

Ray Tracing



[Henrik Wann Jensen](#)

Wojciech Matusik, MIT EECS

Many slides from Jaakko Lehtinen and Fredo Durand

Ray Casting

For every pixel

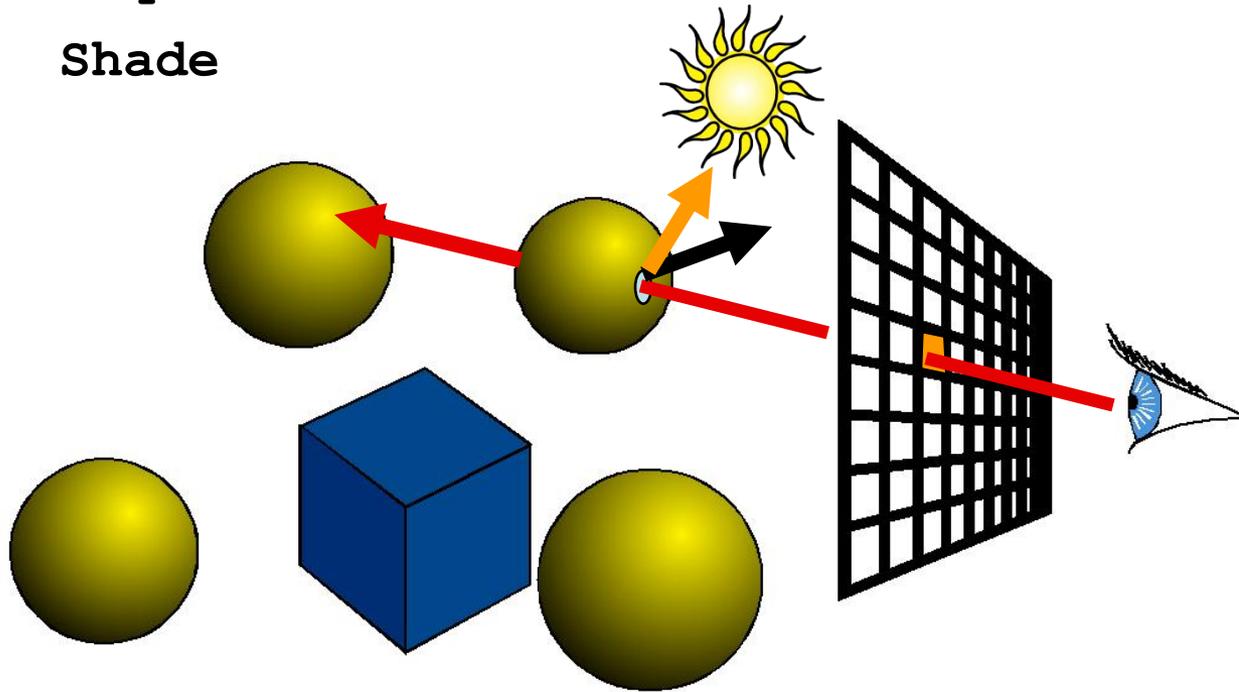
Construct a ray from the eye

For every object in the scene

Find intersection with the ray

Keep if closest

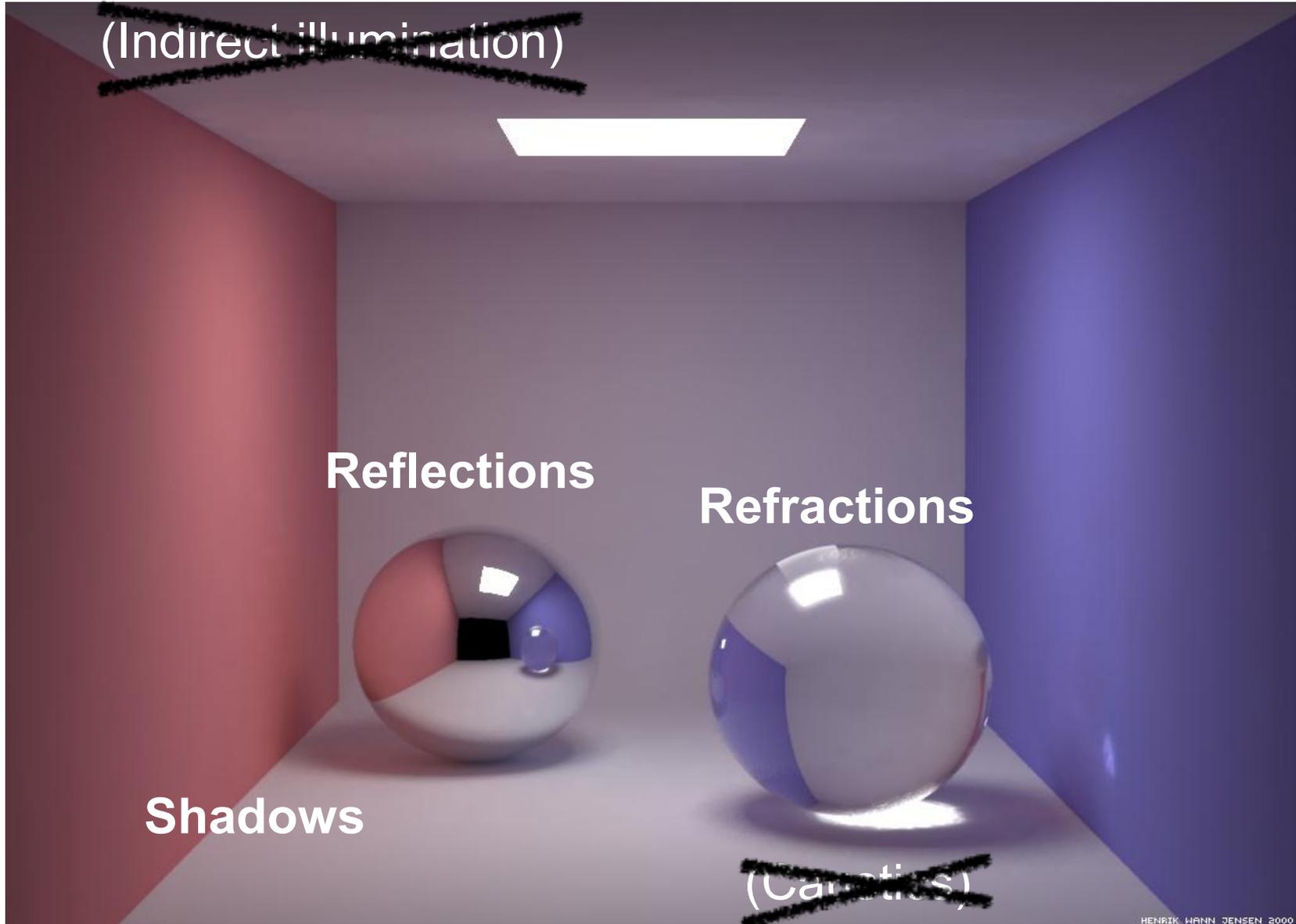
Shade



Earlier

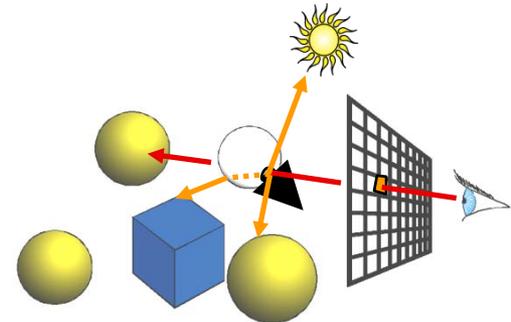
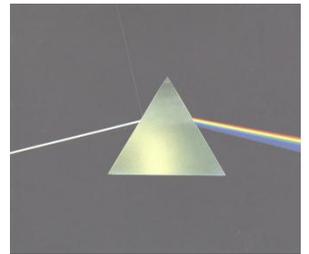
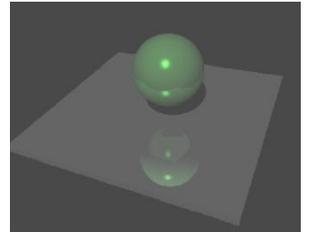
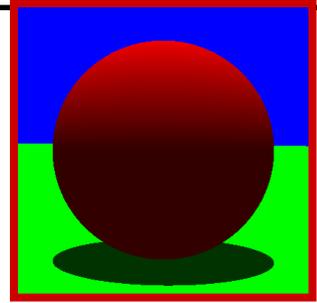
- Camera definitions
 - Perspective and orthographic
 - View coordinate system $[-1,1]$
 - field of view, aspect ratio, etc.
- Ray representation
 - origin + $t * \text{direction}$
 - Generating rays based in image coordinates
- Ray-geometry intersection
 - Planes, spheres, triangles (barycentric coordinates)
 - CSG
 - Transformations

Today – Ray Tracing



Overview of Today

- Shadows
- Reflection
- Refraction
- Recursive Ray Tracing
 - “Hall of mirrors”



How Can We Add Shadows?

For every pixel

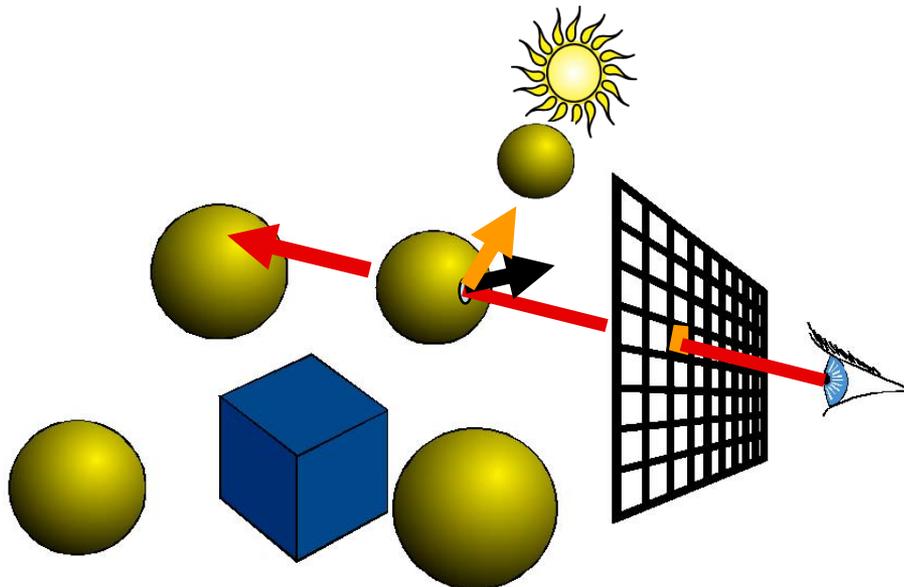
Construct a ray from the eye

For every object in the scene

Find intersection with the ray

Keep if closest

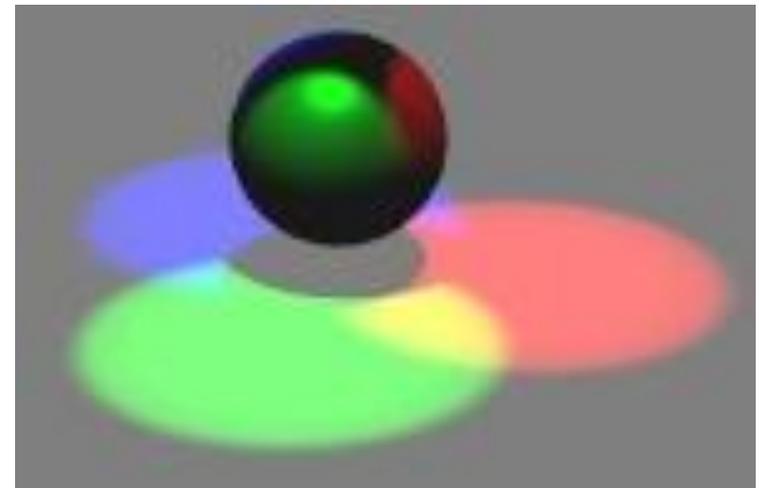
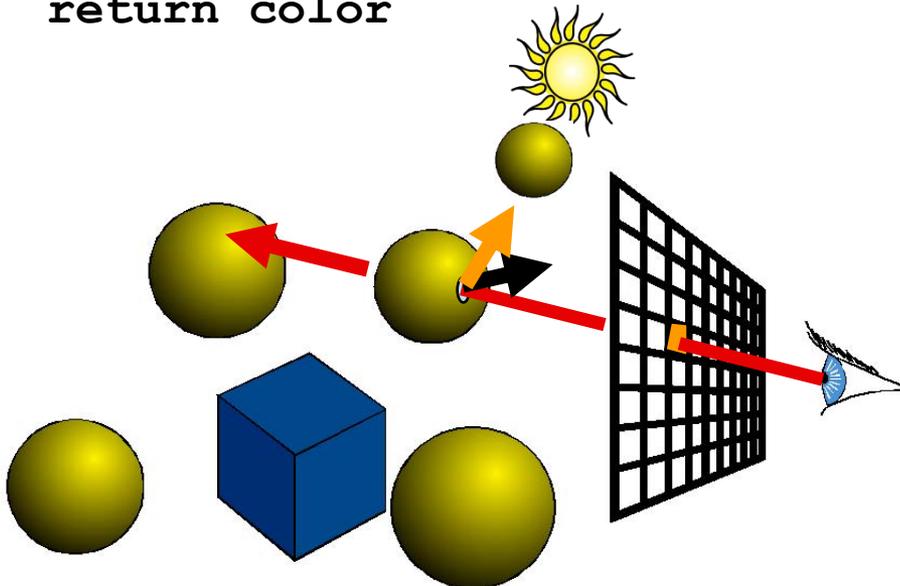
Shade



How Can We Add Shadows?

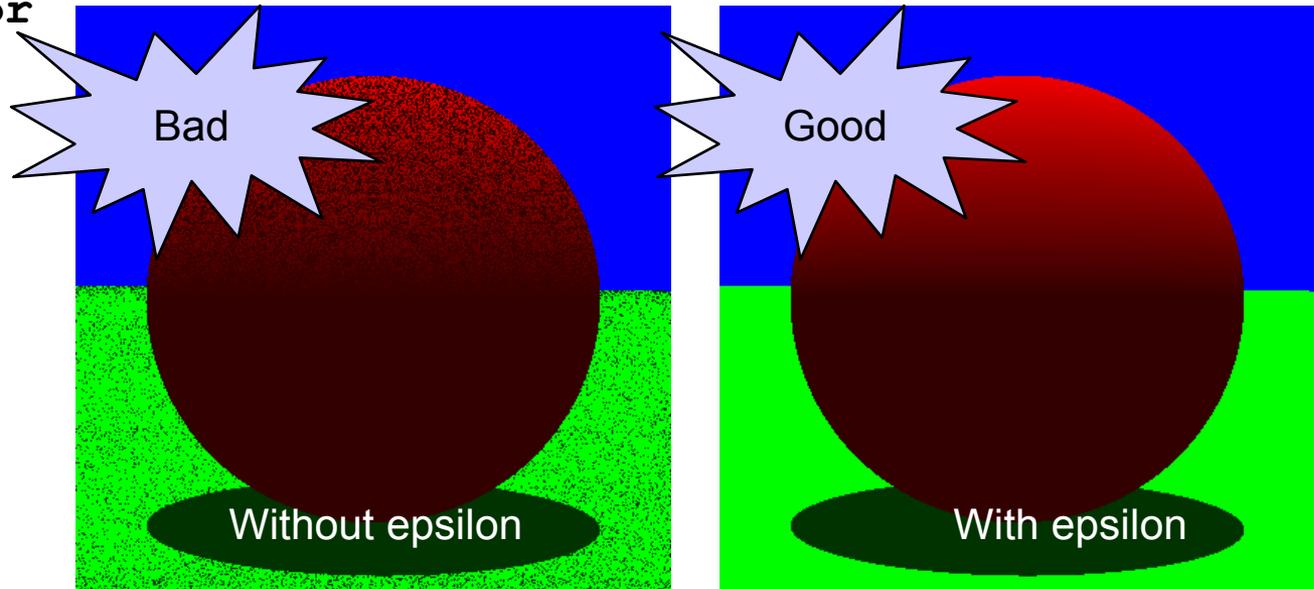
```
color = ambient*hit->getMaterial()->getDiffuseColor()
for every light
    Ray ray2(hitPoint, directionToLight)
    Hit hit2(distanceToLight, NULL, NULL)
    For every object
        object->intersect(ray2, hit2, 0)
    if (hit2->getT() = distanceToLight)
        color += hit->getMaterial()->Shade
            (ray, hit, directionToLight, lightColor)
return color
```

ambient = k_a diffuseColor = k_d



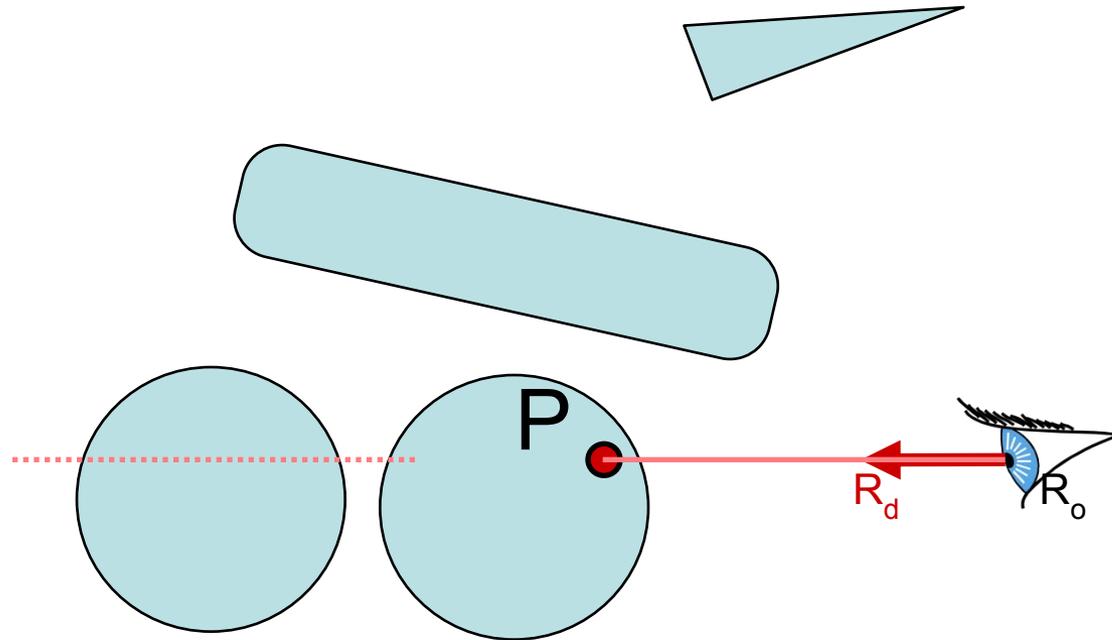
Problem: Self-Shadowing

```
color = ambient*hit->getMaterial()->getDiffuseColor()
for every light
  Ray ray2(hitPoint, directionToLight)
  Hit hit2(distanceToLight, NULL, NULL)
  For every object
    object->intersect(ray2, hit2, epsilon)
  if (hit2->getT() = distanceToLight)
    color += hit->getMaterial()->Shade
      (ray, hit, directionToLight, lightColor)
return color
```



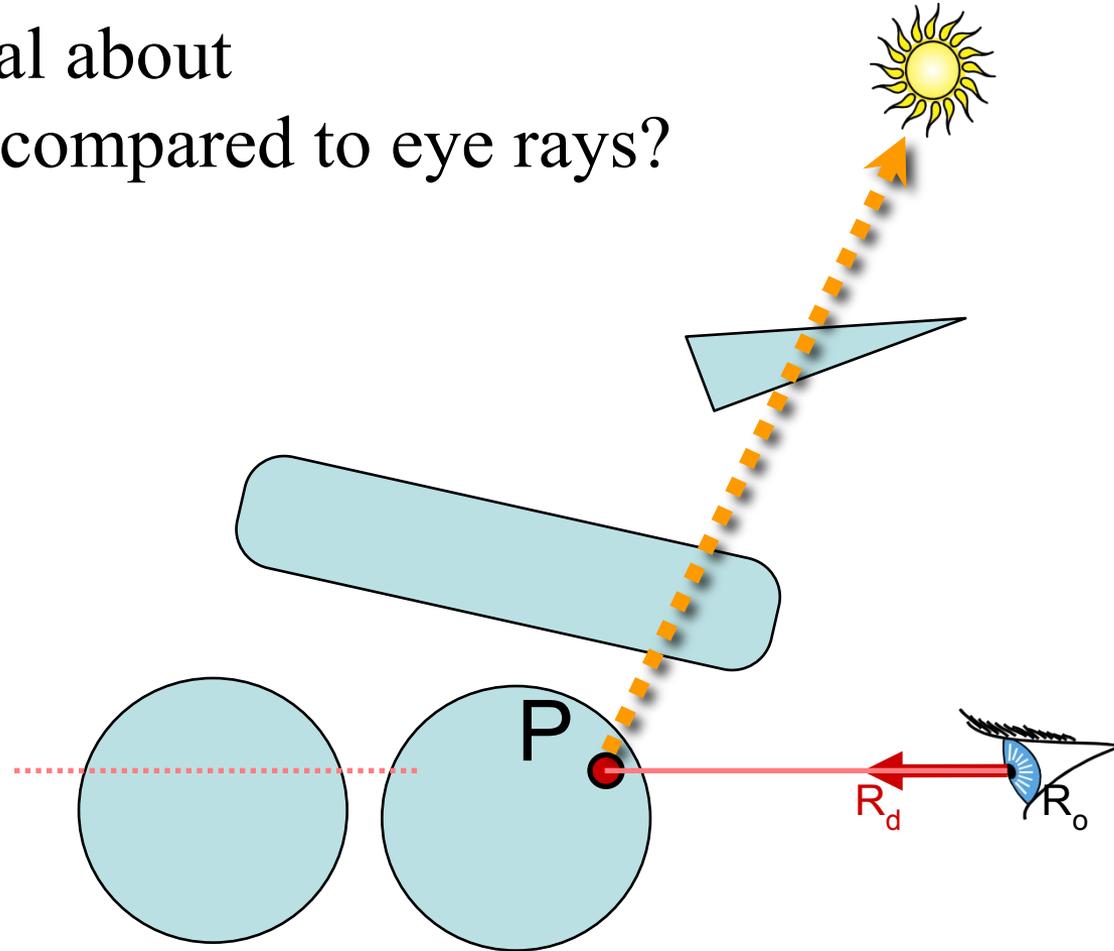
Let's Think About Shadow Rays

- What's special about shadow rays compared to eye rays?



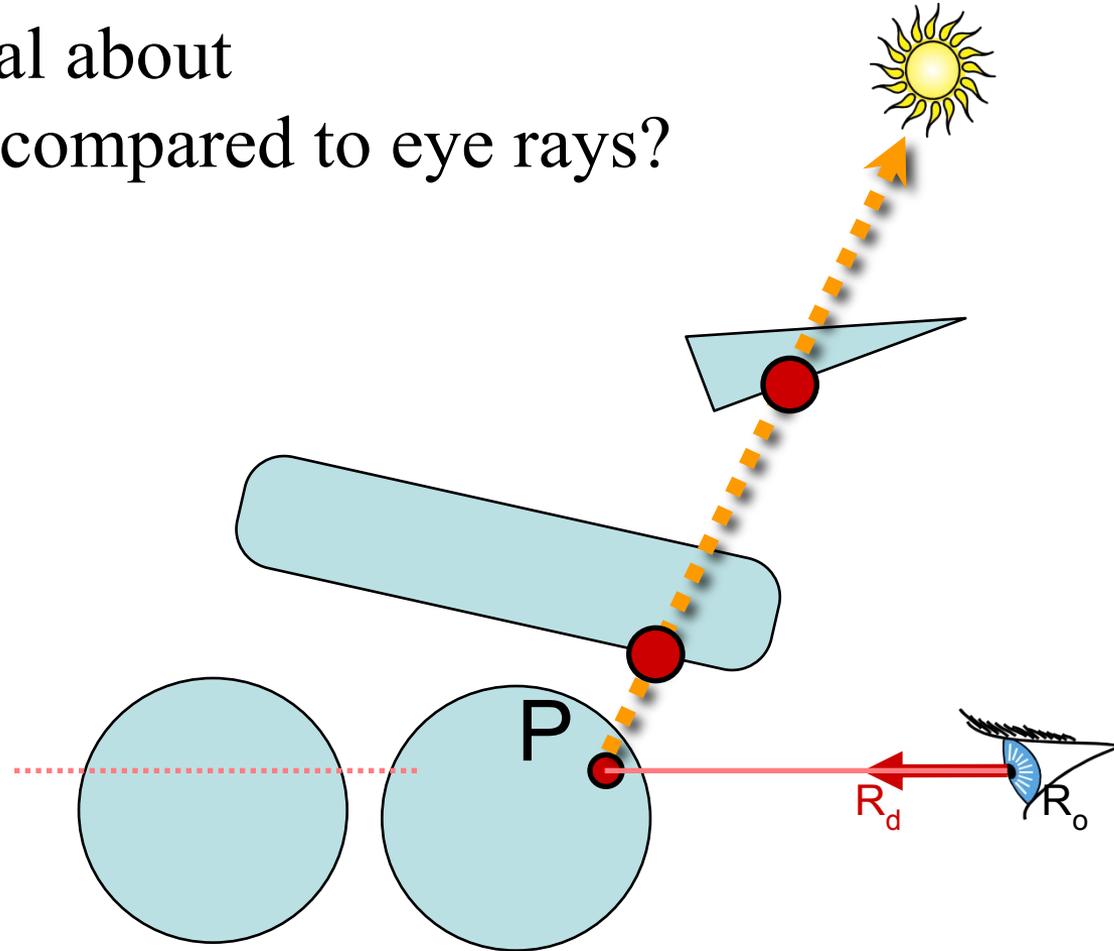
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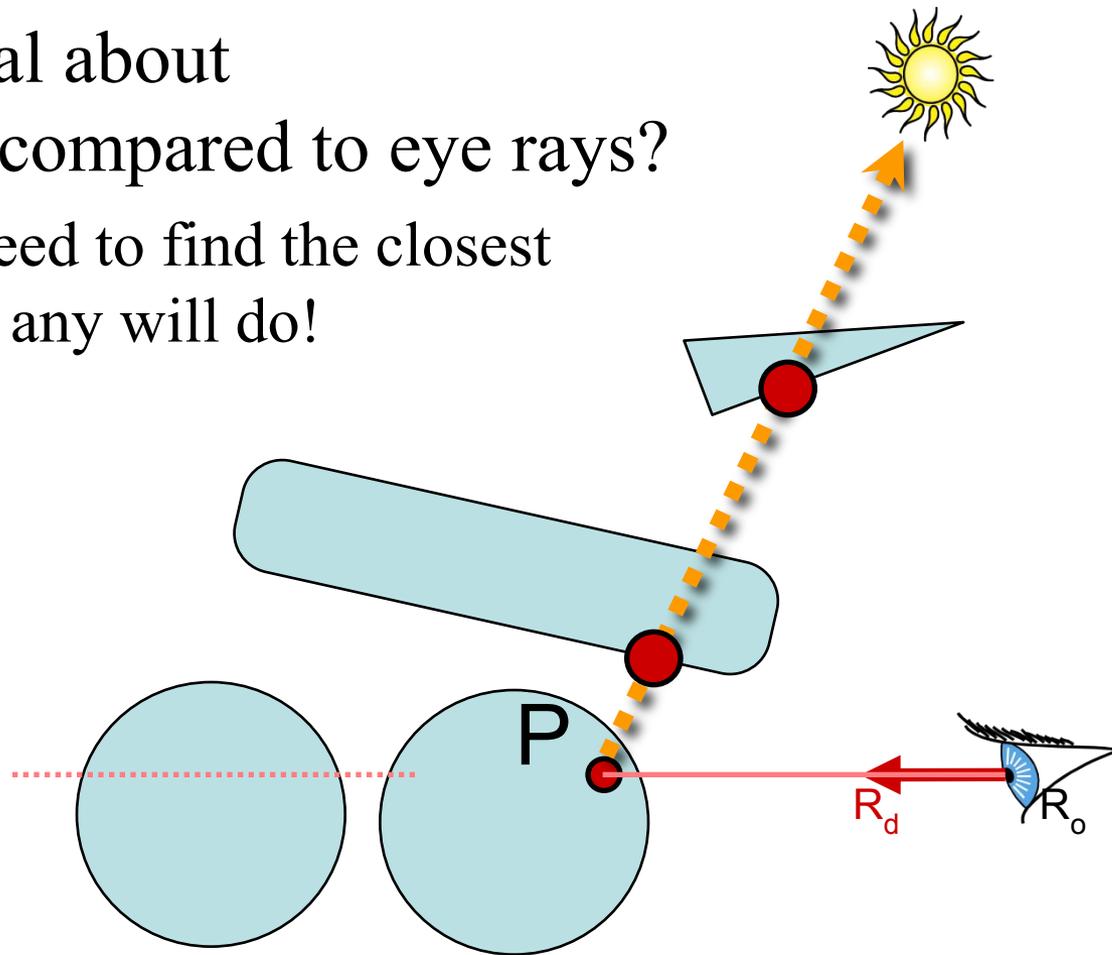
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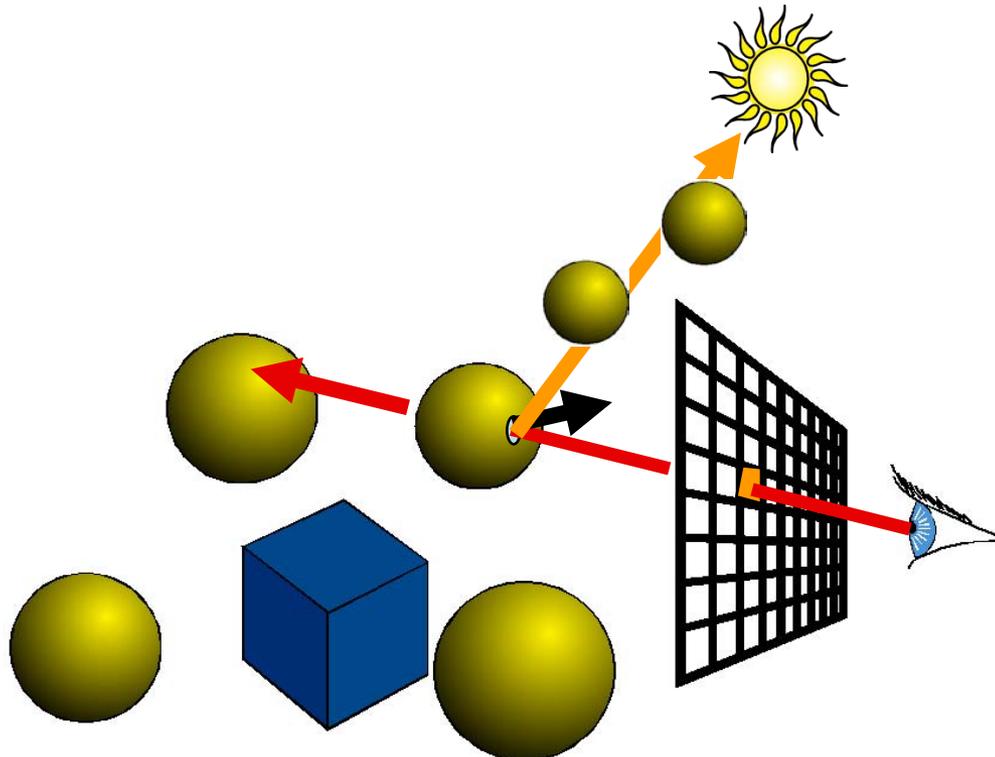
Let's Think About Shadow Rays

- What's special about shadow rays compared to eye rays?
 - We do not need to find the closest intersection, any will do!



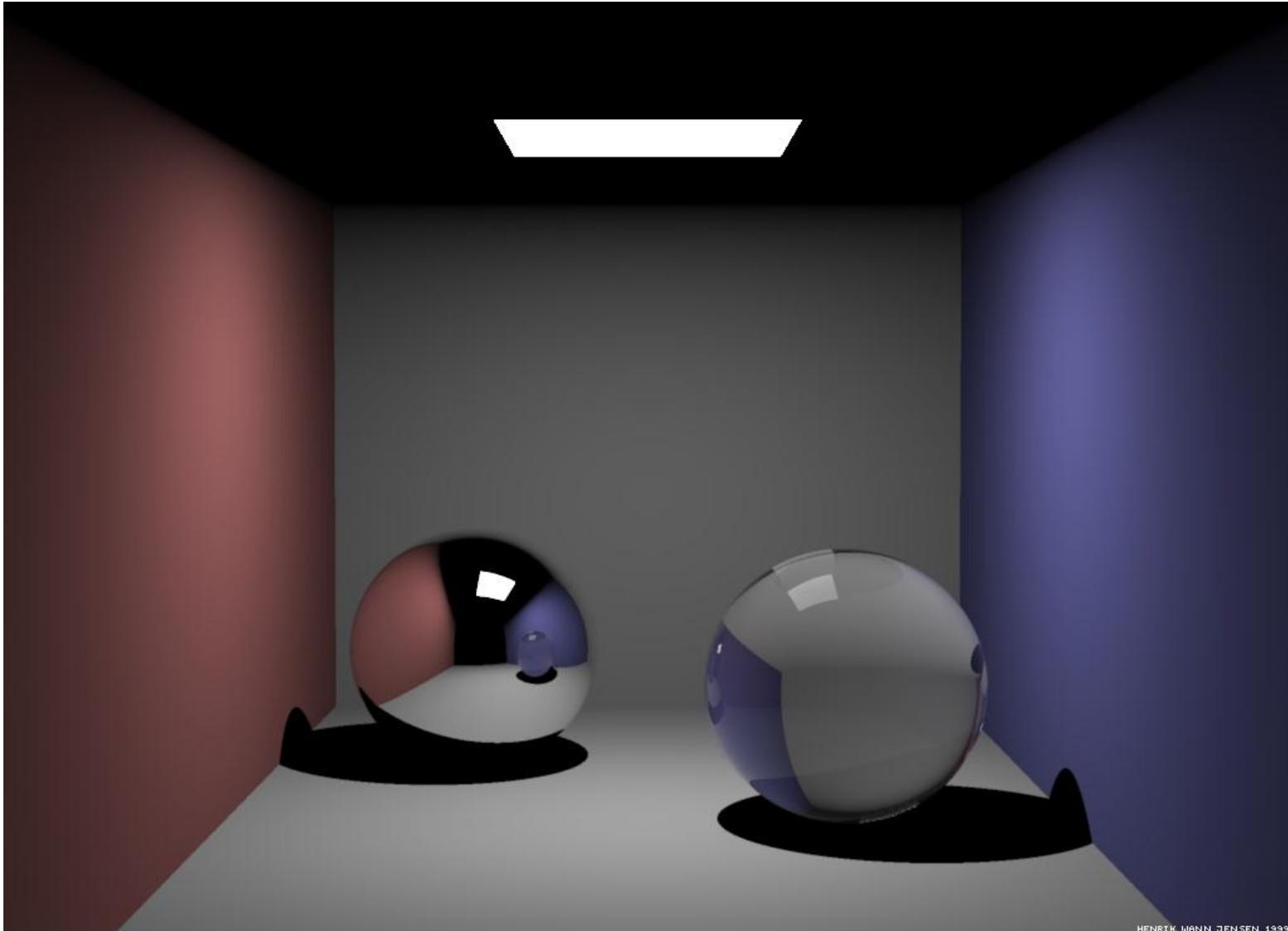
Shadow Optimization

- We only want to know whether there is an intersection, *not* which one is closest
- **Special routine** `Object3D::intersectShadowRay()`
 - Stops at first intersection



Questions?

Henrik Wann Jensen

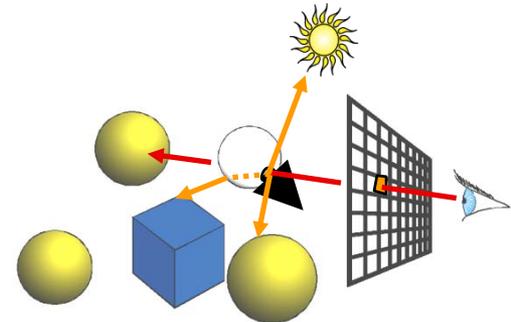
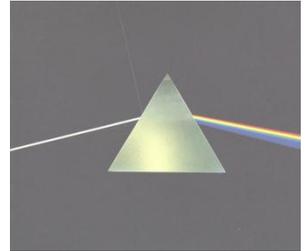
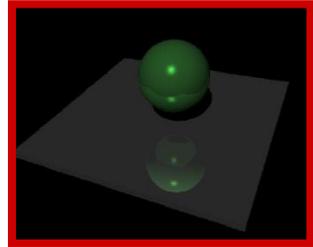
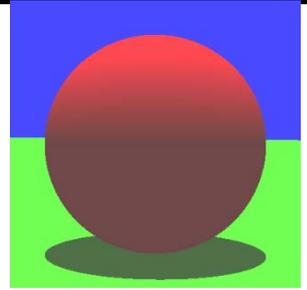


HENRIK WANN JENSEN 1999

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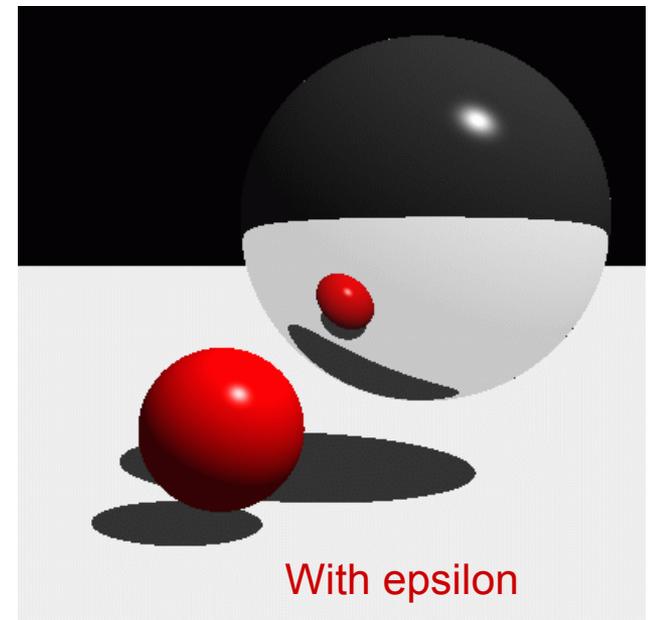
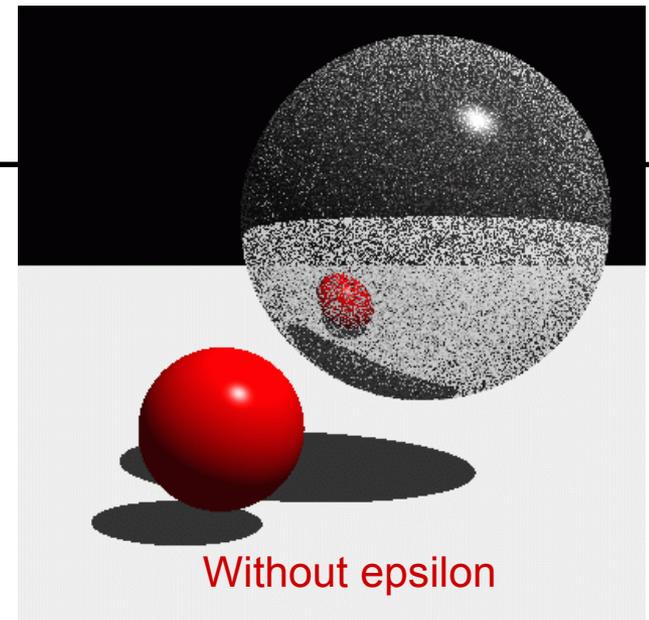
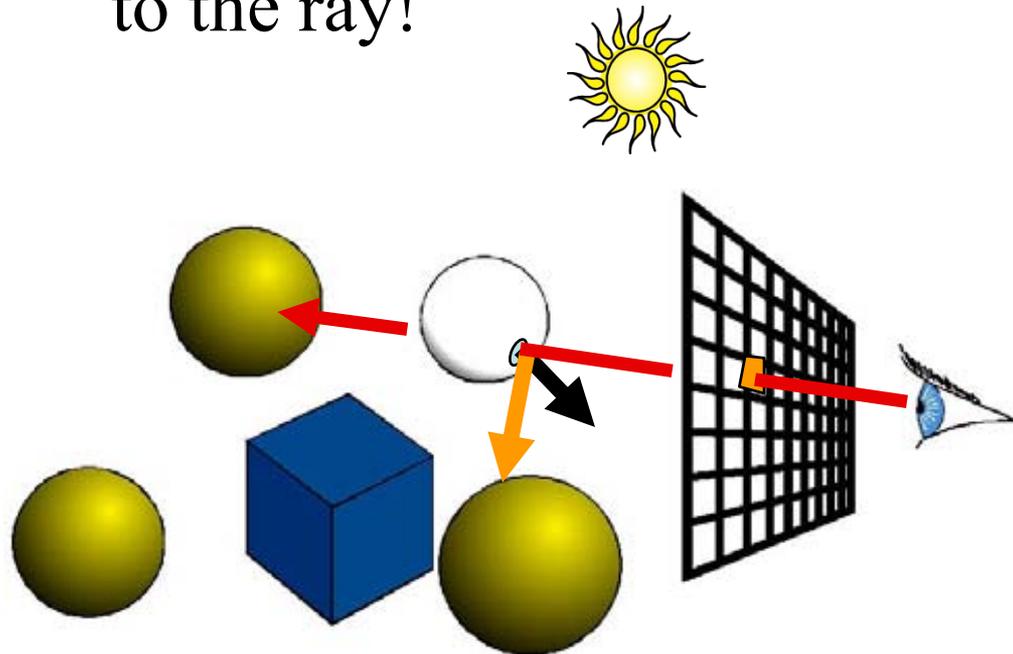
Overview of Today

- Shadows
- Reflection
- Refraction
- Recursive Ray Tracing



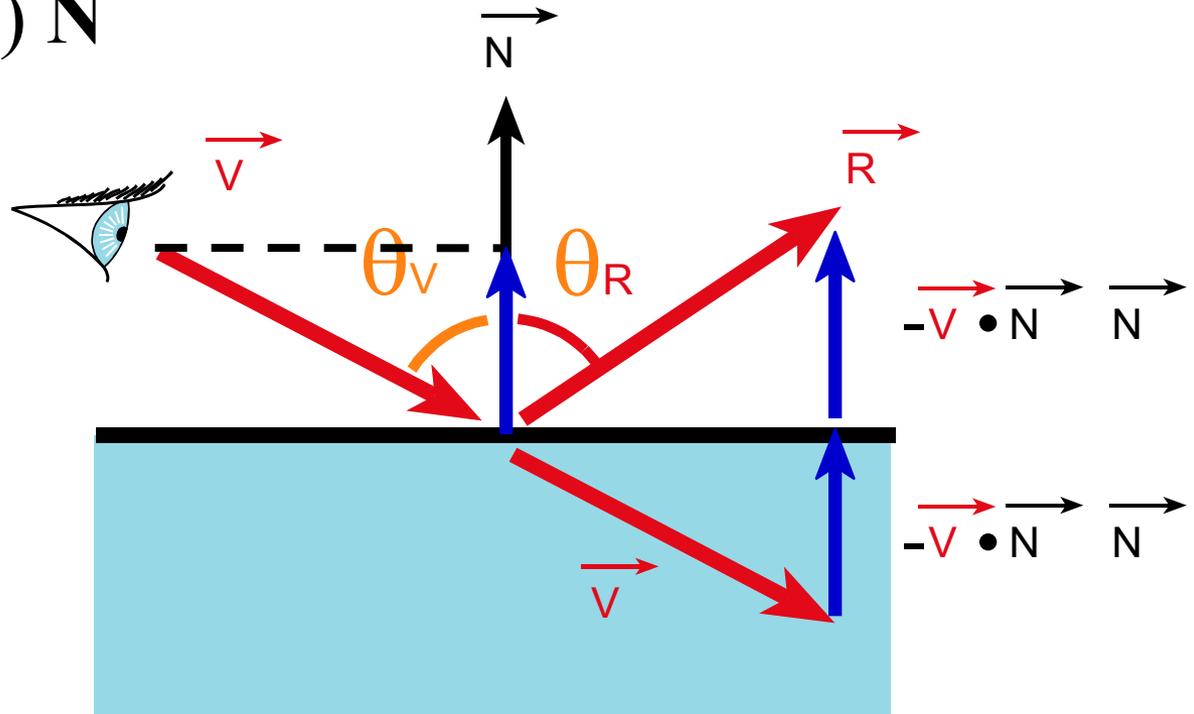
Mirror Reflection

- Cast ray symmetric with respect to the normal
- Multiply by reflection coefficient k_s (color)
- Don't forget to add epsilon to the ray!



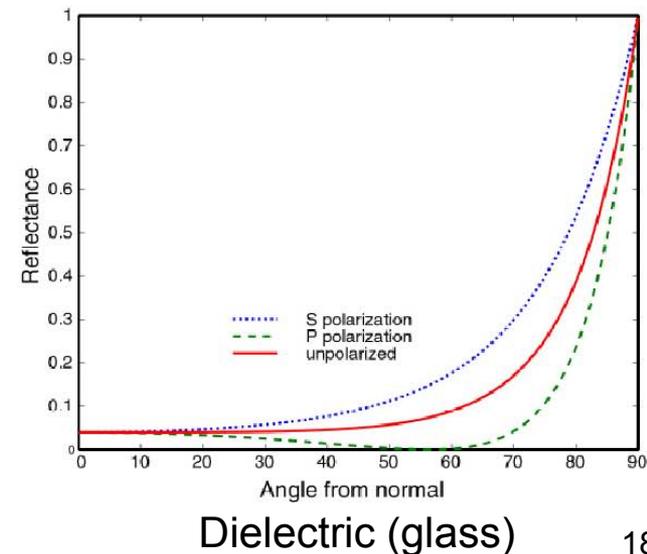
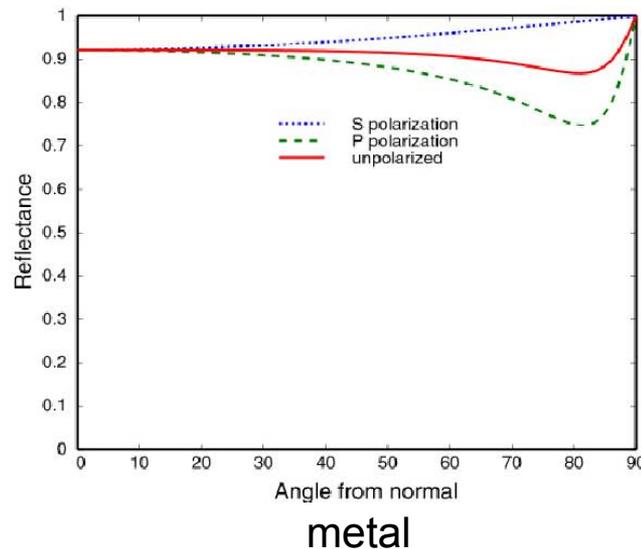
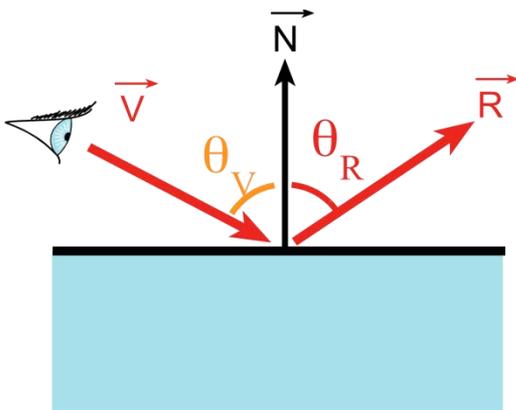
Perfect Mirror Reflection

- Reflection angle = view angle
 - Normal component is negated
 - Remember particle collisions?
- $\mathbf{R} = \mathbf{V} - 2 (\mathbf{V} \cdot \mathbf{N}) \mathbf{N}$



Amount of Reflection

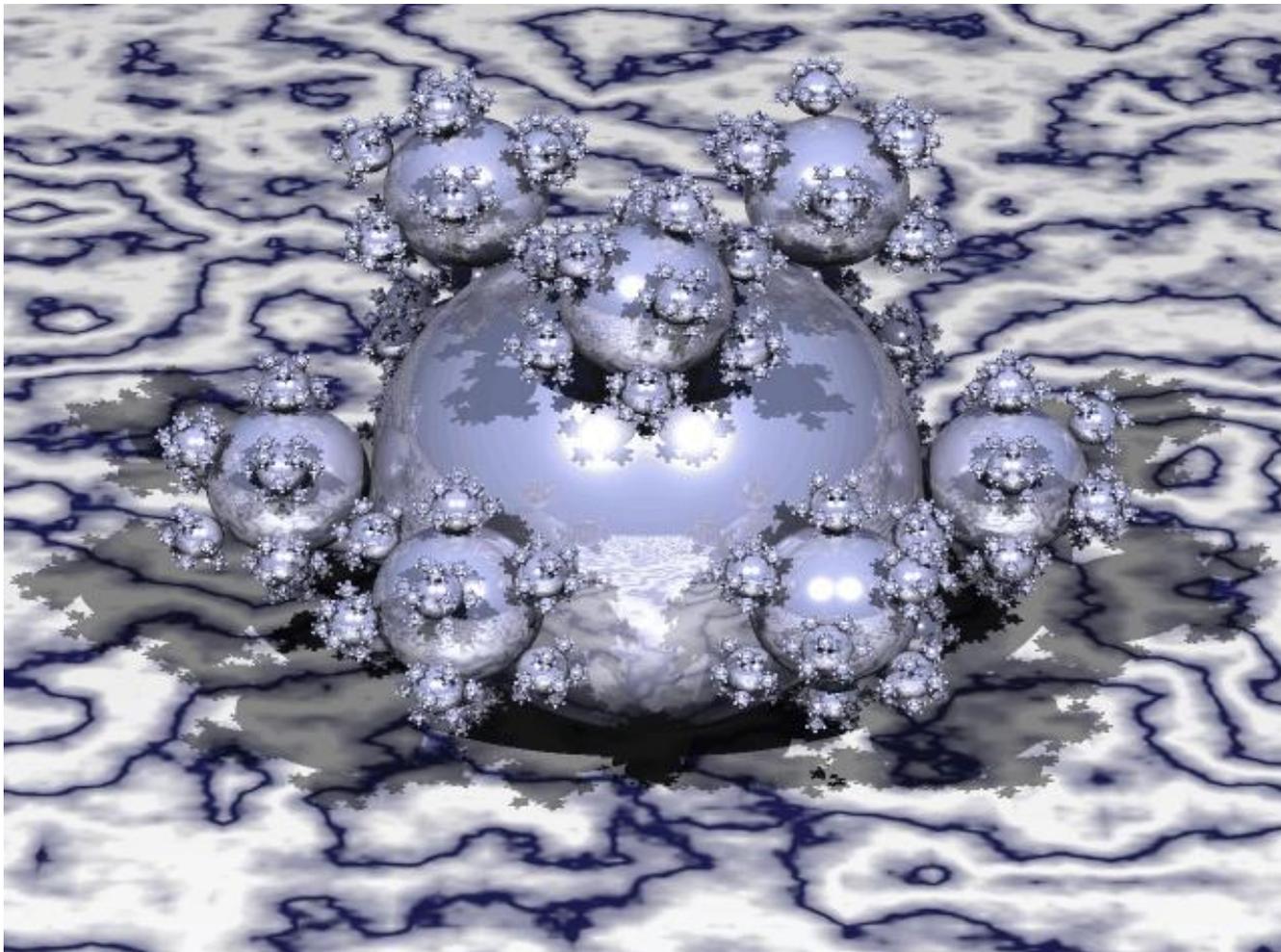
- Traditional ray tracing (hack)
 - Constant k_s
- More realistic (we'll do this later):
 - Fresnel reflection term (more reflection at grazing angle)
 - Schlick's approximation: $R(\theta) = R_0 + (1 - R_0)(1 - \cos \theta)^5$
- Fresnel makes a big difference!



Questions?

“Spheraflake” fractal

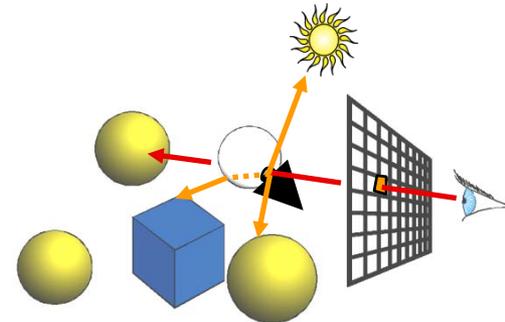
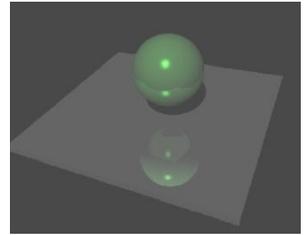
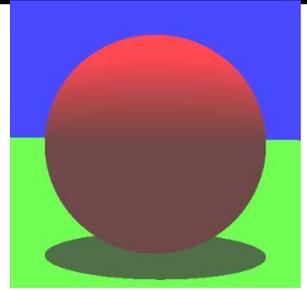
Henrik Wann Jensen



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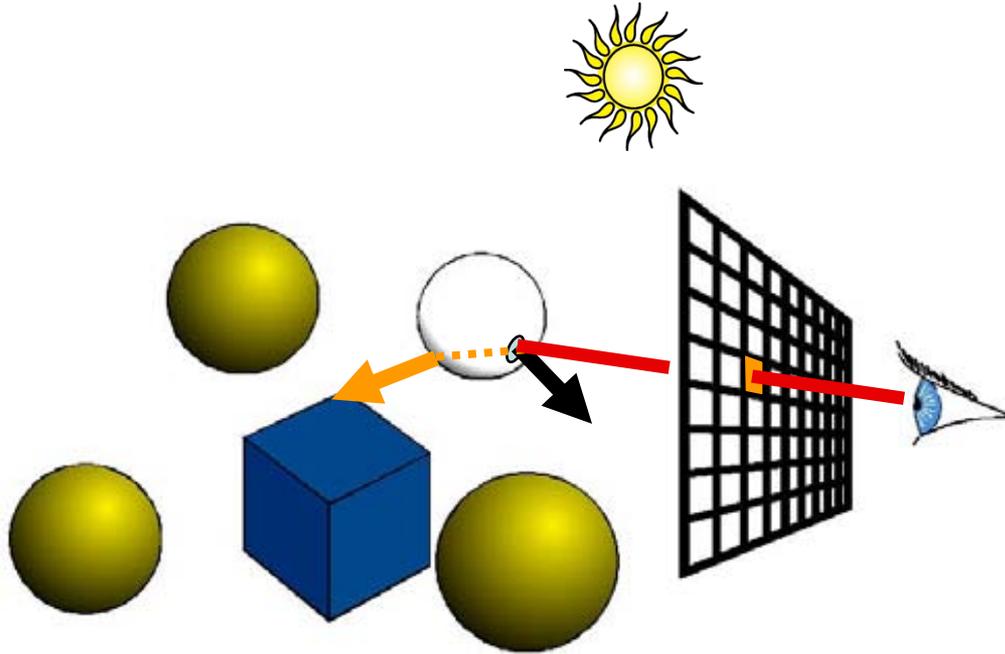
Overview of Today

- Shadows
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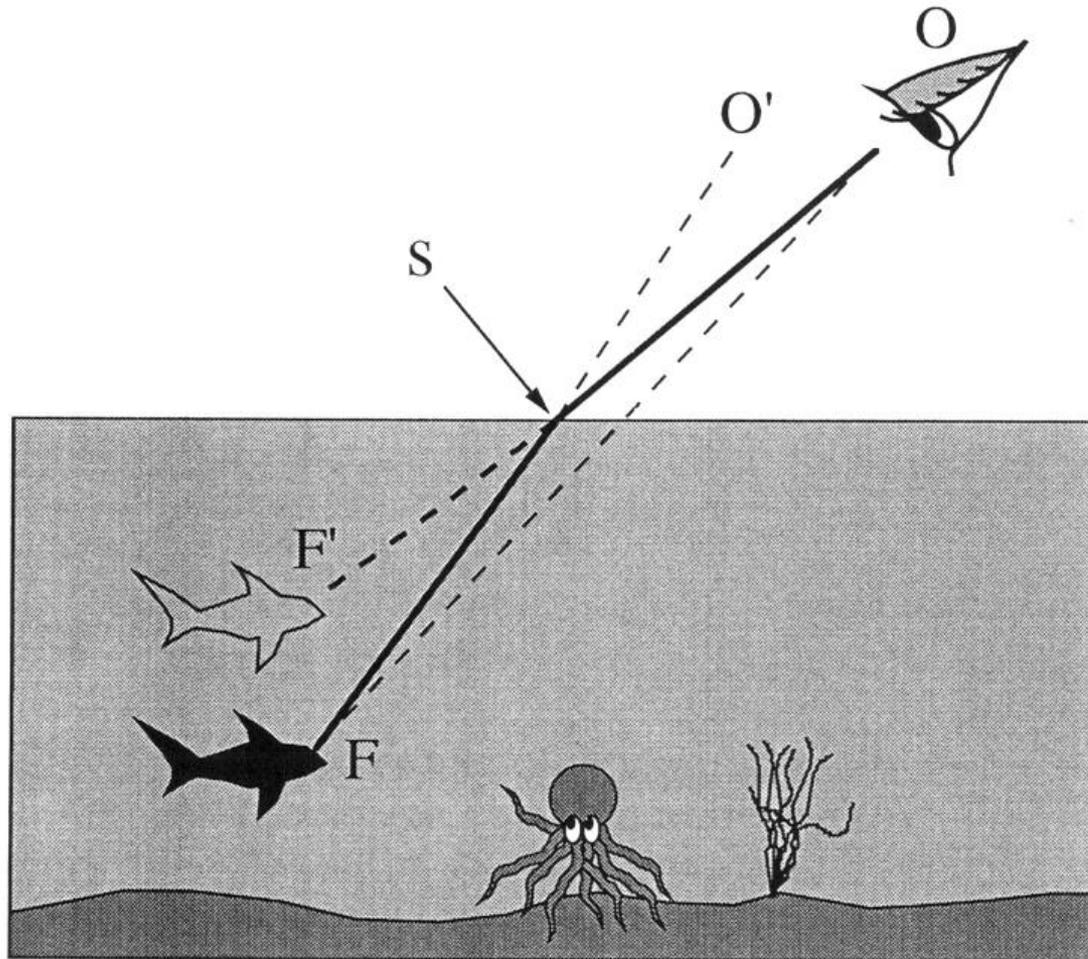


Transparency (Refraction)

- Cast ray in refracted direction
- Multiply by transparency coefficient k_t (color)

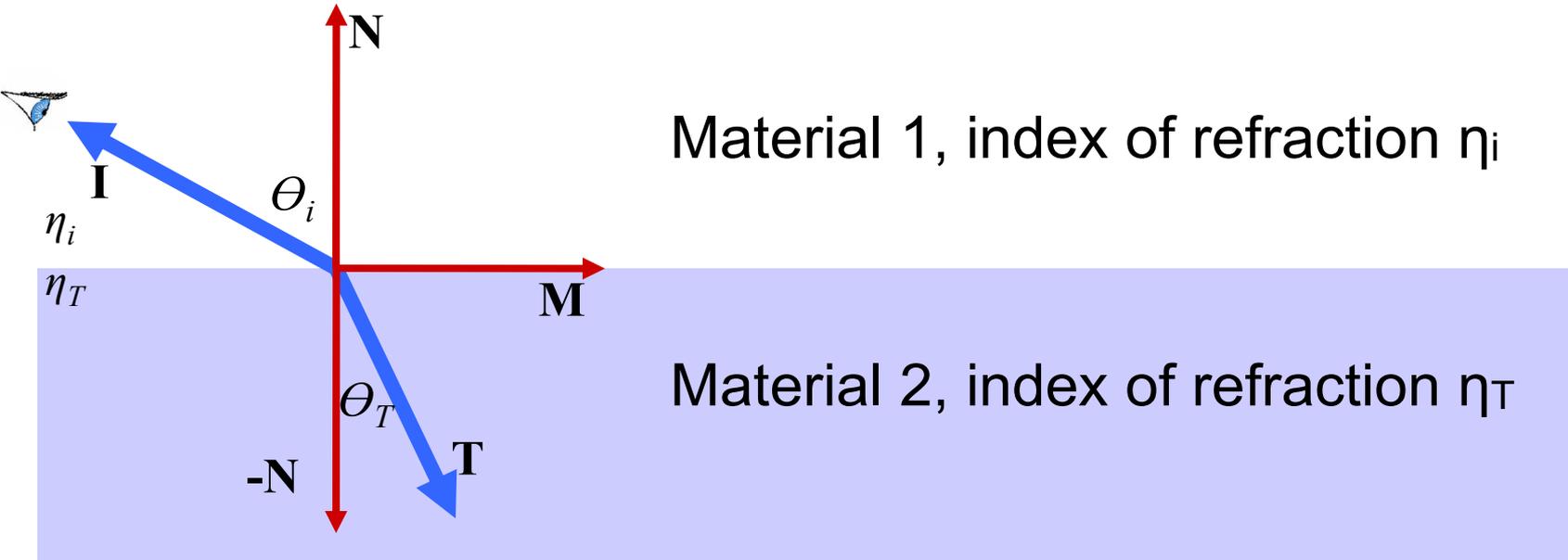


Qualitative Refraction



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Refraction



Material 1, index of refraction η_i

Material 2, index of refraction η_T

Snell-Descartes Law:

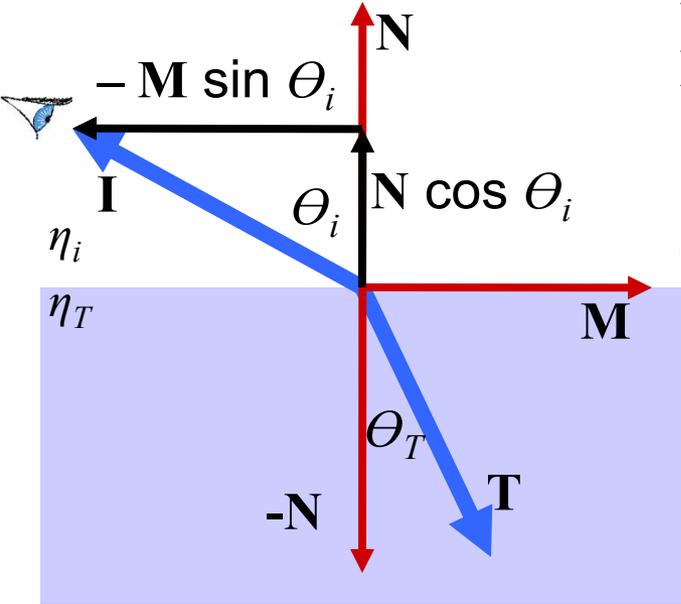
$$n_i \sin \theta_i = n_T \sin \theta_T$$

$$\frac{\sin \theta_T}{\sin \theta_i} = \frac{n_i}{n_T} = n_r$$

Relative index of refraction

Refracted direction \mathbf{T} ?

Refraction



$$\mathbf{I} = \mathbf{N} \cos \theta_i - \mathbf{M} \sin \theta_i$$

$$\mathbf{M} = (\mathbf{N} \cos \theta_i - \mathbf{I}) / \sin \theta_i$$

$$\mathbf{T} = -\mathbf{N} \cos \theta_T + \mathbf{M} \sin \theta_T$$

$$= -\mathbf{N} \cos \theta_T + (\mathbf{N} \cos \theta_i - \mathbf{I}) \sin \theta_T / \sin \theta_i \quad \text{Plug M}$$

$$= -\mathbf{N} \cos \theta_T + (\mathbf{N} \cos \theta_i - \mathbf{I}) \eta_r \quad \text{let's get rid of the cos \& sin}$$

$$= [\eta_r \cos \theta_i - \cos \theta_T] \mathbf{N} - \eta_r \mathbf{I}$$

$$= [\eta_r \cos \theta_i - \sqrt{1 - \sin^2 \theta_T}] \mathbf{N} - \eta_r \mathbf{I}$$

$$= [\eta_r \cos \theta_i - \sqrt{1 - \eta_r^2 \sin^2 \theta_i}] \mathbf{N} - \eta_r \mathbf{I}$$

$$= [\eta_r \cos \theta_i - \sqrt{1 - \eta_r^2 (1 - \cos^2 \theta_i)}] \mathbf{N} - \eta_r \mathbf{I}$$

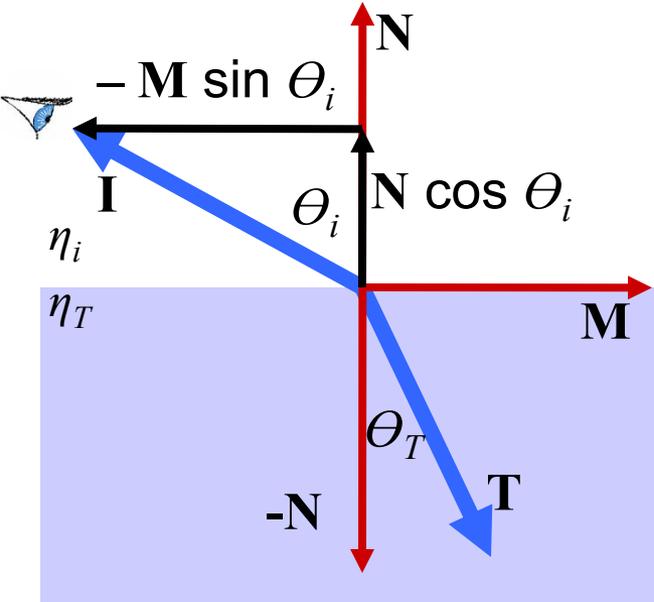
$$= [\eta_r (\mathbf{N} \cdot \mathbf{I}) - \sqrt{1 - \eta_r^2 (1 - (\mathbf{N} \cdot \mathbf{I})^2)}] \mathbf{N} - \eta_r \mathbf{I}$$

Snell-Descartes Law:

$$n_i \sin \theta_i = n_T \sin \theta_T$$

$$\frac{\sin \theta_T}{\sin \theta_i} = \frac{n_i}{n_T} = n_r$$

Refraction



$$\mathbf{I} = \mathbf{N} \cos \theta_i - \mathbf{M} \sin \theta_i$$

$$\mathbf{M} = (\mathbf{N} \cos \theta_i - \mathbf{I}) / \sin \theta_i$$

- **Total internal reflection** when the square root is imaginary (no refraction, just reflection)

Snell-Descartes Law:

$$n_i \sin \theta_i = n_T \sin \theta_T$$

$$\frac{\sin \theta_T}{\sin \theta_i} = \frac{n_i}{n_T} = n_r$$

$$= [\eta_r (\mathbf{N} \cdot \mathbf{I}) - \sqrt{1 - \eta_r^2 (1 - (\mathbf{N} \cdot \mathbf{I})^2)}] \mathbf{N} - \eta_r \mathbf{I}$$

Total Internal Reflection

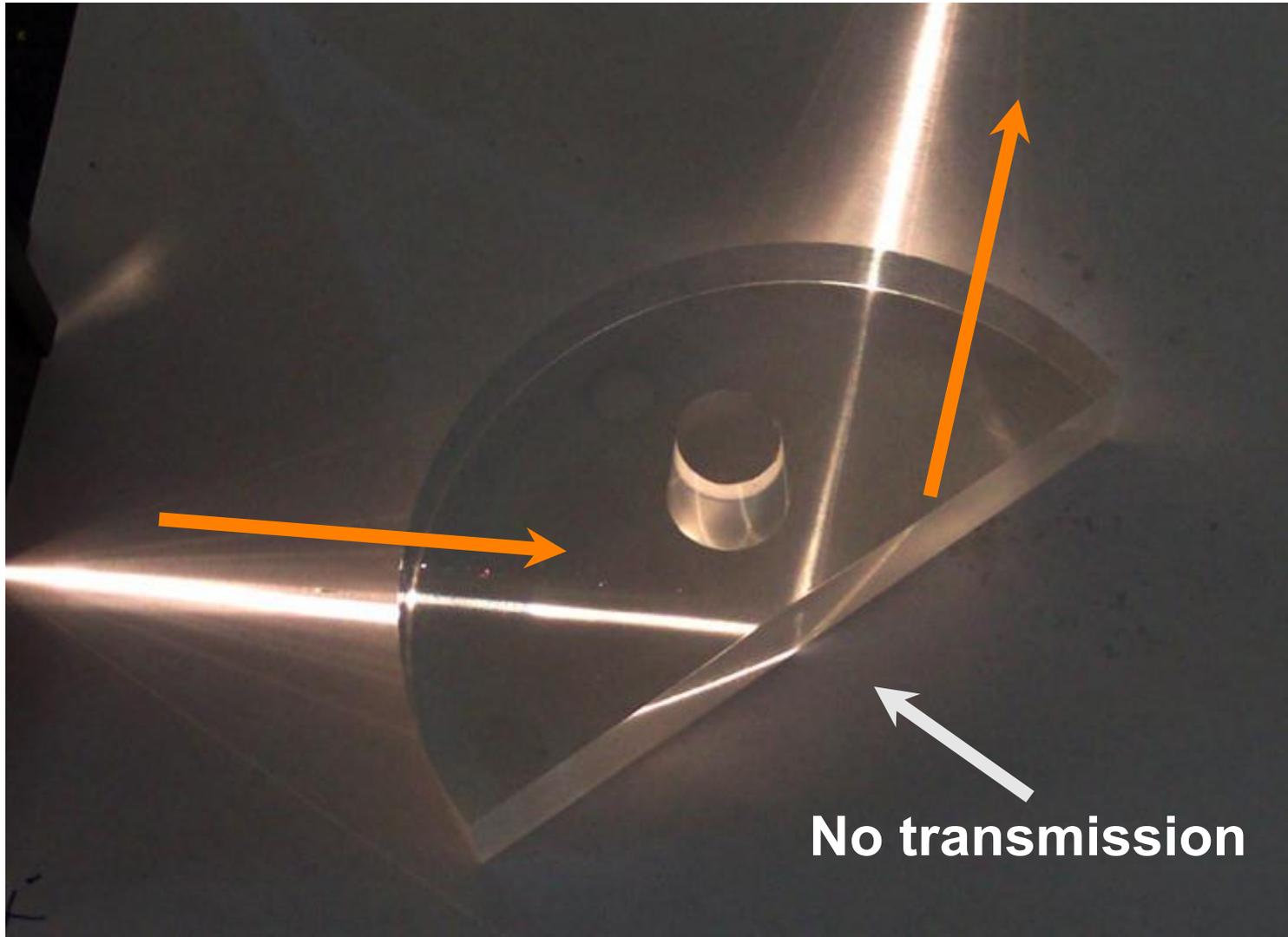


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Total Internal Reflection



Fig. 3.7A The optical manhole. From under water, the entire celestial hemisphere is compressed into a circle only 97.2° across. The dark boundary defining the edges of the manhole is not sharp due to surface waves. The rays are analogous to the crepuscular type seen in hazy air, Section 1.9. (Photo by D. Granger)

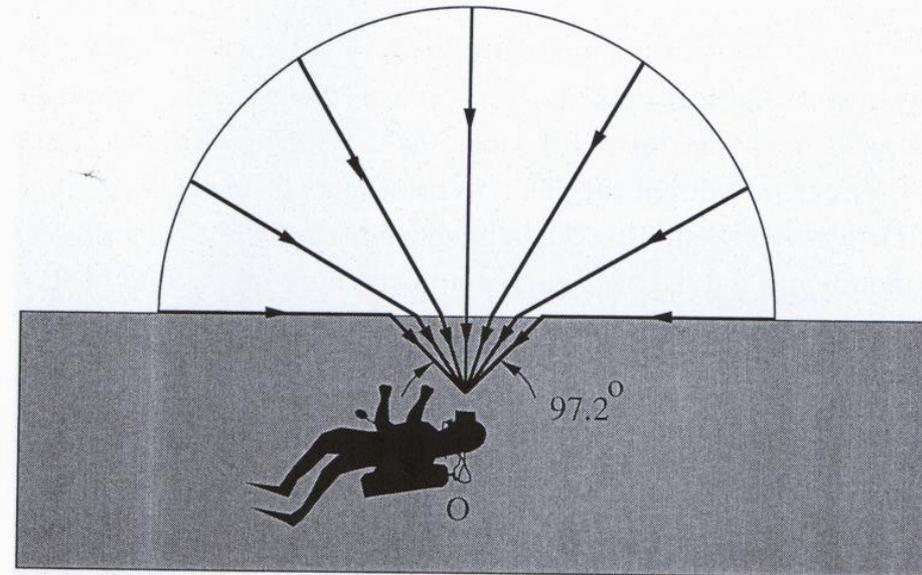
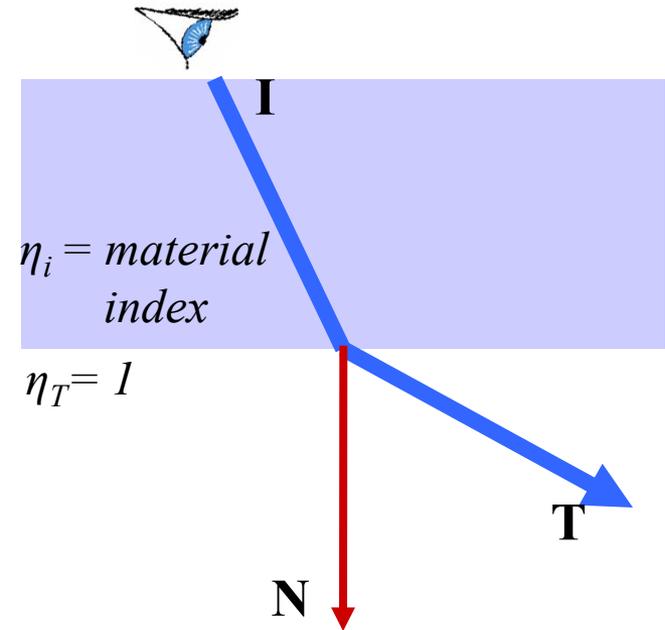
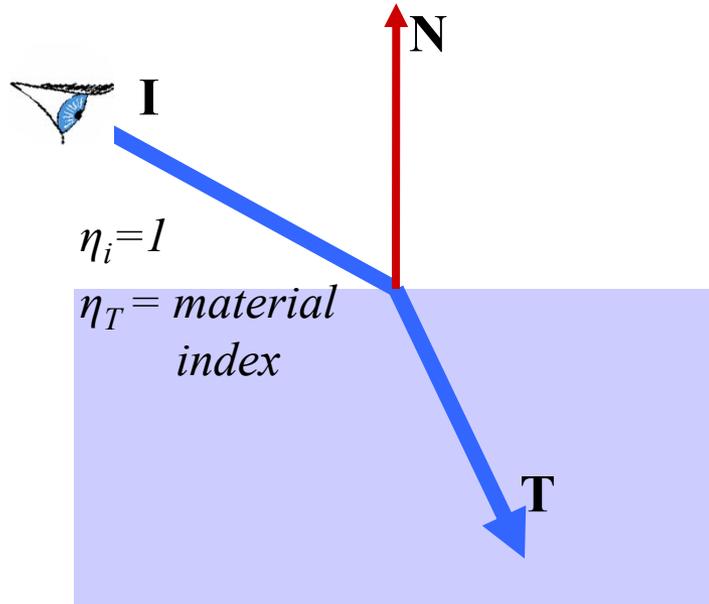


Fig. 3.7B The optical manhole. Light from the horizon (angle of incidence = 90°) is refracted downward at an angle of 48.6° . This compresses the sky into a circle with a diameter of 97.2° instead of its usual 180° .

Refraction & Sidedness of Objects

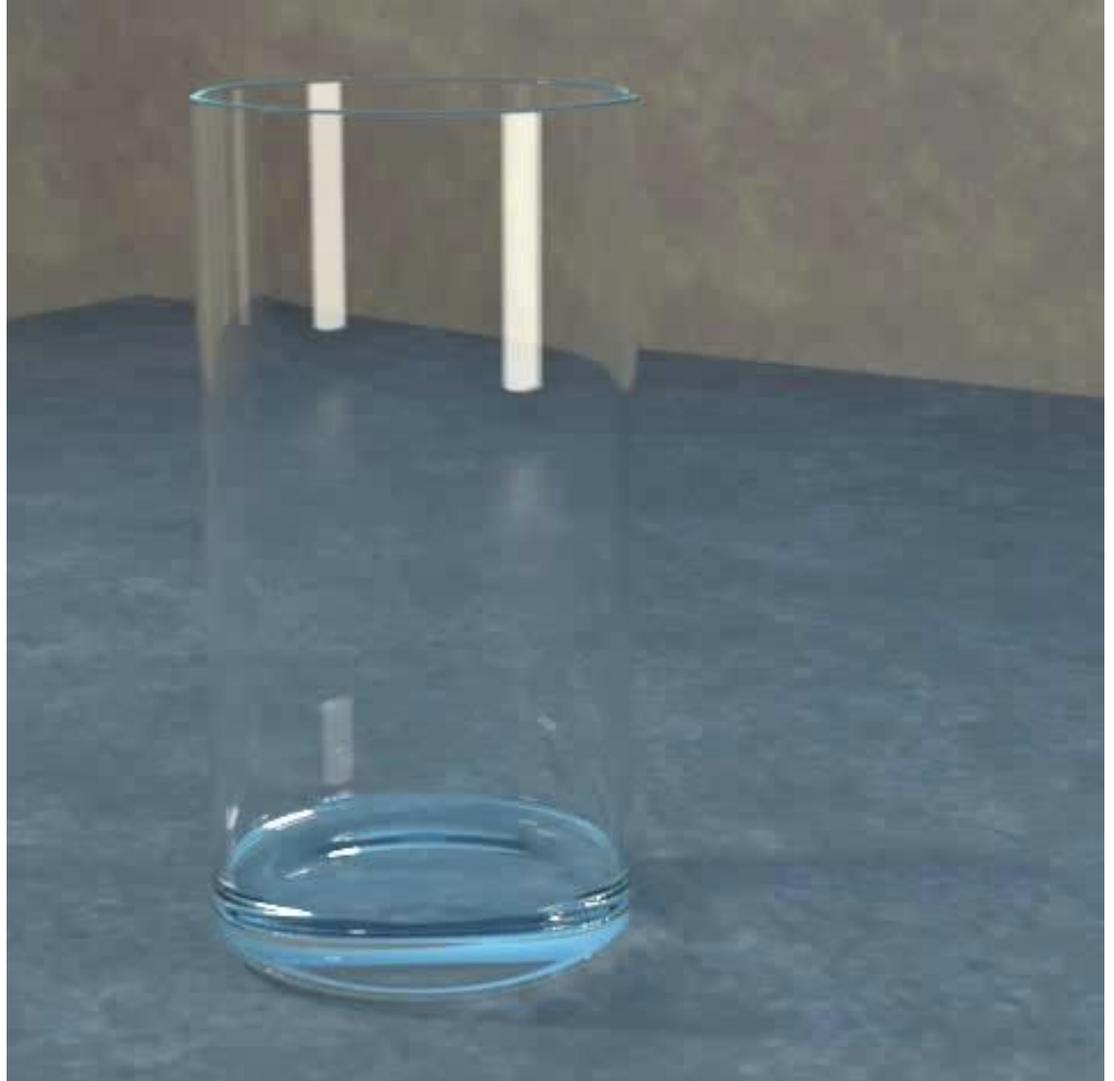
- Make sure you know whether you're entering or leaving the transmissive material:



- Note: We won't ask you to trace rays through intersecting transparent objects :-)

Cool Refraction Demo

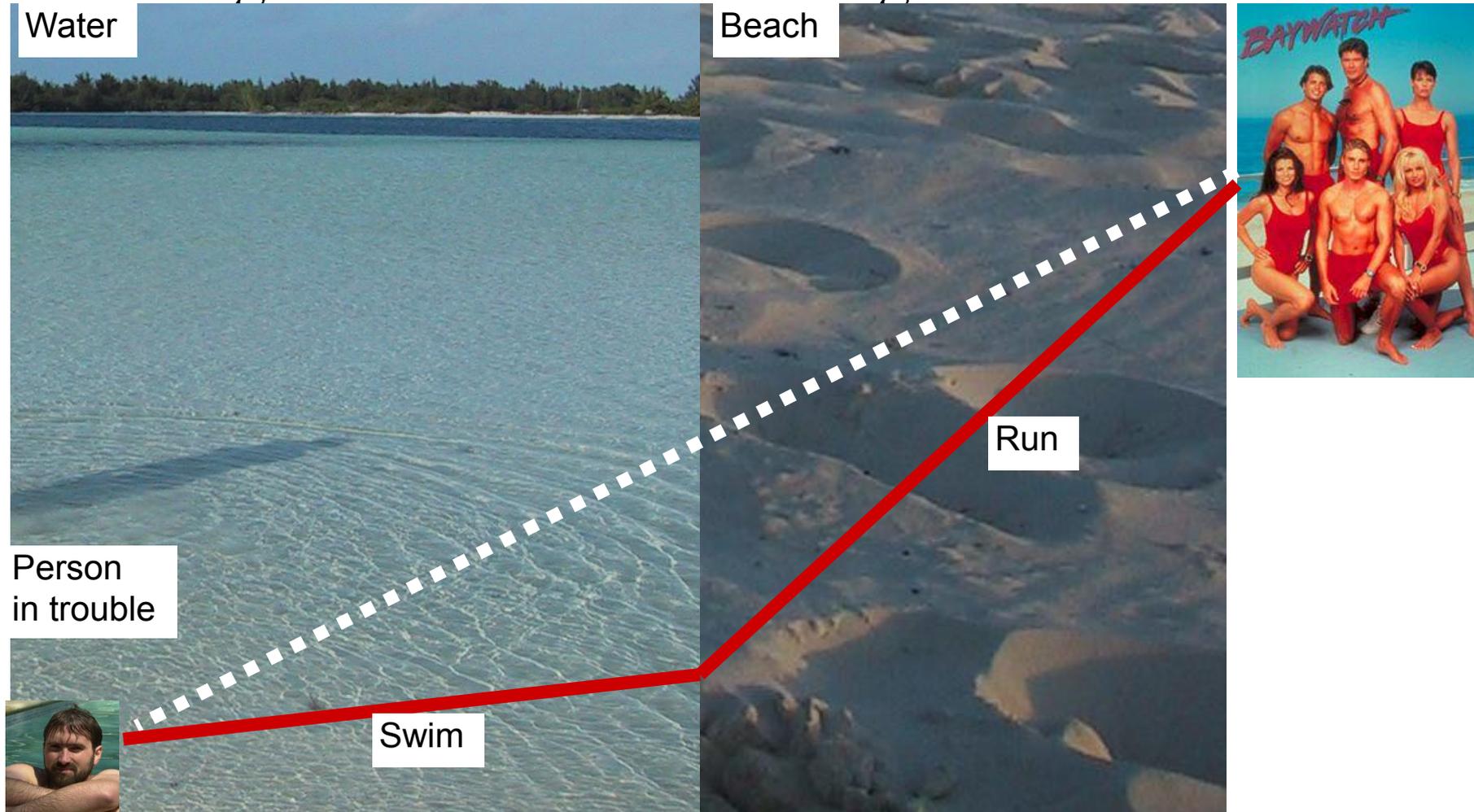
- Enright, D.,
Marschner, S.
and Fedkiw,
R.,
SIGGRAPH
2002



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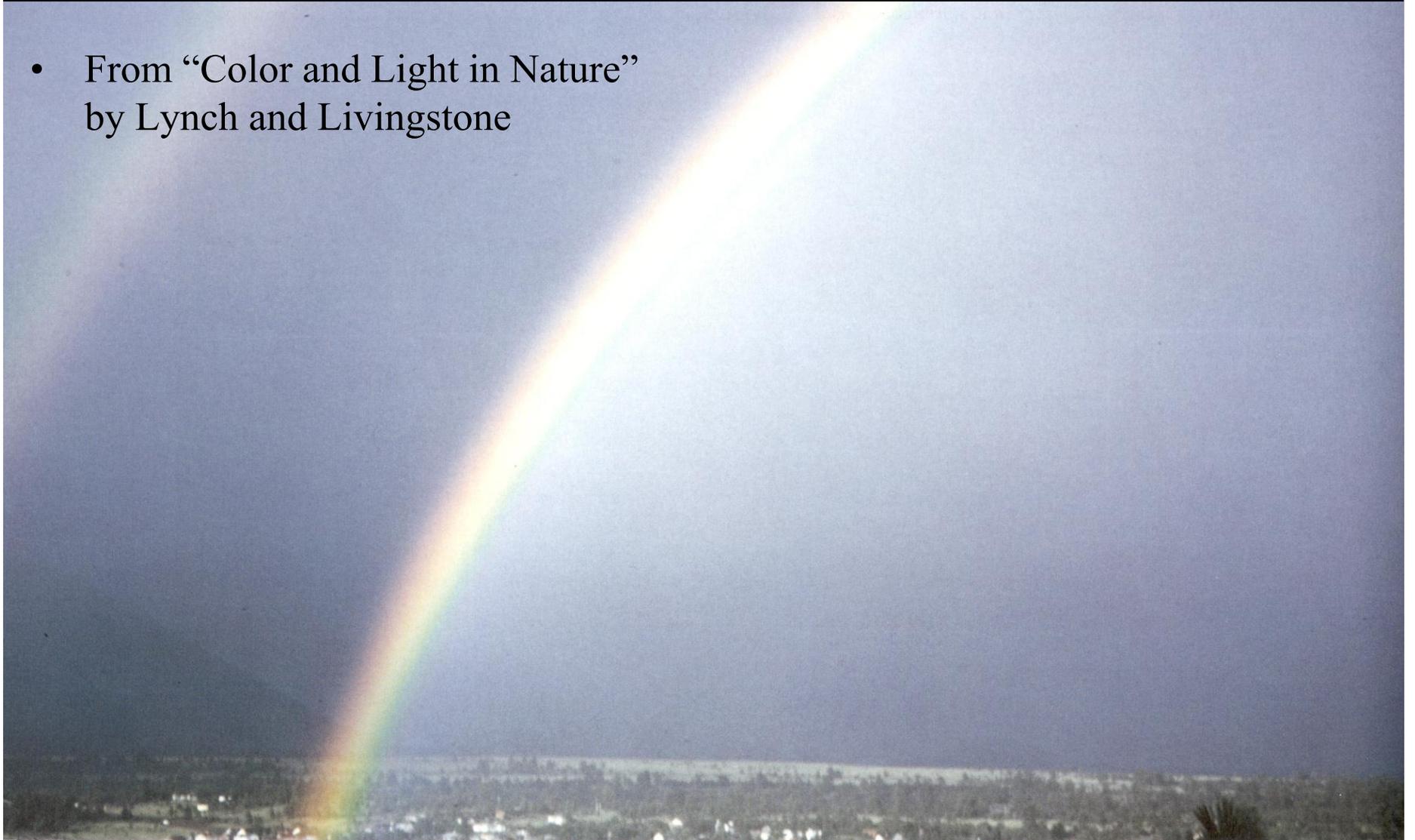
Refraction and the Lifeguard Problem

- Running is faster than swimming



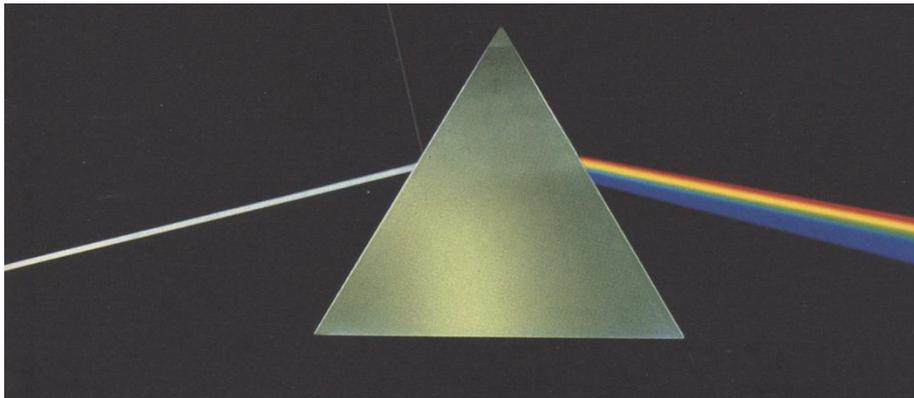
How Does a Rainbow Work?

- From “Color and Light in Nature”
by Lynch and Livingstone



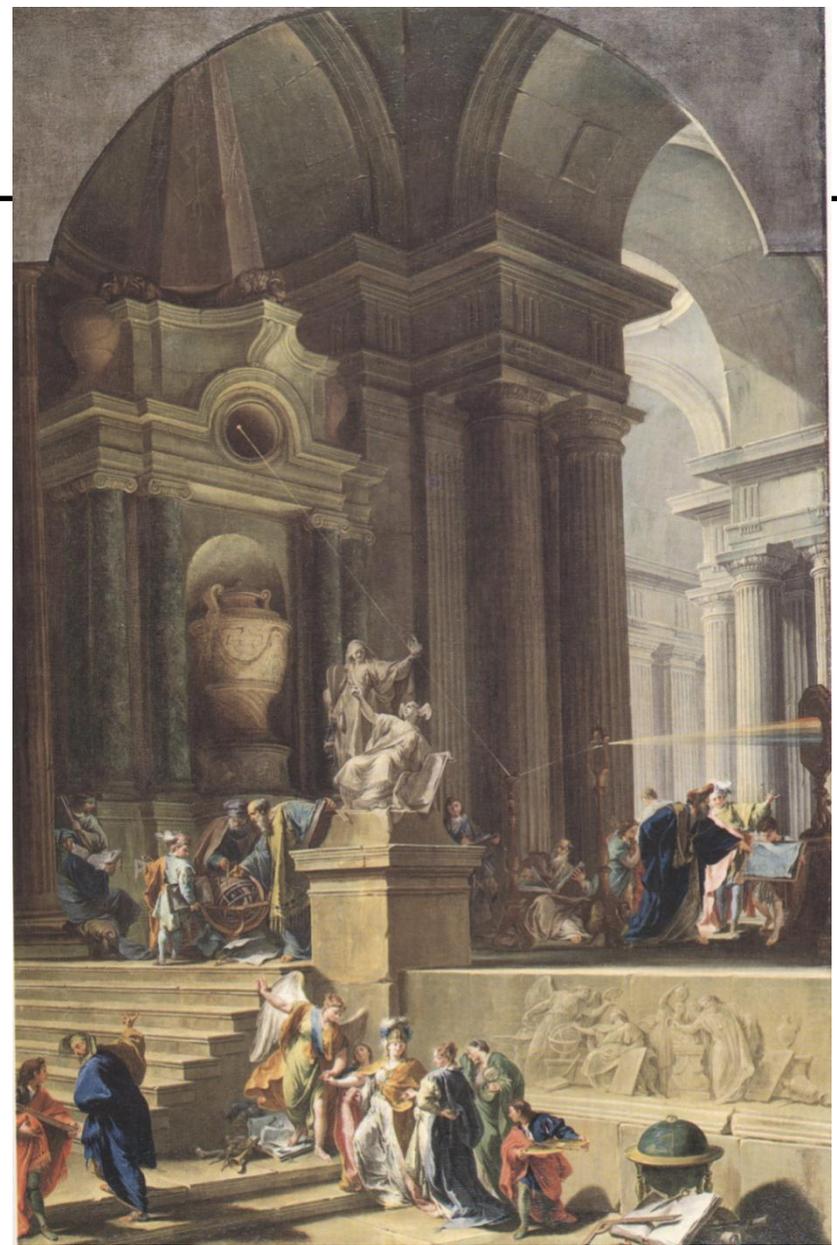
Wavelength

- Refraction is wavelength-dependent (dispersion)
 - Refraction increases as the wavelength of light decreases
 - violet and blue experience more bending than orange and red
- **Newton's** prism experiment
- **Usually ignored in graphics**



Pink Floyd, *The Dark Side of the Moon*

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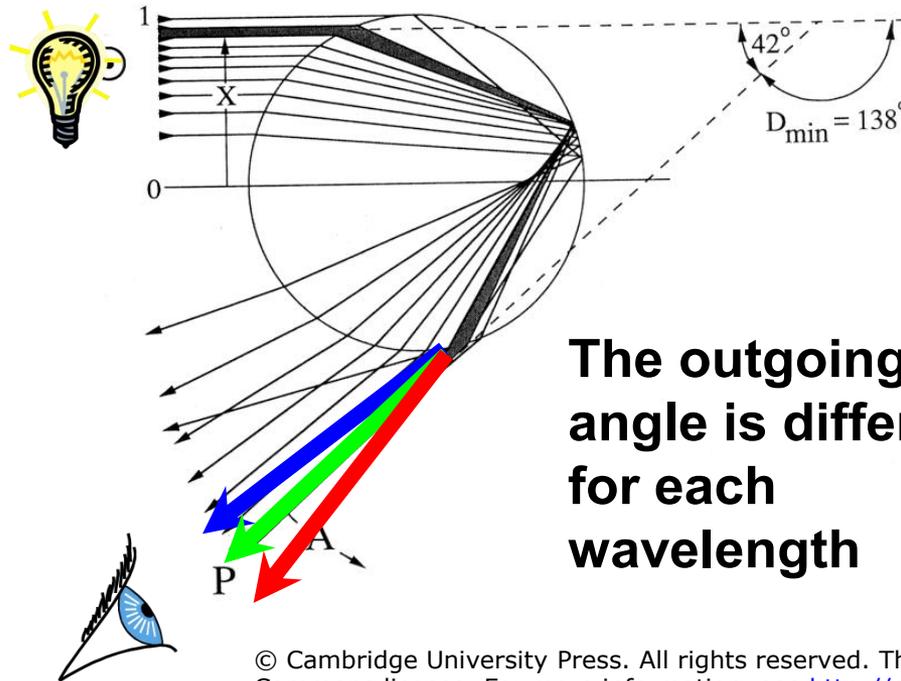


Pittoni, 1725, Allegory to Newton

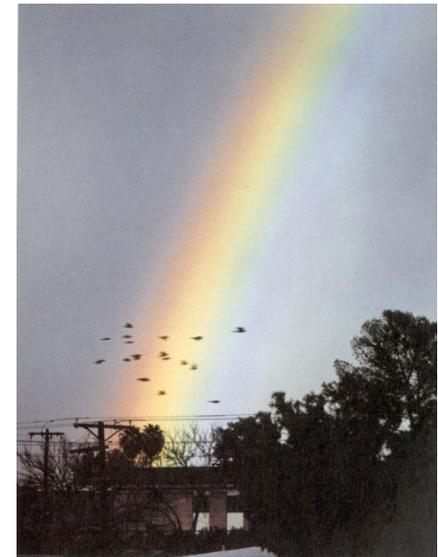
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Rainbow

- Rainbow is caused by refraction + internal reflection + refraction
- Maximum for angle around 42 degrees
- Refraction depends on wavelength (dispersion)



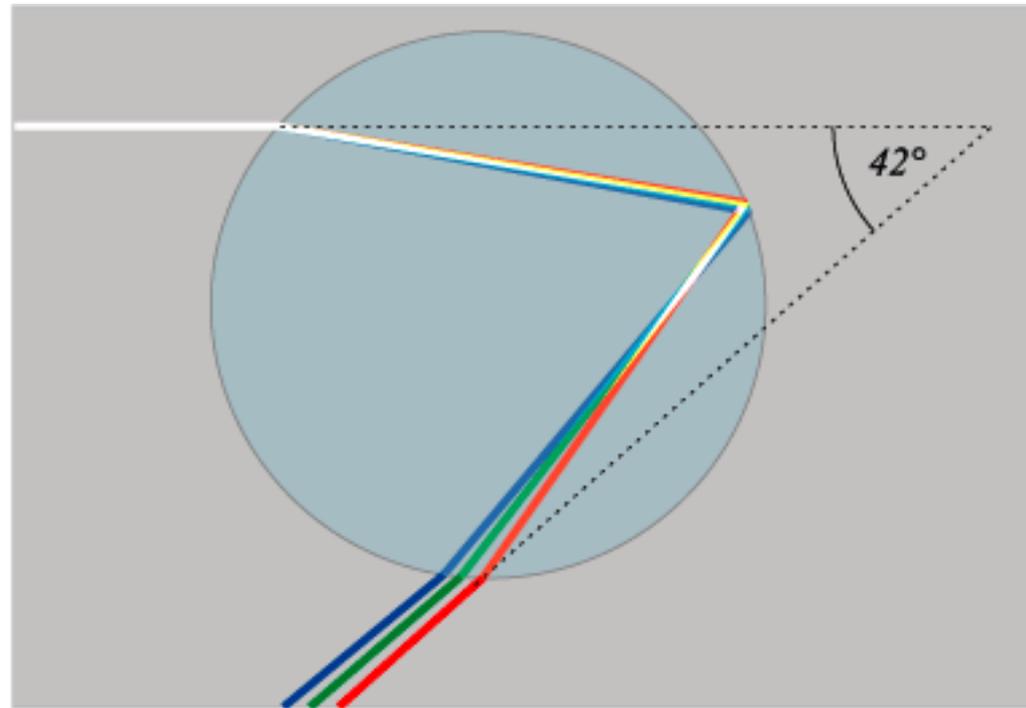
The outgoing angle is different for each wavelength



“Color and Light in Nature”
by Lynch and Livingstone

Rainbow

- Rainbow is caused by refraction + internal reflection + refraction
- Maximum for angle around 42 degrees
- Refraction depends on wavelength (dispersion)



This image is in the public domain. Source: [Wikipedia](#).

Dispersion

- Image by Henrik Wann Jensen using Photon Mapping



Courtesy of Henrik Wann Jensen. Used with permission.

Questions?

Image removed due to copyright restrictions.

Application: CAD for lenses

- Has revolutionized lens design
 - E.g. zoom lenses are good now

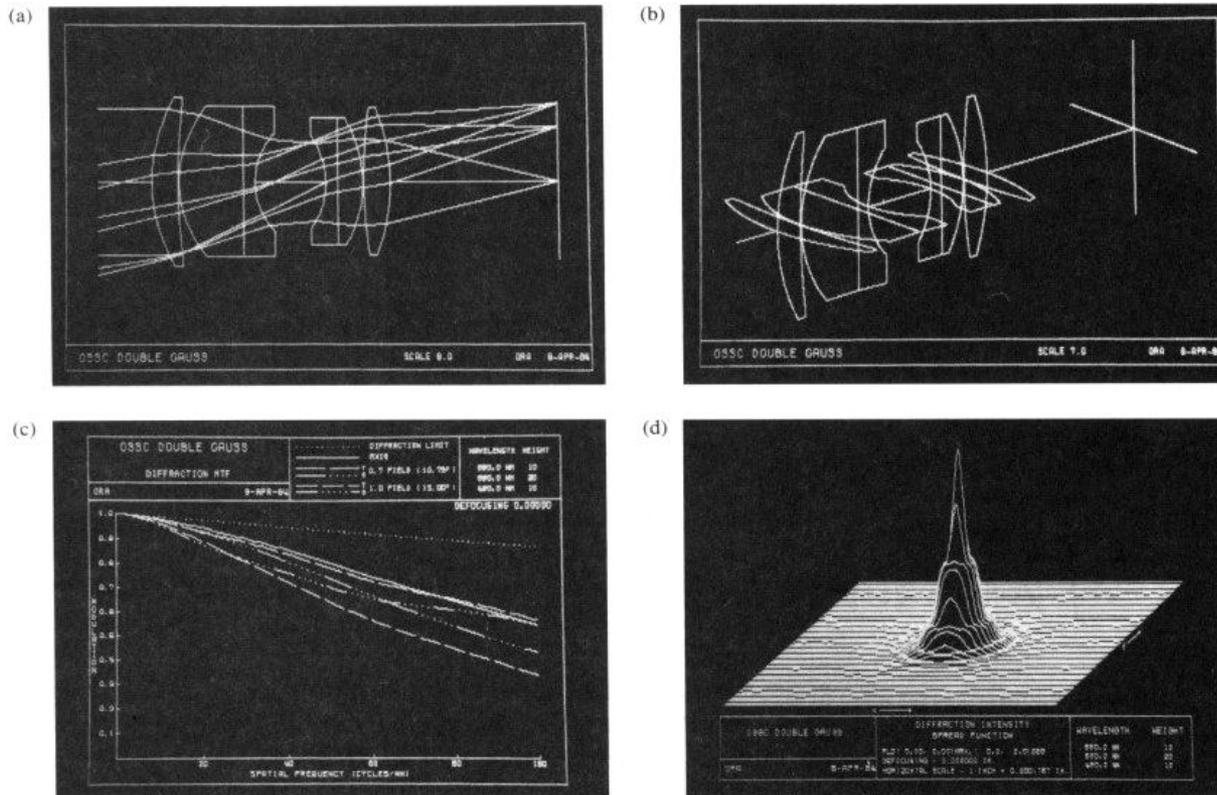


Figure 11.50 An example of the kind of lens design information available via computer techniques. (Photos courtesy Optical Research Associates.)

From Hecht's Optics

Lens design by Ray Tracing

- Used to be done manually, by rooms full of engineers who would trace rays.
- Now software, e.g. Zemax
- More in 6.815/6.865 Computational Photography

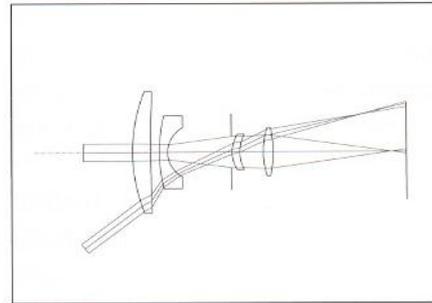


Figure-5

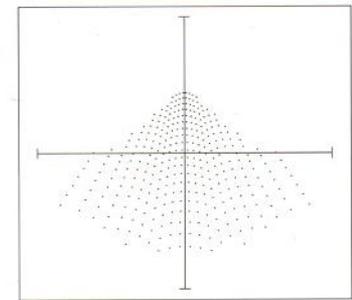


Figure-8

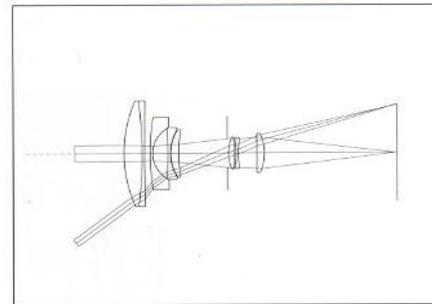


Figure-6

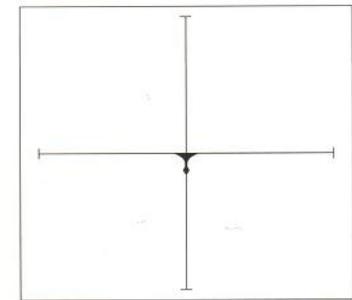


Figure-9

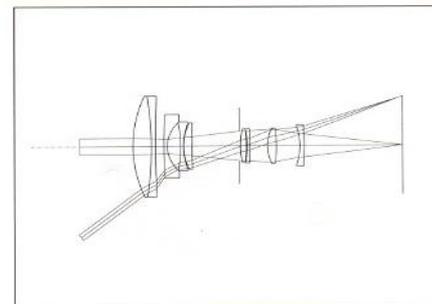


Figure-7

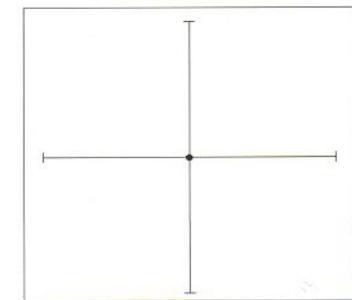
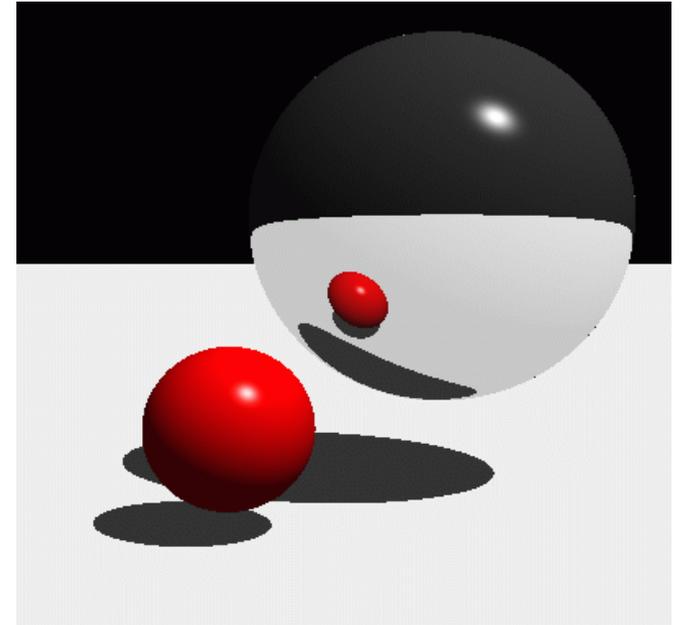
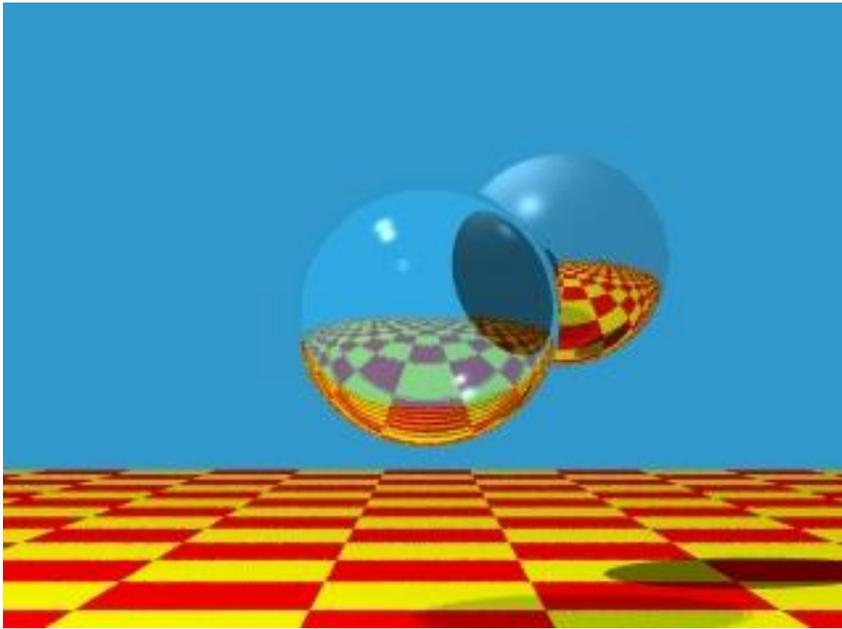


Figure-10

Let's Pause for a Moment...

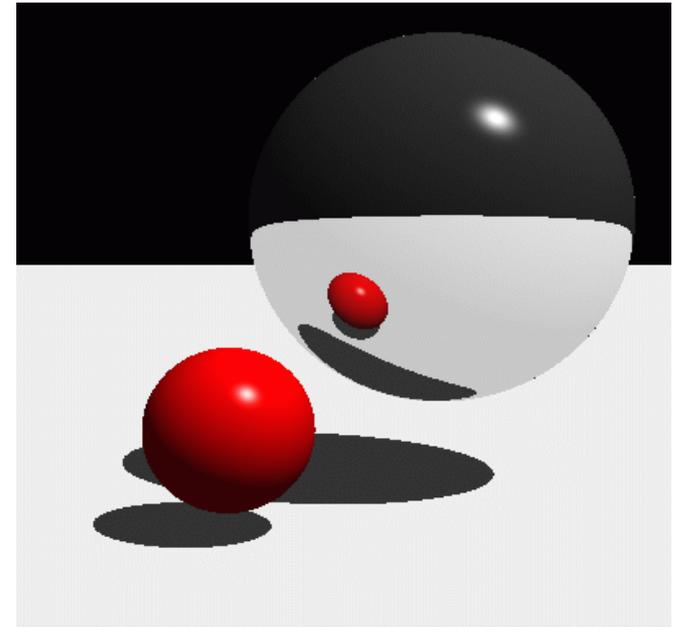
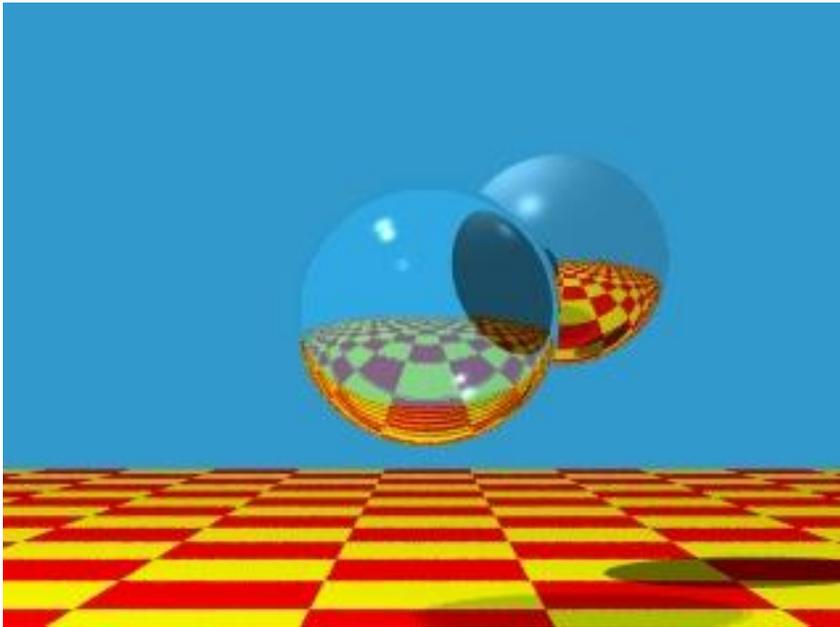
- Do these pictures look real?



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What's Wrong then?

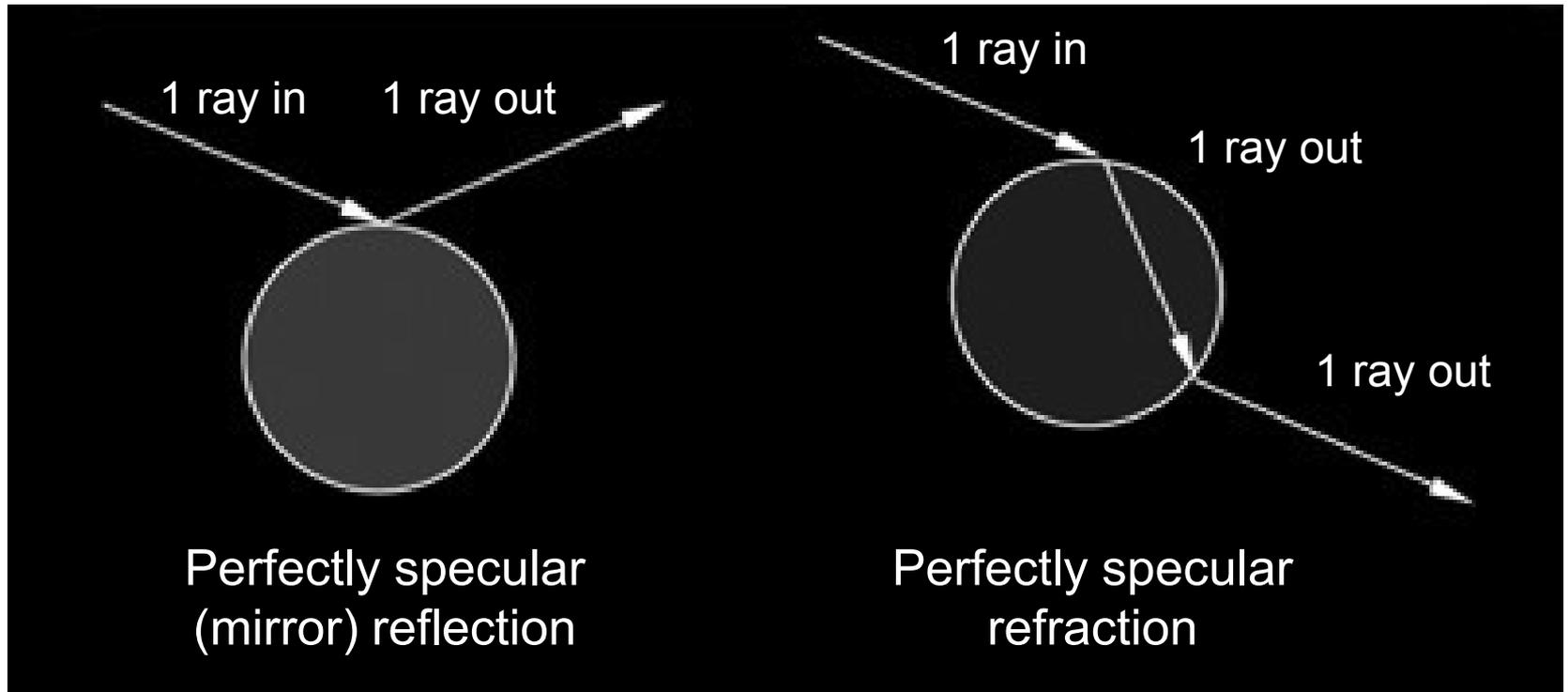
- No surface is a perfect mirror,
no material interface is perfectly smooth



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What's Wrong then?

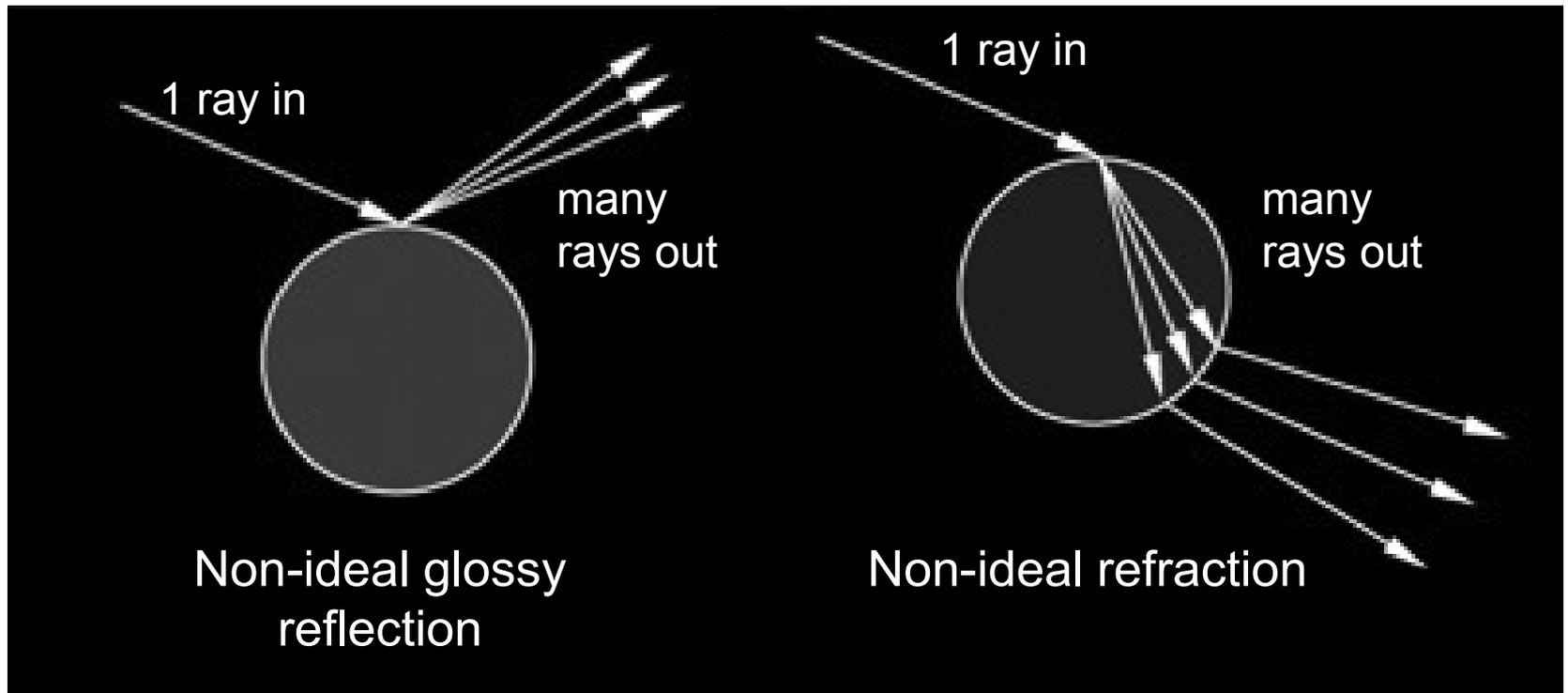
- No surface is a perfect mirror,
no material interface is perfectly smooth



Adapted from blender.org

Non-Ideal Reflection/Refraction

- No surface is a perfect mirror, no material interface is perfectly smooth

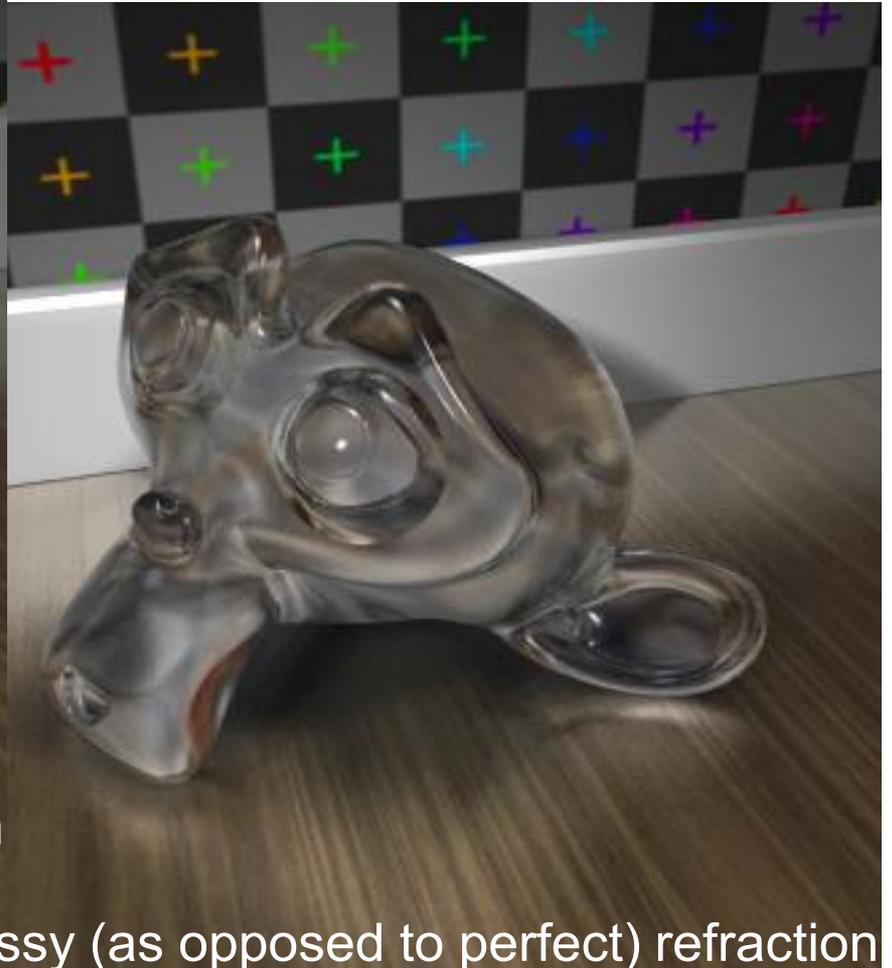


Adapted from blender.org

Non-Ideal Reflection/Refraction



Glossy (as opposed to mirror) reflection

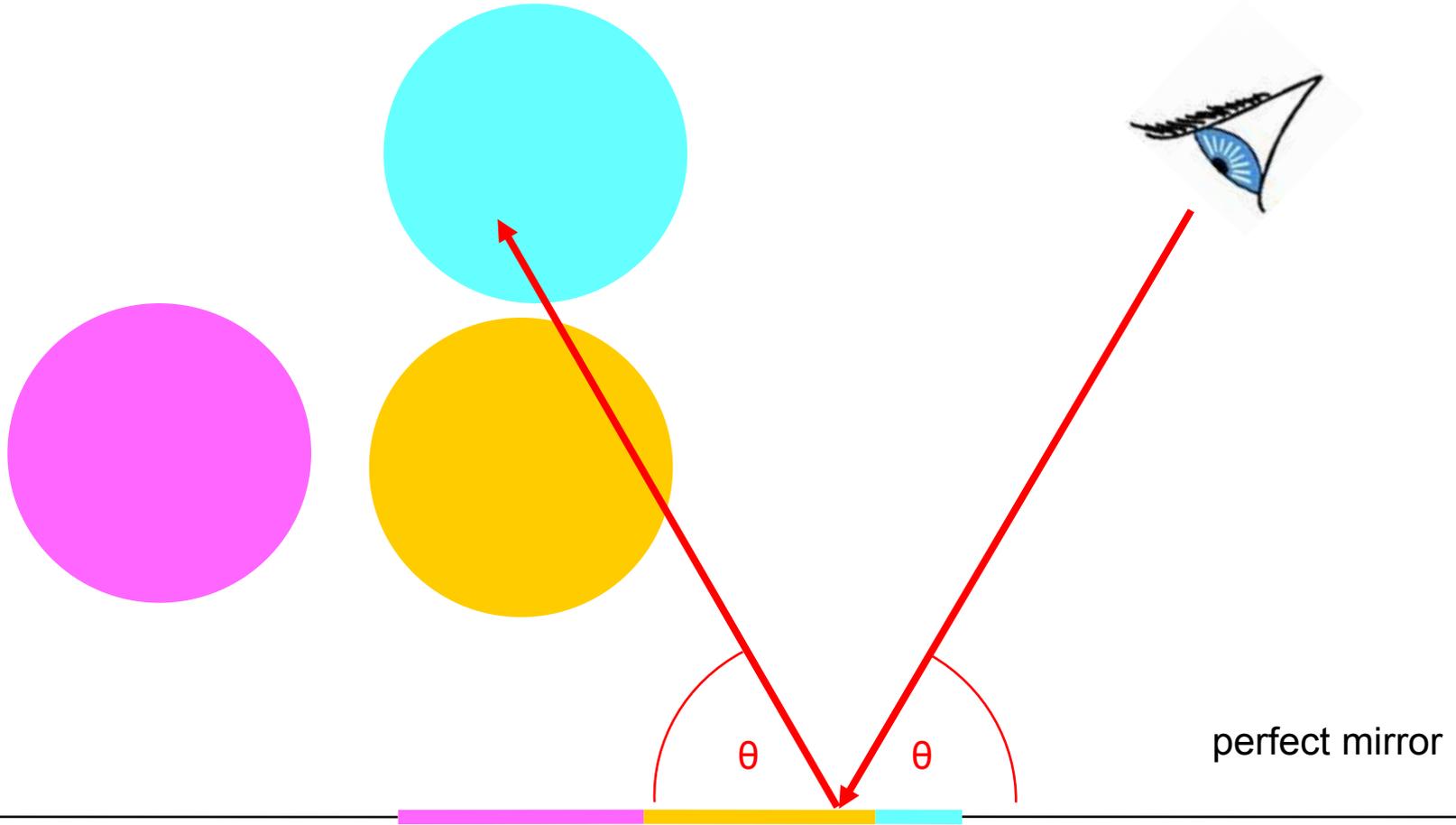


Glossy (as opposed to perfect) refraction

Courtesy of Blender Foundation. License CC-BY. This content is excluded from our Creative Commons license. For more information, see <http://ocw.mit.edu/help/faq-fair-use/>.

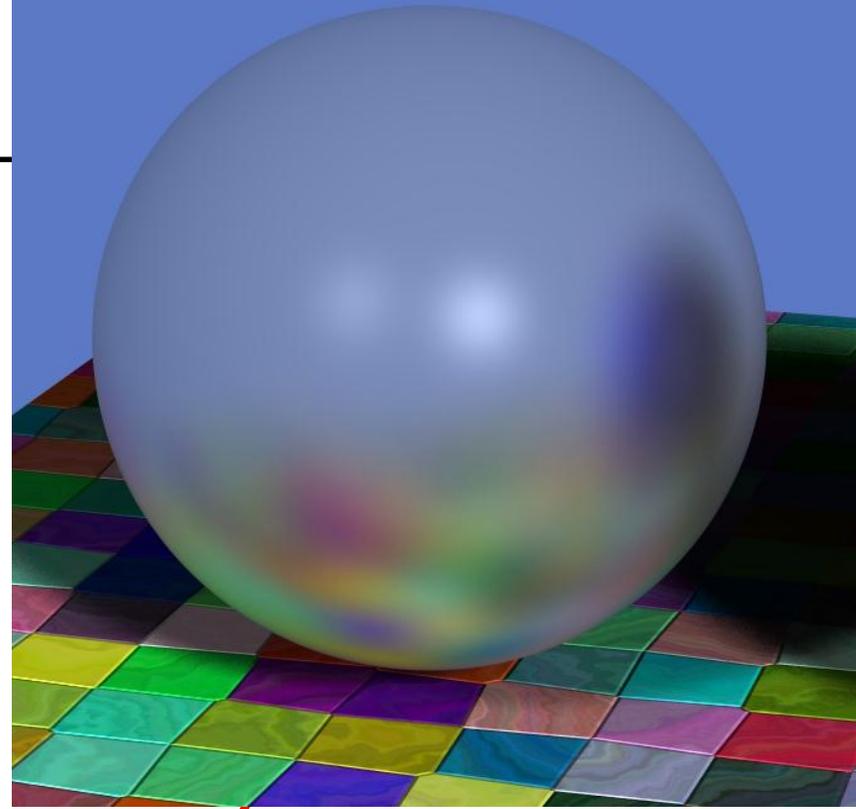
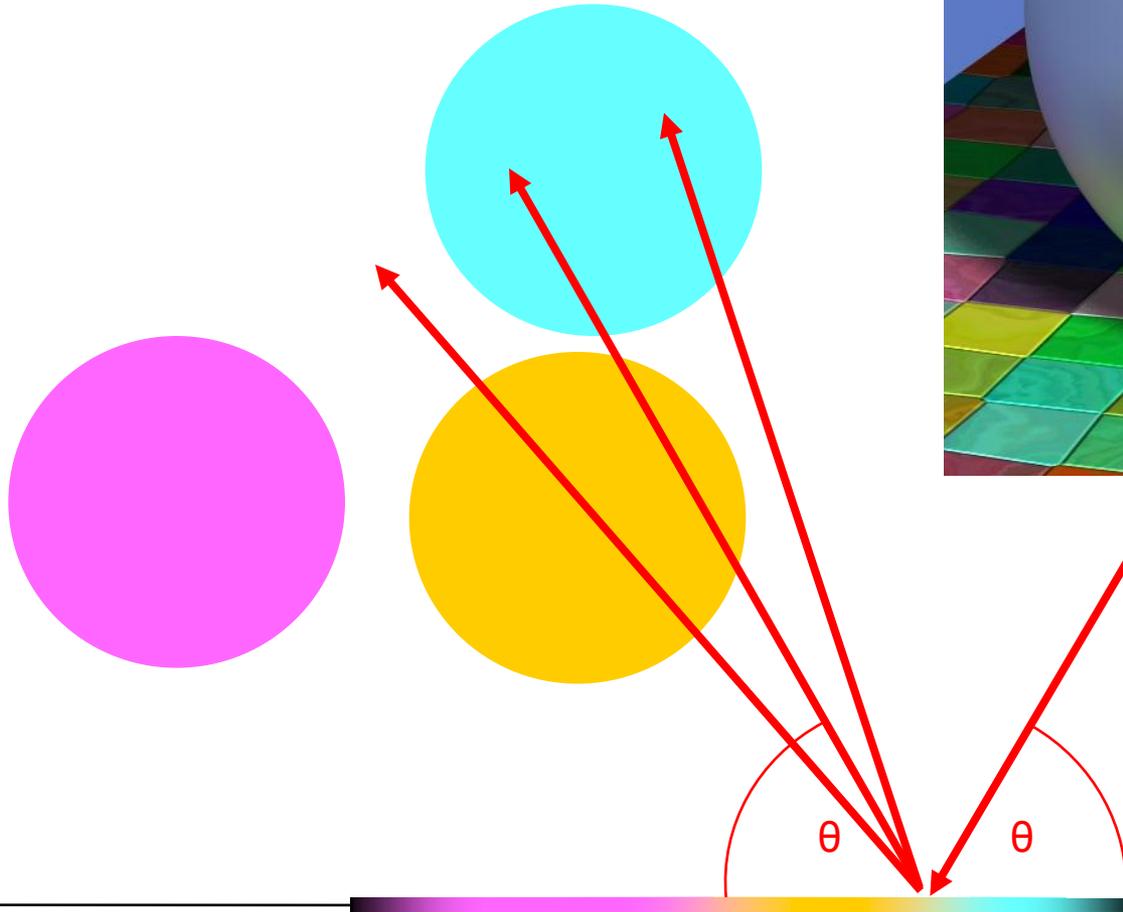
Reflection

- One reflection ray per intersection



Glossy Reflection

- Multiple reflection rays



Courtesy of Justin Legakis.

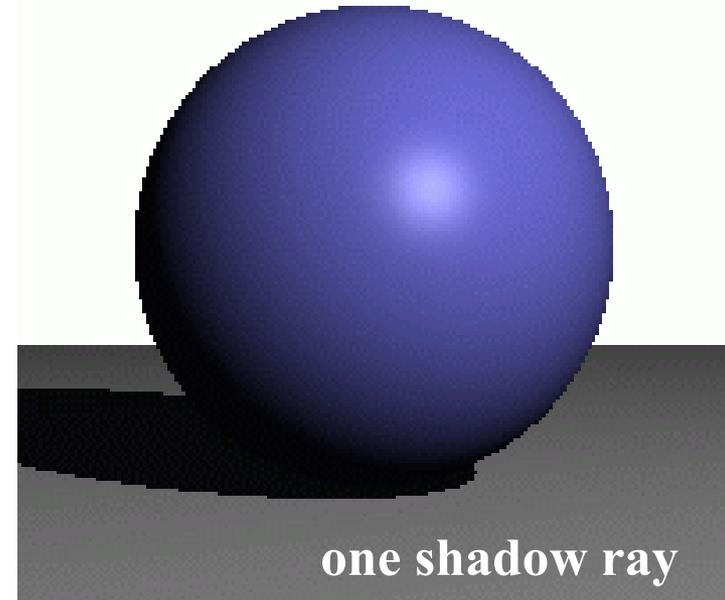
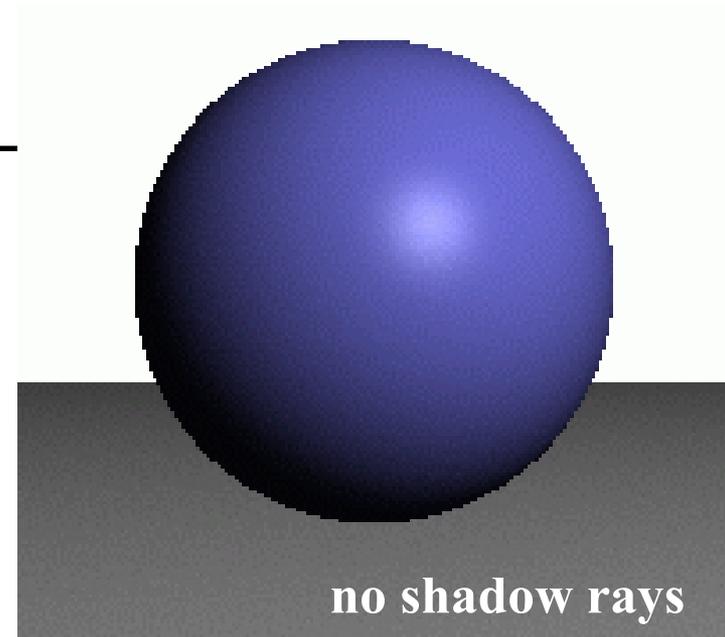
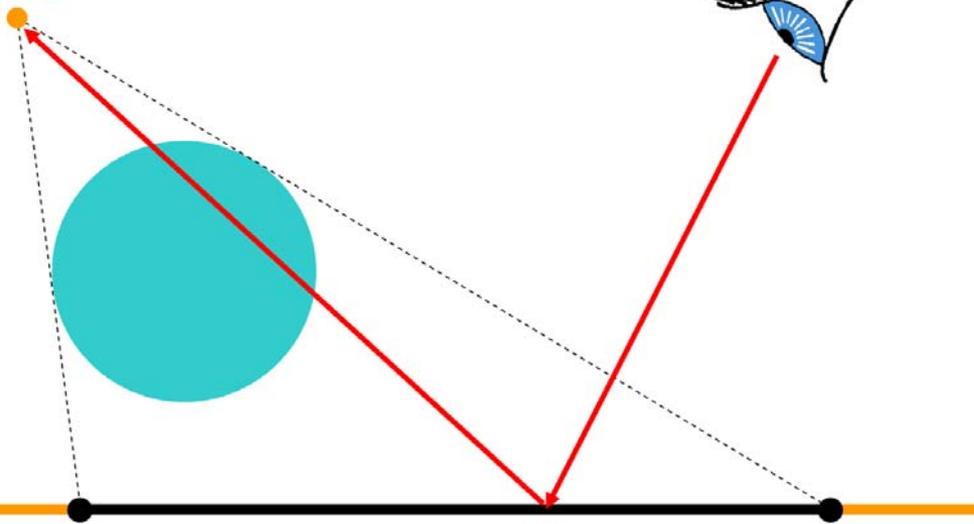
Justin Legakis

polished surface

Shadows

- One shadow ray per intersection per point light source

point light source



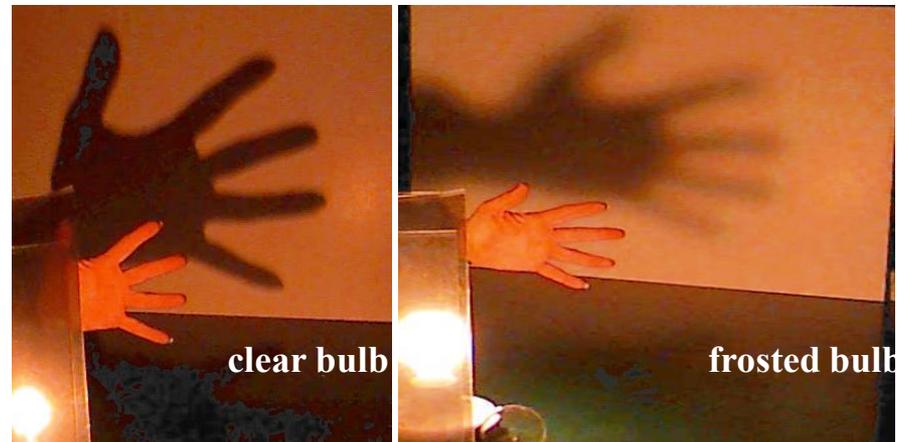
Shadows & Light Sources

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<http://www.davidfay.com/index.php>



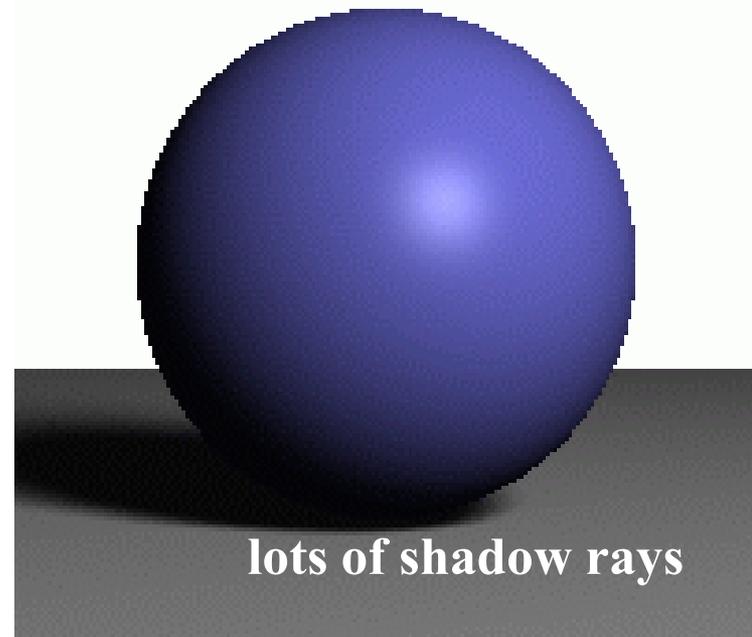
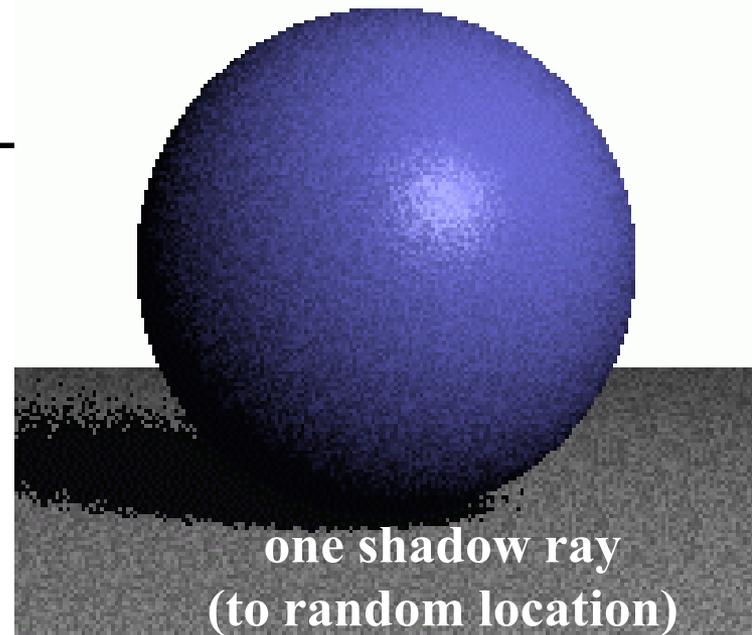
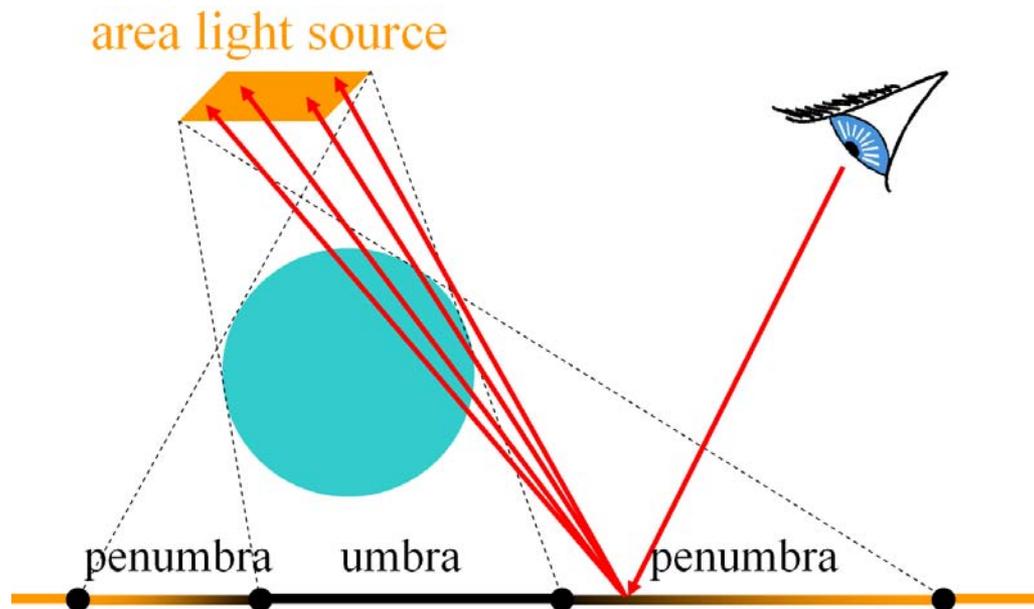
http://3media.initialized.org/photos/2000-10-18/index_gall.htm

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<http://www.pa.uky.edu/~sciworks/light/preview/bulb2.htm>

Soft Shadows

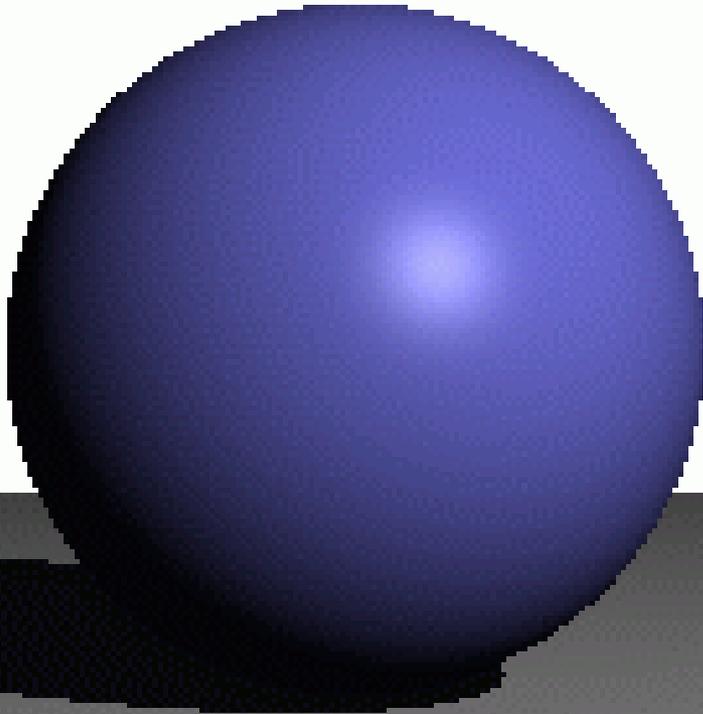
- Multiple shadow rays to sample area light source



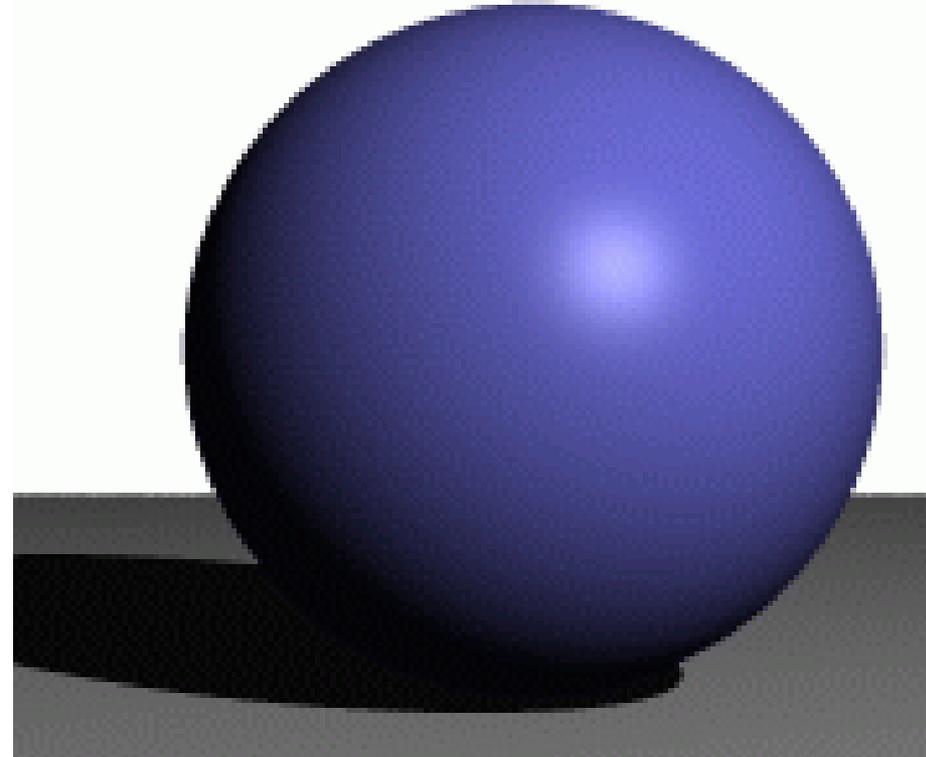
Antialiasing – Supersampling

- Multiple rays per pixel

jaggies

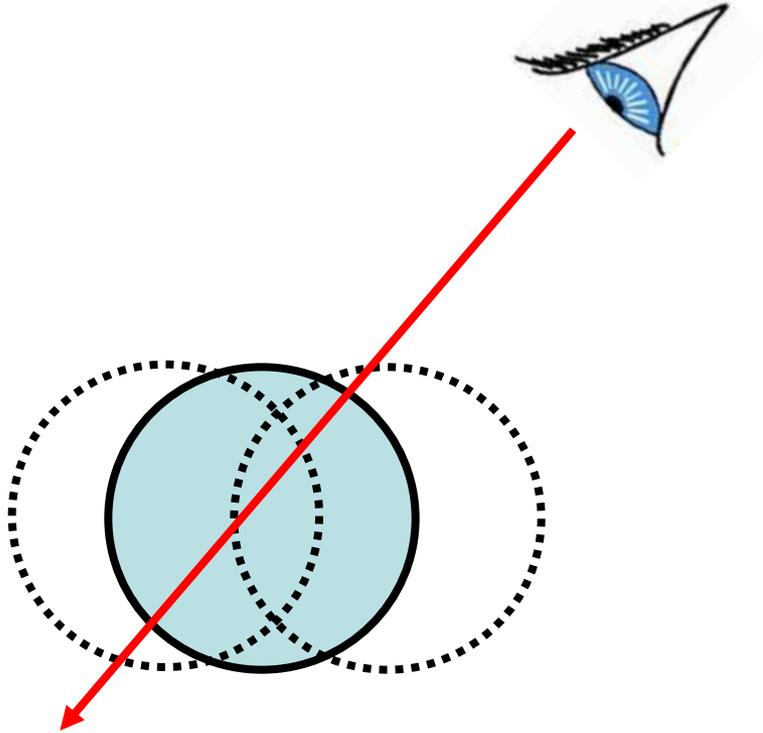


w/ antialiasing



Motion Blur

- Sample objects temporally over time interval

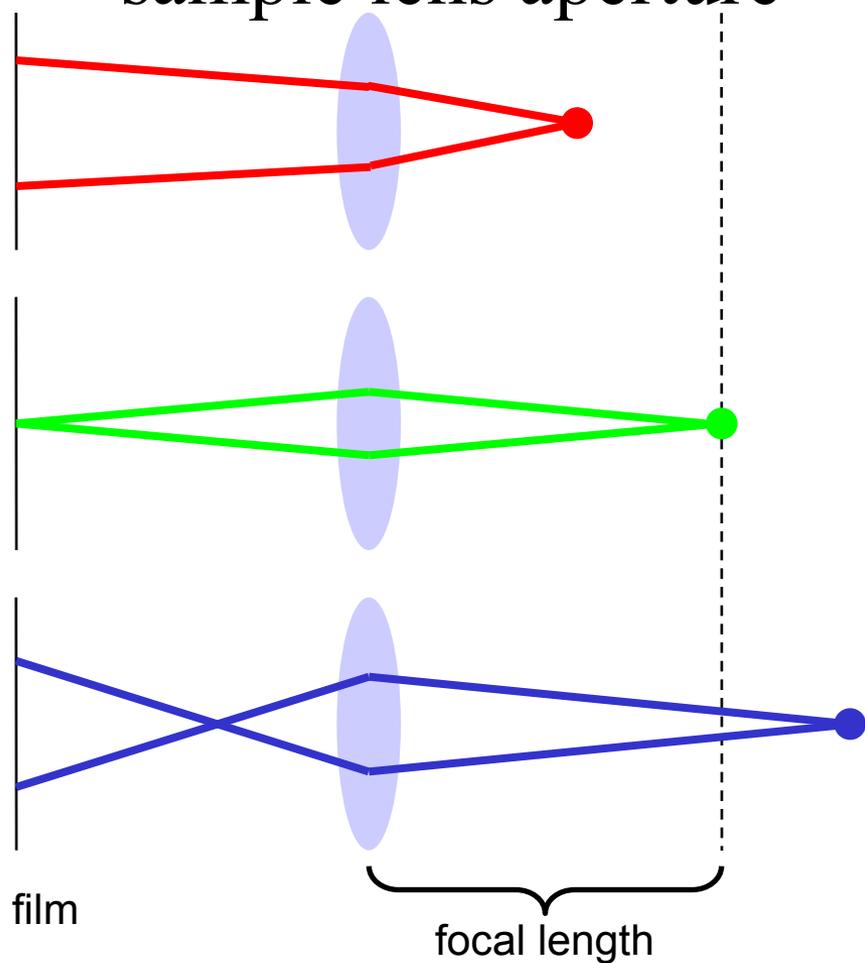


Rob Cook

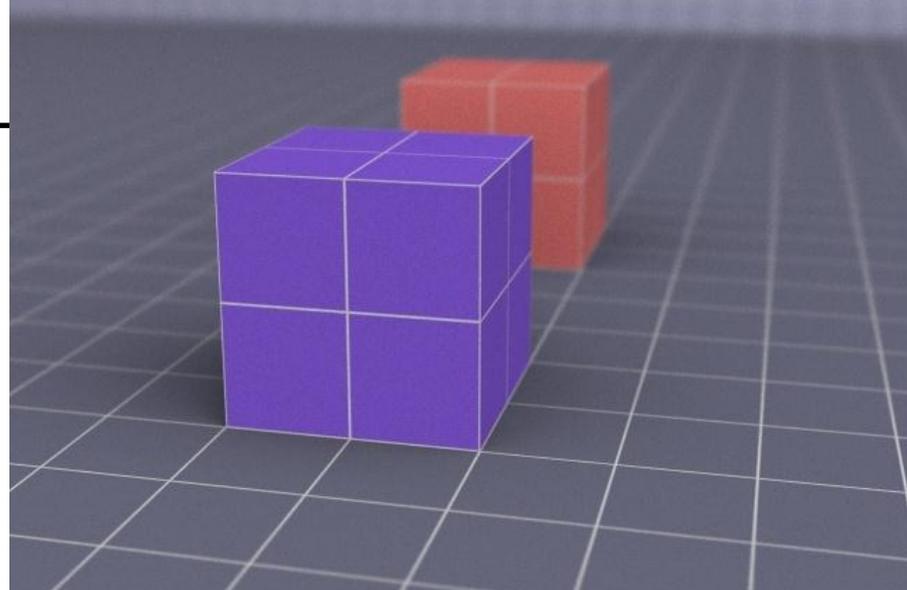
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Depth of Field

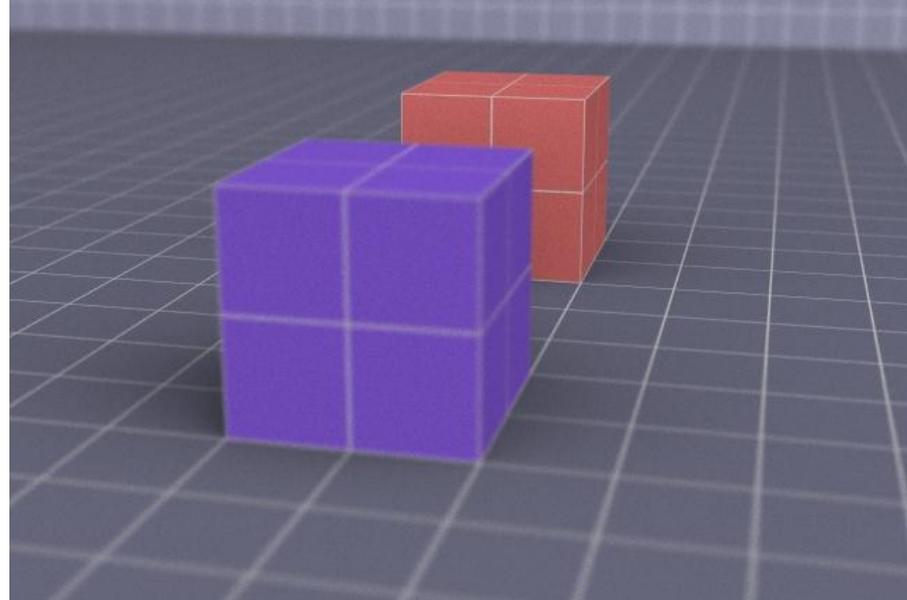
- Multiple rays per pixel:
sample lens aperture



out-of-focus blur



out-of-focus blur



Questions?

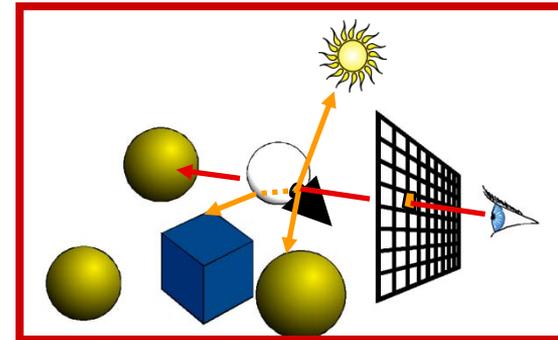
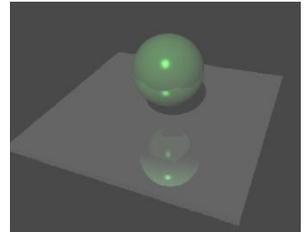
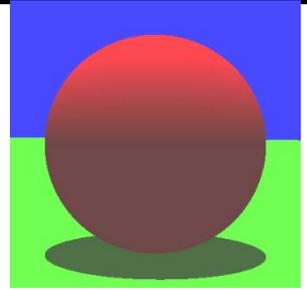
Henrik Wann Jensen



Courtesy of Henrik Wann Jensen. Used with permission.

Overview of Today

- Shadows
- Reflection
- Refraction
- Recursive Ray Tracing



Recap: Ray Tracing

trace ray

Intersect all objects

color = ambient term

For every light

 cast shadow ray

 color += local shading term

If mirror

 color += $color_{refl} *$

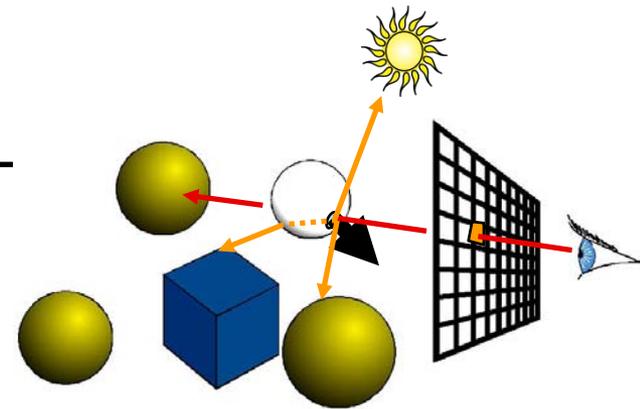
 trace reflected ray

If transparent

 color += $color_{trans} *$

 trace transmitted ray

- *Does it ever end?*



Stopping criteria:

- Recursion depth
 - Stop after a number of bounces
- Ray contribution
 - Stop if reflected / transmitted contribution becomes too small

Recursion For Reflection: None

Images removed due to copyright restrictions -- please see the images of "Scene with no reflection rays." "Scene with one layer of reflection." "Scene with two layers of reflection." available at <http://www.siggraph.org/education/materials/HyperGraph/raytrace/rtrace1.htm> for further details.

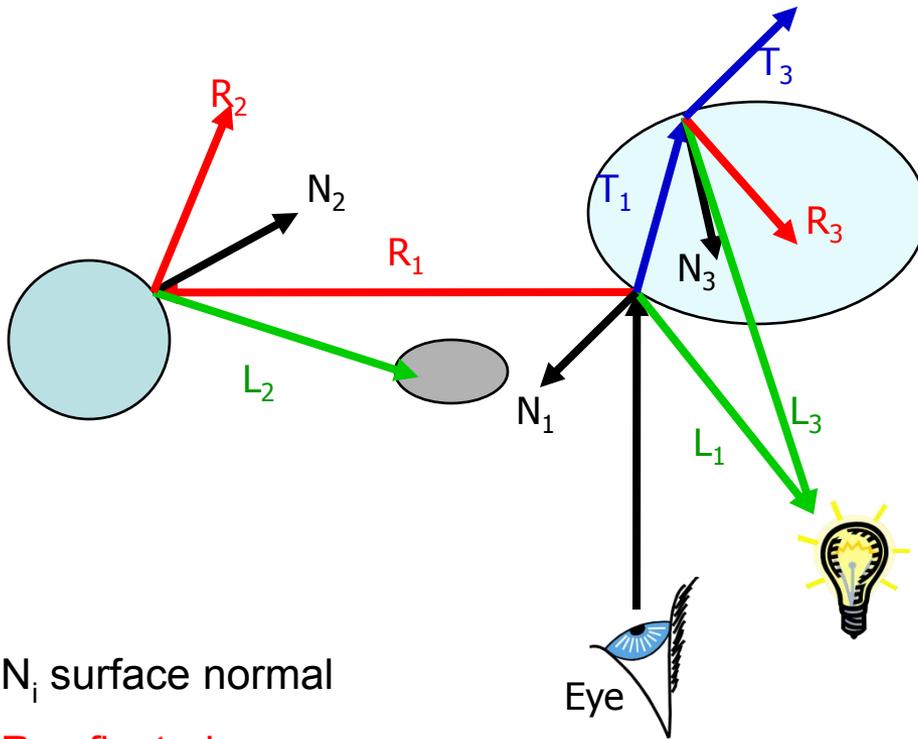
Recursion For Reflection: 1

Images removed due to copyright restrictions -- please see the images of "Scene with no reflection rays." "Scene with one layer of reflection." "Scene with two layers of reflection." available at <http://www.siggraph.org/education/materials/HyperGraph/raytrace/rtrace1.htm> for further details.

Recursion For Reflection: 2

Images removed due to copyright restrictions -- please see the images of "Scene with no reflection rays." "Scene with one layer of reflection." "Scene with two layers of reflection." available at <http://www.siggraph.org/education/materials/HyperGraph/raytrace/rtrace1.htm> for further details.

The Ray Tree

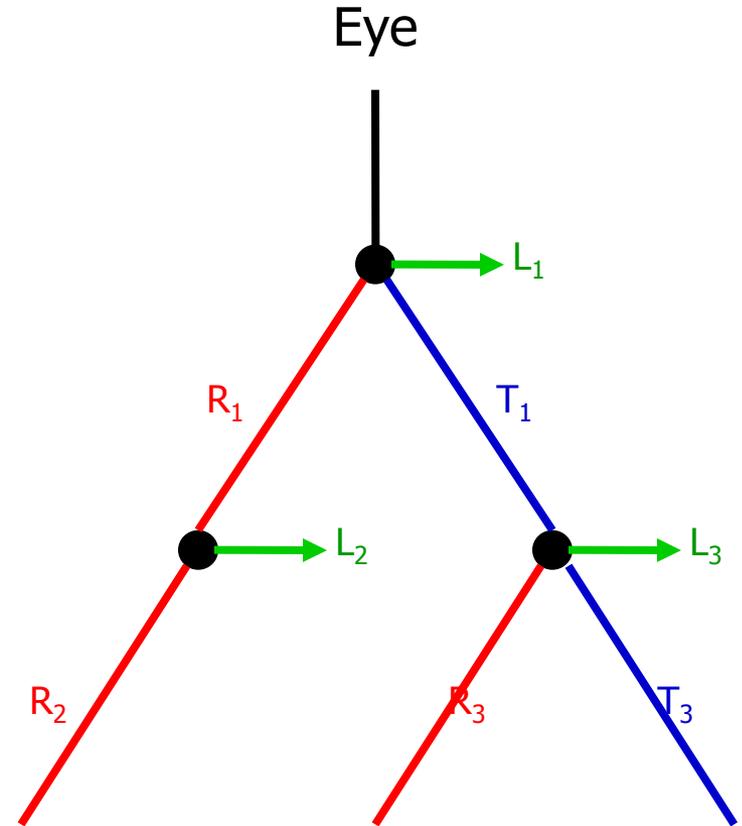


N_i surface normal

R_i reflected ray

L_i shadow ray

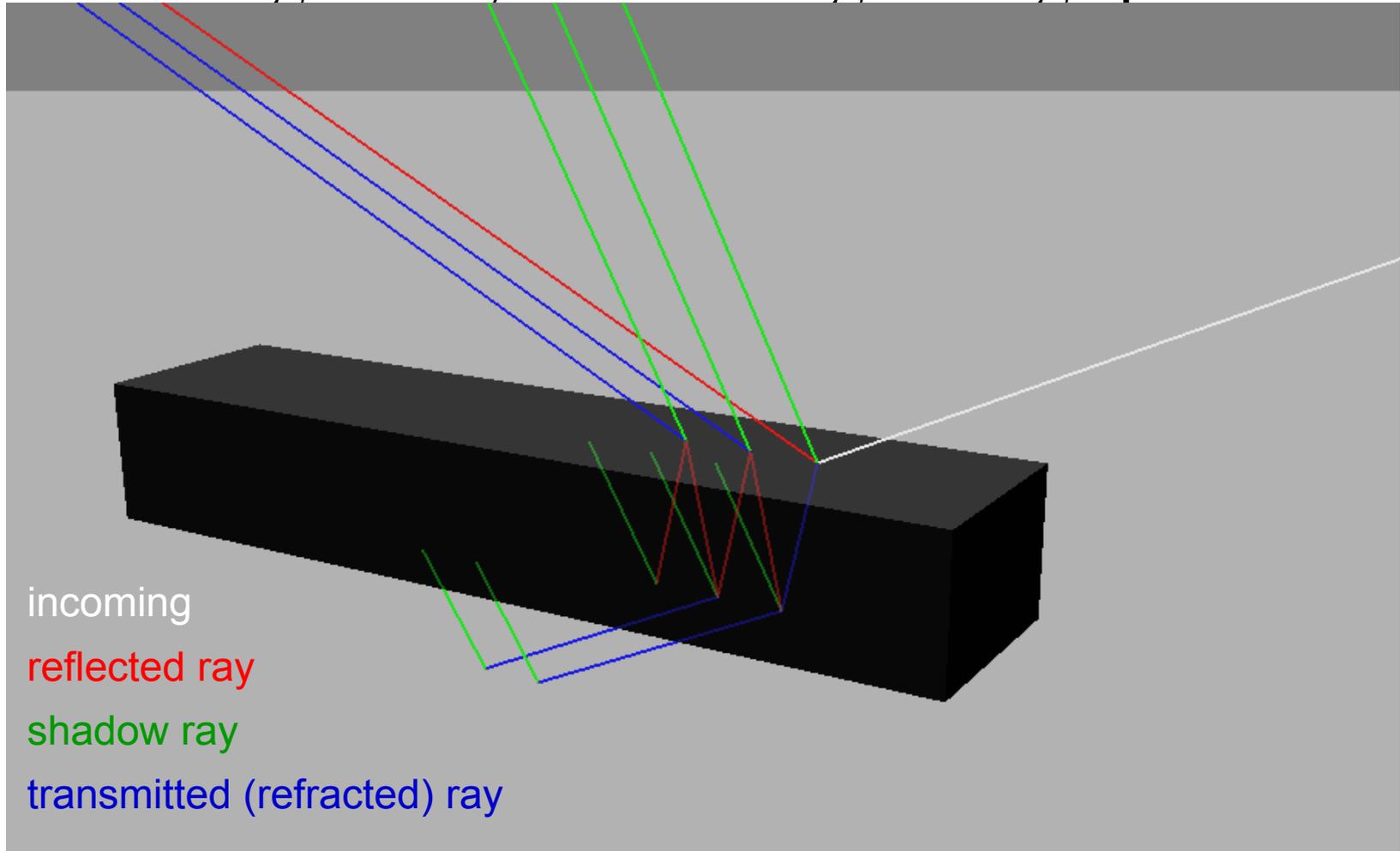
T_i transmitted (refracted) ray



Complexity?

Ray tree

- Visualizing the ray tree for single image pixel



Stack Studios, Rendered using Maxwell

That's All for Today

Further reading:

- [Shirley: Realistic Ray Tracing](#)
- [Dutre et al.: Advanced Global Illumination](#)

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6.837 Computer Graphics
Fall 2012

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