

- Box pleating history
 - Moosers train [Raymond McLain, 1967]
 - Black Forest Cuckoo Clock [Lang 1987]
- OPEN: universal folding of e.g.
polytetrahedra or polyoctahedra
from triangular grid?
- Maze folding examples
 - our print designs

- Meaning of NP-hardness:
 - doesn't mean anything about specific instances
 - about scaling of running time as problem size n grows
 - e.g. 8×8 Chess is "trivial"
 $n \times n$ Chess is EXP-hard
 \Rightarrow running time scales exponentially

- Simple fold hardness review:

- convert Partition instance (a_1, a_2, \dots, a_n) into equivalent simple-fold instance (polygon + creases)
 - \hookrightarrow solution for Partition exists
 - \hookleftarrow solution for simple folds exists

\Leftarrow vertical creases will bind otherwise

\Rightarrow fold creases between a_i & a_{i+1}
 when in different halves
 fold both vertical creases
 fold rest

- Flat foldability hardness review:
 - convert NAE triples into crease pattern
- (\Leftarrow) gadgets force NAE constraints
read T/F assignment off M/V assignment
- (\Rightarrow) verify gadgets do fold as needed
patch together (glue) foldings together

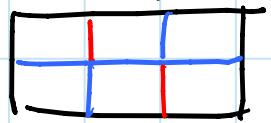
OPEN: Simpler proof?

[Tom Hull]

- NP-hardness even given M/V assignment:
[Bern & Hayes 1996]

Map folding: (nonsimple folds, unlike L2)

- horizontal & vertical creases
in rectangular paper



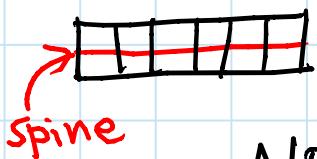
- given M/V assignment, does it fold flat?
- OPEN: polynomial? NP-hard?

[posed by Edmonds 1997]

$2 \times n$ has polynomial-time algorithm

[Demaine, Liu, Morgan 2012]

(from 6.849 project in 2010)



- NEWS labeling: for each vertex, mark which emanating crease is different

- top edge view: top of folded map
= N & S sides of unfolded map

- nested pairings from map spine

- N = left turn



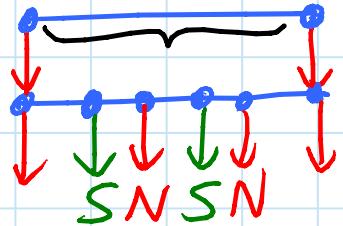
- E = "in"



- S = right turn

- W = "out"

- ray diagram: [Charlton & Zhou, 6.849, 2007]
 - follow map spine (merging N & S sides)
 - y coord. = "nesting depth"; x coord. flexible
 - E = down turn ↘/↙ - W = up turn ↗/↗
 - N & S shoot downward rays ↘_N ↗_S
 - rules: (equivalent to flat folding)
 - spine doesn't self-intersect
 - N rays must hit N rays or go to ∞
 - S rays ditto
 - constrained spine segment (with no view to infinity below it) have equal number of N & S vertices below it



- spaces between spine in ray diagram forms a tree structure
- "guess" this tree structure
(effectively trying them all)
using dynamic programming

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<http://ocw.mit.edu>

6.849 Geometric Folding Algorithms: Linkages, Origami, Polyhedra
Fall 2012

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