## Massachusetts Institute of Technology

## Department of Electrical Engineering & Computer Science

## **6.041/6.431:** Probabilistic Systems Analysis (Fall 2010)

## Tutorial/Recitation 9: Solutions

- 1. Problem 7.1, page 380 in textbook. See online solutions.
- 2. (a) Recurrent: 1, 2, 4, 5, 6; Transient: 3; Periodic: 4,5,6.
  - (b)  $0.2^n$
  - (c) This is a geometric random variable with parameter p = 0.5 + 0.3. Hence, the expected number of trials up to and including the trial on which the process leaves state 3 is  $\mathbf{E}[X] = 1/p = 5/4$ .
  - (d) 3/8
  - (e)  $\mathbf{P}(A) = 0.3 + 0.2^3 \cdot 0.3 + 0.2^6 \cdot 0.3 + 0.2^9 \cdot 0.3 = 0.3024.$
  - (f)  $0.3/\mathbf{P}(A) = 0.992$ .
- 3. Problem 7.13, page 385 in textbook. See online solutions.

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