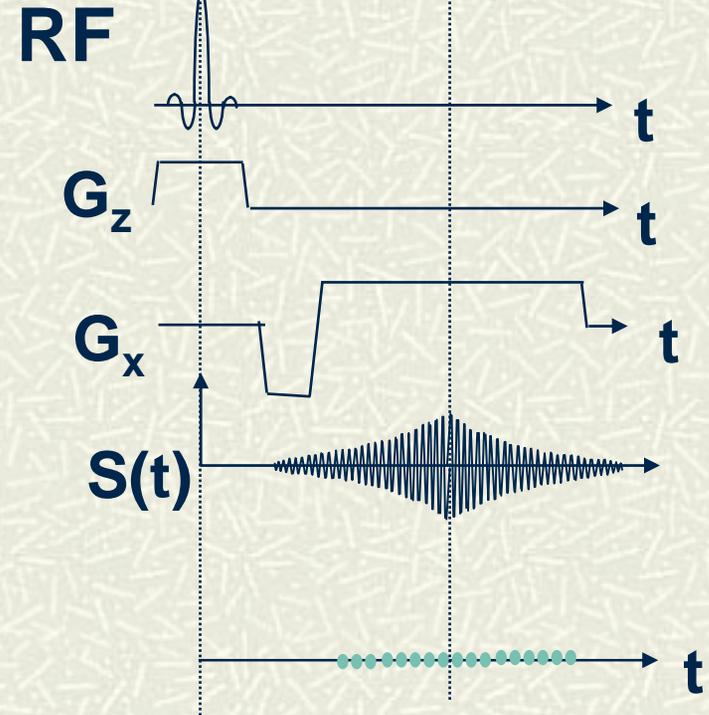
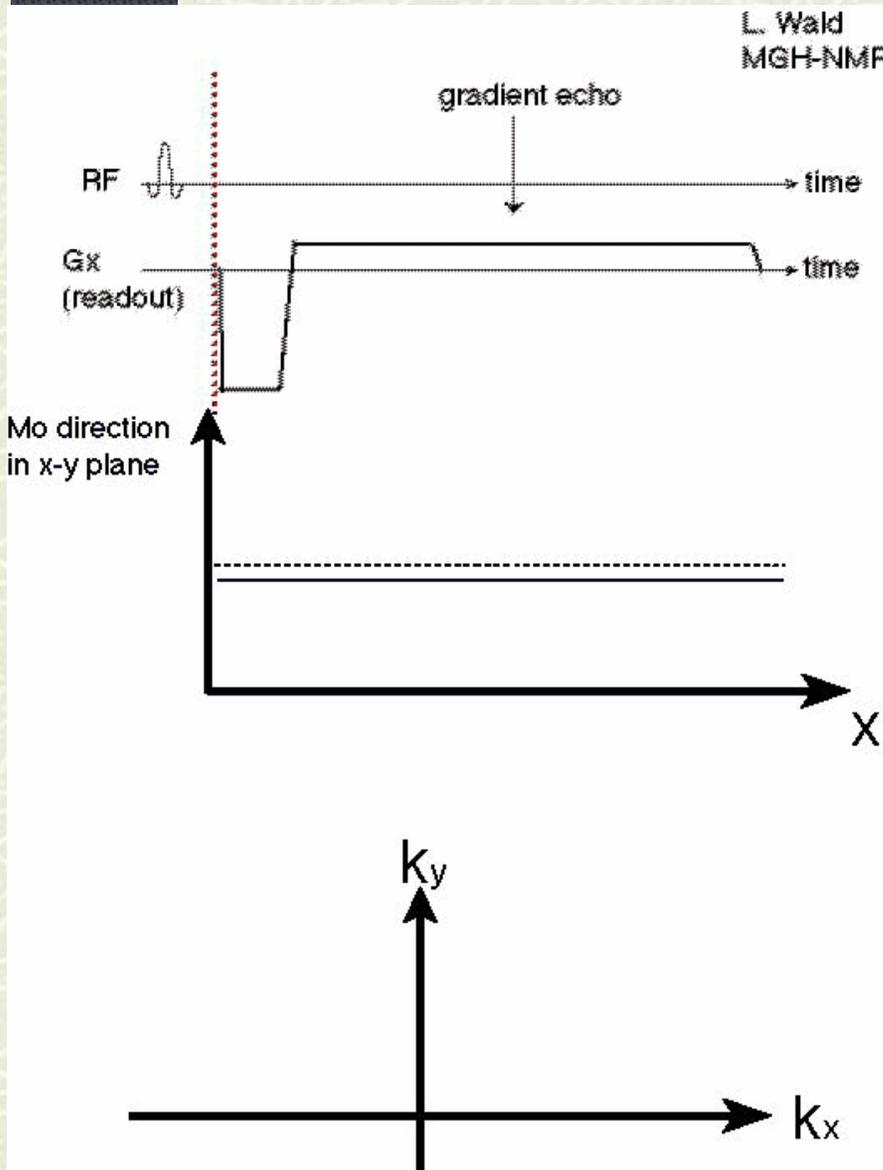


# Fourier transform



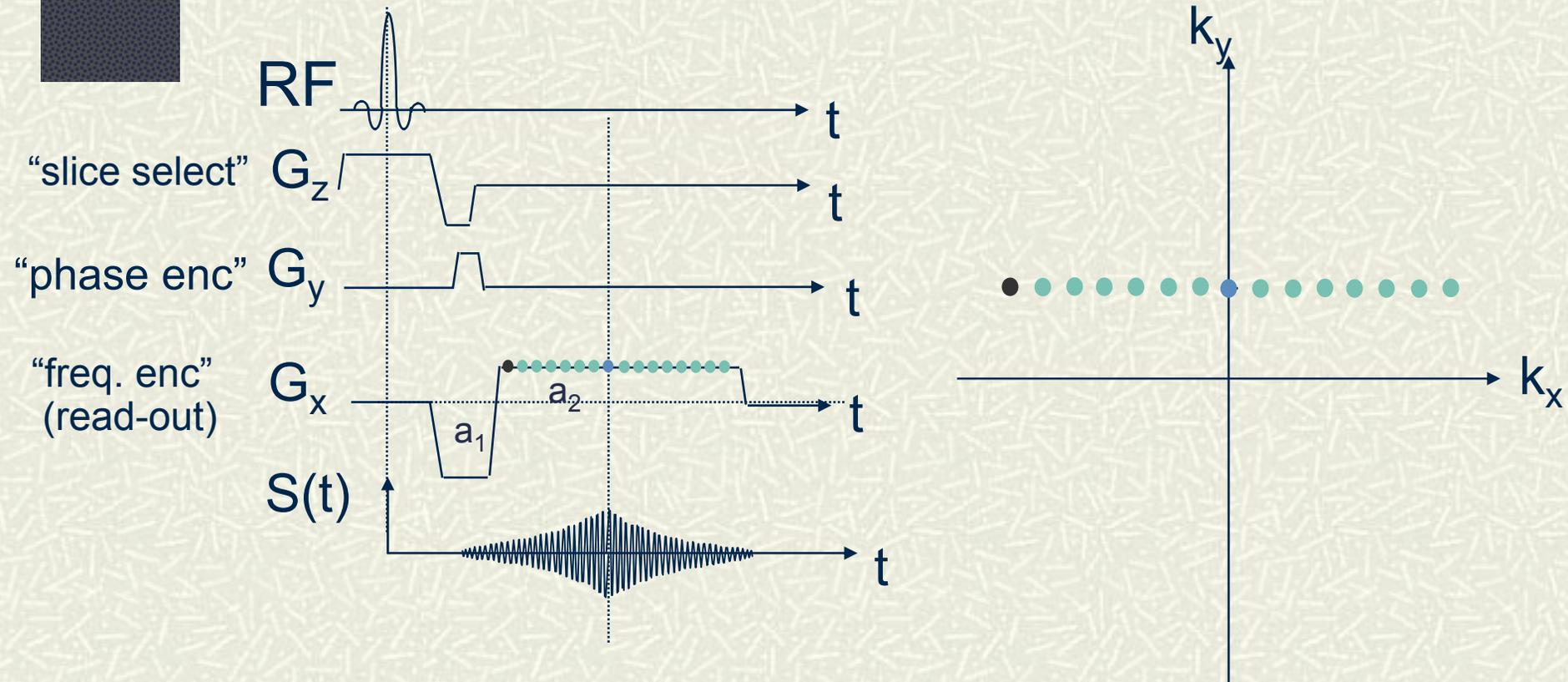
FOV<sub>x</sub> = matrix \* Res<sub>x</sub>

# Frequency encoding revisited



*Kspace, the movie...*

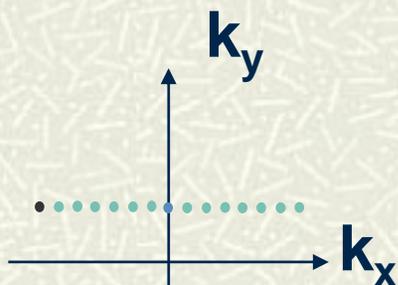
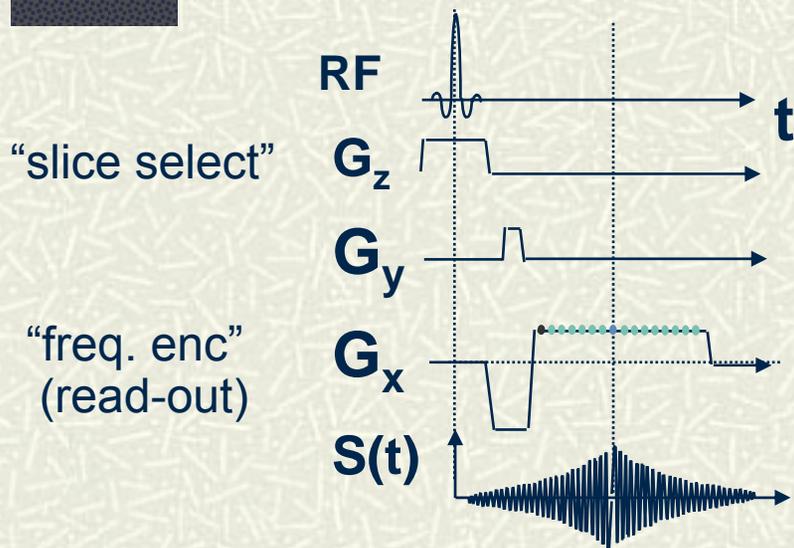
# “Spin-warp” encoding



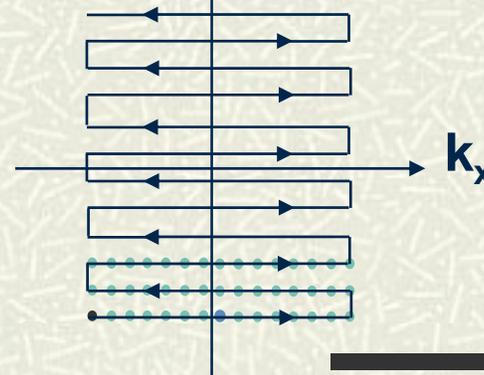
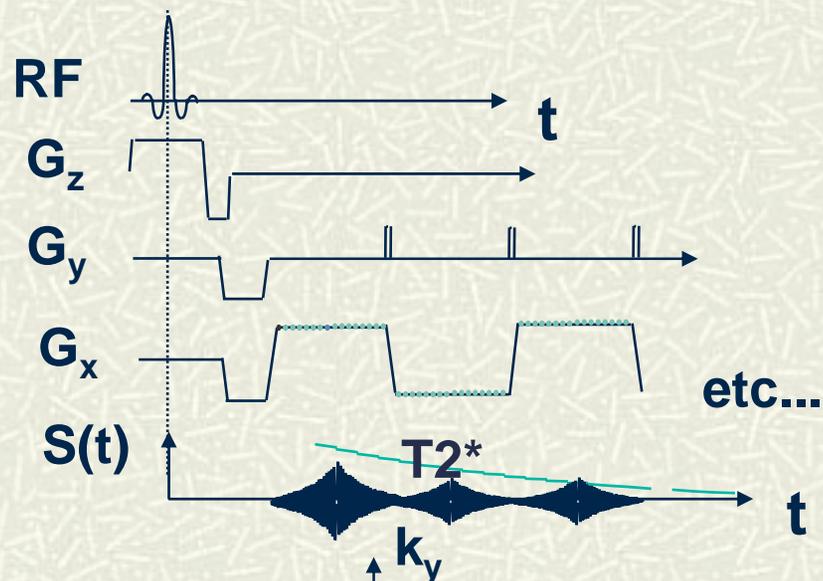
one excitation, one line of kspace...

# What's the difference?

## conventional MRI



## “fast” imaging



# “Spin-warp” encoding mathematics

Keep track of the phase...

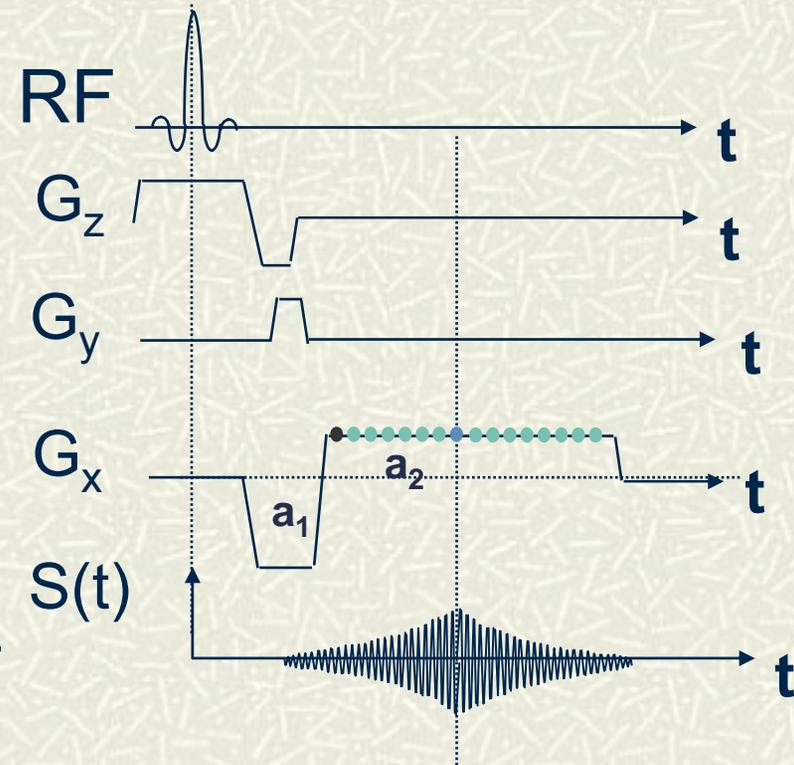
Phase due to readout:

$$\theta(t) = \omega_0 t + \gamma G_x x t$$

Phase due to P.E.

$$\theta(t) = \omega_0 t + \gamma G_y y \tau$$

$$\Delta\theta(t) = \omega_0 t + \gamma G_x x t + \gamma G_y y \tau$$



# “Spin-warp” encoding mathematics

Signal at time  $t$  from location  $(x,y)$

$$S(t) = \rho(x, y) e^{i\gamma G_x x t + i\gamma G_y y t}$$

The coil integrates over object:

$$S(t) = \iint_{\text{object}} \rho(x, y) e^{i\gamma G_x x t + i\gamma G_y y t} dx dy$$

Substituting  $k_x = -\gamma G_x t$  and  $k_y = -\gamma G_y t$ :

$$S(k_x, k_y) = \iint_{\text{object}} \rho(x, y) e^{-ik_x x - ik_y y} dx dy$$

# “Spin-warp” encoding mathematics

View signal as a matrix in  $k_x, k_y \dots$

$$S(k_x, k_y) = \iint_{\text{object}} \rho(x, y) e^{-ik_x x - ik_y y} dx dy$$

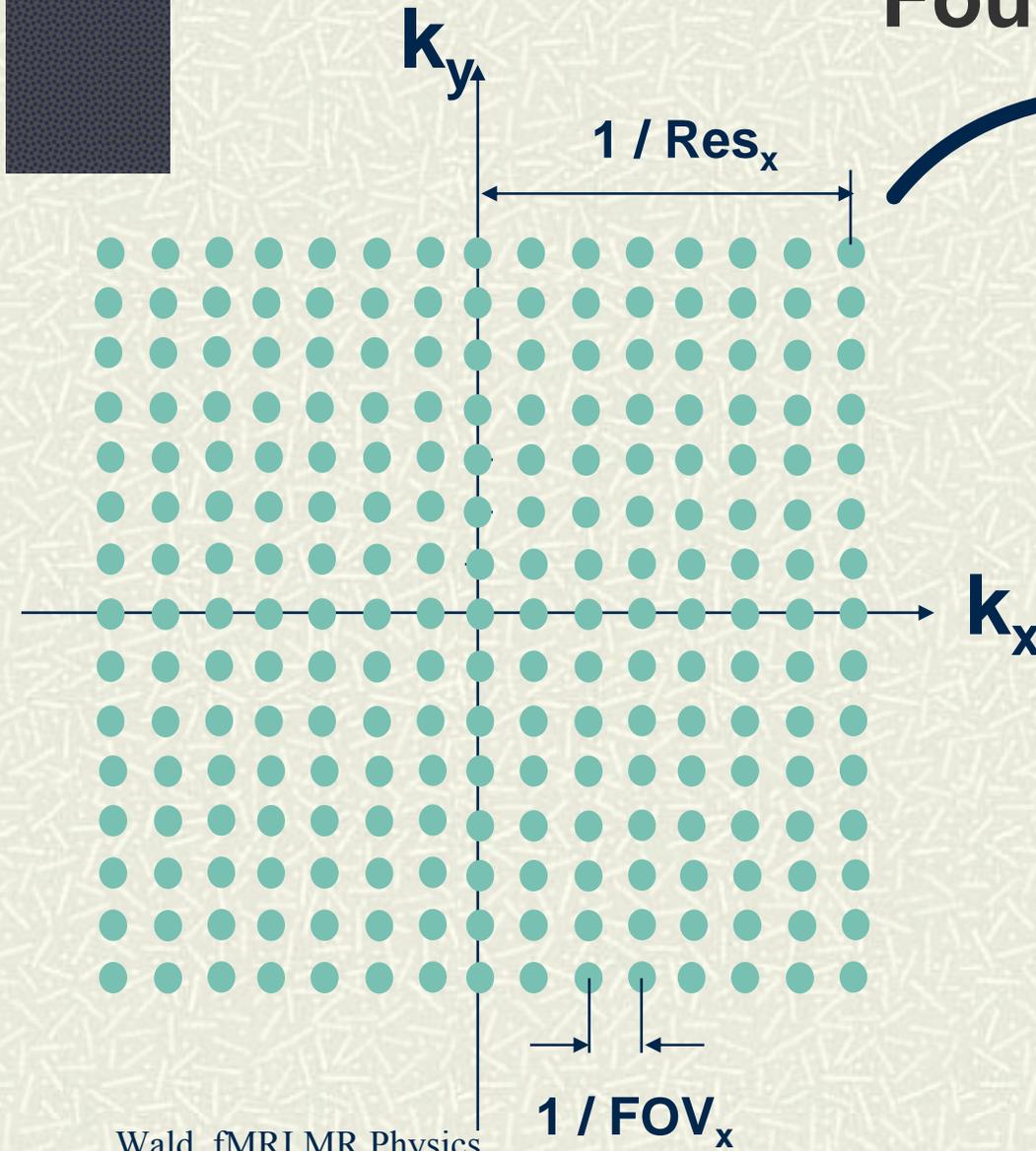
:

Solve for  $\rho(x, y)$

$$\rho(x, y) = FT^{-1} [S(k_x, k_y)]$$

$$\rho(x, y) = \iint_{\text{kspace}} S(k_x, k_y) e^{ik_x x + ik_y y} dk_x dk_y$$

# Fourier transform



FOV<sub>x</sub> = matrix \* Res<sub>x</sub>

**B**lood  
**O**xygenation  
**L**evel  
**D**ependant

**BOLD** Can see change in  $T2^*$  image due to hemodynamic response associated with neuronal activation.

Ogawa et al.

# Basis of fMRI

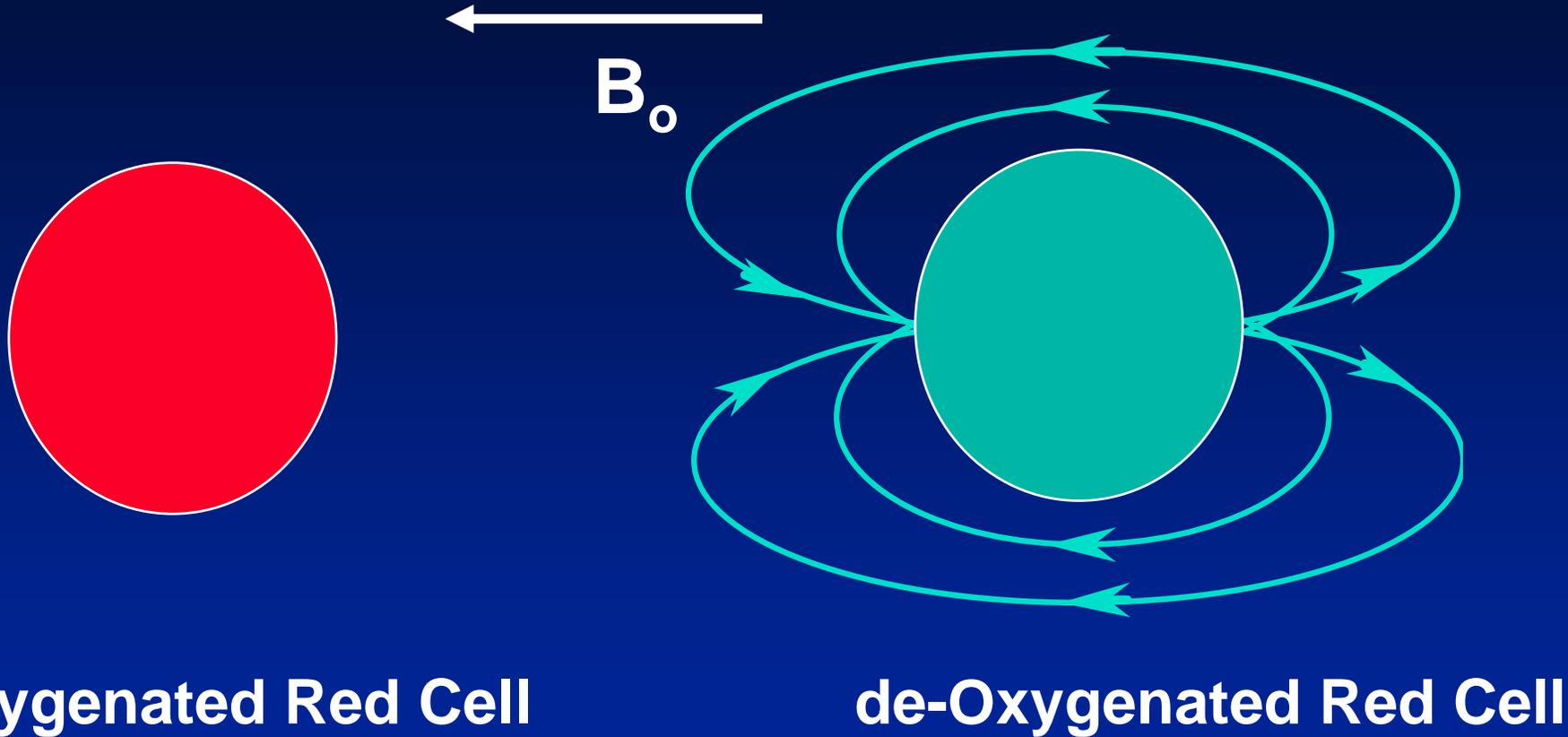
Qualitative Changes during activation

Observation of Hemodynamic Changes

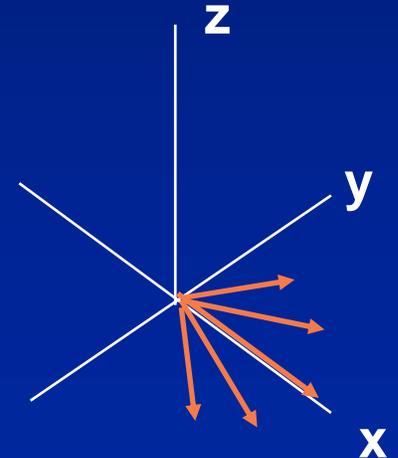
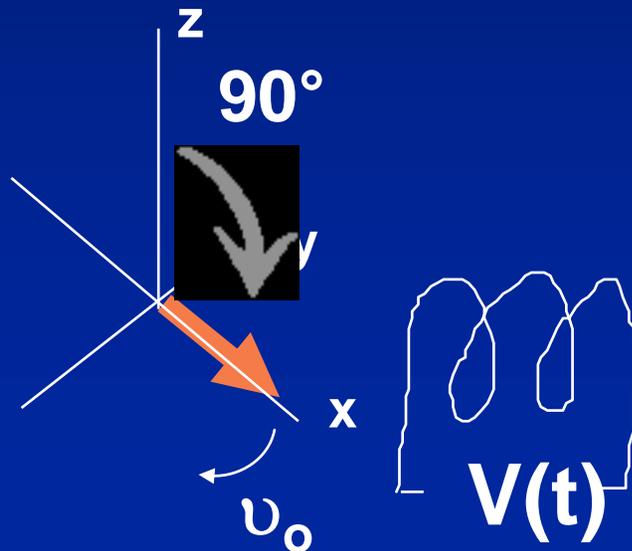
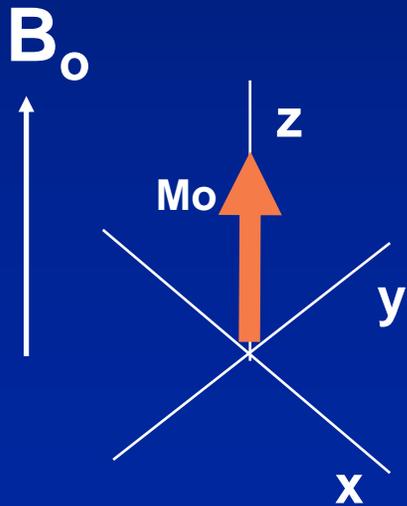
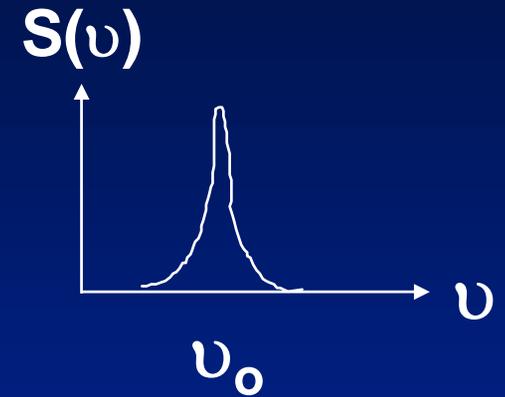
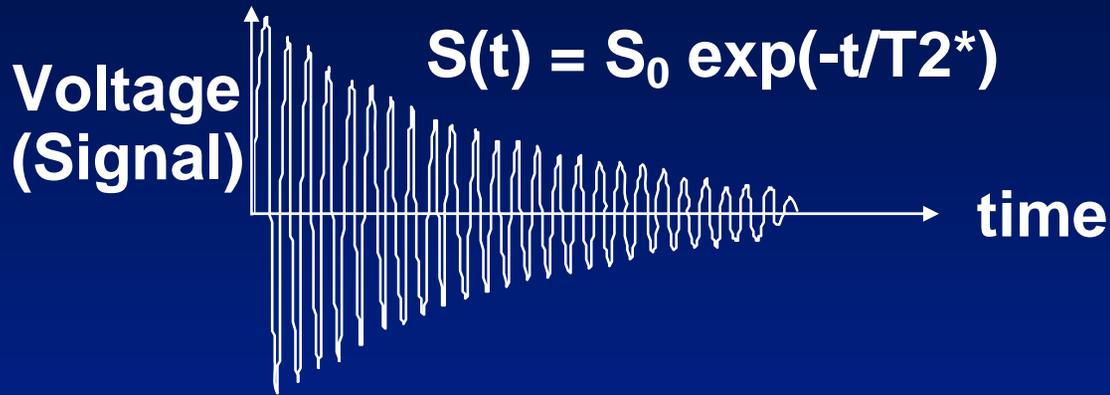
- Direct Flow effects
  - Blood Oxygenation

effects

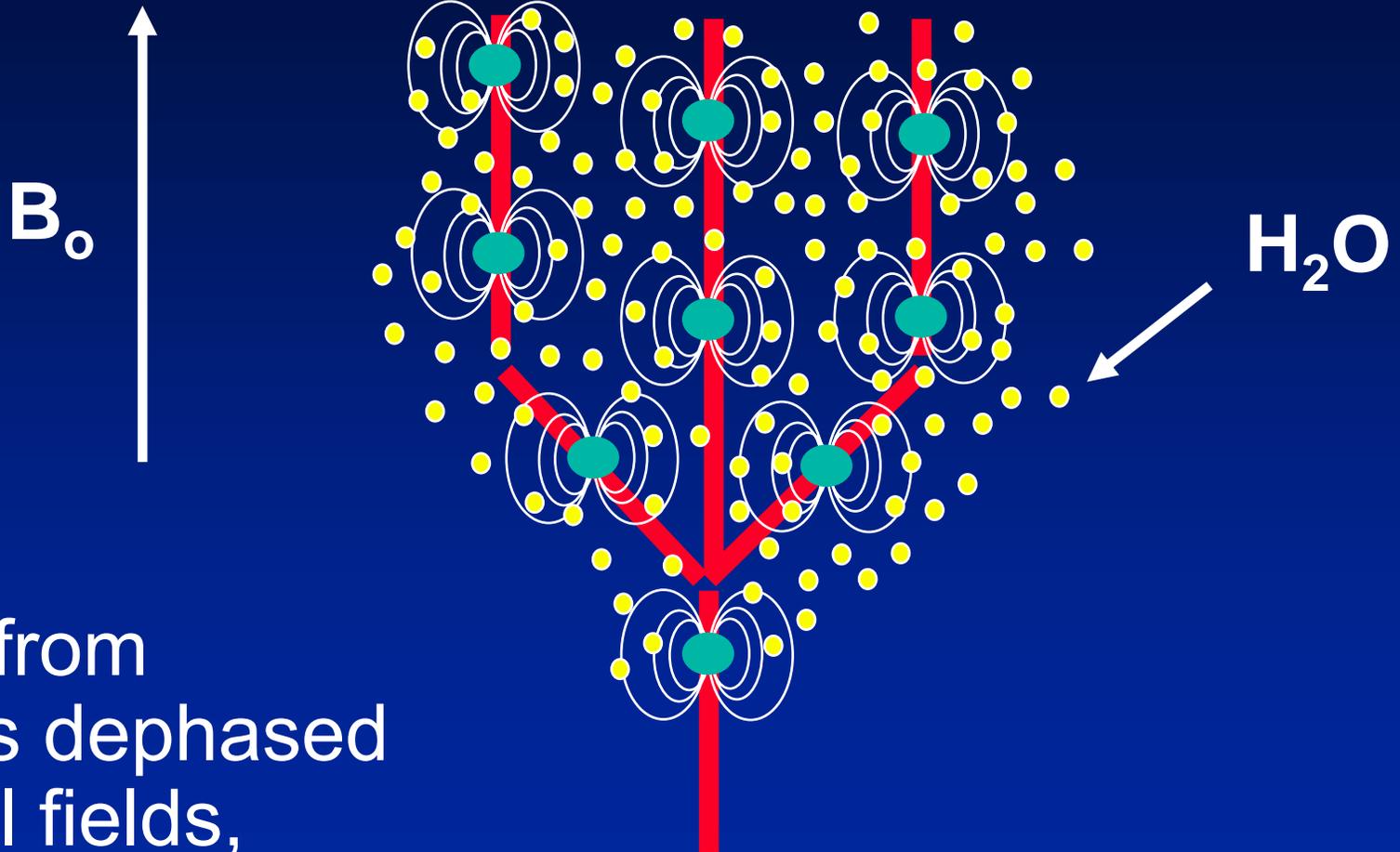
# Field Homogeneity and Oxygen State



# BOLD: blood effects $T2^*$



# Addition of paramagnetic compound to blood



Signal from water is dephased by local fields,  $T_2^*$  shortens, S goes down on EPI

# Addition of paramagnetic compound to blood

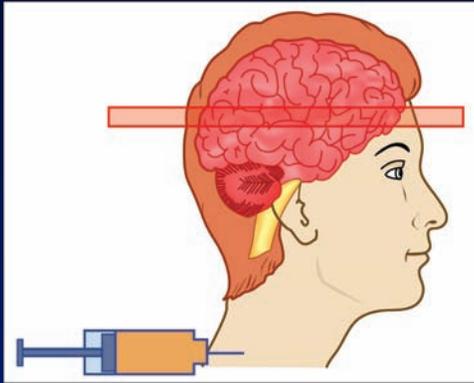
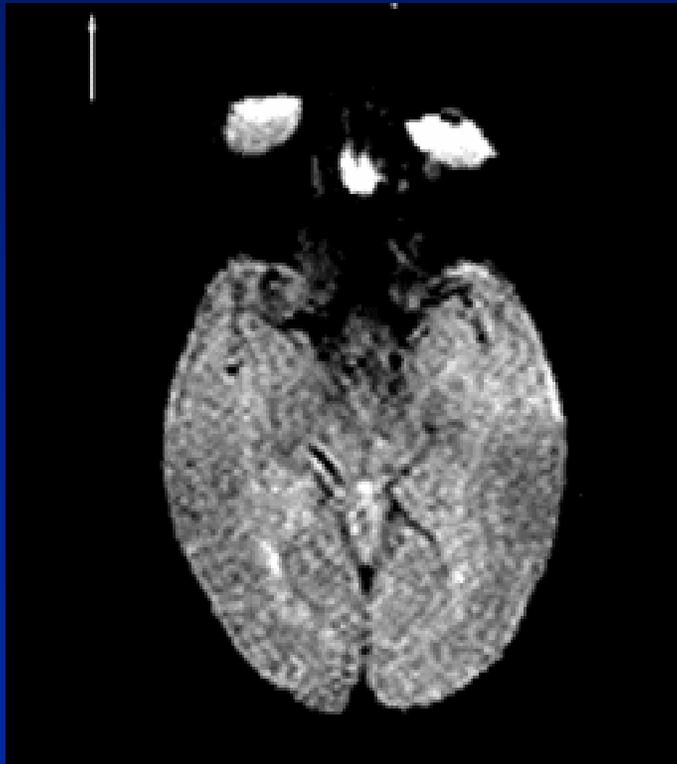
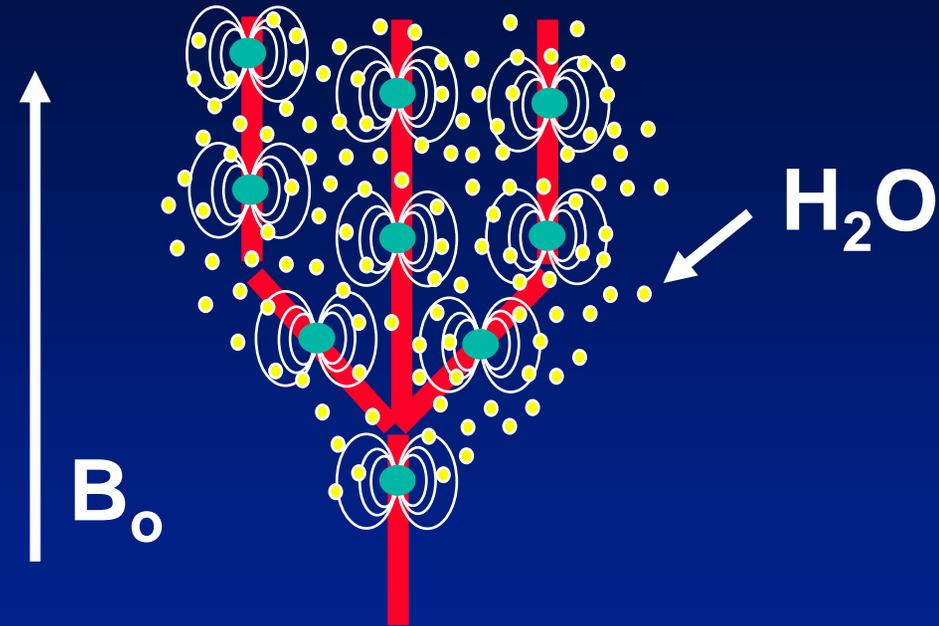


Figure by MIT OpenCourseWare.



Wald



Signal from water is dephased by local fields ( $T_2^*$  shortens), S goes down on EPI  
**Magnetic stuff**  $\uparrow$  **MR signal**  $\downarrow$

MGH-NMR Center

# Conversely,

Reducing amount of a paramagnetic substance in the blood will make the image intensity go up.

Magnetic stuff ↓    MR signal ↑

What happens during neuronal activation?

# Neuronal Activation . . .

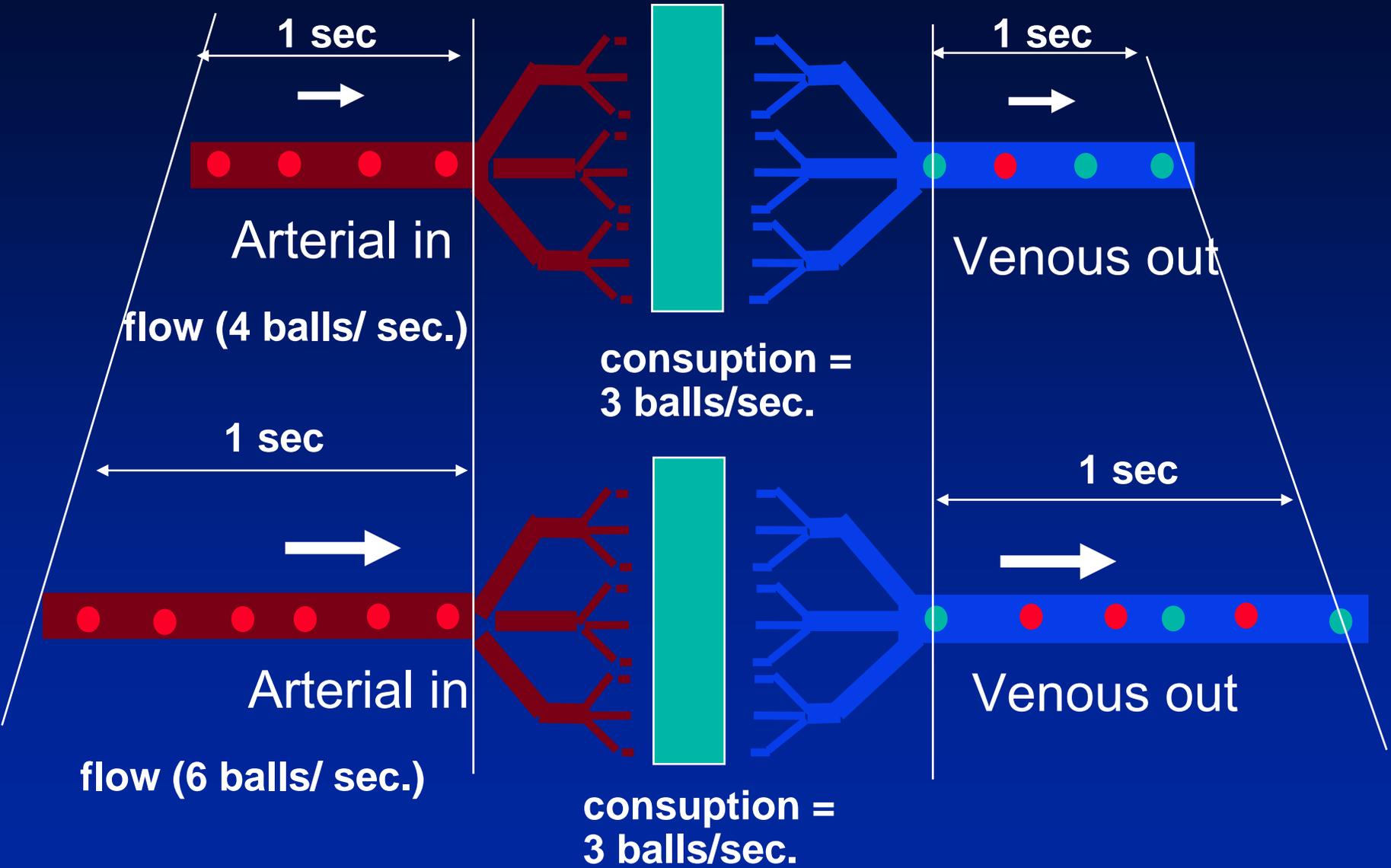
Produces *local* hemodynamic changes  
(Roy and Sherrington, 1890)

Increases local blood flow

Increases local blood volume

**BUT**, relatively little change in oxygen  
consumption

# decrease in deoxygenated red cell concentration



# NMR and Activation

## Summary:

- Flow ↑** increases signal on “T1-weighted” or flow weighted scans
- DeoxyHb ↓** increases signal on “T2/T2\*-weighted” scans
- Blood Vol. ↑** Decreases signal on contrast agent CBV scans.

# Why does flow go up so much?

If O<sub>2</sub> consumption rises only modestly (15%), why does flow need to go up a lot (50%)?

“Uncoupling” between flow and metabolism?

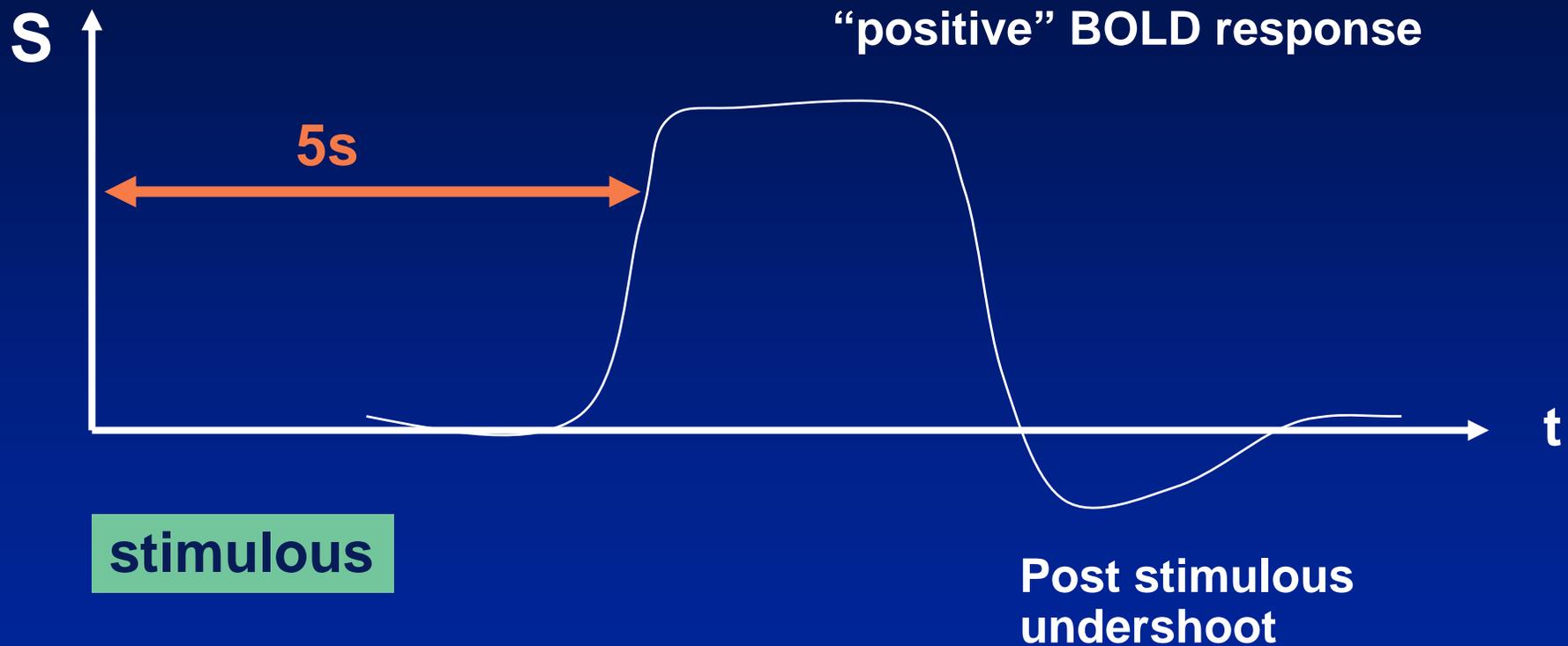
No real paradox: as flow<sup>↑</sup> oxygen extraction is hampered by decreased capillary transit time.

The simple answer is it takes a lot of flow increase...

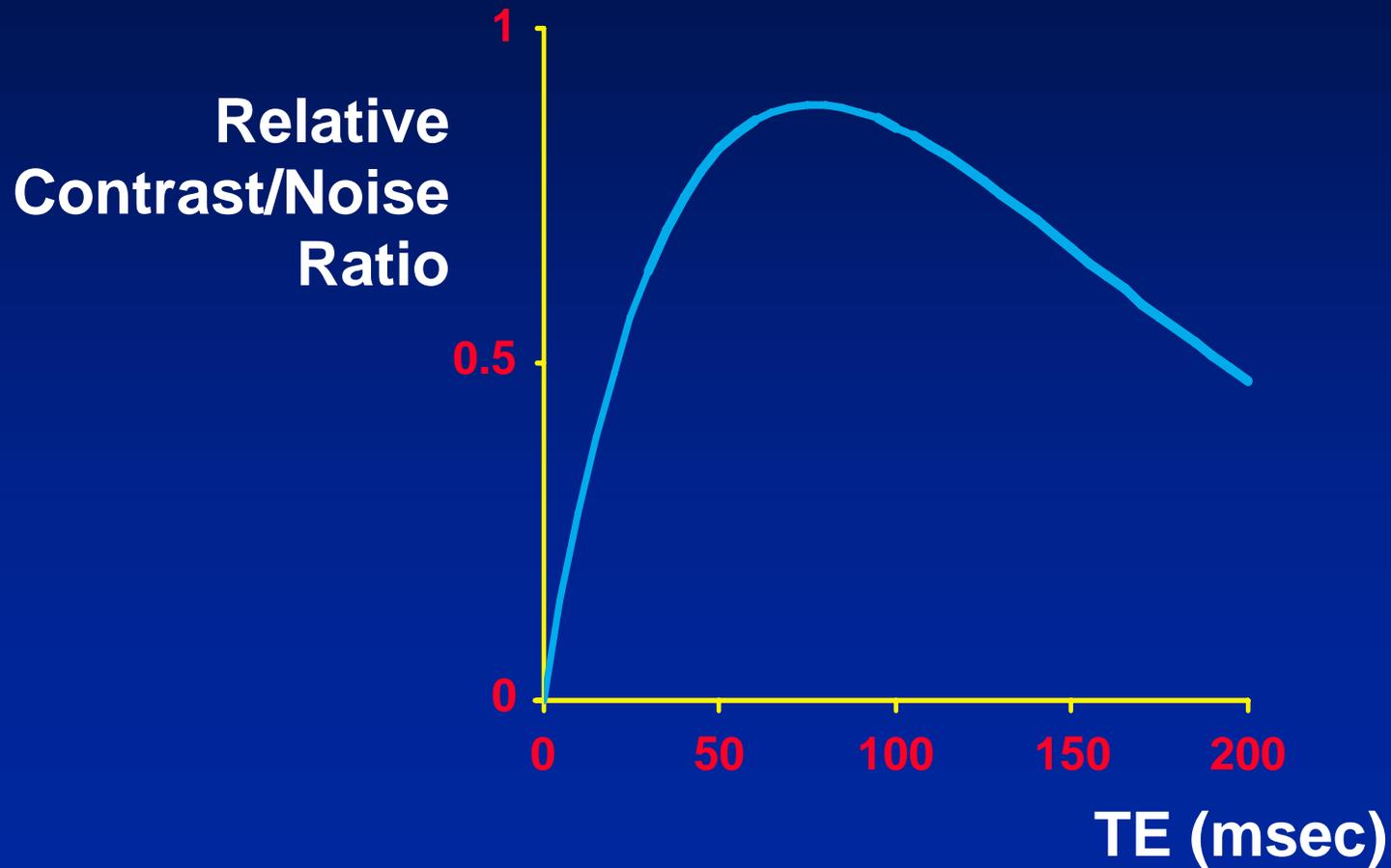
“Balloon model”

Buxton et al. Magn. Reson. Med. 39, p855, 1998

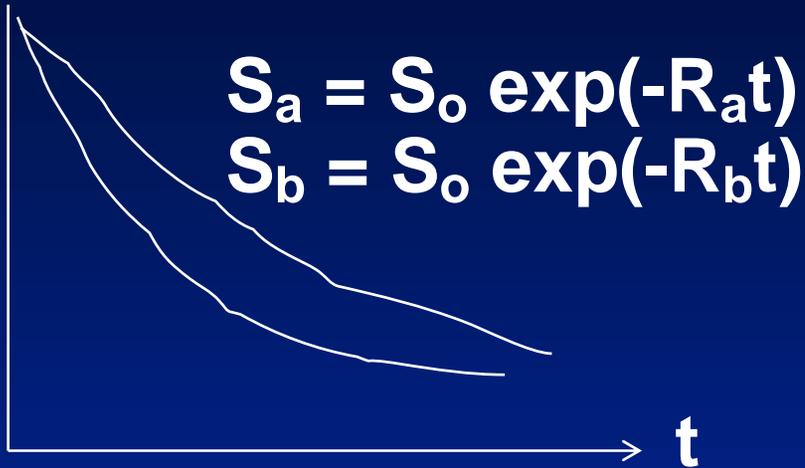
# Time response of BOLD



# Contrast/Noise Ratio and Echo Time (TE)



# Contrast/Noise Ratio and Echo Time (TE)



$$R_a = 1/T_{2a}^*$$

$$R_b = 1/T_{2b}^*$$

$$\Delta R = R_a - R_b$$

$$\Delta S = S_o e^{-R_a t} - S_o e^{-R_b t}$$

$$\Delta S = S_o e^{-R_a t} - S_o e^{-(R_a - \Delta R) R_b t}$$

$$\Delta S = S_o e^{-R_a t} (1 - e^{\Delta R t})$$

$$\Delta S = -S_o e^{-R_a t} \Delta R t$$

$$\frac{\partial}{\partial t} (\Delta S) = 0$$

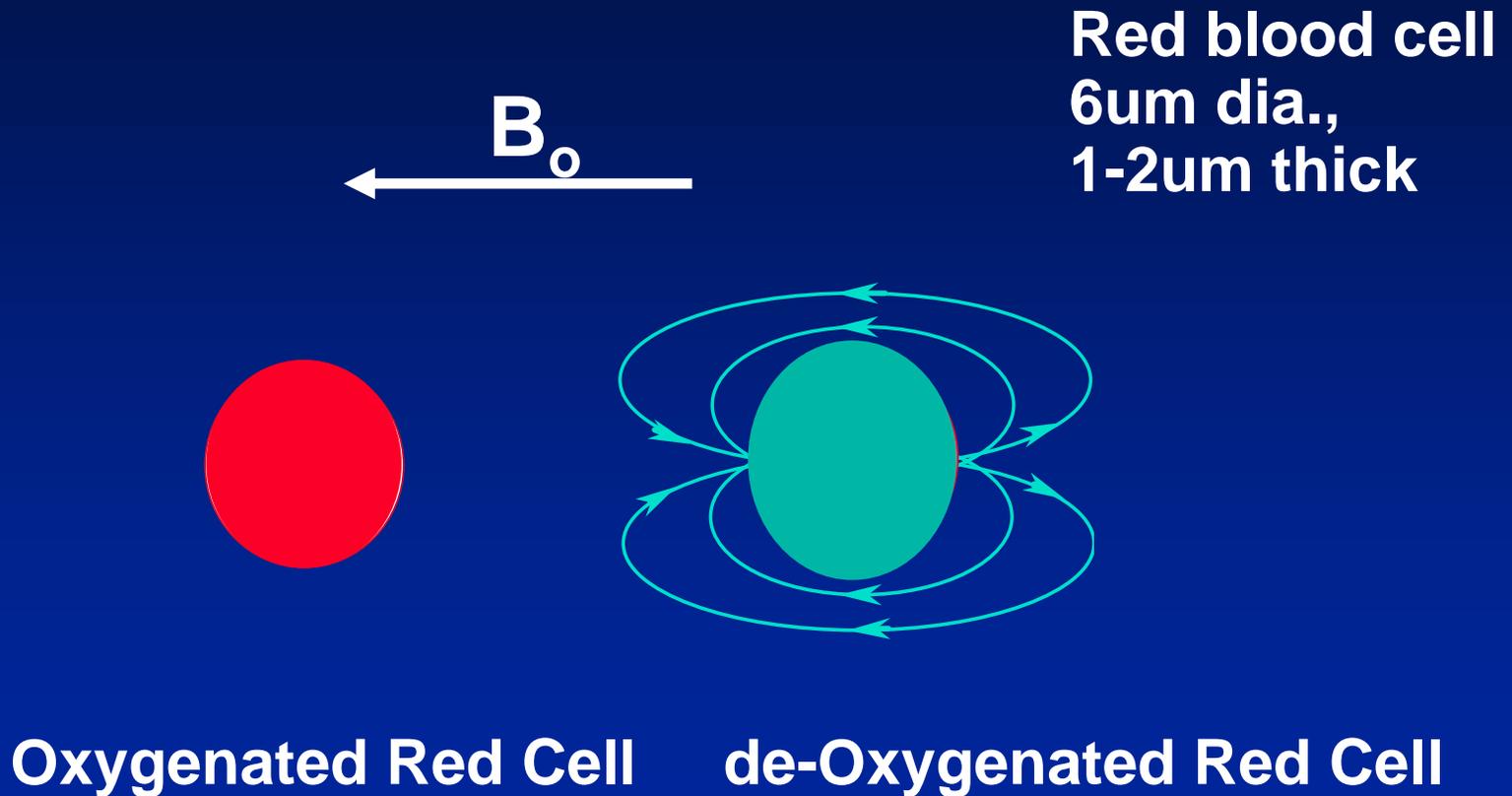
$$t = 1/R_a$$

$$TE = T_{2a}^*$$

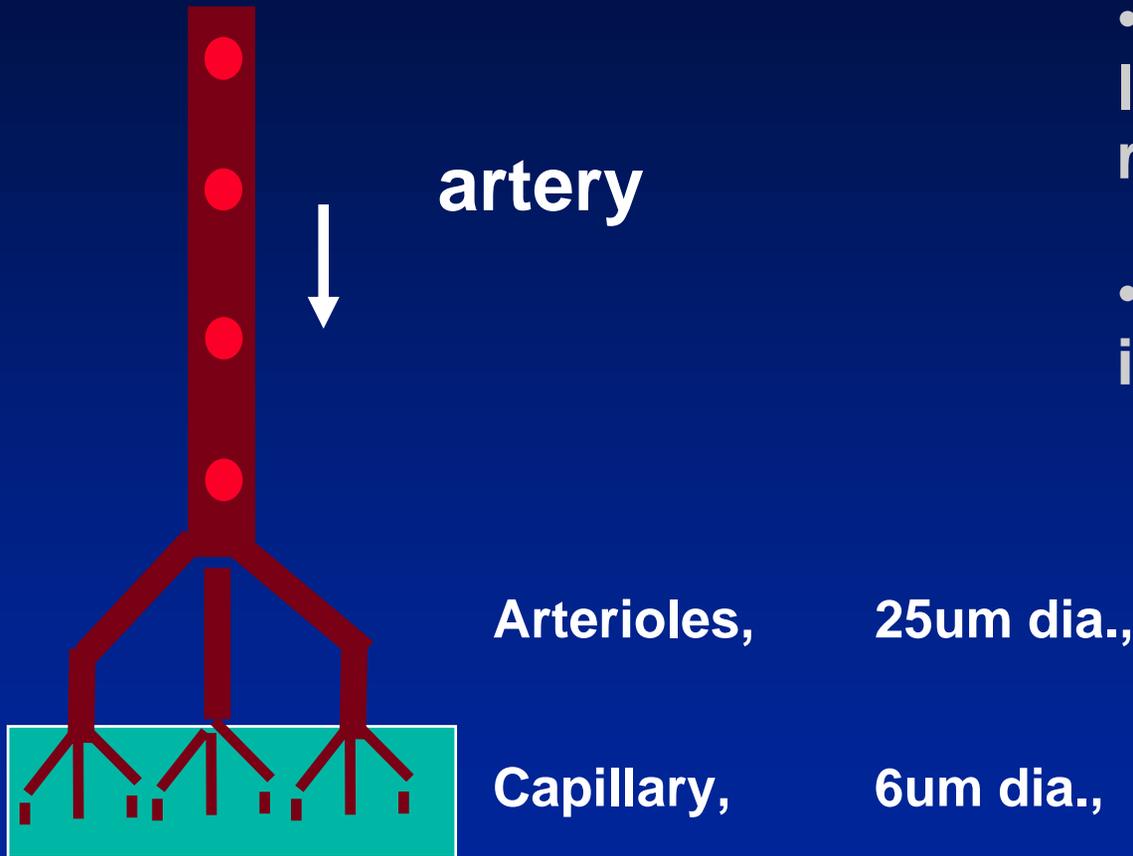
**Signal dephasing changes that  
accompany activation (BOLD  
effect)**

**a more detailed look...**

# Internal contrast agent: the deoxygenated red blood cell



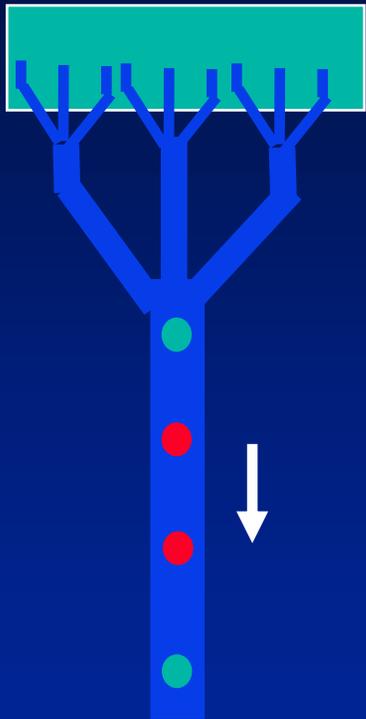
# Brain: Arterial side



- Capillaries are long and skinny, randomly oriented

- O<sub>2</sub> exchange is in capillary

# Brain: venous side



Venules, 25-50um dia.,

Collecting veins

Veins

Blood Oxygen saturation  
~60% oxygenated for  
resting individual.

- Venules have the same BV as caps

- Venules have 2x the deOxyHb conc. Of caps.

>> venules are more magnetic.

Venules are ~ randomly oriented, but many veins on surface

# Brain vessel facts

resting state  
saturation.

60% venous oxygen

80% sat. in capillaries

100% sat. in arteries.

activated state (with 70% increase in flow and  
20% increase in  
CMRO<sub>2</sub>)

saturation

72% venous oxygen

86% sat. in caps.

100% sat. in arteries

# What does the water see?

Freely diffusing water is the source of image signal

In 50ms, water diffuses 25 $\mu$ m on average  
thus moves  $\sim$ 4x diameter of capillary...

Water diffuses readily in and out of red blood cells. (spends about 5ms in a red blood cell)

In the 50ms timescale of fMRI, only 5% of H<sub>2</sub>O leaves the cap. bed.

# Two water spaces: Extravascular (tissue) and Intravascular (blood)

Water does not exchange between these pools (in  $<0.1s$ )

The blood component has 2 sub spaces (capillaries and venules) with different vessel size and oxygenation levels.

Water diffuses freely in the extravascular space.

There is 20x more water in the extravascular space.

**Which contributes more to BOLD signal?**

# T2 or T2\* changes?

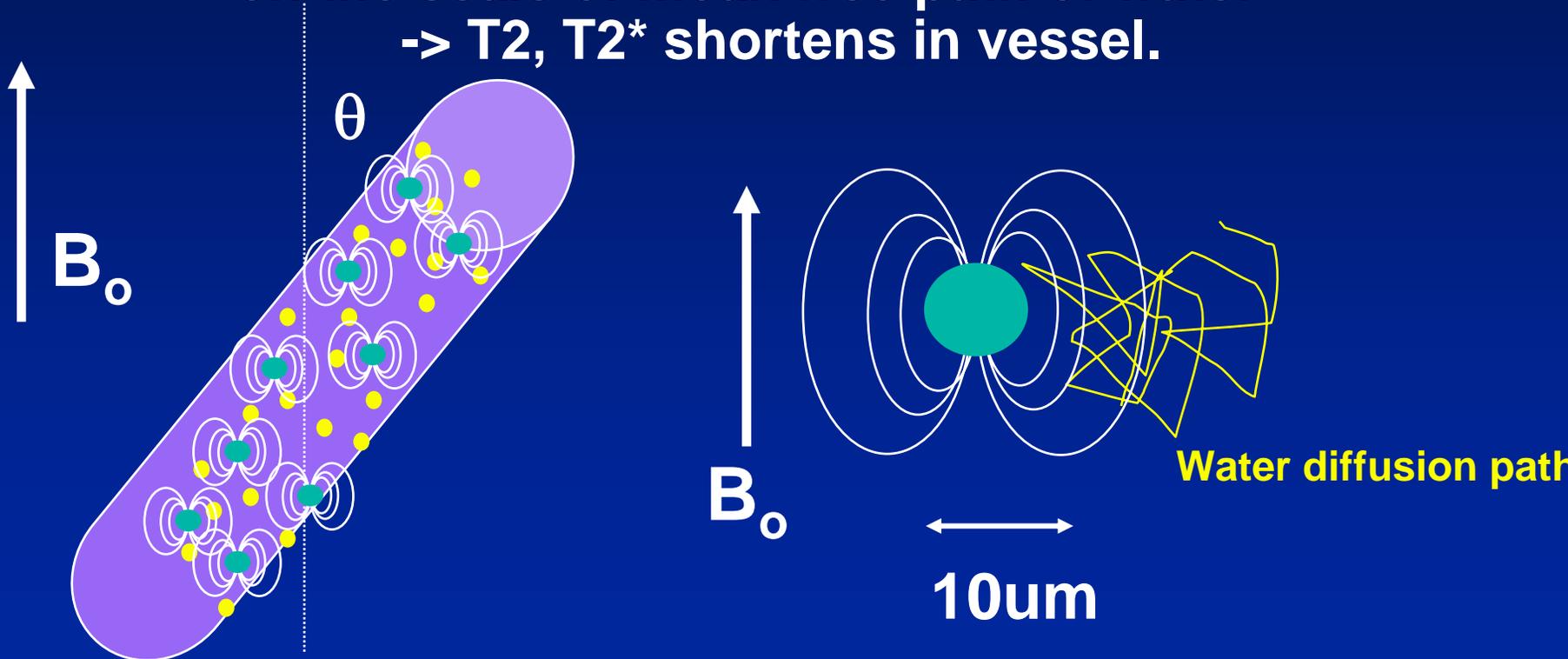
**T2 changes require the water dynamically move in a local field distribution.**

Water diffuses ~25 $\mu$ m during encoding.

If field is changing in 25 $\mu$ m scale, water will see dynamic dephasing (not refocused by spin echo).

# Intravascular: T2 or T2\* changes?

Both: Field around red blood cell  
changes  
on the scale of mean free path of water  
-> T2, T2\* shortens in vessel.



# T2 changes in the blood

Dynamic dephasing from diffusion in vicinity of the magnetic field of the RBC.

Easier to talk about dephasing rate:  $R_2 = 1/T_2$

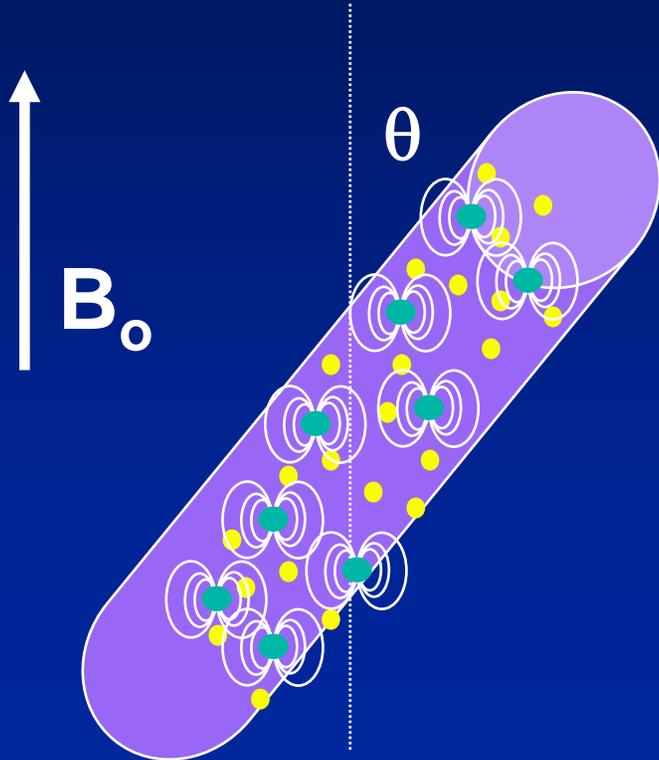
Empirical and Monte Carlo simulations:

$$R_2 = \frac{1}{T_2} = \frac{1}{T_{2o}} + aB_o^2 [Hematocrit] (1 - O_2Sat)^2$$

Blood becomes darker on SE at high field...

# Intravascularity: T2\* changes

Consider the vessel as uniformly magnetized.  
Distribution of angular orientations inside voxel.



Field inside vessel:

$$\Delta\nu = \alpha B_0 (1 - 3\cos^2 \theta) [1 - O_2 Sat]$$

$$\Delta\nu \approx 0 - 10 Hz$$

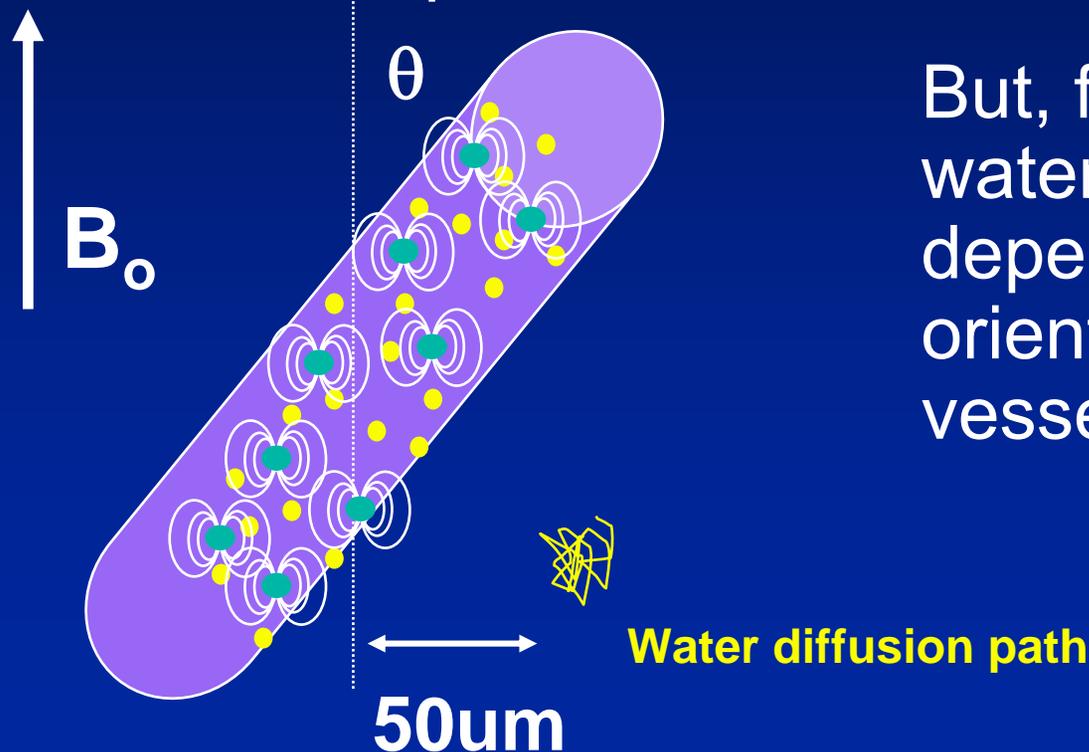
# Intravascular summary

**Both T2 and T2\* changes, must really do a careful simulation to figure out relative contribution.**

**At high enough field we expect T2 to get very short inside vessels.**

# Extravascular: T2 or T2\* changes?

Field outside large “magnetized” venule is approx. constant on length scale of water mean path

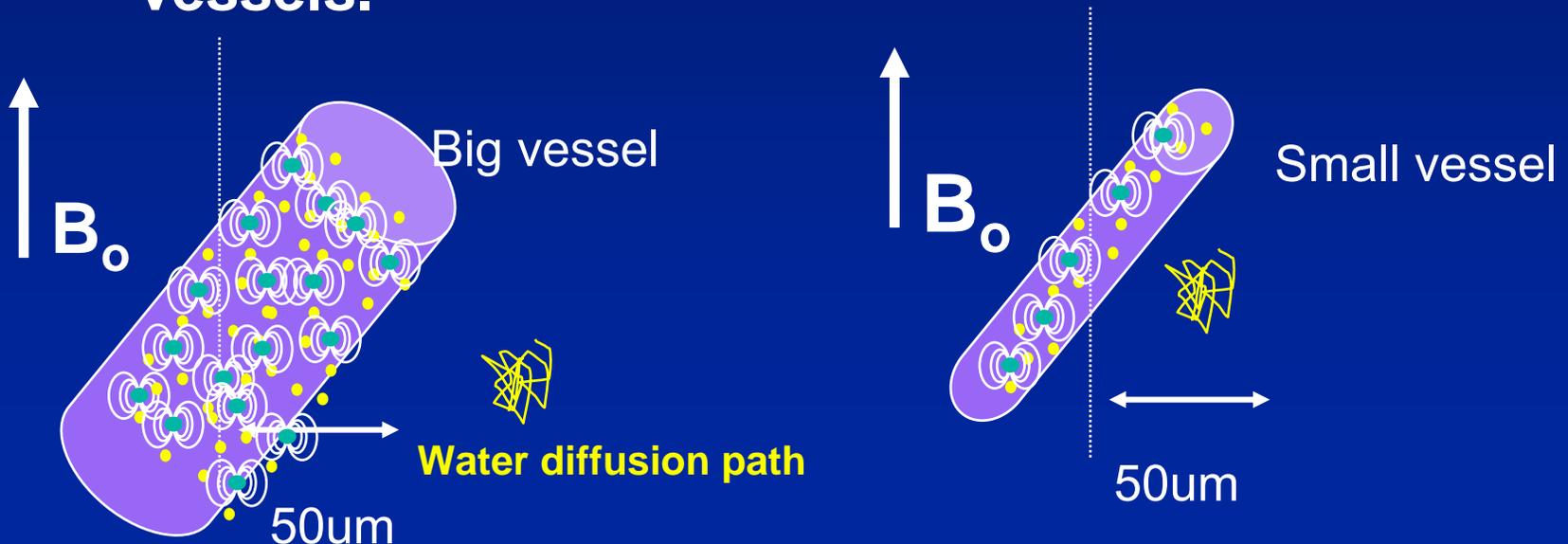


But, field (thus freq.) water experiences will depend on the orientation and size of vessel. Thus T2\* effect.

# Extravascular summary

Both T2 and T2\* changes, must really do a careful simulation to figure out relative contribution.

But, T2 effect mainly comes from the smaller vessels.



# The Boxerman-Weisskoff model

Monte Carlo simulation of dephasing in vascular tree using known size distributions.

Tissue and blood components

Track static and dynamic dephasing.

Include size of RBC ~ size of capillary

Boxerman J et al. Magn. Reson. Med 34 p 4-10

Boxerman J et al. Magn. Reson. Med 34 p 555-566

Good review in fMRI book edited by P. Bandetini

# The B-W model: Intravascular effects

- There are both T2 and T2\* effects.
- But don't forget intravascular space has 20x fewer spins
- Relative importance of blood pool increases at high  $B_0$  or for spin echos.

# The B-W model at 1.5T: Extravascular effects

## T2 vs. T2\*

T2\* effects (gradient echo) are ~3-4x larger

T2\* effects are derived from bigger vessels

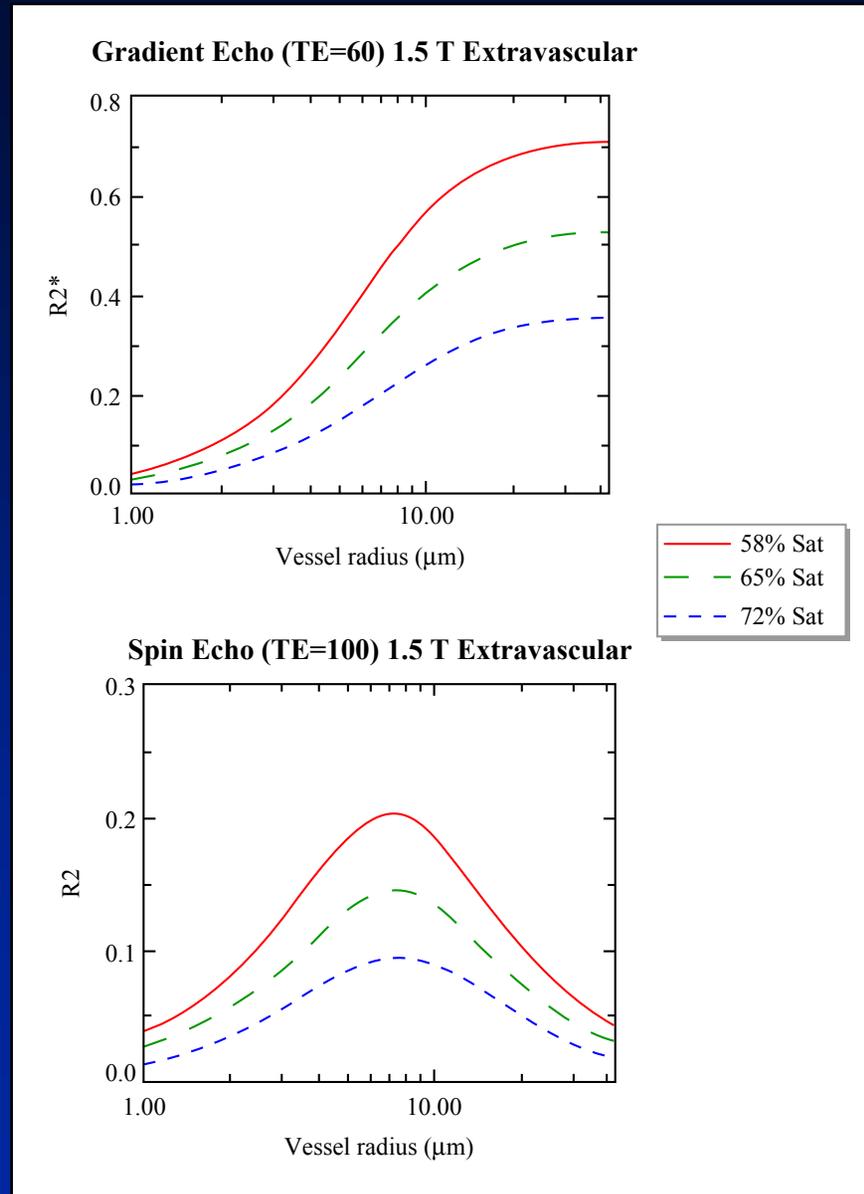


Figure by MIT OpenCourseWare.

# The B-W model at 1.5T: Extravascular vs Intra

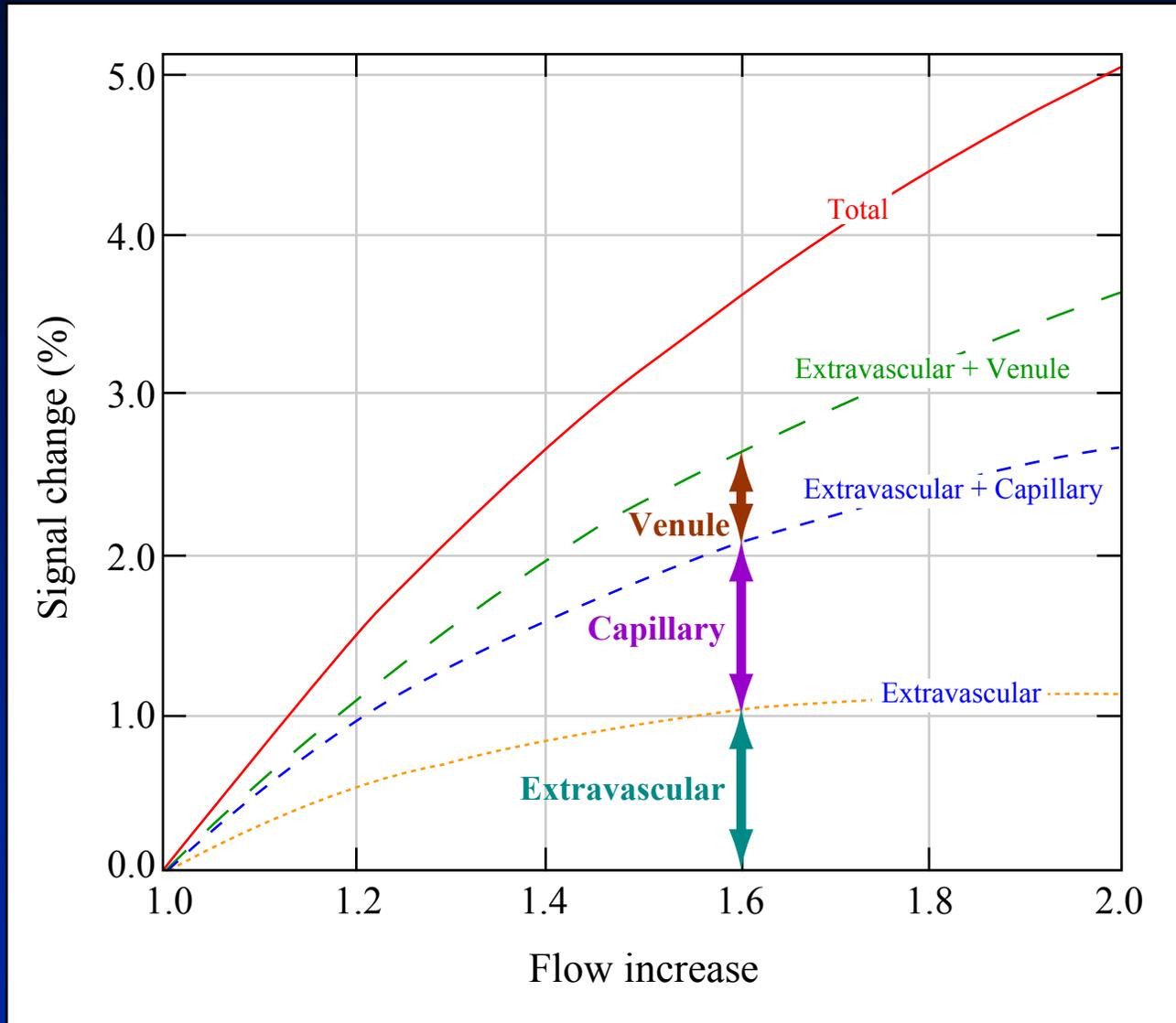


Figure by MIT OpenCourseWare.

At 1.5T 2/3 is intravascular

At 3T, 1/2 is intravascular

# Tests of B-W model dephasing flowing spins

Add a bipolar diffusion gradient to grad echo  
BOLD to remove signal from flowing spins.

Range of flow velocities crushed can be adjusted

spoiling venule flow ( $>10\text{mm/s}$ ) eliminates 30% of  
BOLD

Spoiling capillary + venule flow ( $>0.5\text{mm/s}$ )  
eliminates 60% of signal

The last 30% of the signal must be  
extravascular...

# Effects of going to higher $B_0$

Blood T2s become short enough that activation makes the blood go from really dark to very dark.

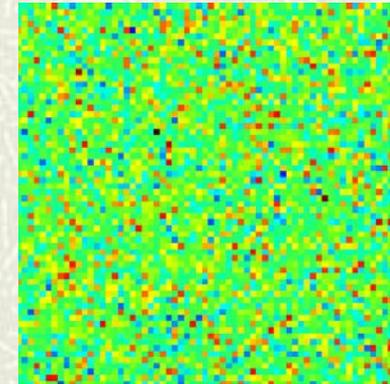
Velocity spoiling that would eliminate 2/3 of the BOLD effect at 1.5T only eliminates half at 3T and has no effect at 9.4T.

>> BOLD signal becomes more extravascular at high field.

# Measuring Noise Components

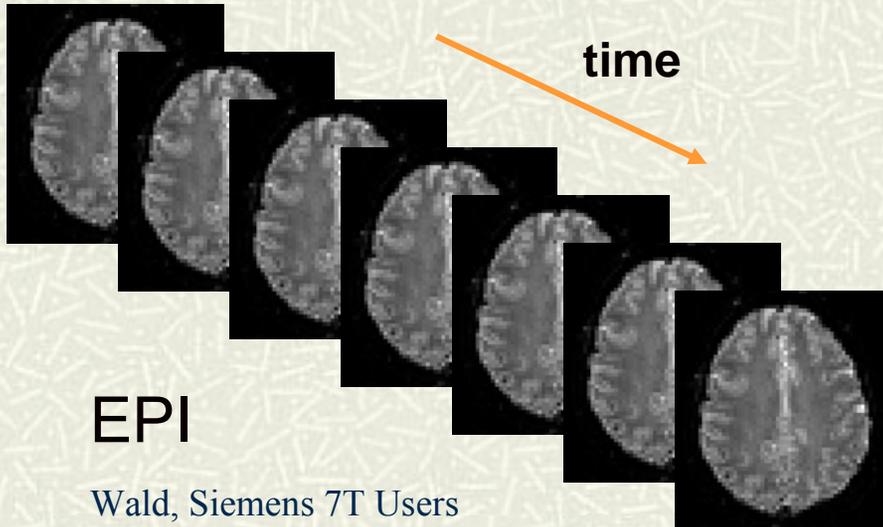
Raw Image Noise,  $S_0$

- EPI, no RF excitation



Time Series Noise,  $\text{SQRT}(s_0 + \sigma_p)$

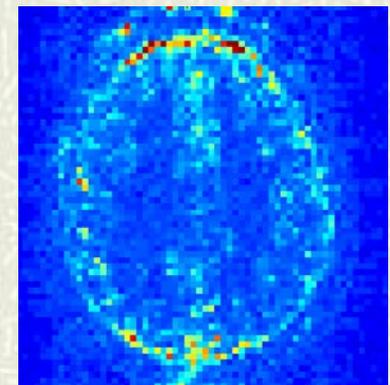
time



EPI

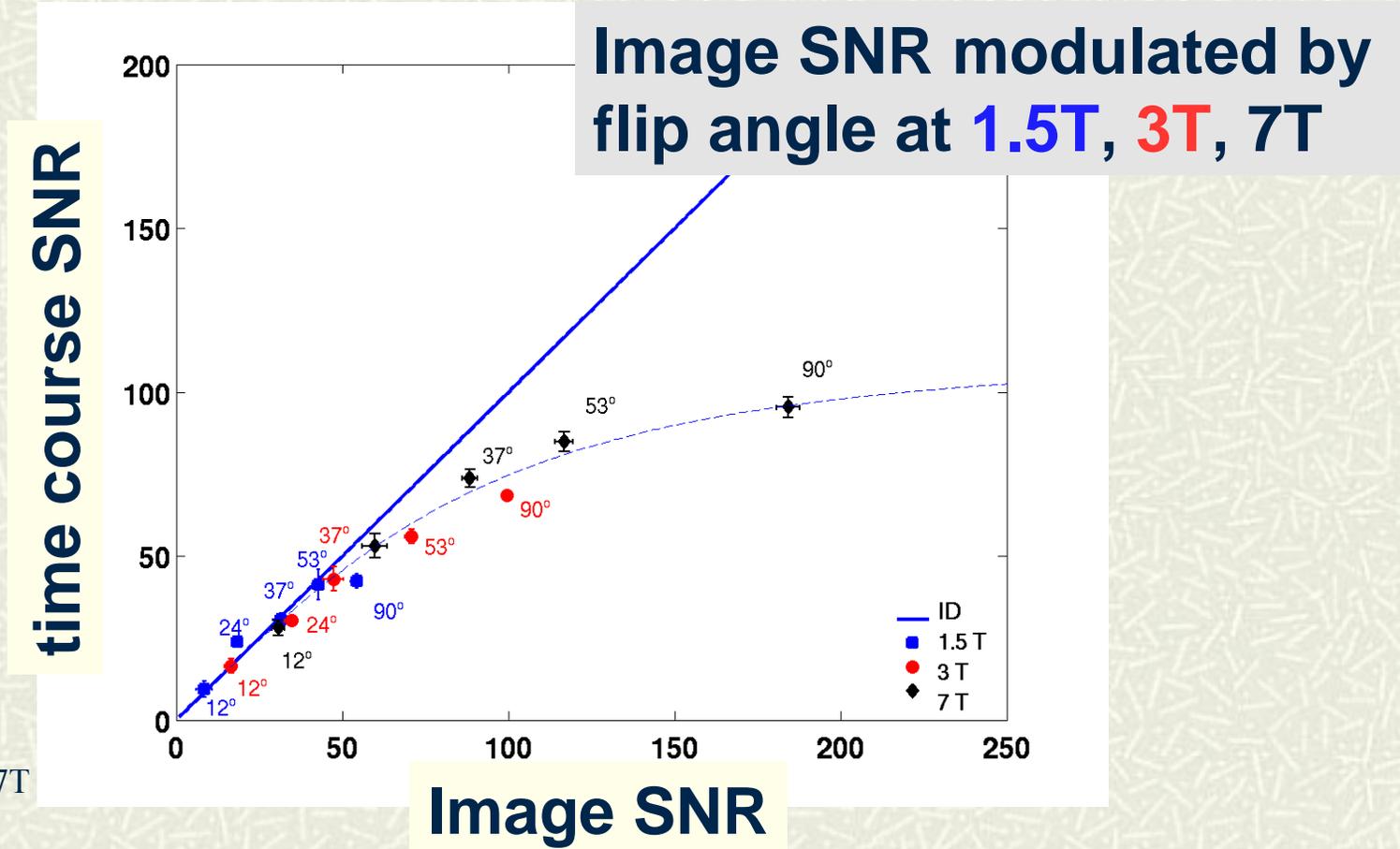


**ROI Analysis:** frontal, parietal and occipital gray matter



# Physiologic noise in fMRI timecourse

Triantafyllou et al. "Comparison of physiological noise at 1.5 T, 3 T and 7 T and optimization of fMRI acquisition parameters."  
Neuroimage. 2005 May 15;26(1):243-50

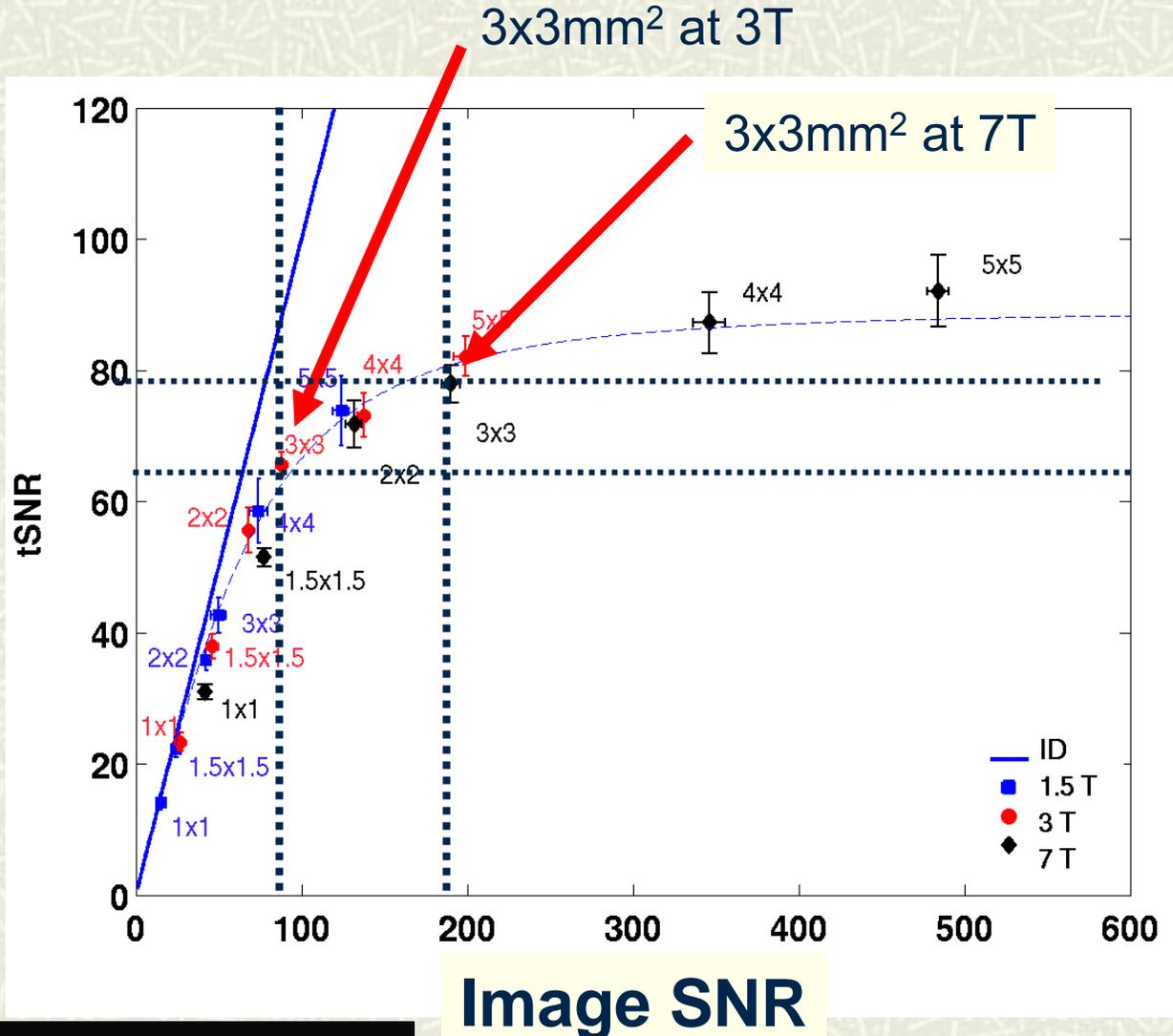


Wald, Siemens 7T Meeting 2005

Courtesy Elsevier, Inc., <http://www.sciencedirect.com>. Used with permission.

# Image SNR modulated by image resolution at 1.5T, 3T, 7T

time course SNR



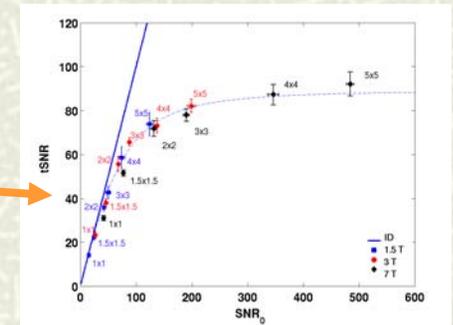
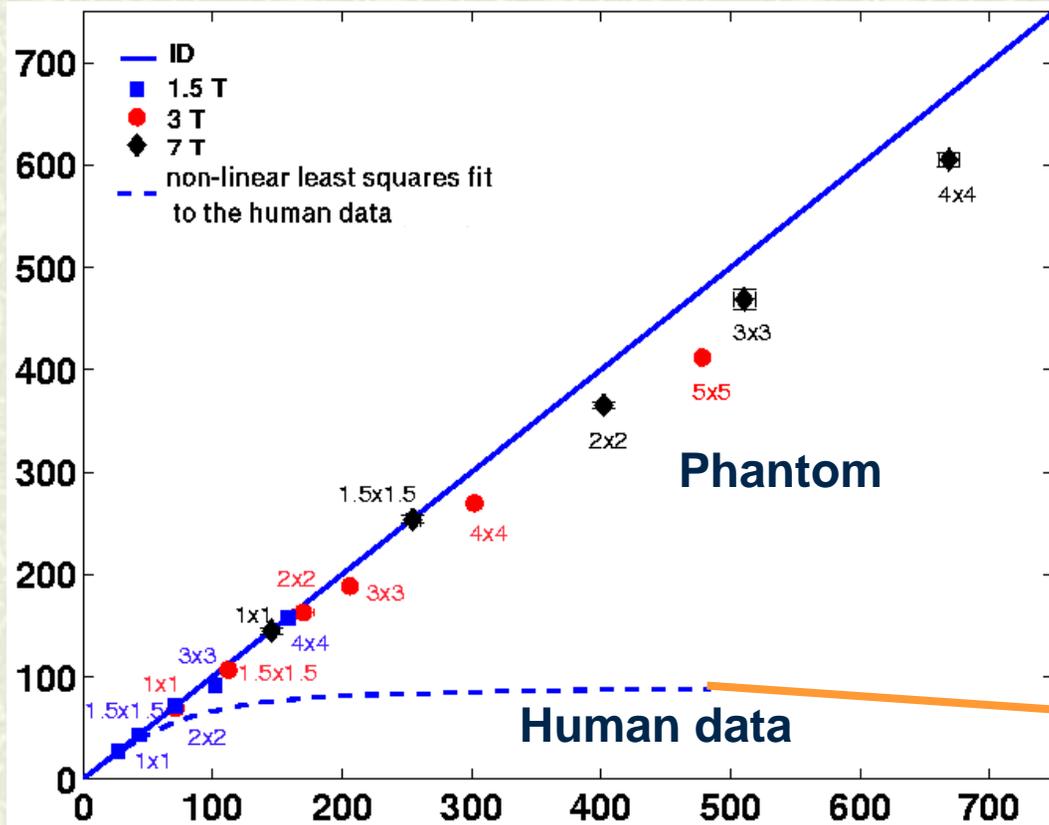
Wald, Siemens 7T Users

Lesson: keep image SNR below ~100

# Physiologic noise in fMRI timecourse

Image SNR modulated by resolution at 1.5T, 3T, 7T

time course SNR

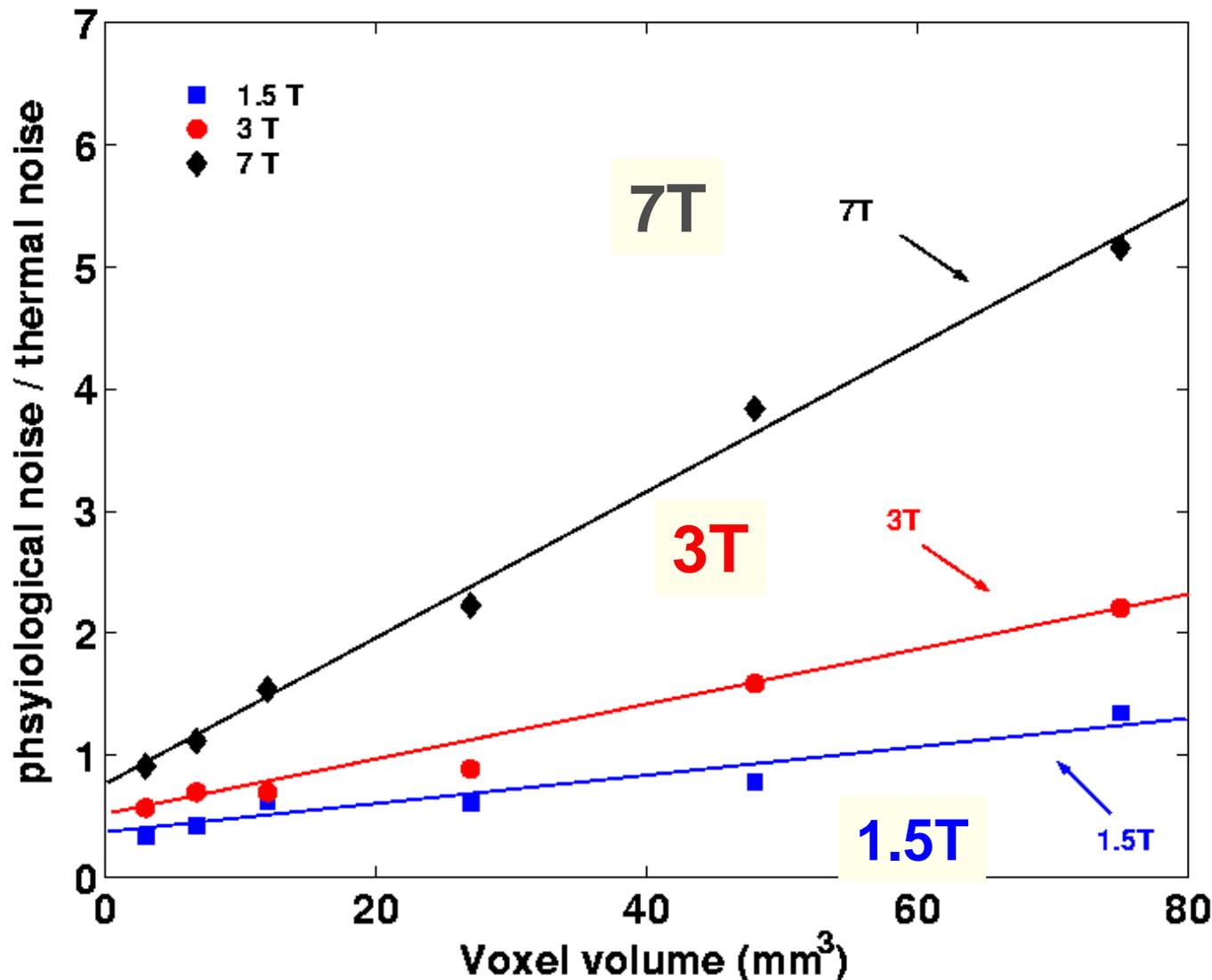


Wald, Siemens 7T Users Meeting 2005

Image SNR

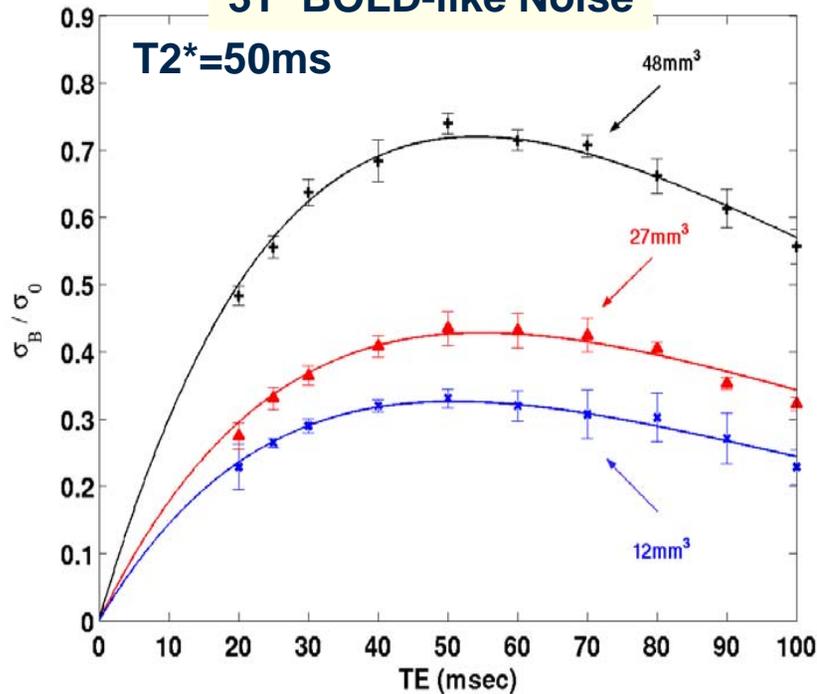
Courtesy Elsevier, Inc., <http://www.sciencedirect.com>. Used with permission.

# High resolution fMRI is needed at 7T to gain tSNR over 3T...

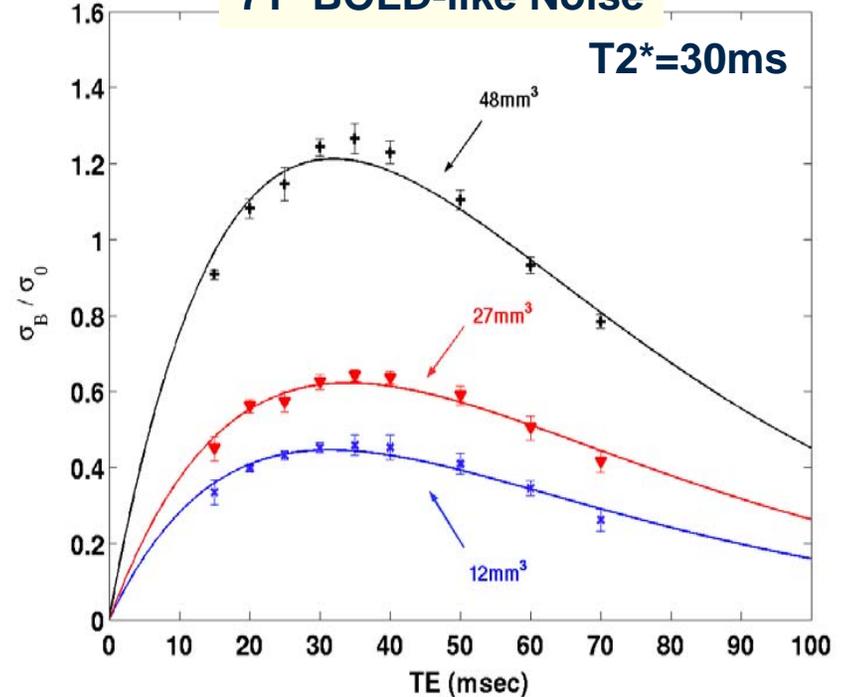


# Physiologic noise is “BOLD noise” dominated at 7T

### 3T BOLD-like Noise

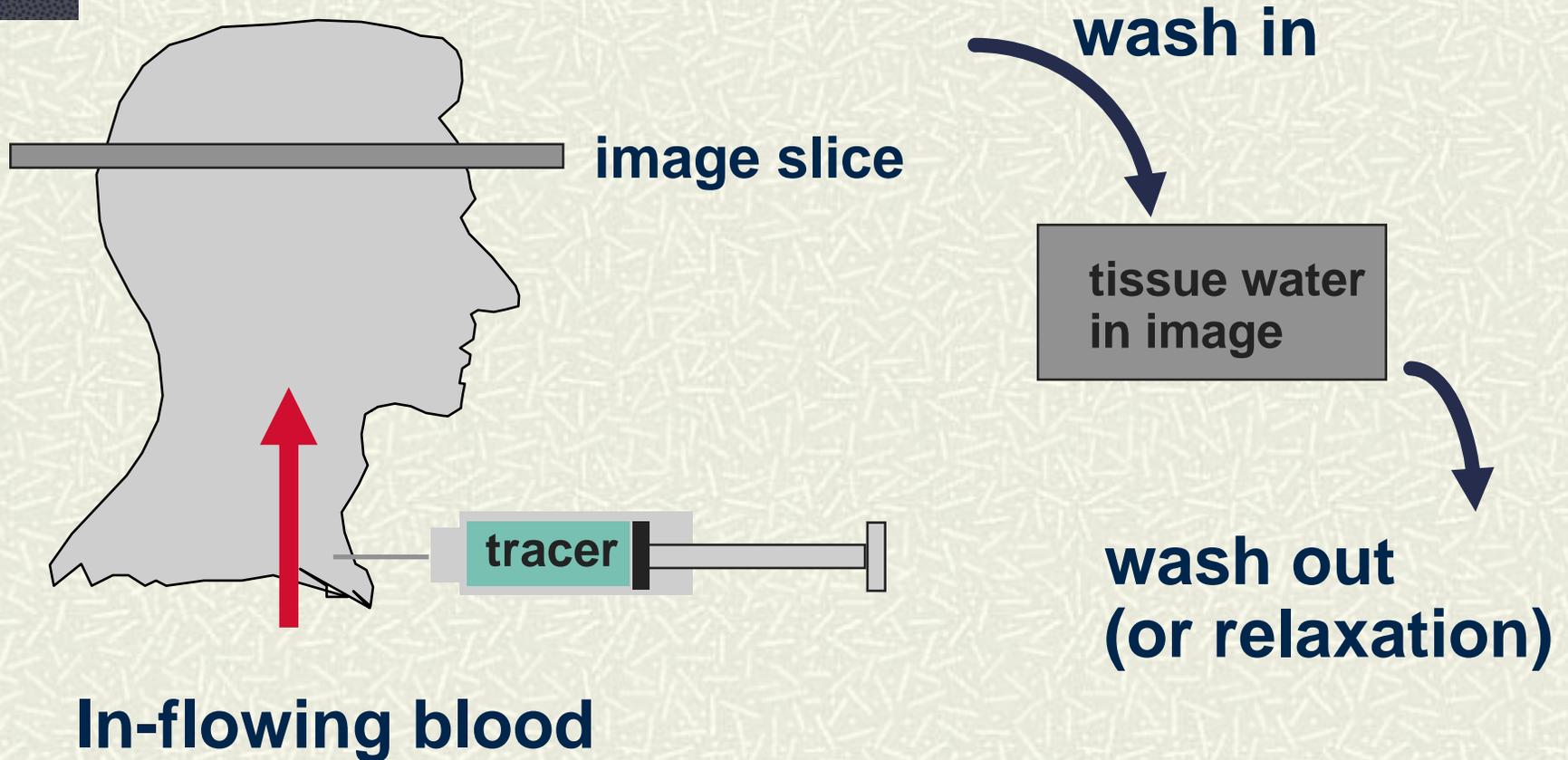


### 7T BOLD-like Noise



Courtesy Elsevier, Inc., <http://www.sciencedirect.com>. Used with permission.

# Perfusion Seq. for direct flow measures



# Bolus Gd(DTPA) MR CBV (Intravascular T2\* agent)

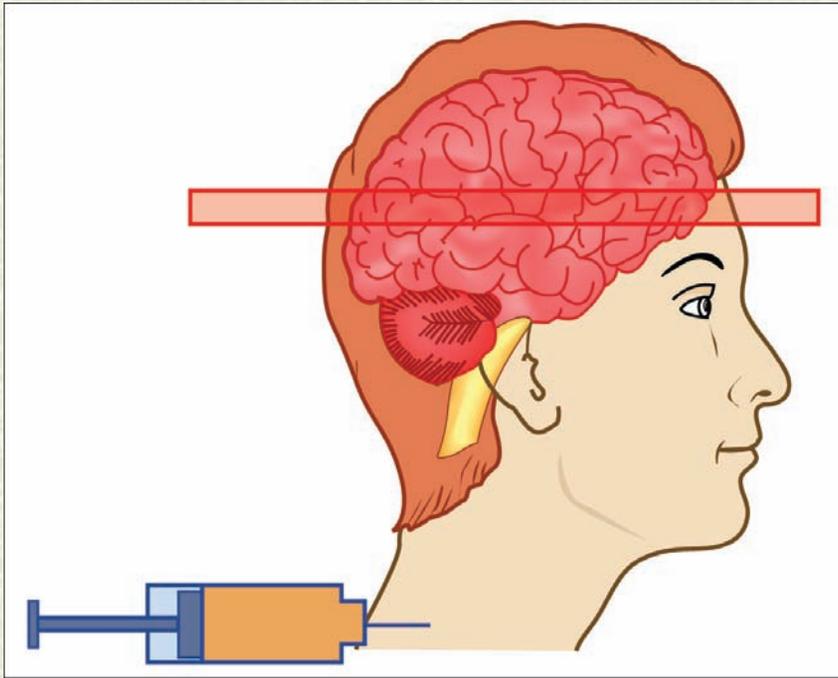
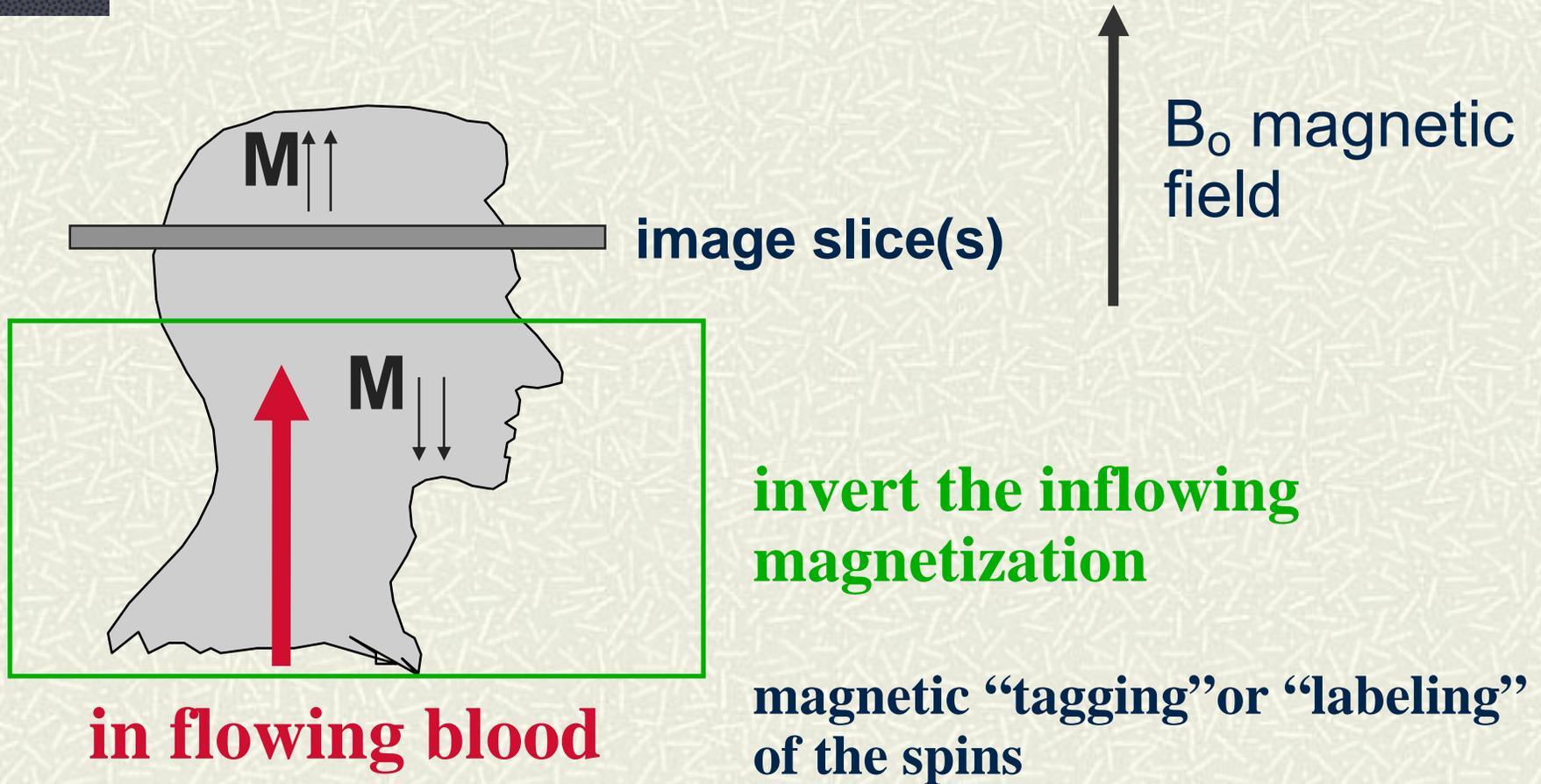


Figure by MIT OpenCourseWare.

- Agent stays in vessels (in brain)
- Integral of concentration timecourse = **rCBV**
- Flow is needed, but integral is flow independent
- To estimate flow, compare transit time and width to arterial input function.
- $T_1$  effects occur if BBB broken

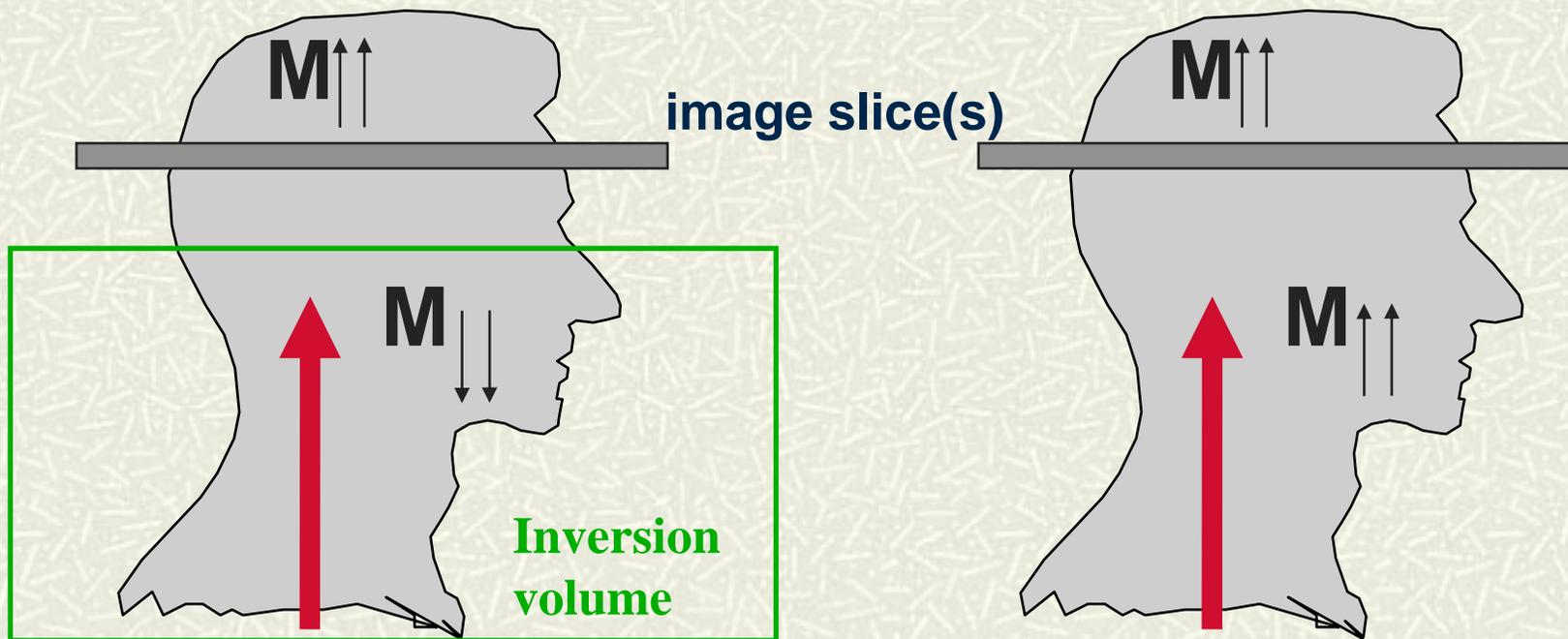
# Using water as a magnetic tracer: Arterial Spin Labeling



# How to create a magnetic tracer: Arterial Spin Labeling

“label”

“control”



**In-flowing blood**

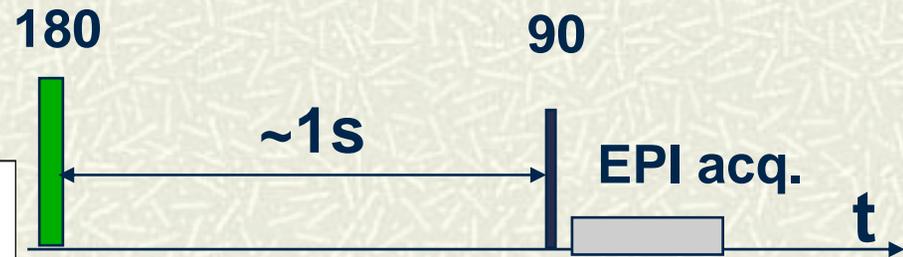
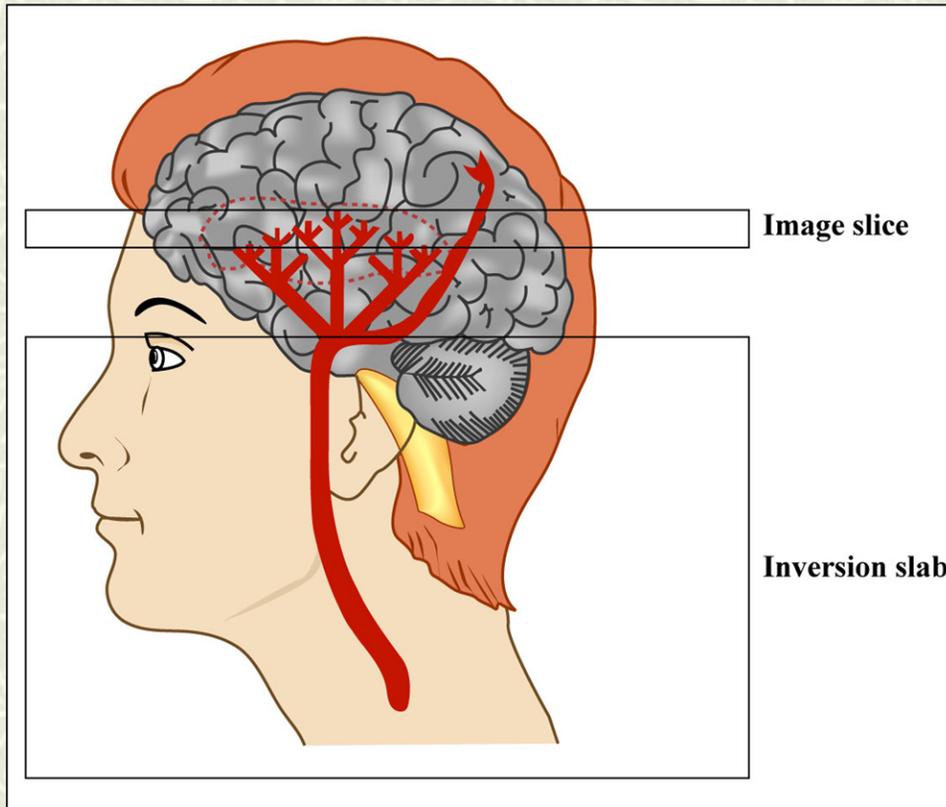
# ASL: subtract labeled image from a control image

Effect of the inverted blood water is  $< 4\%$   
reduction of normal signal. (on order of the %  
blood volume)

=> Requires the labeled image to be  
subtracted from a control acquisition.

Motion is a big problem...

# Pulsed Label ASL (PASL)



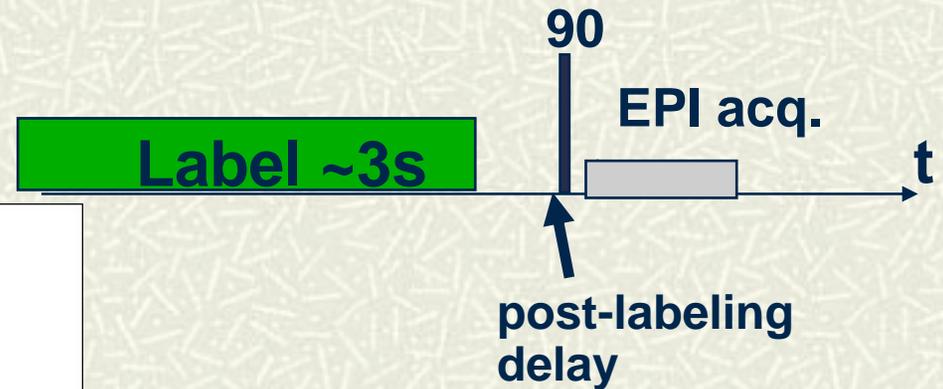
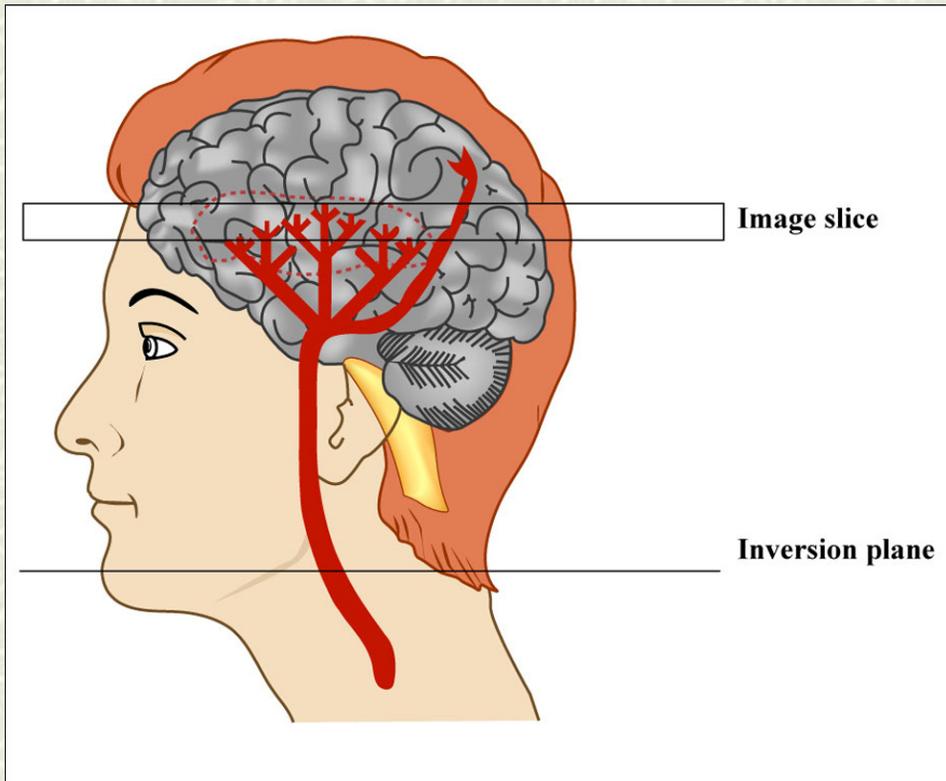
**$T_1$  is important**

**Thru slice arteries  
relatively dark**

**Large inversion  
slab is important**

Figure by MIT OpenCourseWare.

# Continuous label ASL (CASL)

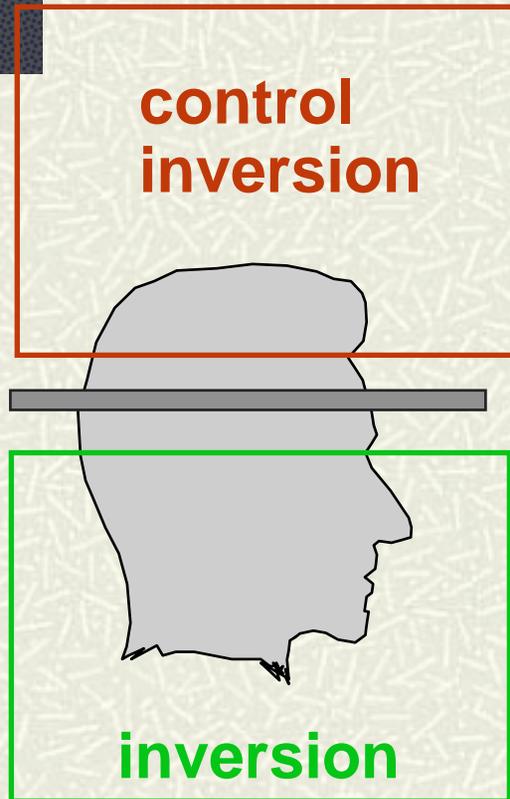


$T_1$  is important

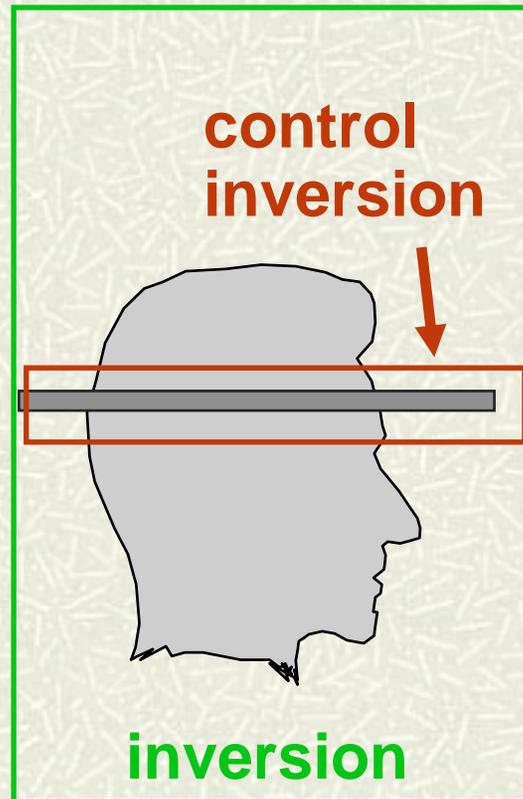
Thru slice arteries  
relatively dark

Less transit time  
sensitive.

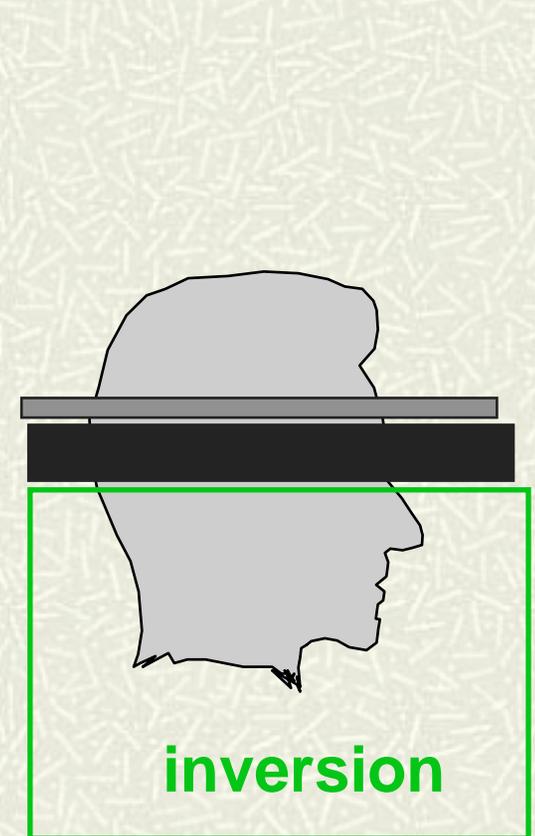
# Three flavors of pulsed ASL



**EPISTAR**

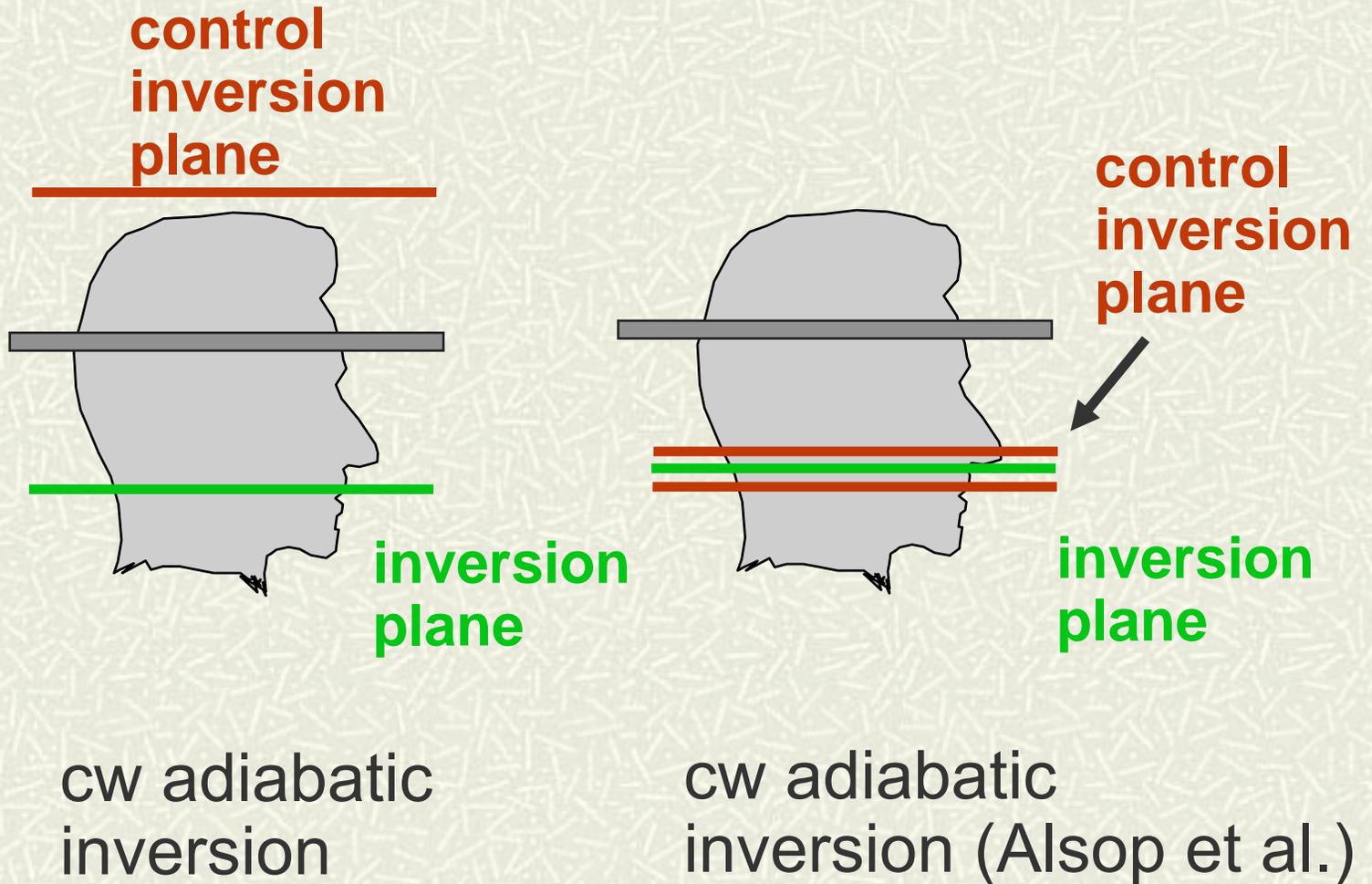


**FAIR**



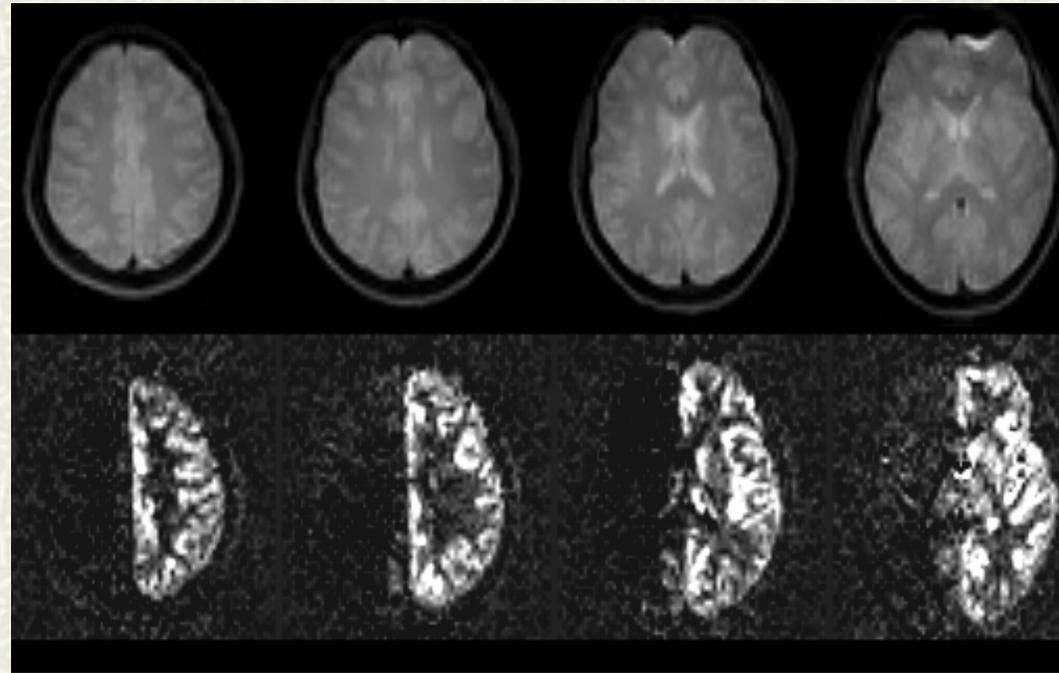
**QUIPPS**

# Continuous ASL



# 2 coil continuous ASL

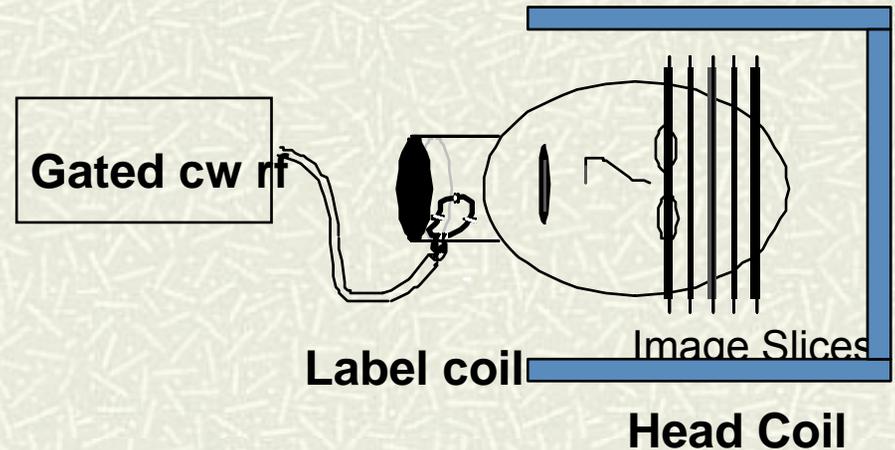
Perfusion territory imaging



**CONTROL**



**LABEL**



# ASL: confounds

- Labeling and control image should have same effect on static tissue to within 0.1%
- Magnetization Transfer: off resonance saturation
  - of image slice during the label but not the control. (esp. continuous ASL)
- Slice profile effects: Label and control have different slice profiles ( $\sim 1\%$ ). (esp. pulsed ASL)

# Be sure to...

## **Pulsed ASL (EPISTAR, FAIR, QUIPPS)**

**Use body coil for slab inversion.**

**Use inversion pulses with high quality spatial profiles**

**Use sufficient TI to ensure capillary flow**

**QUIPPS inferior sat band for transit insensitivity**

## **Continous ASL (single coil, two coil)**

**Use Alsop's control excitation or 2 coil method to allow multi-slice w/o MT.**

**Use sufficient labeling time to ensure capillary flow.**

**Post-labeling delay for transit insensitivity**

# The pros and cons

## **Pulsed ASL (FAIR, QUIPPS)**

**Better suited to fMRI**  
**Limited to axial slices.**  
**veins are labeled in FAIR**  
**Large # of slices cuts into  
labeling slab volume**  
**Label efficiency not velocity  
sensitive**  
**Label is near imaging slices**  
**Intrinsically less efficient  
per unit time (~30%)**

## **Continous ASL (single coil, two coil)**

**Arbitrary slice orientation**  
**Only arteries**  
**# slices doesn't limit label time**  
**Lower efficiency (15-25%) due to  
Laminar flow.**  
**~15ms transit delay per cm**  
**more SAR intensive**

# ASL at 7 Tesla

6 minute pASL flow image

1.56mm x 1.56mm x 4mm  
(at 3T we do 3mmx 3mm x 5mm)

Four times smaller voxel volumes!

