

# Last Week's Lab

## Printing chemical indicators with an inkjet printer...

Photographs of copper electrodes, organic transistors, and polymer LED displays removed due to copyright restrictions.

*PLED Display from  
Philips Research, 2004*

Copper electrodes → **Circuits** ← Organic transistors      Polymer LEDs → **Displays**

*J.S. Kang et al, J Mater Sci: Mater  
Electron, vol 21 (2010)*

*S. Chung et al, Jpn. J. Appl.  
Phys., vol. 50 (2011)*

*B. -J. de Gans et al, Adv.  
Mat., vol. 16 (2004)*

**... a wide range of other functional materials can be printed as well!**

# Nanomaker

## Lab #6: PDMS/Glass Microfluidics

Optical micrograph of the microfluidic comparator chip removed due to copyright restrictions.

Refer to: Fig. 3A in Thorsen, T., S. J. Maerkl, et al. "Microfluidic Large-Scale Integration." *Science* 298, no. 5593 (2002): 580–84.

# **Polydimethylsiloxane (PDMS)**

**PDMS Microfluidics**

**Navier-Stokes' Equation**

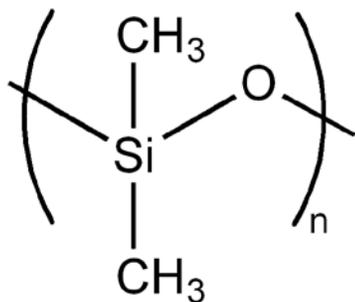
# Polydimethylsiloxane (PDMS)

Photo of silly putty removed due to copyright restrictions.



Photo courtesy of [Achim Hering](#) on Wikimedia Commons.

Silly Putty



Silicone sealant



This image is in the public domain.

Defoaming agent for foods



Photo courtesy of [oskay](#) on Flickr.

Transparent encapsulant for LEDs

- **Strong, flexible Si-O-Si backbone**
- **Low intermolecular force between CH<sub>3</sub> groups – low surface tension, allowing it to fit into small gaps**

# Nanoreplication Using PDMS

Process diagram of "Microcontact Printing" removed due to copyright restrictions.  
Refer to [article](#), page 42.

The PDMS precursor (Sylgard 184 and curing agent) can be poured over a pattern, left to solidify, and peeled off as a negative copy of the pattern.

**Images from:** G. Whitesides and J. Christopher Love, *Scientific American* sp **17**, 12 - 21 (2007)

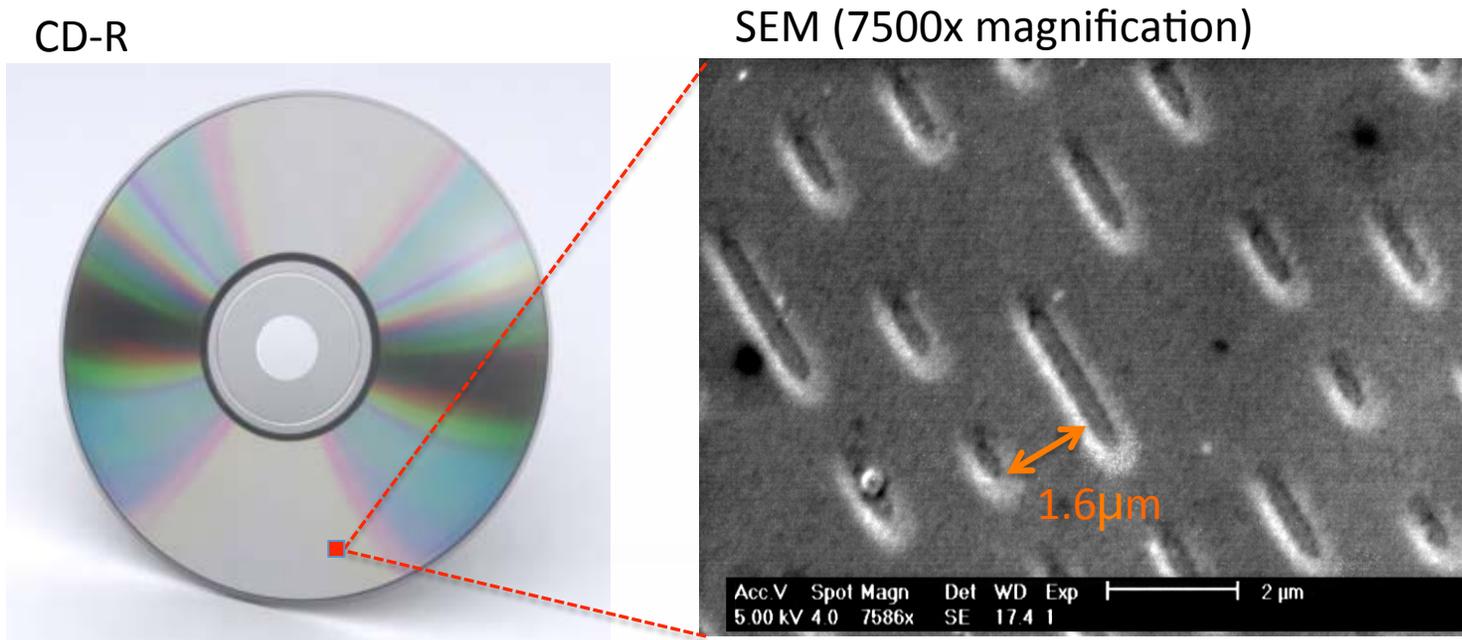
# Nanoprinting Using PDMS

Process diagram of "Making an Electric Stamp" removed due to copyright restrictions.  
Refer to [article](#), page 42.

The PDMS negative can also be inked, just like a rubber stamp, and pressed against another surface to print the pattern.

**Images from:** G. Whitesides and J. Christopher Love, *Scientific American* sp **17**, 12 - 21 (2007)

# PDMS Stamping Example: Compact Disk

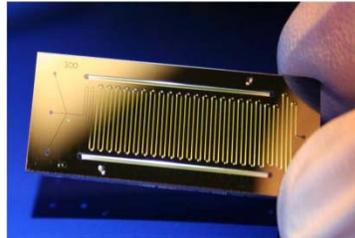
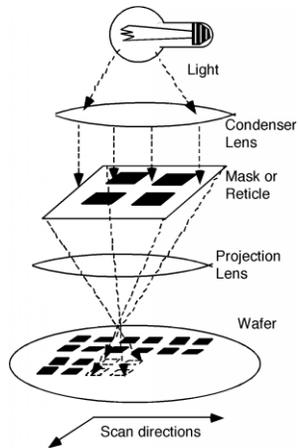


- A CD is made up of a spiral track that is 1.6 $\mu\text{m}$  wide (total write area = 0.0025m<sup>2</sup>)
- Total length of track is 1.54km (0.96 miles)
- Optical diffraction from the tightly-spaced adjacent tracks in the spiral are what produce the lovely rainbow pattern.

- The PDMS precursor can easily conform to the surface to replicate the pits of the CD, and cure to form a rubber stamp.
- Diffraction from the stamp is easy to observe, and can be distorted by stretching the PDMS

Polydimethylsiloxane (PDMS)  
**PDMS Microfluidics**  
Navier-Stokes' Equation

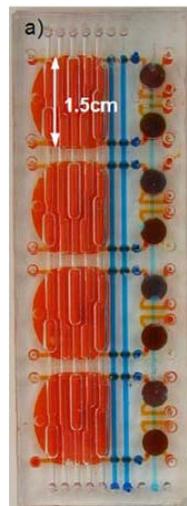
# Varieties of Microfluidics



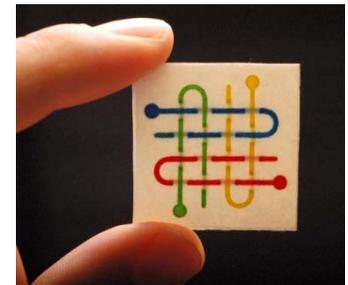
Glass or Silicon microfluidics, patterned using photolithography



Inkjet printed microfluidics in Shrinky Dinks (polystyrene) and Silicone rubber



Milled microfluidics in Polycarbonate



Printed wax microfluidics on filter paper

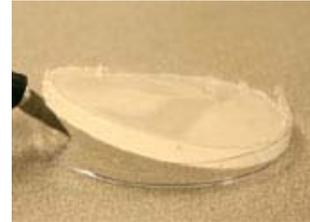
# Fabrication Process



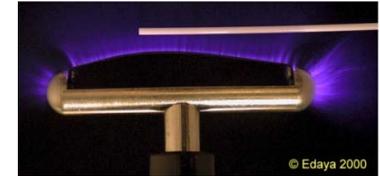
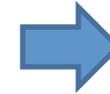
Design



Print wax  
microfluidic  
channels on  
*transparency*

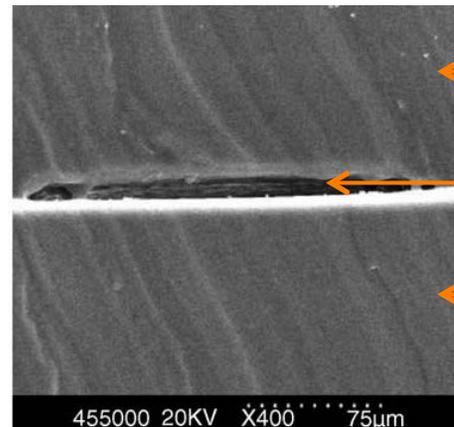


Pour PDMS  
precursor onto  
transparency,  
allow to cure



Courtesy of Edaya. Used with permission.

Corona treat  
PDMS and bond  
to glass slide



← PDMS

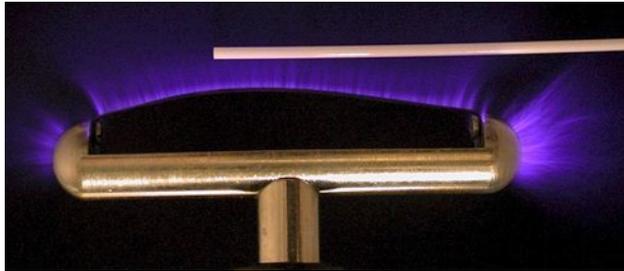
← Microfluidic channel

← PDMS (replaced by glass slide in our process)

Courtesy of Elsevier, Inc., <http://www.sciencedirect.com>. Used with permission.

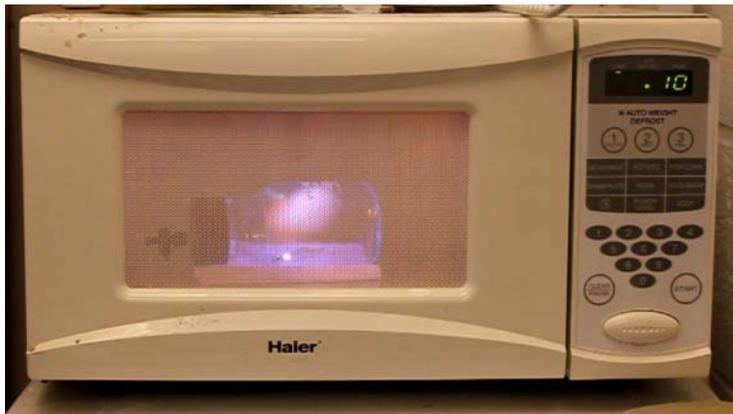
*N. Bao et al, J of Chromatography  
A, vol 1089 (2005)*

# Corona Treatment



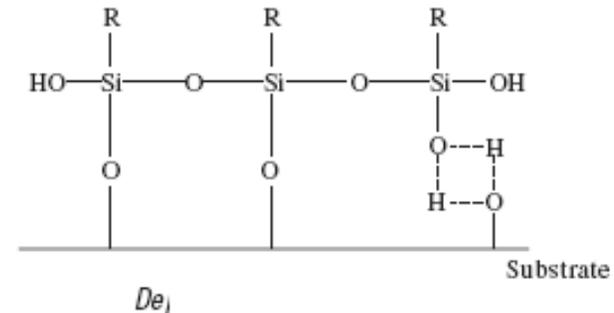
Courtesy of Edaya. Used with permission.

**Corona:** High voltage generates ionized gas, ozone ( $O_3$ ), and UV light



A plasma can also be generated in a microwave oven

## Surface modification and bonding



## Corona turns the surface of PDMS into glass

-Methyl groups get knocked off via energy from UV, ion bombardment...

-OH groups attach to the Si-O backbone to form silanol groups (SiOH), the same as the surface of glass (and hydrophilic like glass)

-PDMS is now brought into contact with glass, and water is released as the two bond together

**Polydimethylsiloxane (PDMS)**  
**PDMS Microfluidics**  
**Navier-Stokes' Equation**

# Navier-Stokes' Equation

The Navier-Stokes' equation for incompressible flow:  
constant density everywhere

$$\rho \frac{dU}{dt} = \eta \nabla^2 U - \nabla P$$

$U$  = velocity

$P$  = pressure

$t$  = time

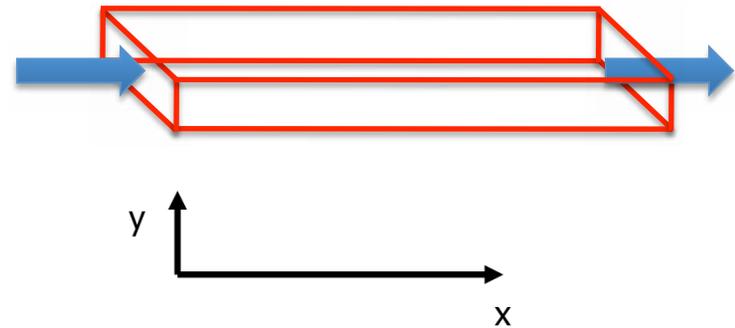
$\rho$  = fluid density ( $10^3$  kg/m<sup>3</sup> for water)

$\eta$  = Viscosity ( $10^{-3}$  Pa-s for water)

# Simplify Our Problem

- No time dependence
- Flow is constant in x-direction and zero in z-direction
- Pressure is only a function of x

$$\rho \frac{dU}{dt} = \eta \nabla^2 U - \nabla P$$



$$\frac{\partial^2 U_x}{\partial y^2} = \frac{K}{\eta}$$

$$\frac{dP}{dx} = K$$

# Poiseuille Flow

- Assume width  $\gg$  height
- Neglect entrance effect
- No slip boundary condition!

zero velocity relative to the boundary

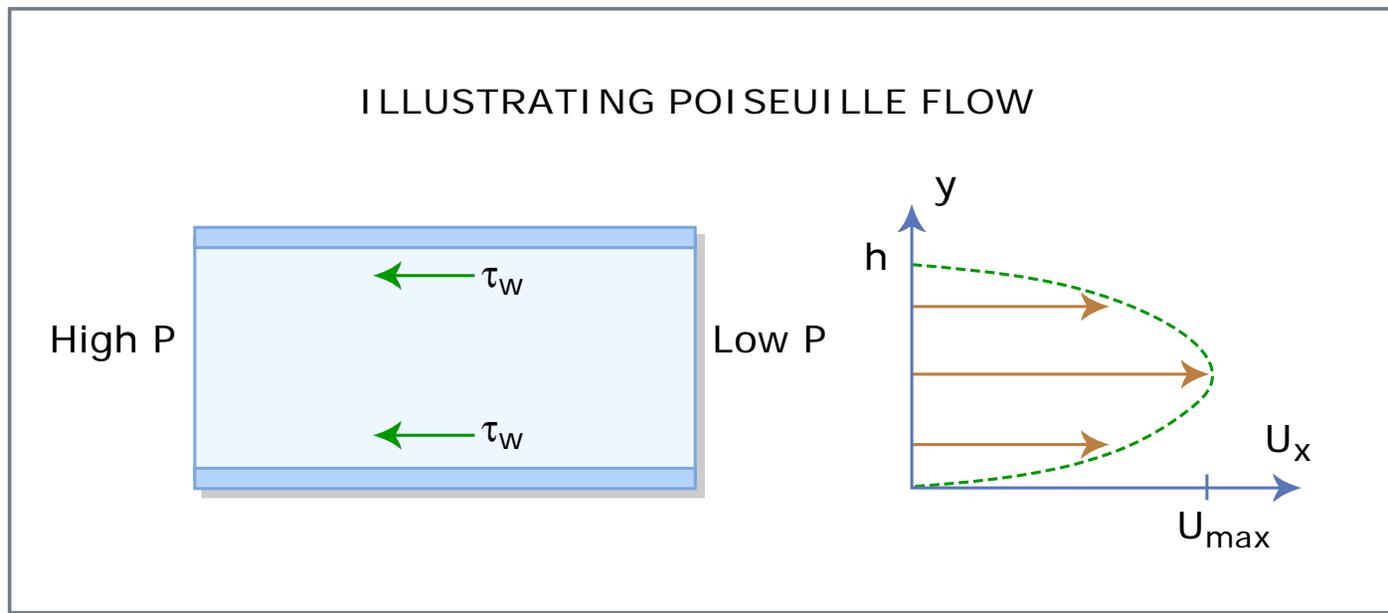
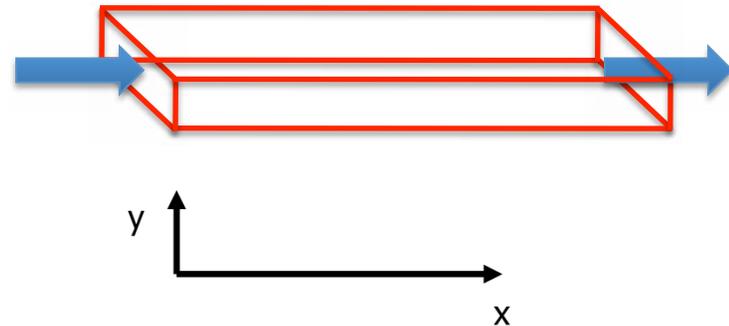


Figure by MIT OCW.

# Solution

- Parabolic profile: 
$$U_x = \frac{1}{2} [y(h - y)] K$$

- Maximum velocity: 
$$U_{max} = \frac{h^2}{8} K$$

$$\frac{dP}{dx} = K$$

- Average velocity: 
$$U_{ave} = \frac{2}{3} U_{max}$$

- Flow rate: 
$$Q = \frac{Wh^3}{12} K$$

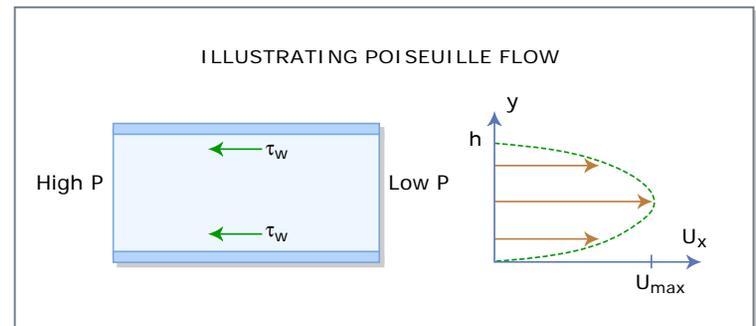
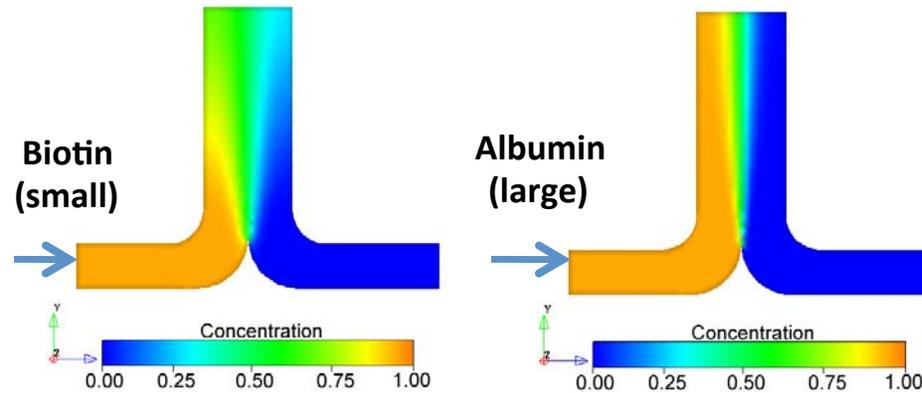


Figure by MIT OCW.



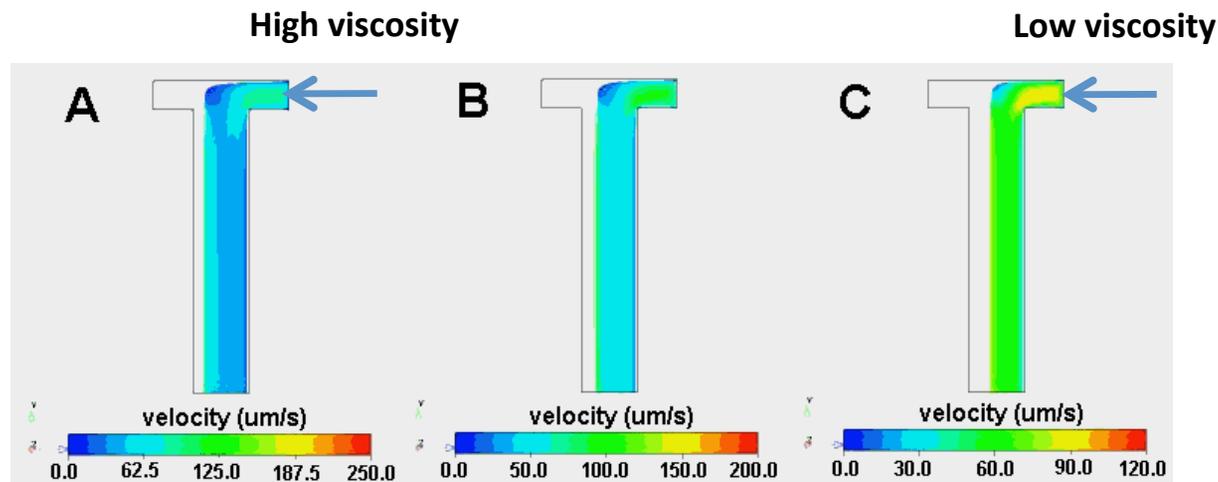
# Applications of Laminar Flow

## Separation using Diffusion



$$Re = \frac{\rho V L}{\mu}$$

## Viscosity and Channel Width



Yager Group, University of Washington

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