

MIT 6.035 Introduction to Shift-Reduce Parsing

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Orientation

- Specify Syntax Using Context-Free Grammar
 - Nonterminals
 - Terminals
 - Productions
- Given a grammar, Parser Generator produces a parser
 - Starts with input string
 - Produces parse tree

$$Expr \rightarrow Expr \ Op \ Expr$$
$$Expr \rightarrow (Expr)$$
$$Expr \rightarrow - Expr$$
$$Expr \rightarrow num$$
$$Op \rightarrow +$$
$$Op \rightarrow -$$
$$Op \rightarrow *$$

Today's Lecture

- How generated parser works
- How parser generator produces parser
- Central mechanism
 - Pushdown automaton, which implements
 - Shift-reduce parser

Pushdown Automata

- Consists of
 - Pushdown stack (can have terminals and nonterminals)
 - Finite state automaton control
- Can do one of three actions (based on state and input):
 - Shift:
 - Shift current input symbol from input onto stack
 - Reduce:
 - If symbols on top of stack match right hand side of some grammar production $NT \rightarrow \beta$
 - Pop symbols (β) off of the stack
 - Push left hand side nonterminal (NT) onto stack
 - Accept the input string

Shift-Reduce Parser Example

$Expr \rightarrow Expr \text{ } Op \text{ } Expr$

$Expr \rightarrow (Expr)$

$Expr \rightarrow - Expr$

$Expr \rightarrow num$

$Op \rightarrow +$

$Op \rightarrow -$

$Op \rightarrow *$

Stack

Input String

num	*	(num	+	num)
-----	---	---	-----	---	-----	---

Shift-Reduce Parser Example

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num	*	(num	+	num)
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SHIFT

num	*	(num	+	num)
-----	---	---	-----	---	-----	---

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num

SHIFT

*	(num	+	num)
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Shift-Reduce Parser Example

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num

REDUCE

*	(num	+	num)
---	---	-----	---	-----	---

Shift-Reduce Parser Example

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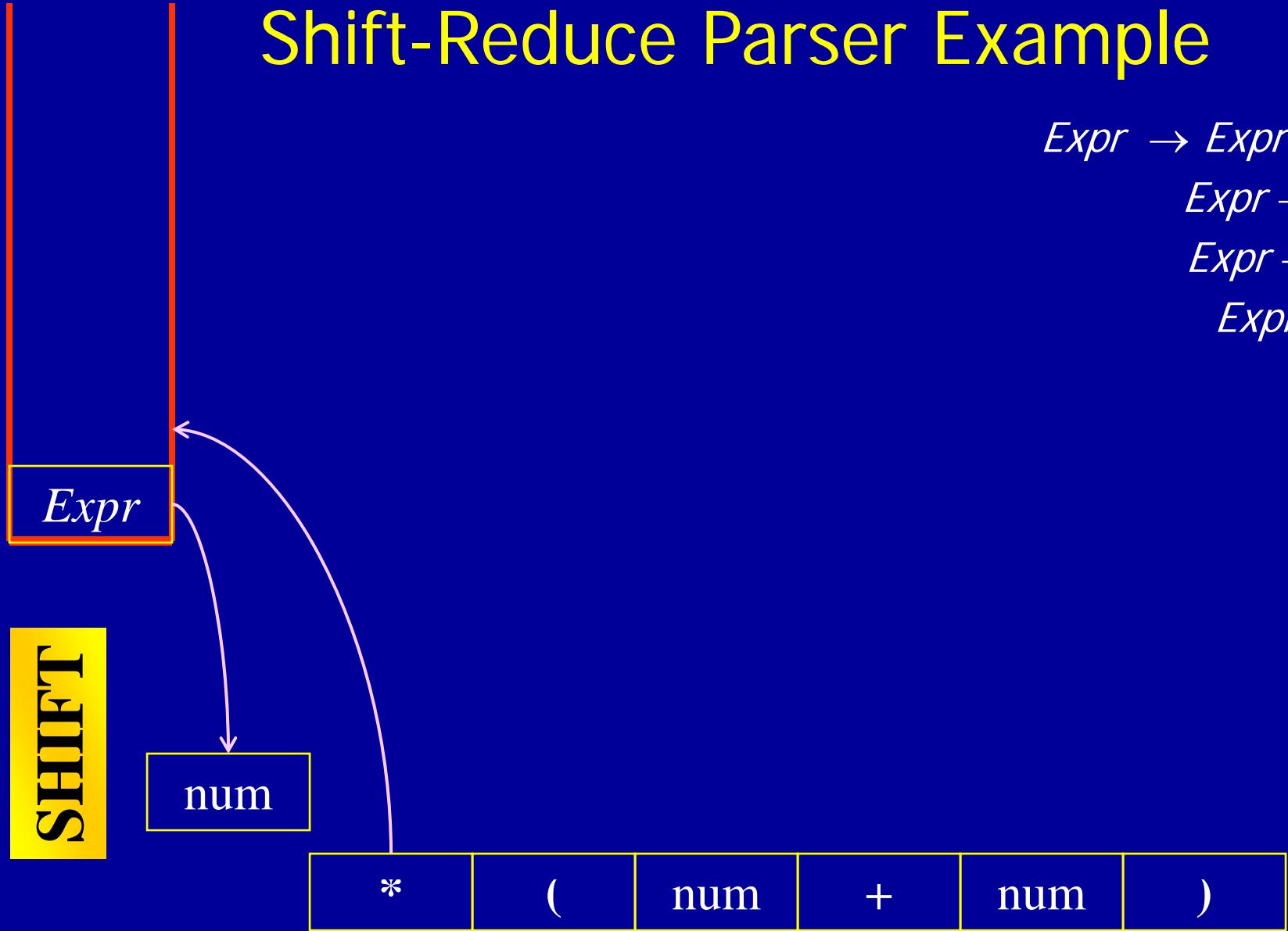
$Expr$

REDUCE

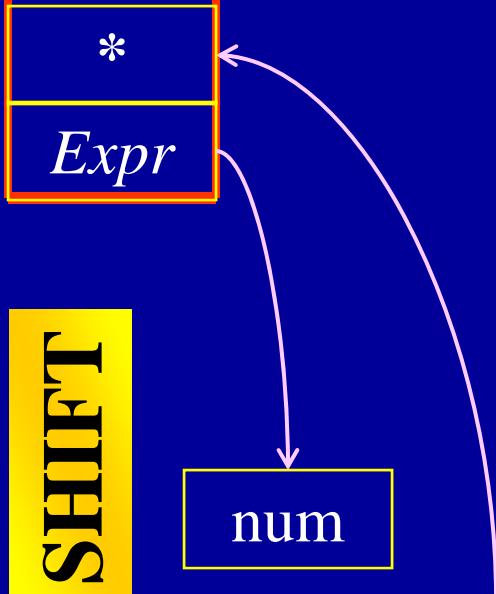
num

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REDUCE



Shift-Reduce Parser Example

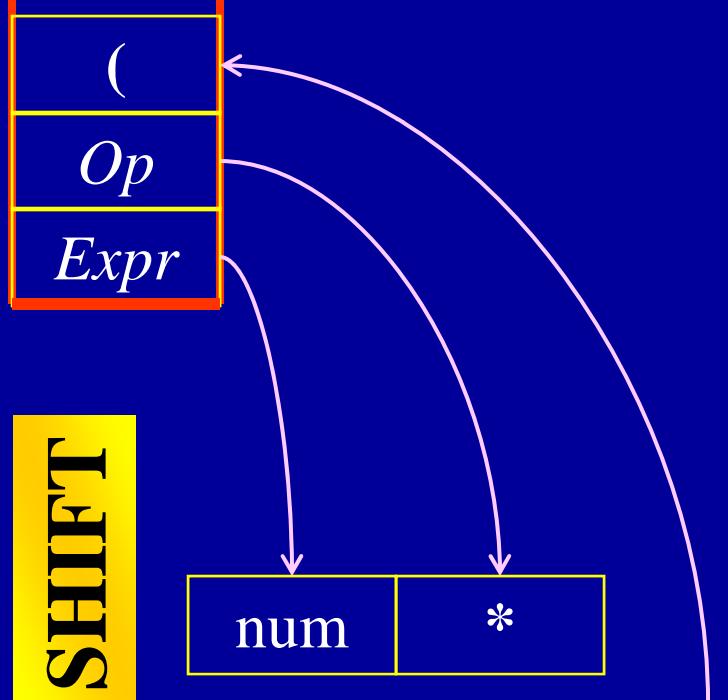
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SHIFT

A horizontal row of tokens represented by a box divided into two equal-sized cells. The left cell contains the text "num" and the right cell contains the symbol "*".

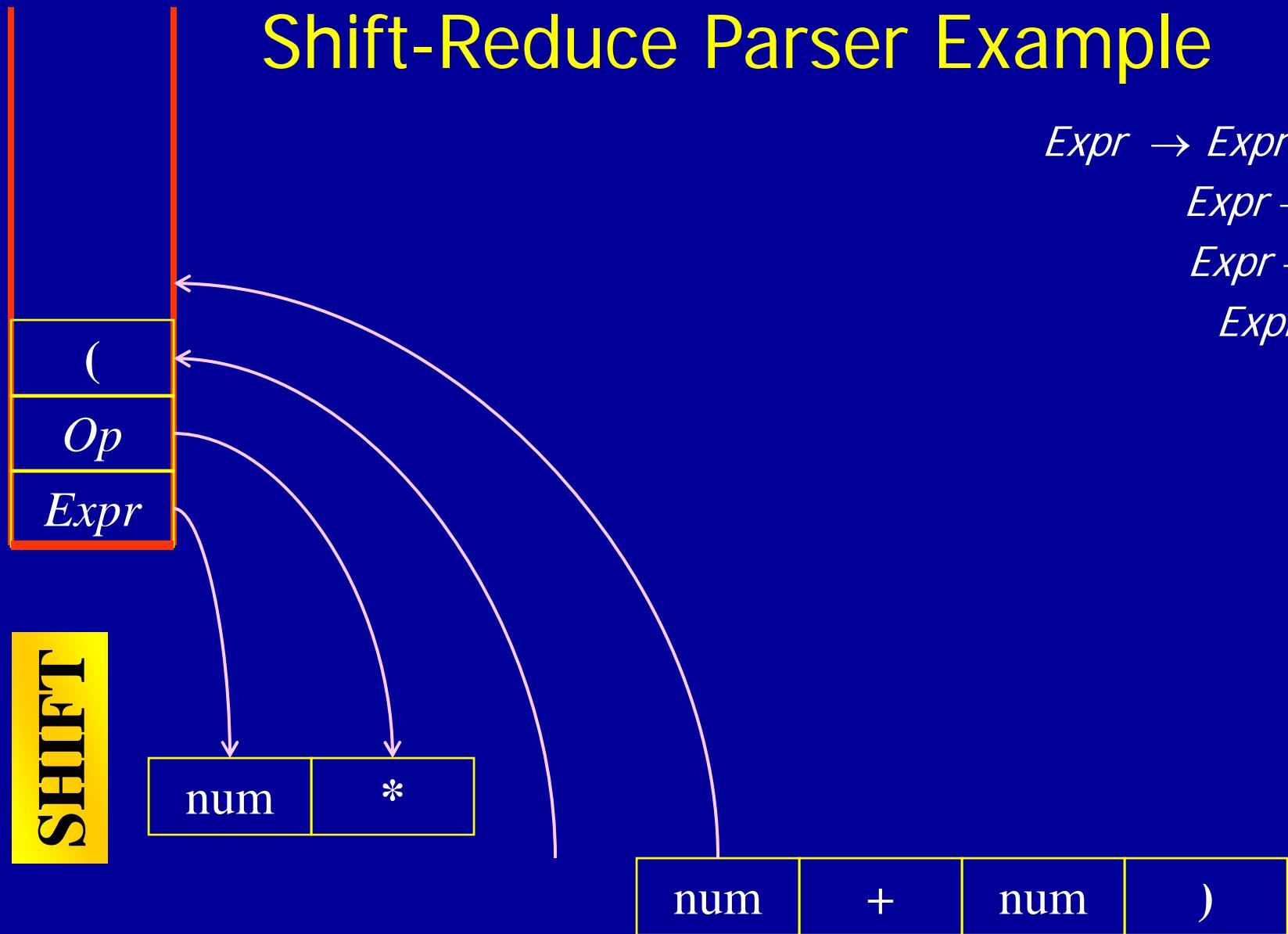
A horizontal row of tokens represented by a box divided into five equal-sized cells. The first cell contains the symbol "(", the second cell contains "num", the third cell contains "+", the fourth cell contains "num", and the fifth cell contains ")".

Shift-Reduce Parser Example

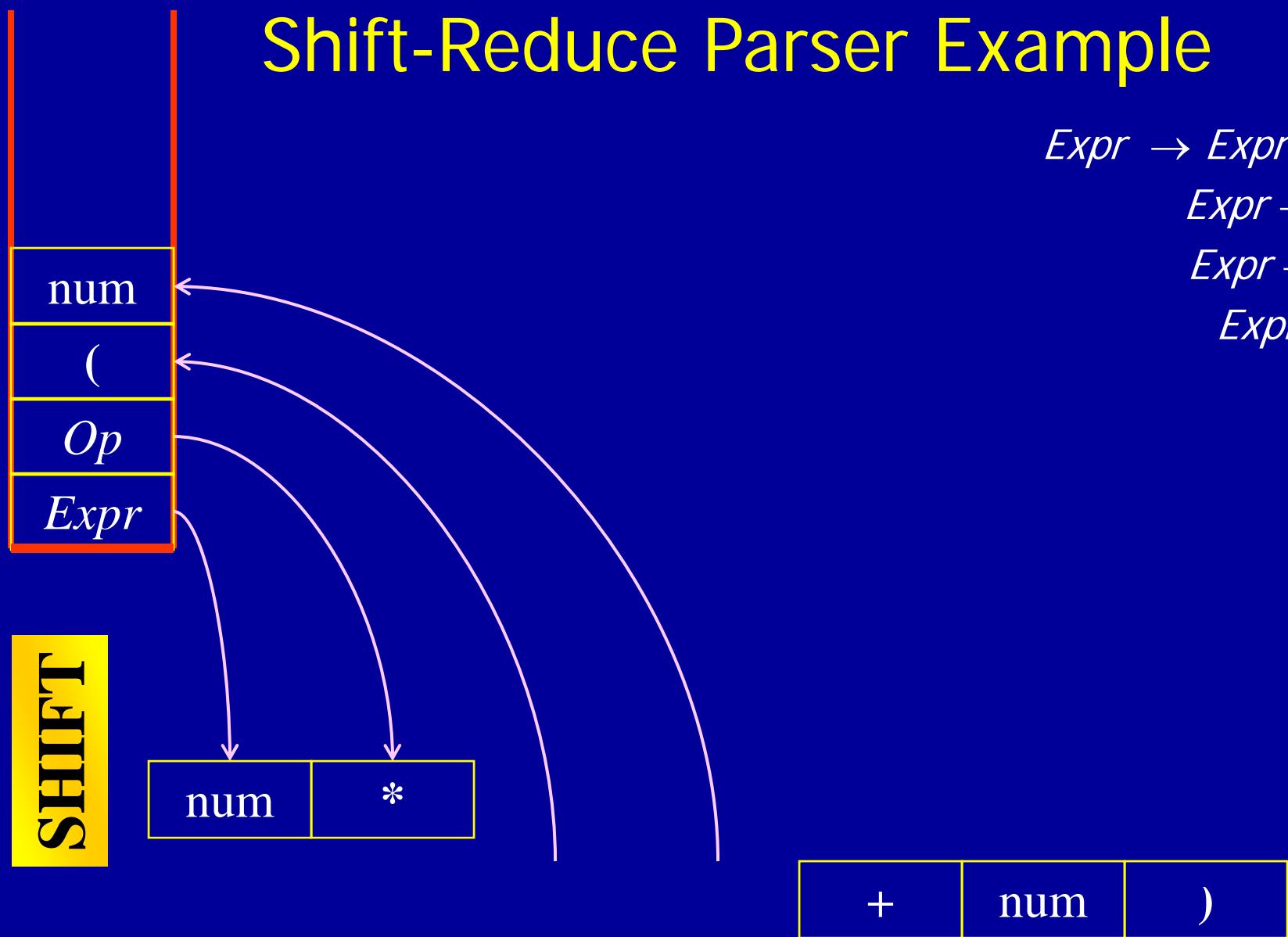
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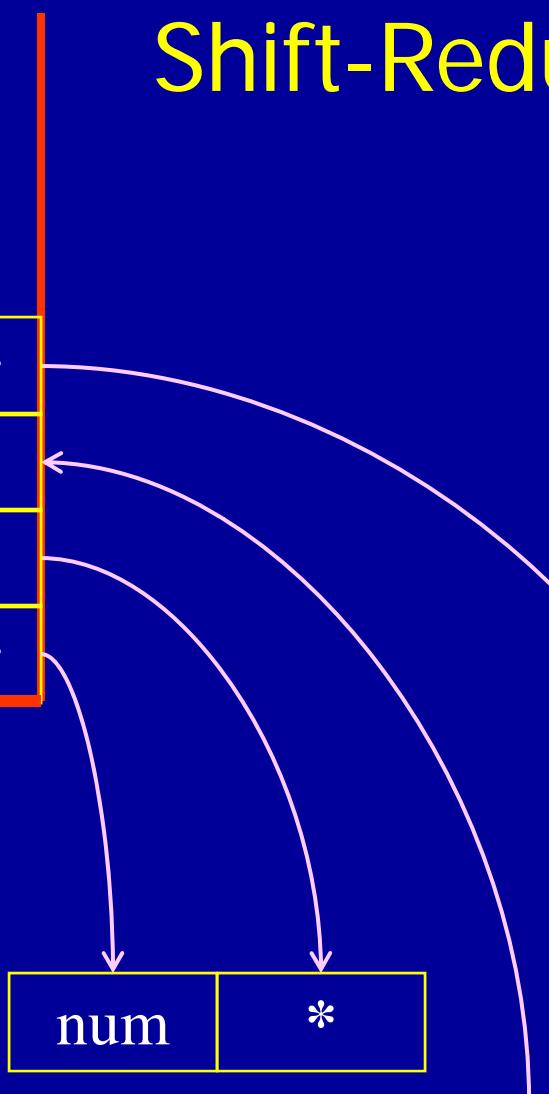
$Expr$
(
 Op
 $Expr$

REDUCE

num | $*$

num

$+$ | num | $)$



Shift-Reduce Parser Example

Expr → *Expr Op Expr*

Expr → (*Expr*)

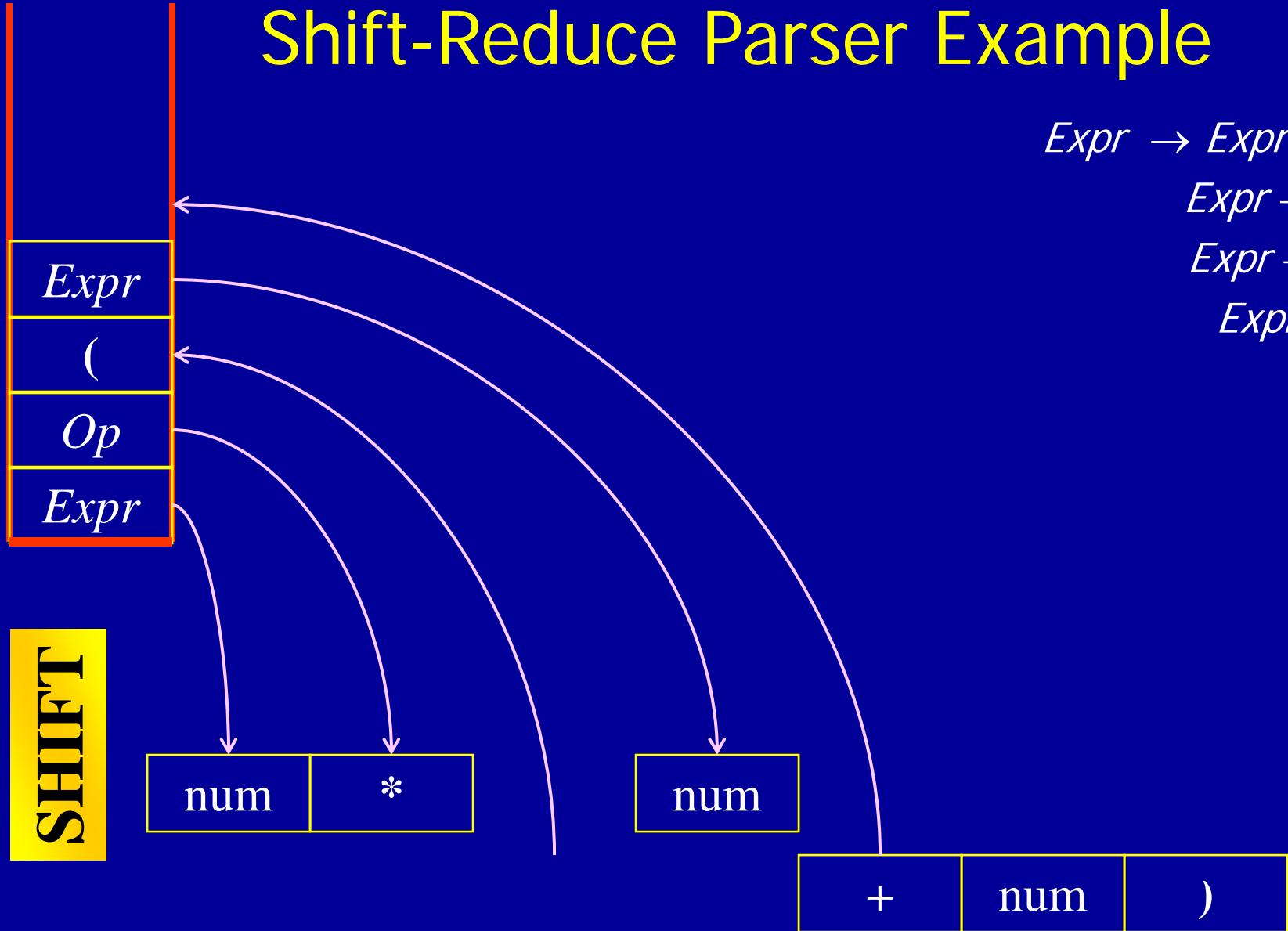
Expr → - *Expr*

Expr → num

Op → +

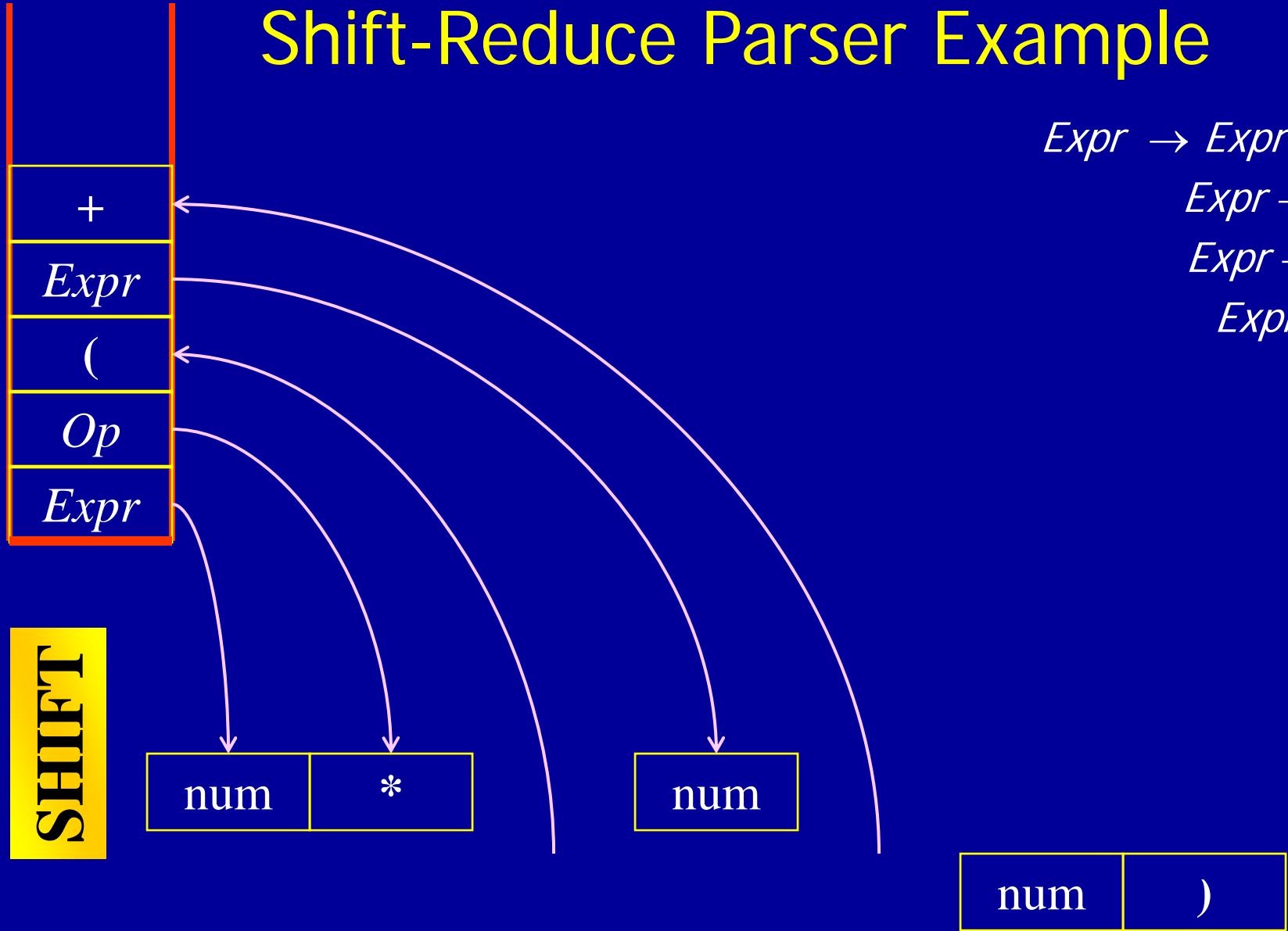
Op → -

Op → *



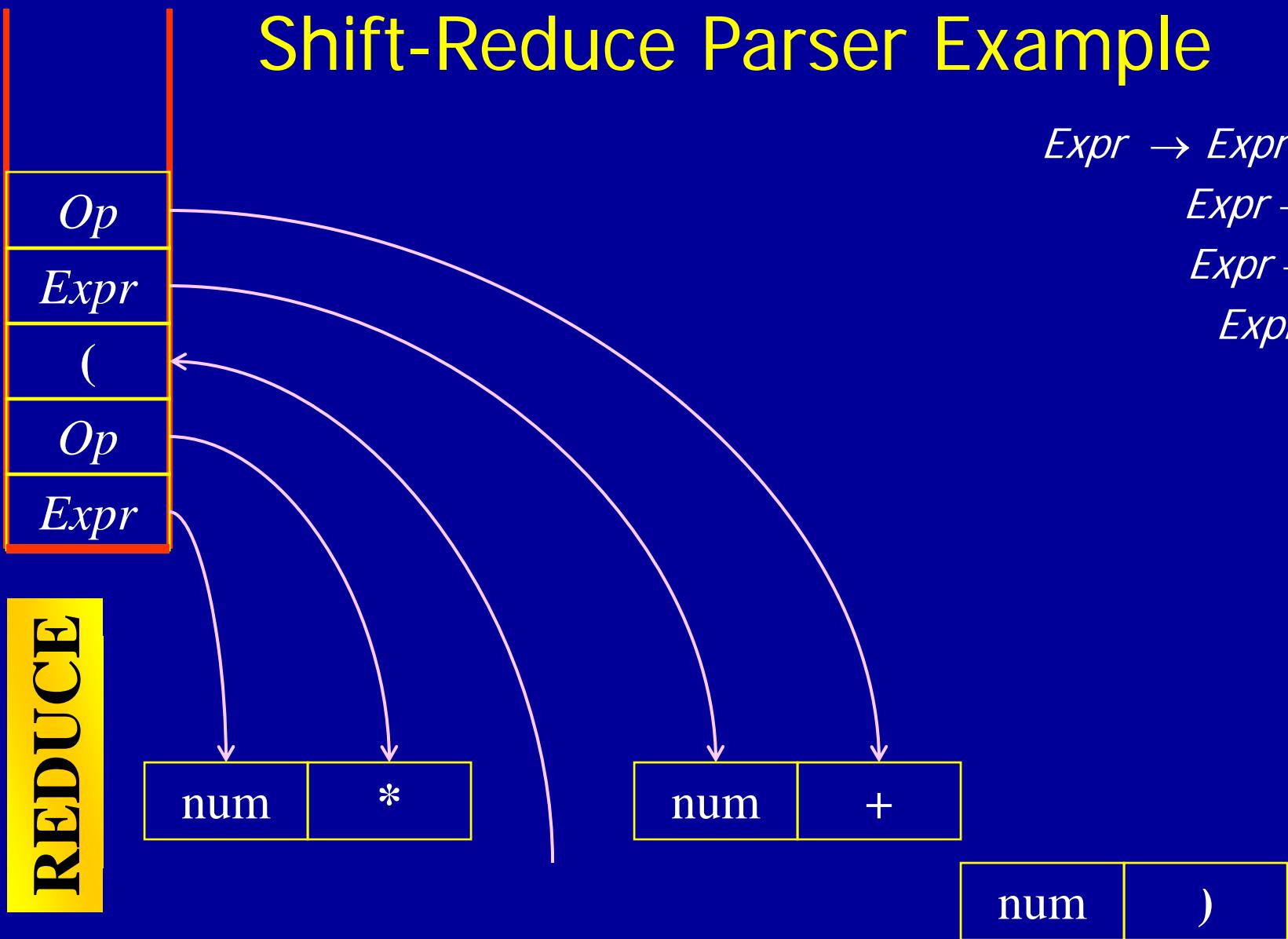
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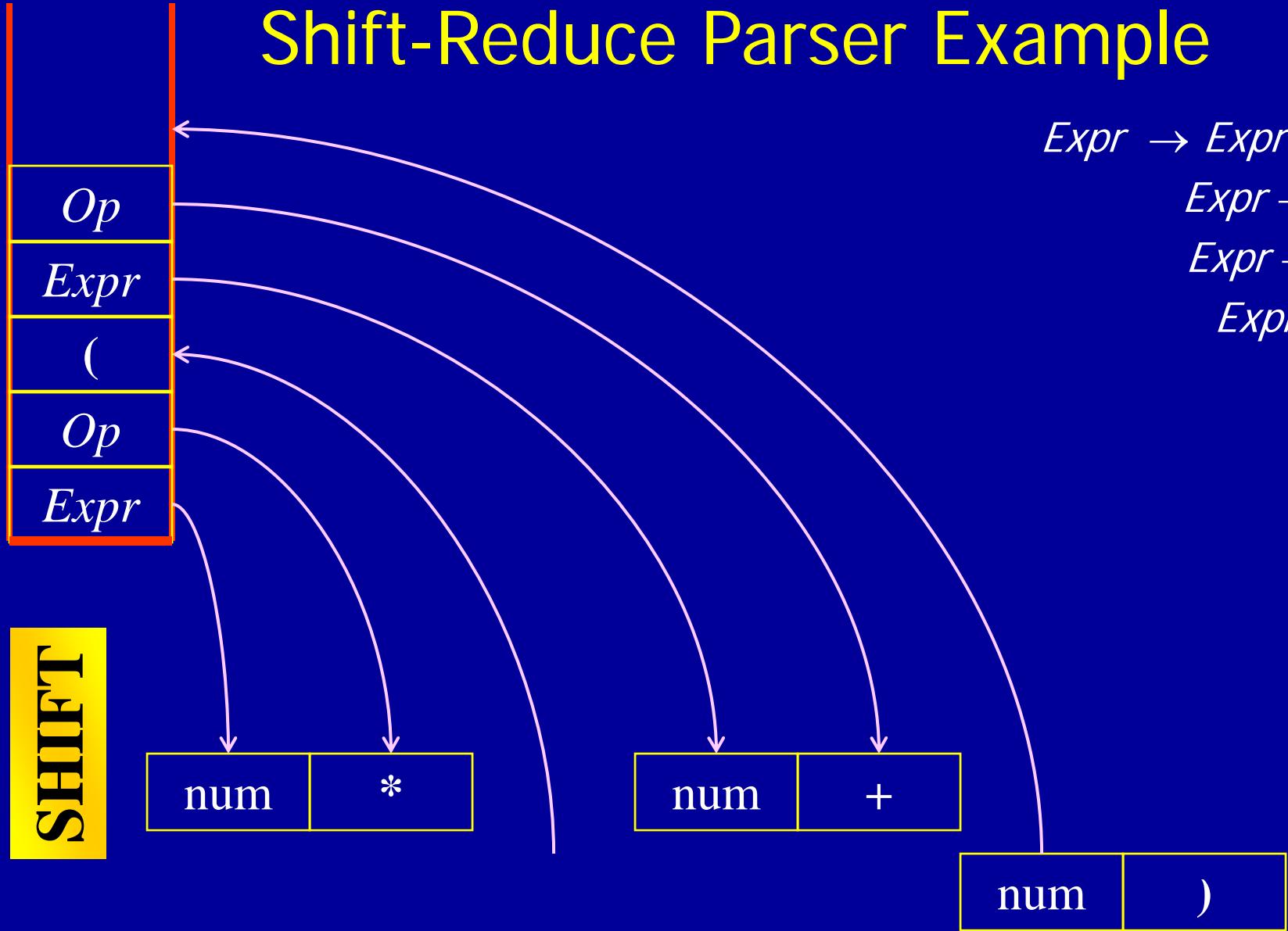
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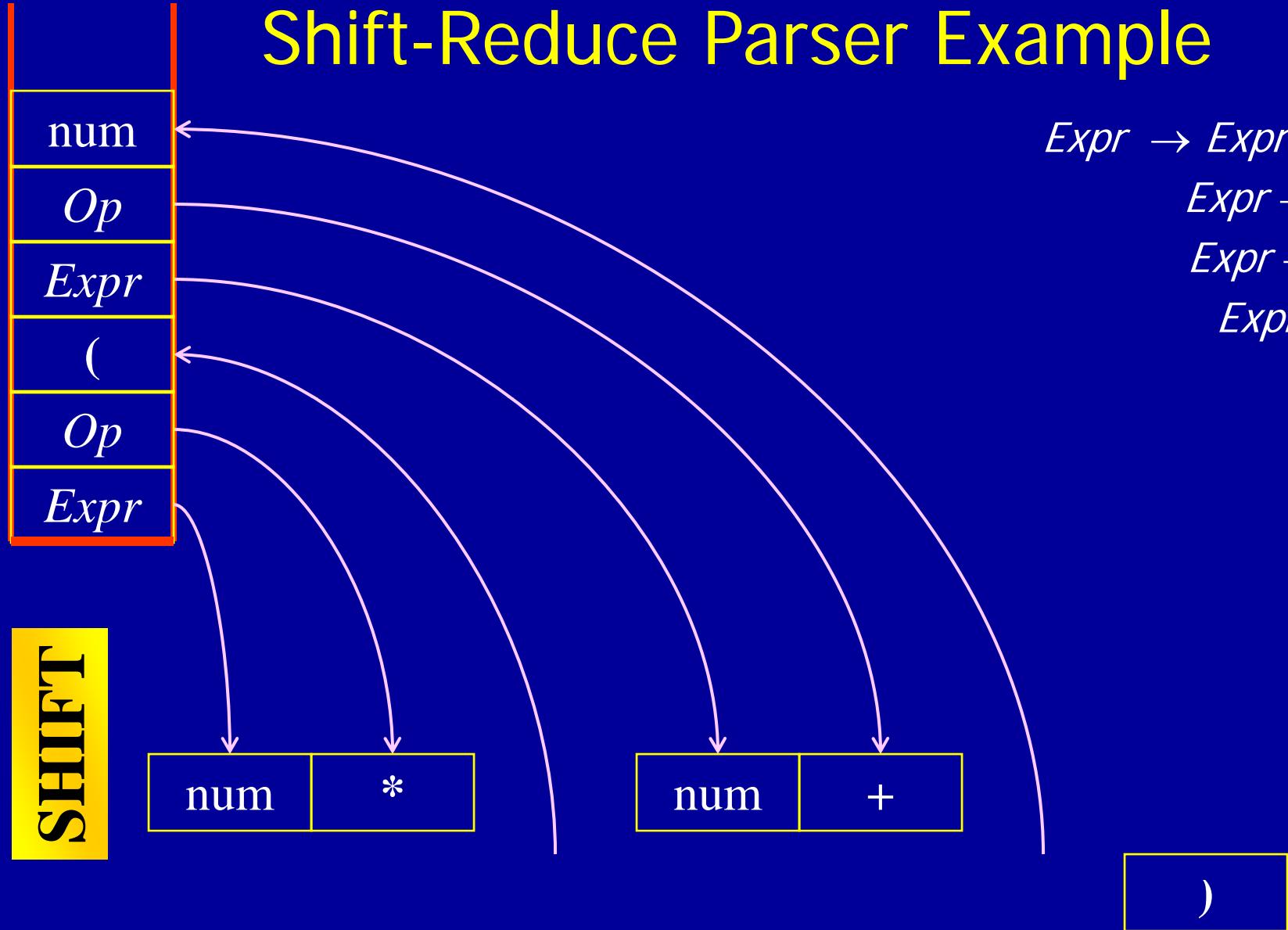


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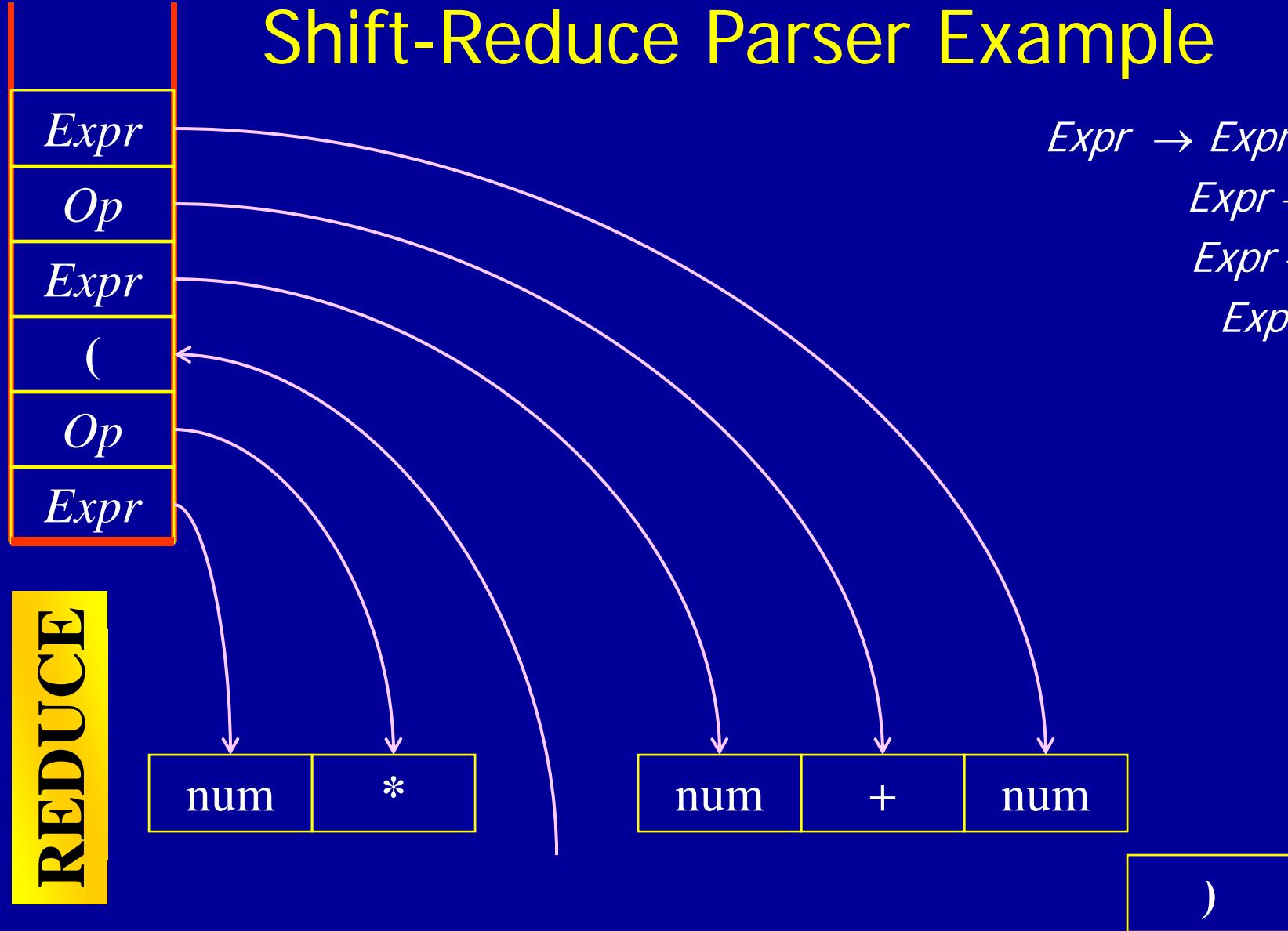


Shift-Reduce Parser Example



$Expr \rightarrow Expr \ Op \ Expr$
 $Expr \rightarrow (Expr)$
 $Expr \rightarrow - Expr$
 $Expr \rightarrow num$
 $Op \rightarrow +$
 $Op \rightarrow -$
 $Op \rightarrow *$

Shift-Reduce Parser Example



Shift-Reduce Parser Example

Expr
(
Op
Expr

$$Expr \rightarrow Expr \ Op \ Expr$$

$$Expr \rightarrow (Expr)$$

$$Expr \rightarrow - Expr$$

$$Expr \rightarrow num$$

$$Op \rightarrow +$$

$$Op \rightarrow -$$

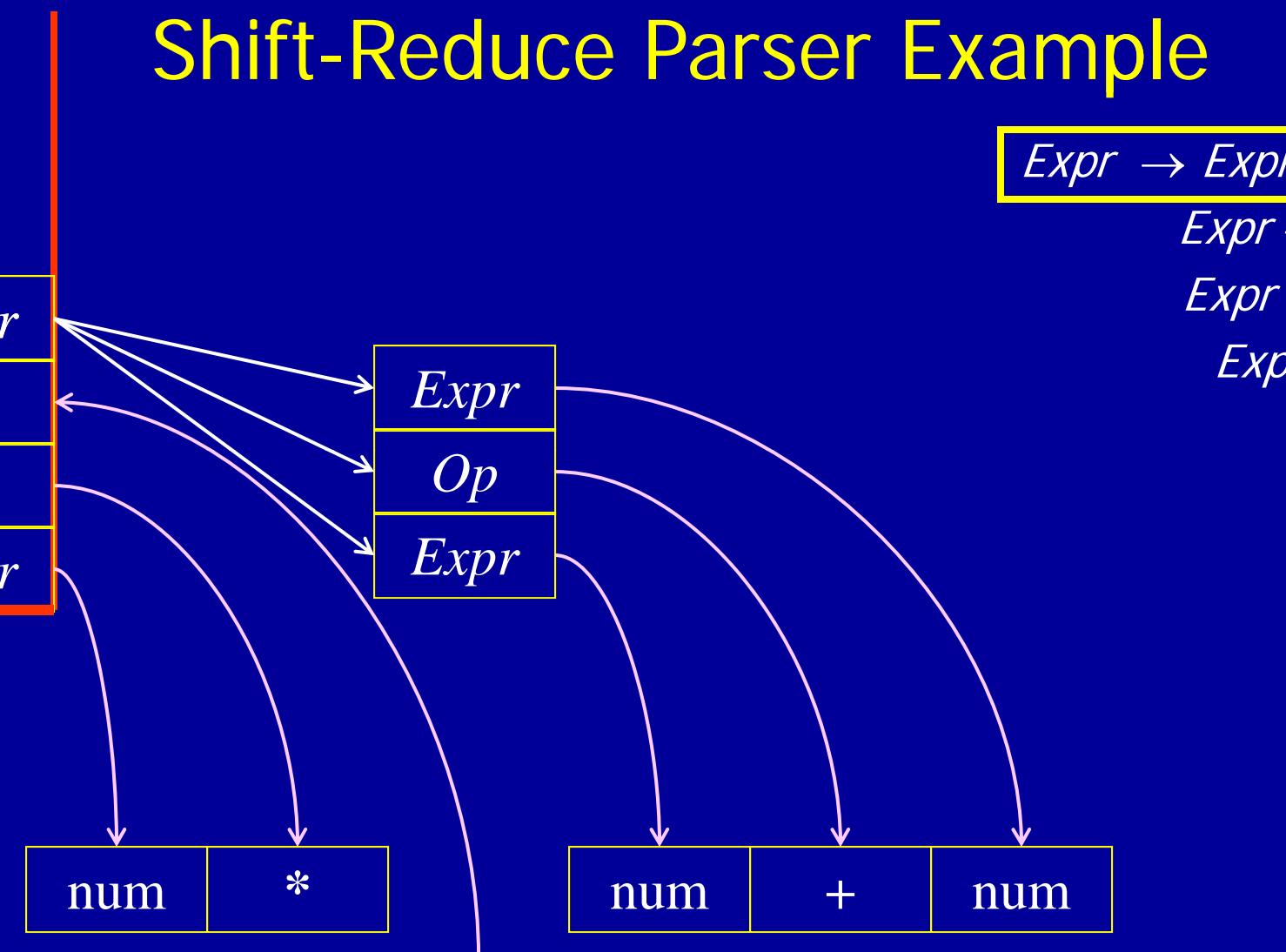
$$Op \rightarrow *$$

REDUCE

num | *

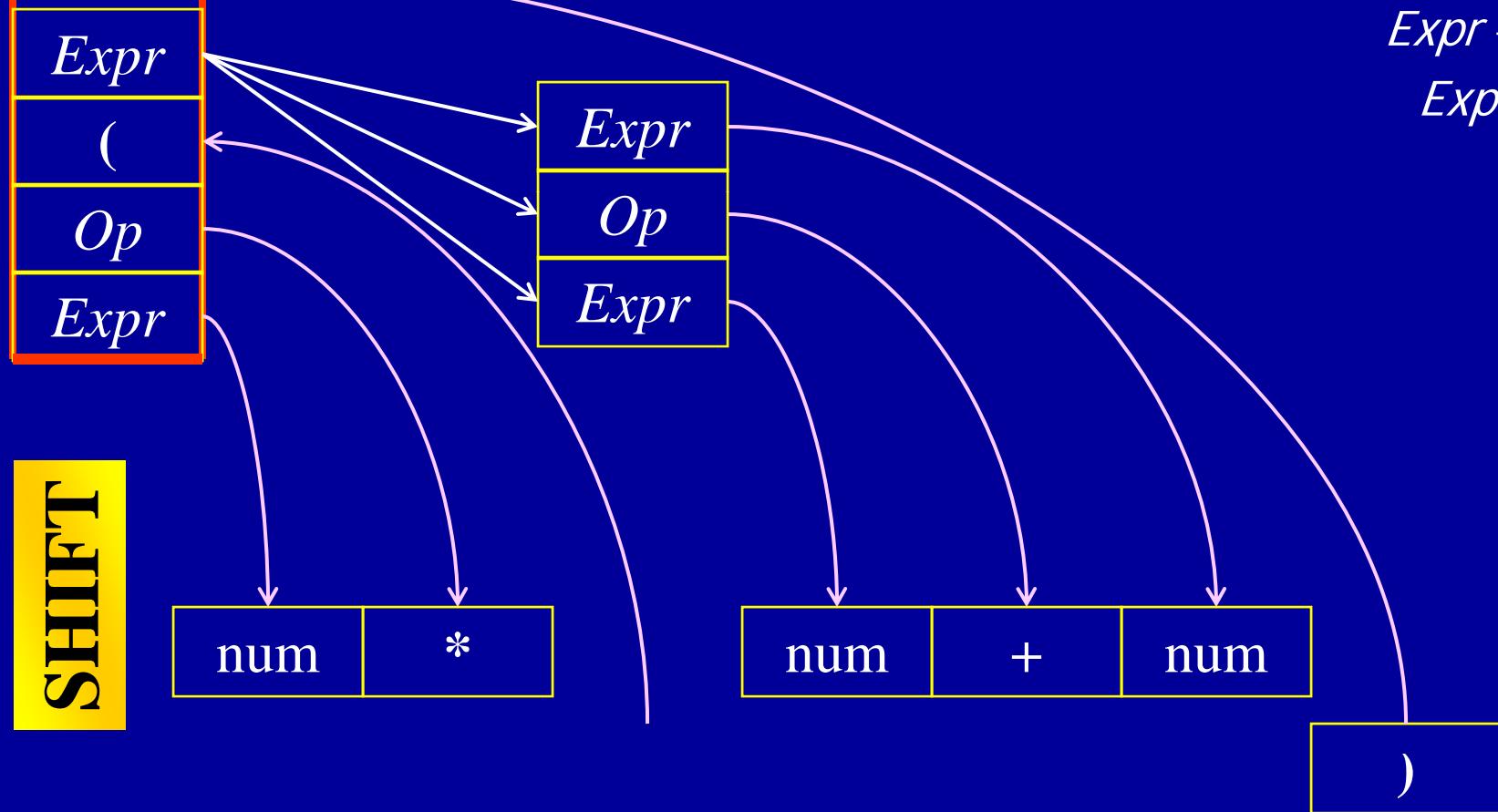
num | + | num

)



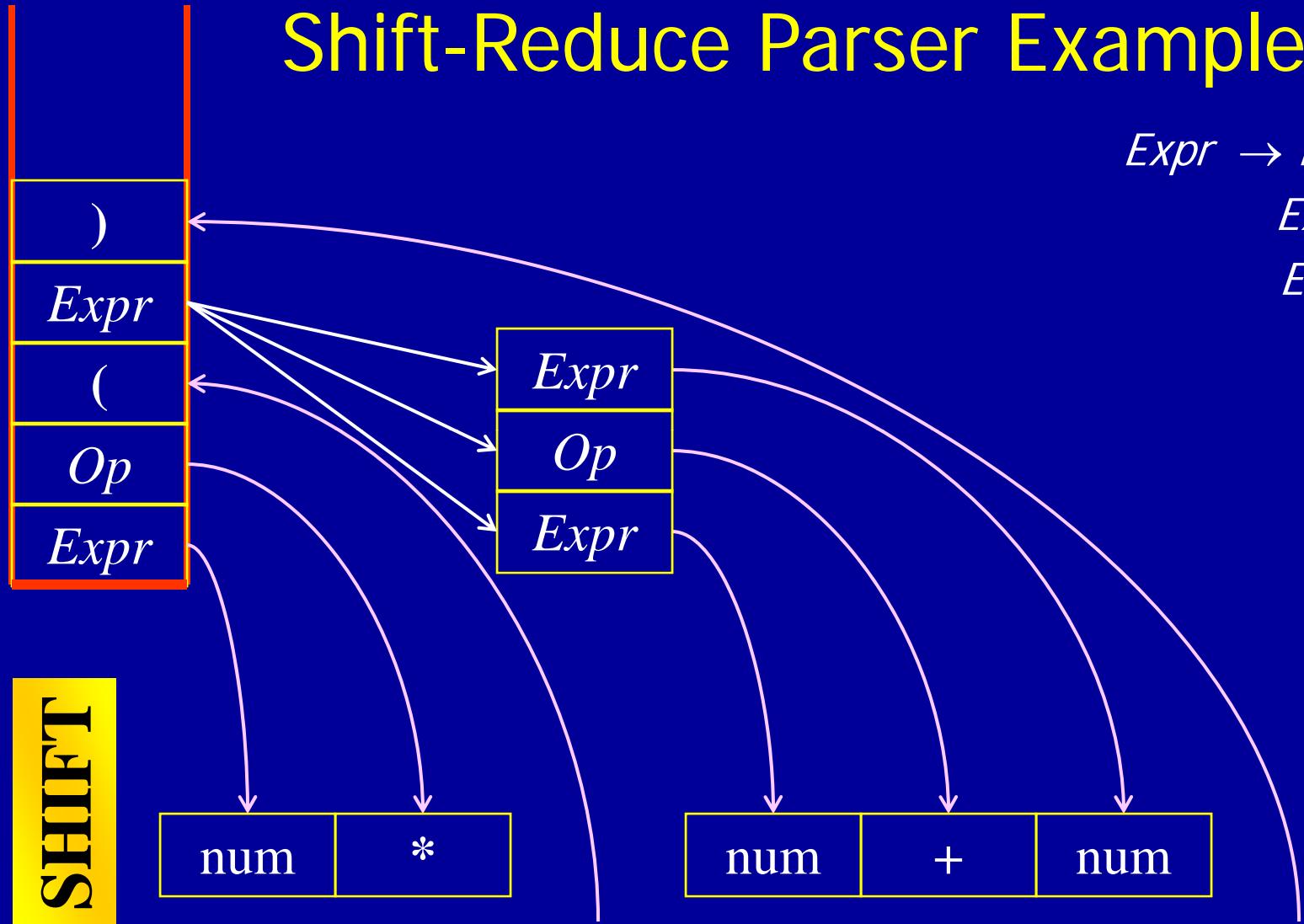
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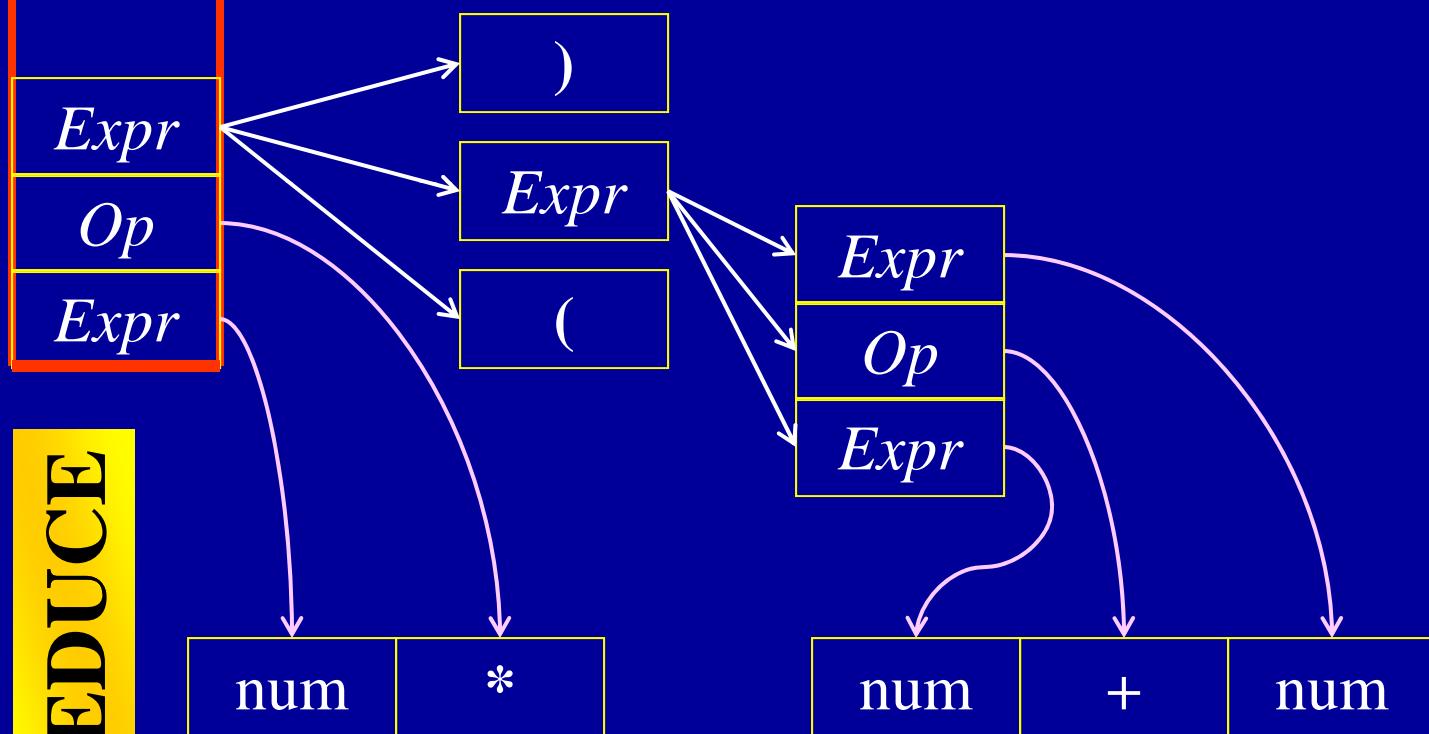
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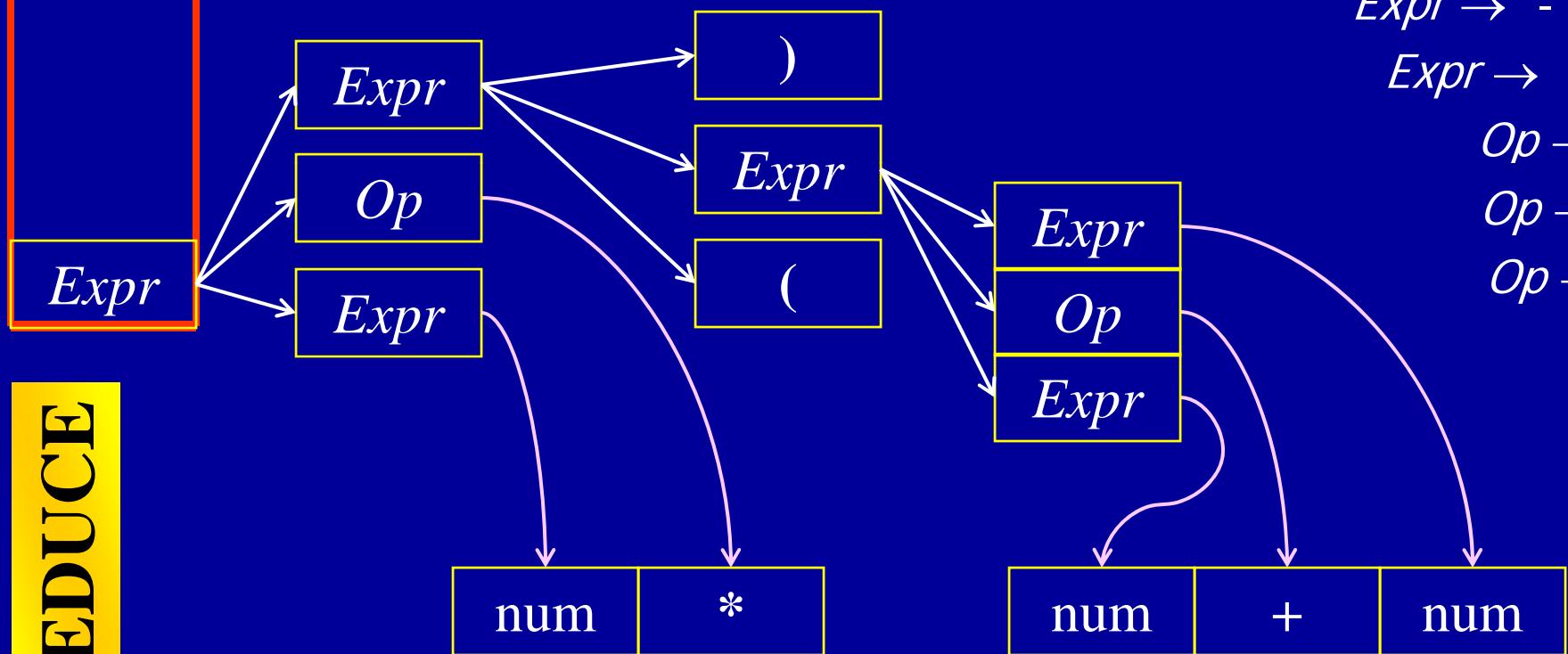
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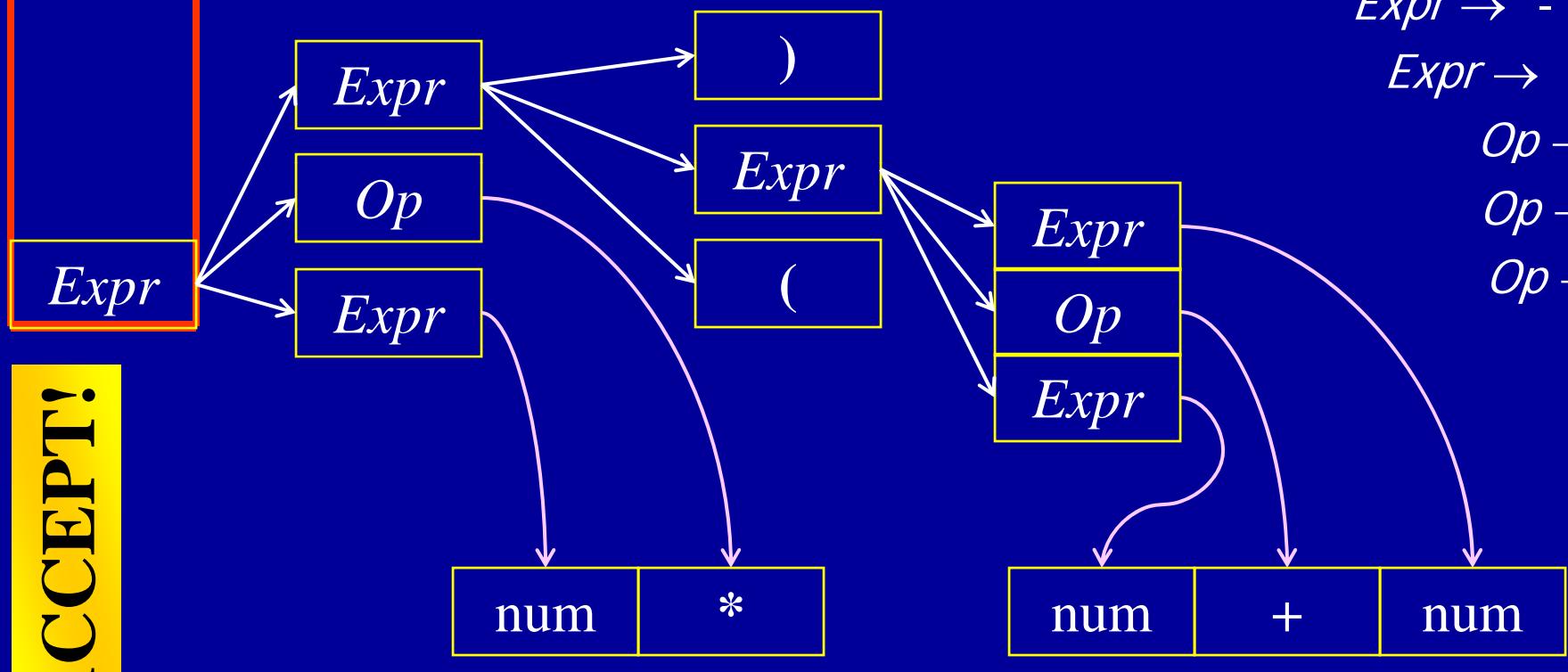
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Shift-Reduce Parser Example

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Basic Idea

- Goal: reconstruct parse tree for input string
- Read input from left to right
- Build tree in a bottom-up fashion

Use stack to hold pending sequences of terminals
and nonterminals

Potential Conflicts

- Reduce/Reduce Conflict
 - Top of the stack may match RHS of multiple productions
 - Which production to use in the reduction?
- Shift/Reduce Conflict
 - Stack may match RHS of production
 - But that may not be the right match
 - May need to shift an input and later find a different reduction

Conflicts

- Original Grammar

$$Expr \rightarrow Expr \text{ } Op \text{ } Expr$$
$$Expr \rightarrow (Expr)$$
$$Expr \rightarrow - \text{ } Expr$$
$$Expr \rightarrow \text{num}$$
$$Op \rightarrow +$$
$$Op \rightarrow -$$
$$Op \rightarrow *$$

- New Grammar

$$Expr \rightarrow Expr \text{ } Op \text{ } Expr$$
$$Expr \rightarrow Expr - Expr$$
$$Expr \rightarrow (Expr)$$
$$Expr \rightarrow Expr -$$
$$Expr \rightarrow \text{num}$$
$$Op \rightarrow +$$
$$Op \rightarrow -$$
$$Op \rightarrow *$$

Conflicts

$Expr \rightarrow Expr \text{ } Op \text{ } Expr$

$Expr \rightarrow Expr \text{ - } Expr$

$Expr \rightarrow (Expr)$

$Expr \rightarrow Expr \text{ - }$

$Expr \rightarrow num$

$Op \rightarrow +$

$Op \rightarrow -$

$Op \rightarrow *$

num	-	num
-----	---	-----

Conflicts

$Expr \rightarrow Expr \text{ } Op \text{ } Expr$
 $Expr \rightarrow Expr \text{ - } Expr$
 $Expr \rightarrow (Expr)$
 $Expr \rightarrow Expr \text{ - }$
 $Expr \rightarrow \text{num}$
 $Op \rightarrow +$
 $Op \rightarrow -$
 $Op \rightarrow *$

SHIFT

num	-	num
-----	---	-----



Conflicts

$Expr \rightarrow Expr \text{ } Op \text{ } Expr$

$Expr \rightarrow Expr - Expr$

$Expr \rightarrow (Expr)$

$Expr \rightarrow Expr -$

$Expr \rightarrow num$

$Op \rightarrow +$

$Op \rightarrow -$

$Op \rightarrow *$

num

SHIFT

- num

Conflicts

$Expr \rightarrow Expr \text{ } Op \text{ } Expr$
 $Expr \rightarrow Expr \text{ - } Expr$
 $Expr \rightarrow (Expr)$
 $Expr \rightarrow Expr \text{ - }$
 $Expr \rightarrow num$
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 $Op \rightarrow *$

REDUCE

$Expr$

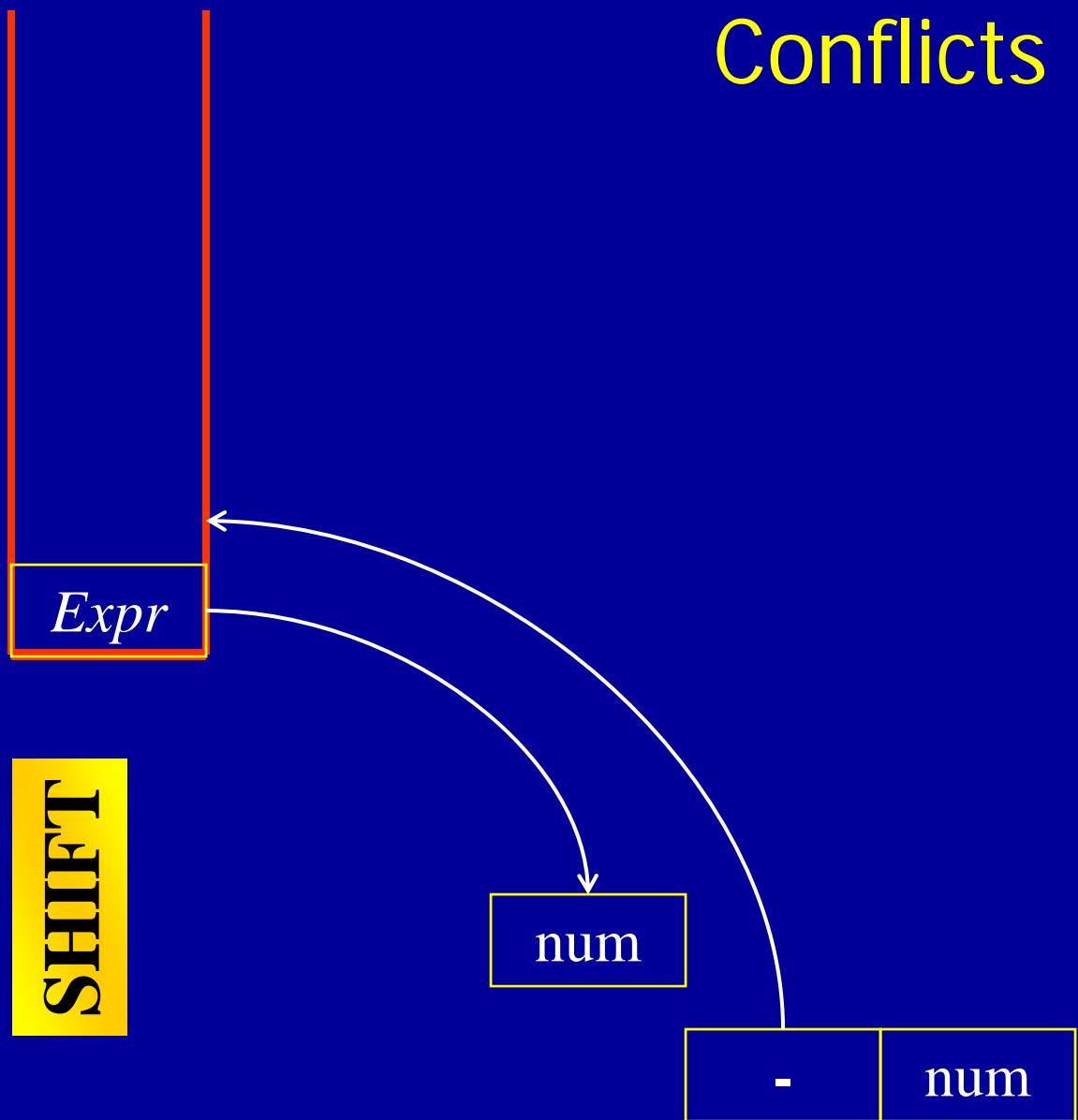
num

-

num

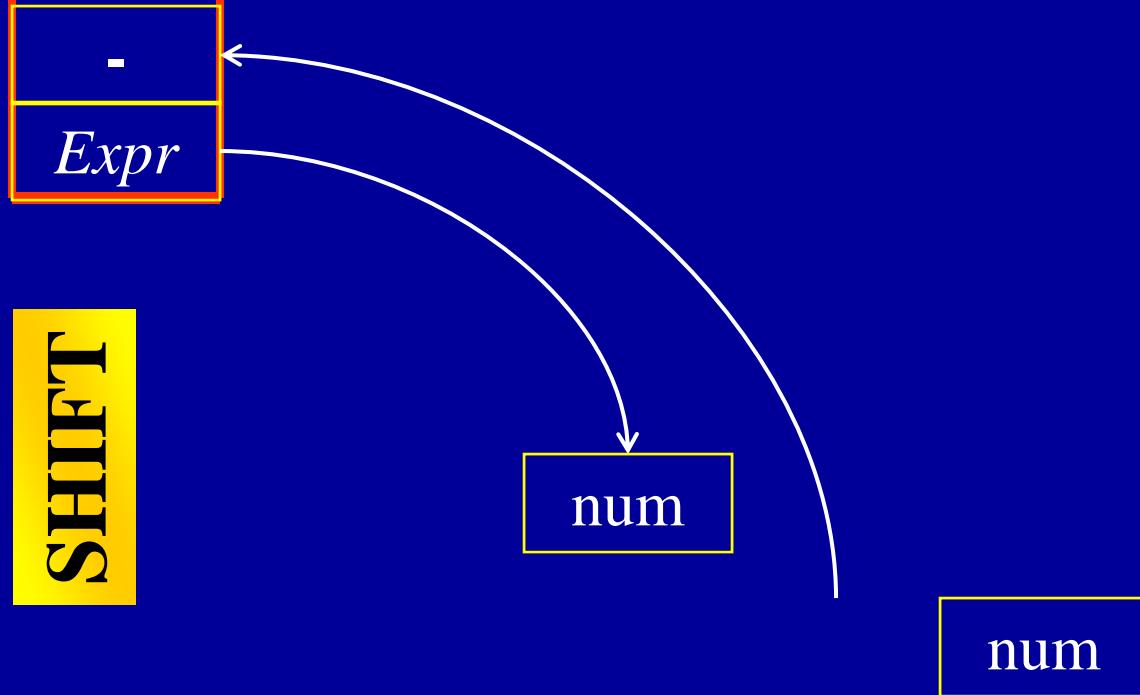
Conflicts

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Conflicts

$Expr \rightarrow Expr \text{ } Op \text{ } Expr$
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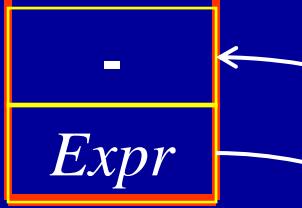
Shift/Reduce/Reduce Conflict

Options:

Reduce

Reduce

Shift



$Expr \rightarrow Expr \text{ } Op \text{ } Expr$
 $Expr \rightarrow Expr \text{ - } Expr$
 $Expr \rightarrow (Expr)$
 $Expr \rightarrow Expr \text{ - }$
 $Expr \rightarrow num$
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num

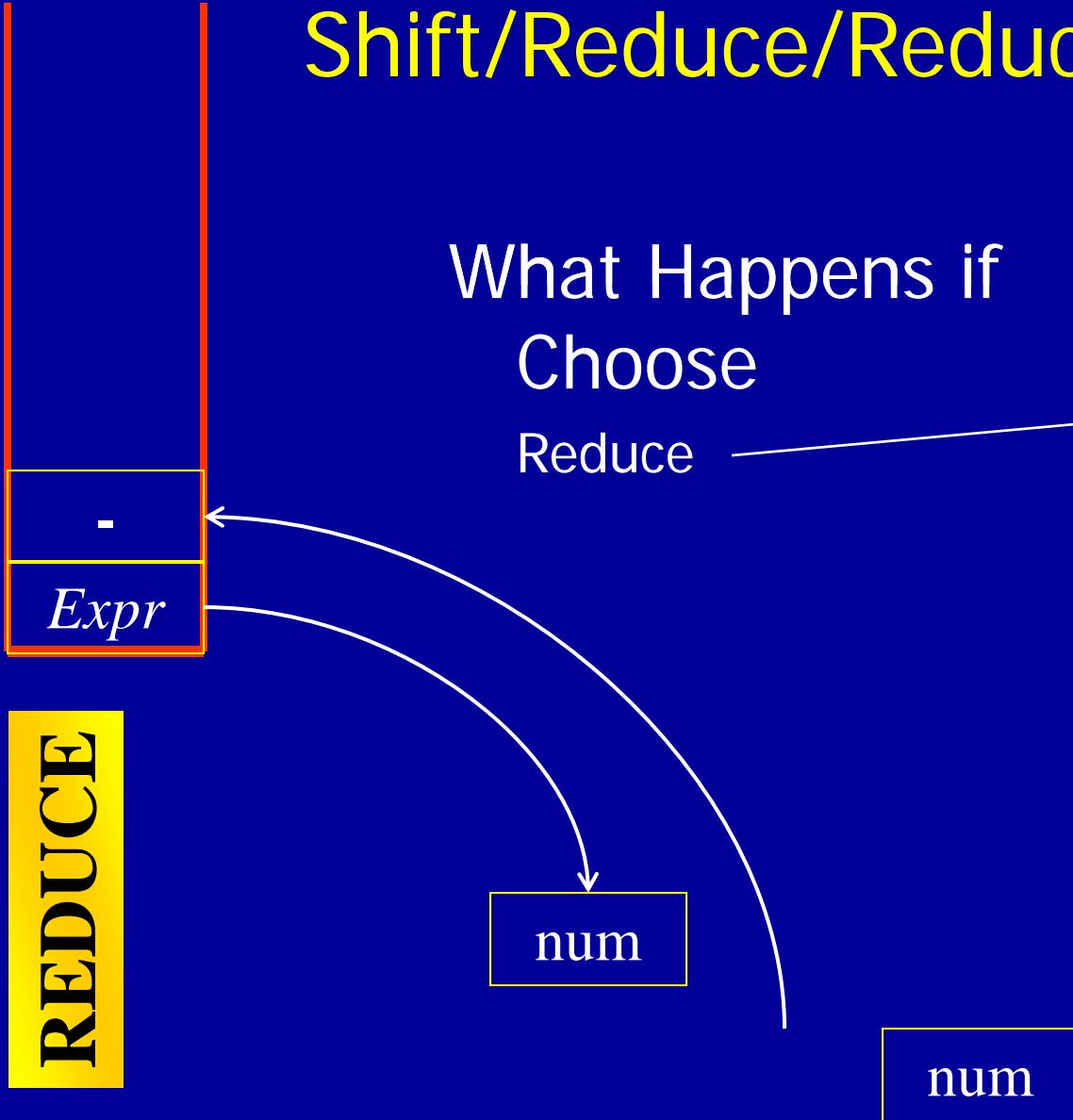
num

Shift/Reduce/Reduce Conflict

What Happens if
Choose
Reduce

$Expr \rightarrow Expr \ Op \ Expr$
 $Expr \rightarrow Expr - Expr$
 $Expr \rightarrow (Expr)$
 $Expr \rightarrow Expr -$
 $Expr \rightarrow num$
 $Op \rightarrow +$
 $Op \rightarrow -$
 $Op \rightarrow *$

REDUCE



Shift/Reduce/Reduce Conflict

What Happens if
Choose
Reduce

$$\begin{aligned} Expr &\rightarrow Expr \text{ } Op \text{ } Expr \\ Expr &\rightarrow Expr - Expr \\ Expr &\rightarrow (Expr) \\ Expr &\rightarrow Expr - \\ Expr &\rightarrow num \\ Op &\rightarrow + \\ Op &\rightarrow - \\ Op &\rightarrow * \end{aligned}$$

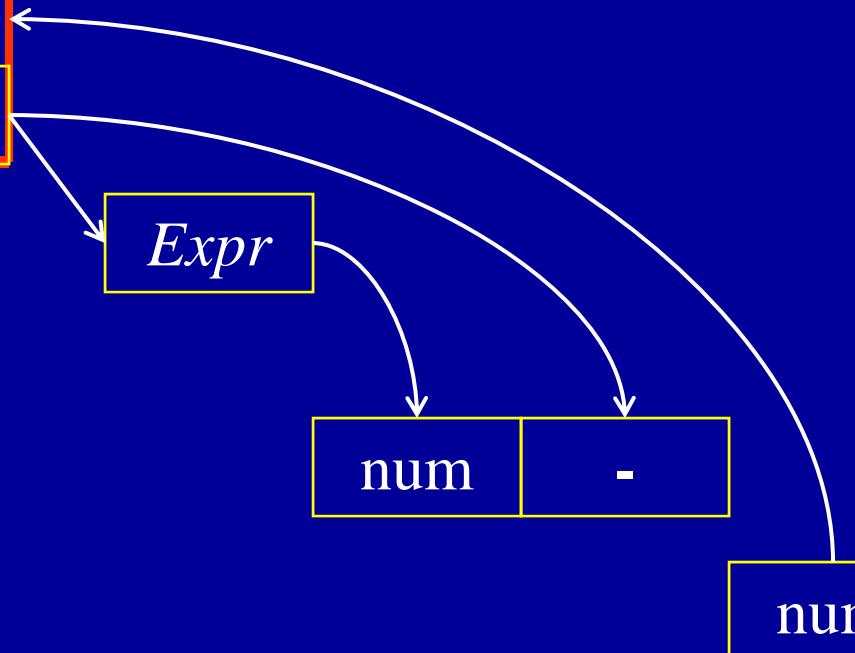
Expr

Expr

num | -

num

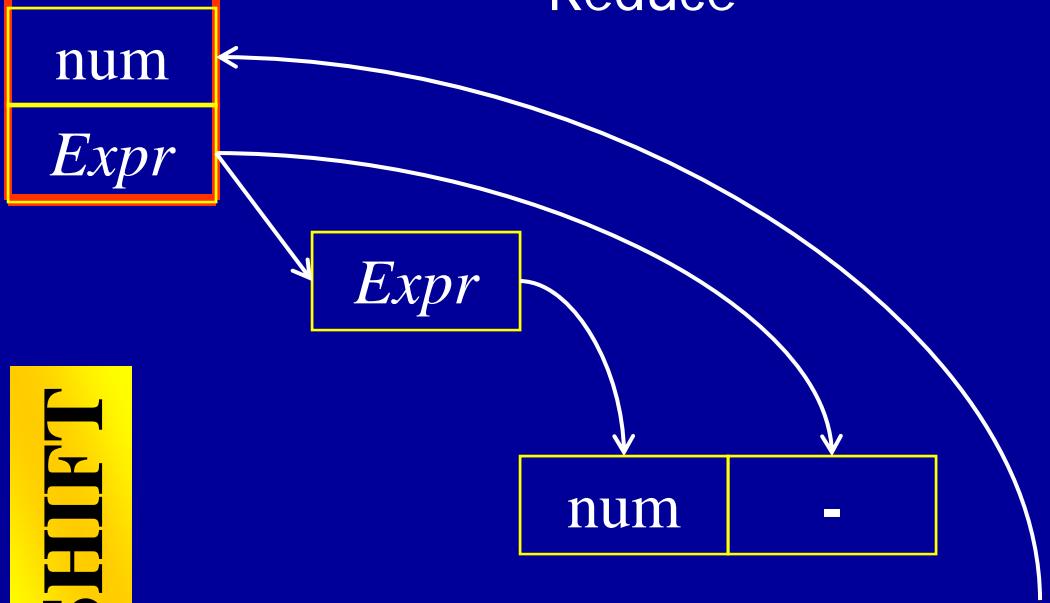
SHIFT



Shift/Reduce/Reduce Conflict

What Happens if
Choose
Reduce

$$\begin{aligned} Expr &\rightarrow Expr \text{ } Op \text{ } Expr \\ Expr &\rightarrow Expr \text{ } - \text{ } Expr \\ Expr &\rightarrow (Expr) \\ Expr &\rightarrow Expr \text{ } - \\ Expr &\rightarrow \text{num} \\ Op &\rightarrow + \\ Op &\rightarrow - \\ Op &\rightarrow * \end{aligned}$$



Shift/Reduce/Reduce Conflict

What Happens if
Choose
Reduce

$Expr \rightarrow Expr \ Op \ Expr$
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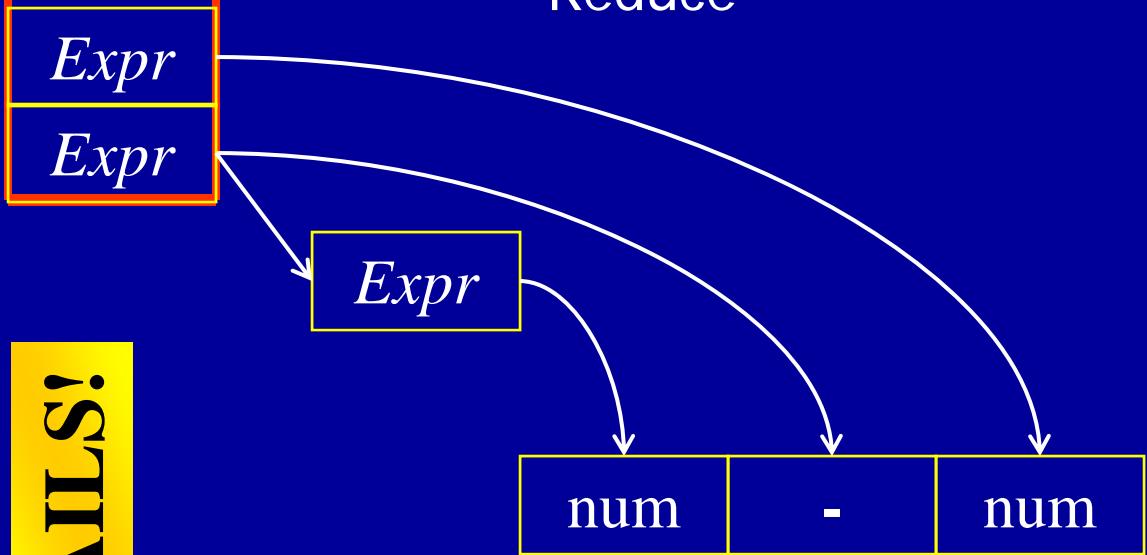
REDUCE



Shift/Reduce/Reduce Conflict

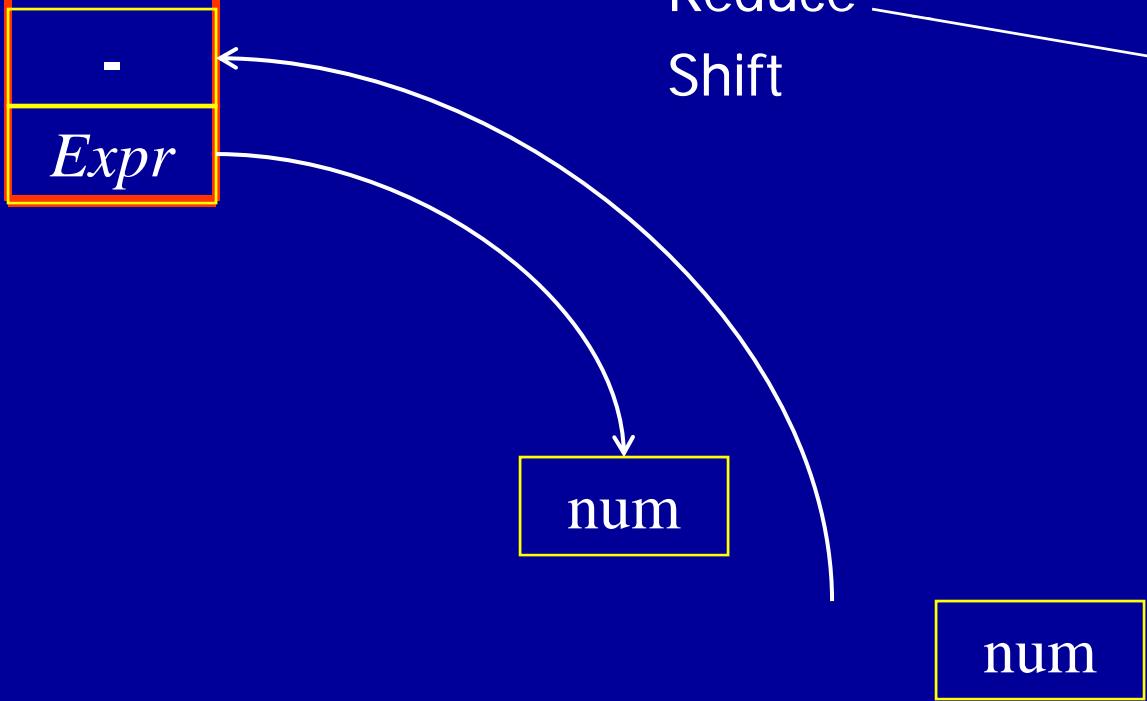
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Shift/Reduce/Reduce Conflict

Both of These
Actions Work

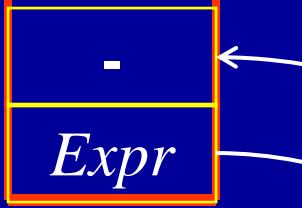


$Expr \rightarrow Expr \text{ } Op \text{ } Expr$
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 $Expr \rightarrow (Expr)$
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Shift/Reduce/Reduce Conflict

What Happens if
Choose

Reduce



num

num

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Shift/Reduce/Reduce Conflict

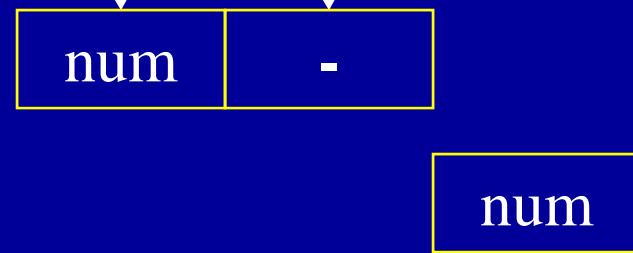
What Happens if
Choose

Reduce

Op
Expr

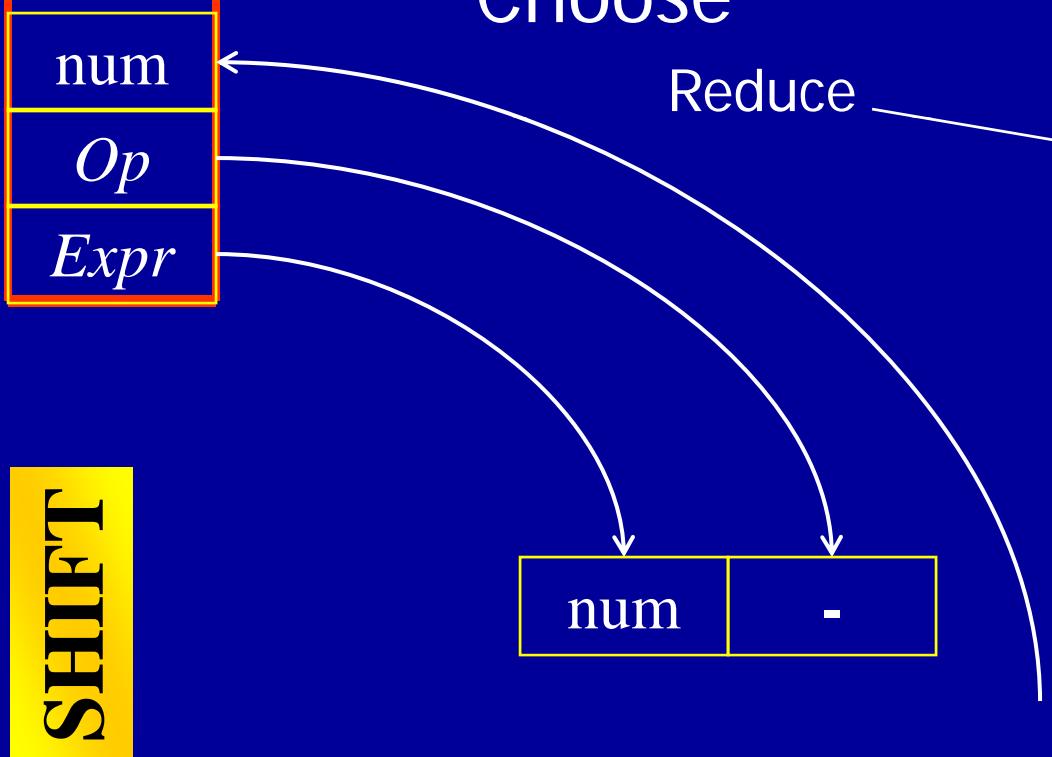
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REDUCE



Shift/Reduce/Reduce Conflict

What Happens if
Choose



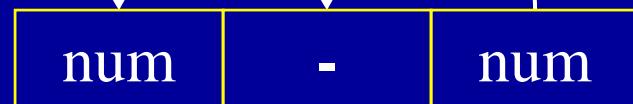
Shift/Reduce/Reduce Conflict

What Happens if
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Reduce



REDUCE

Shift/Reduce/Reduce Conflict

What Happens if
Choose

Expr

Expr
Op
Expr

Reduce

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REDUCE

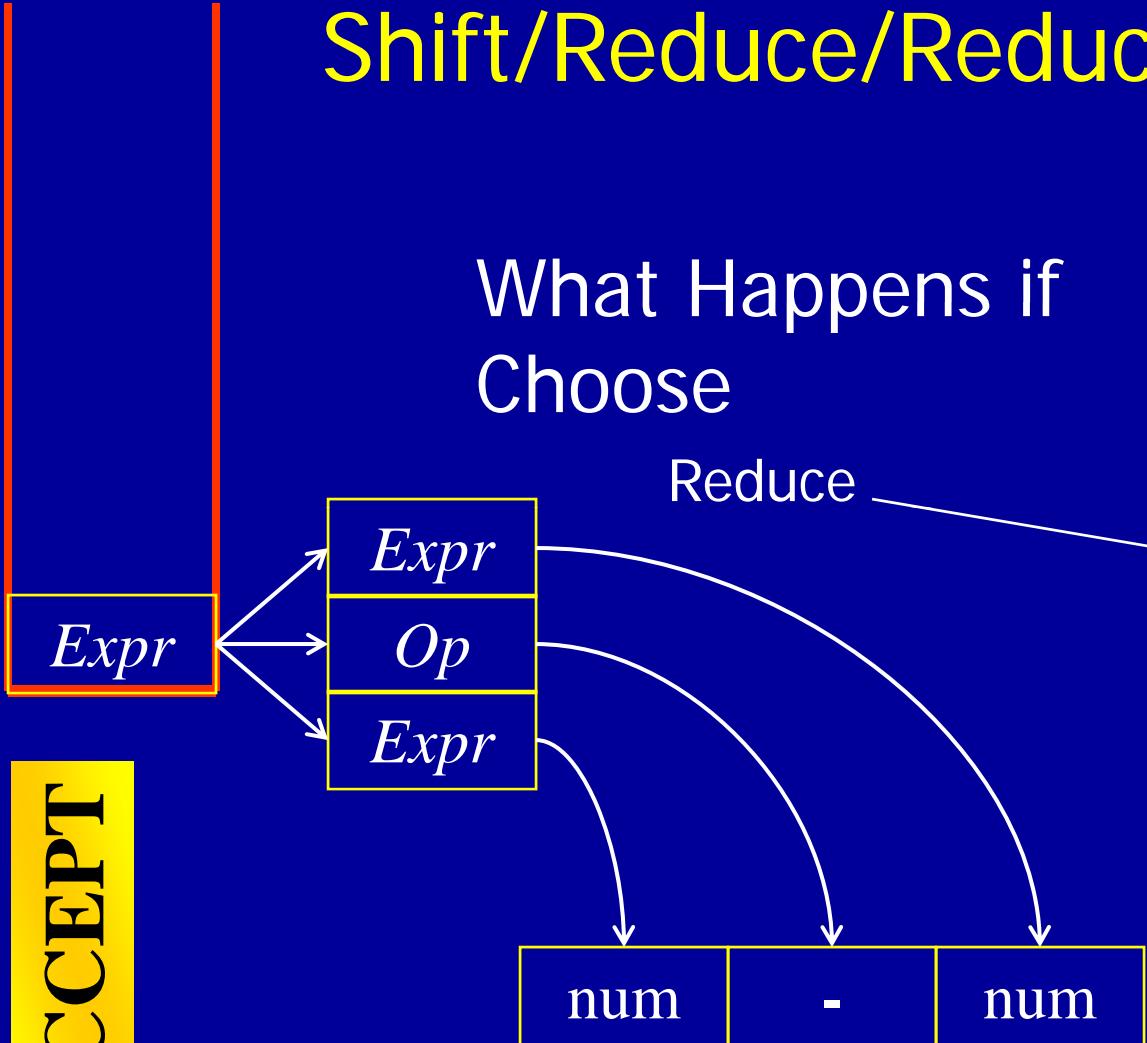
num | - | num

Shift/Reduce/Reduce Conflict

What Happens if
Choose

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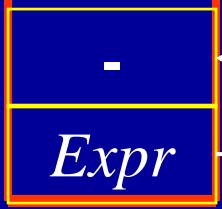
ACCEPT



Conflicts

What Happens if
Choose

Shift



SHIFT

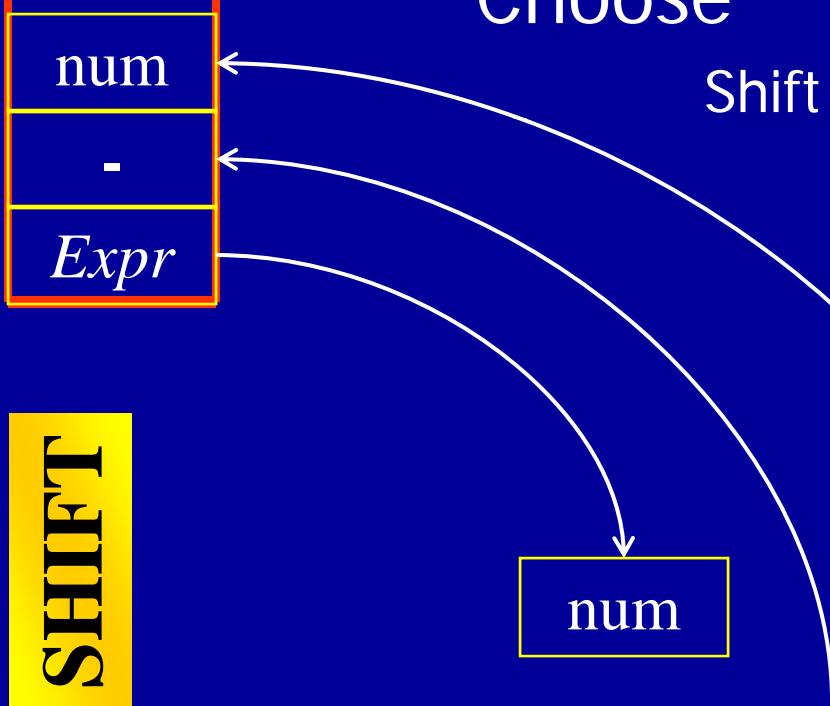
num

num

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Conflicts

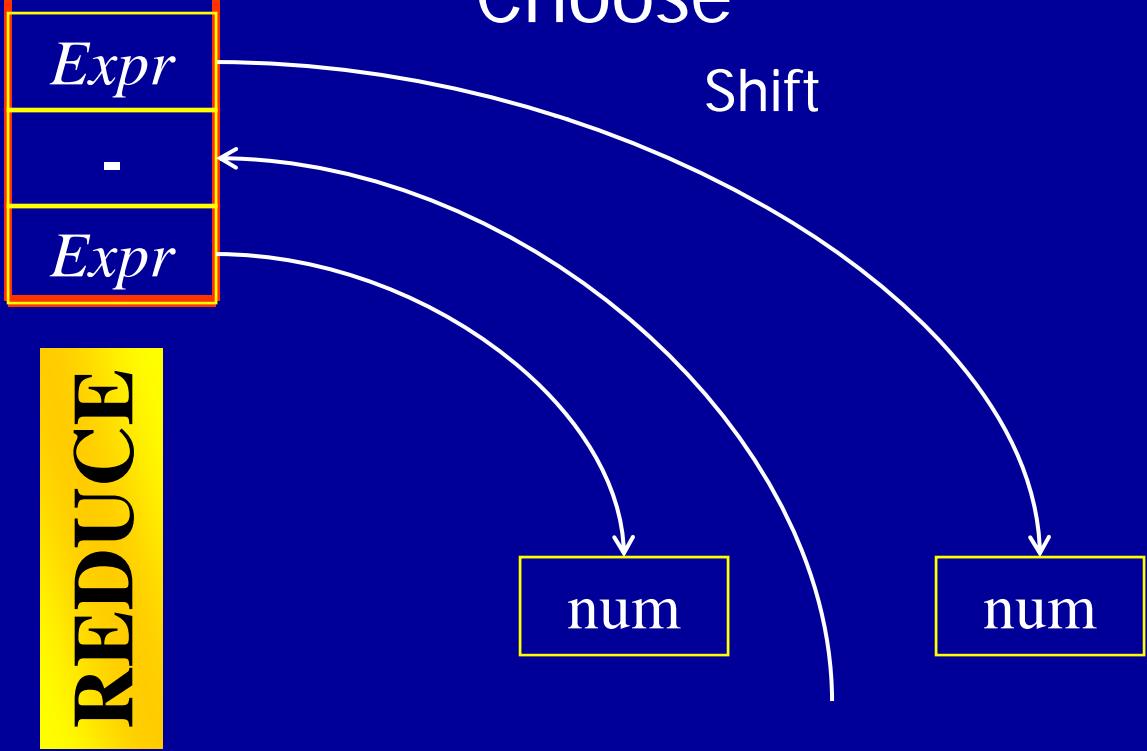
What Happens if
Choose



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 $Expr \rightarrow Expr \text{ - } Expr$
 $Expr \rightarrow (Expr)$
 $Expr \rightarrow Expr \text{ - }$
 $Expr \rightarrow num$
 $Op \rightarrow +$
 $Op \rightarrow -$
 $Op \rightarrow *$

Conflicts

What Happens if
Choose



$Expr \rightarrow Expr \text{ } Op \text{ } Expr$
 $Expr \rightarrow Expr \text{ - } Expr$
 $Expr \rightarrow (Expr)$
 $Expr \rightarrow Expr \text{ - }$
 $Expr \rightarrow \text{ num}$
 $Op \rightarrow +$
 $Op \rightarrow -$
 $Op \rightarrow *$

Conflicts

What Happens if
Choose

Shift

Expr

Expr

Expr

REDUCE

num | - | num

$Expr \rightarrow Expr \text{ } Op \text{ } Expr$
 $Expr \rightarrow Expr \text{ } - \text{ } Expr$
 $Expr \rightarrow (Expr)$
 $Expr \rightarrow Expr \text{ } -$
 $Expr \rightarrow \text{num}$
 $Op \rightarrow +$
 $Op \rightarrow -$
 $Op \rightarrow *$

Conflicts

What Happens if
Choose

Shift

Expr

Expr

Expr

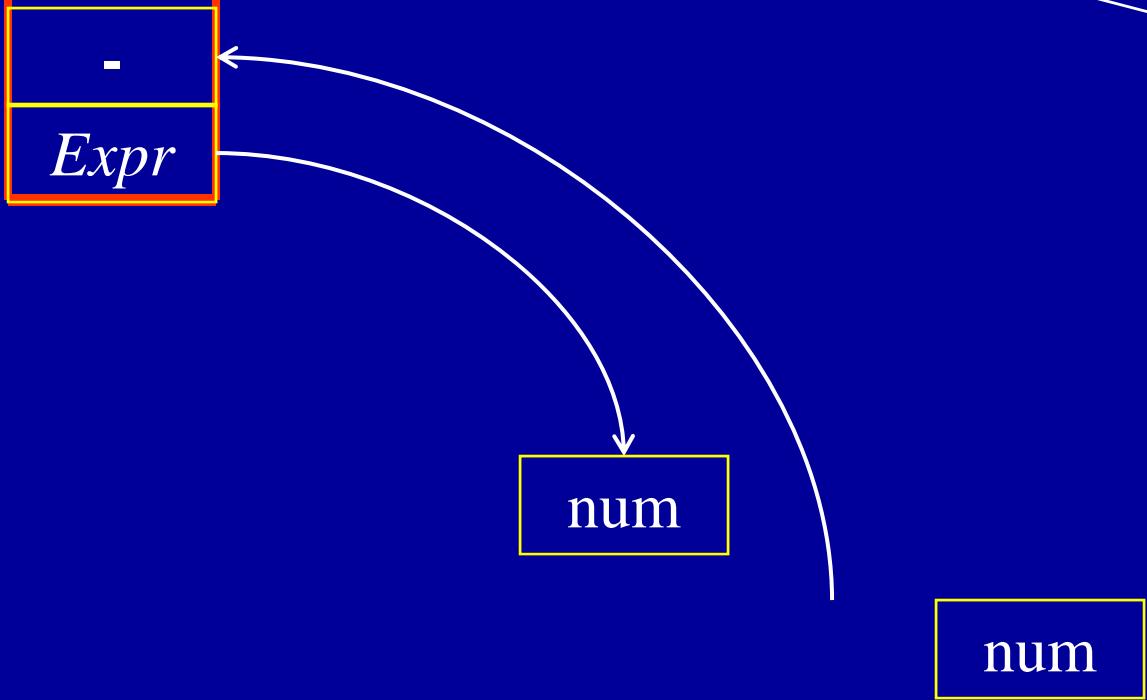
ACCEPT

num | - | num

$Expr \rightarrow Expr \text{ } Op \text{ } Expr$
 $Expr \rightarrow Expr \text{ } - \text{ } Expr$
 $Expr \rightarrow (Expr)$
 $Expr \rightarrow Expr \text{ } -$
 $Expr \rightarrow \text{num}$
 $Op \rightarrow +$
 $Op \rightarrow -$
 $Op \rightarrow *$

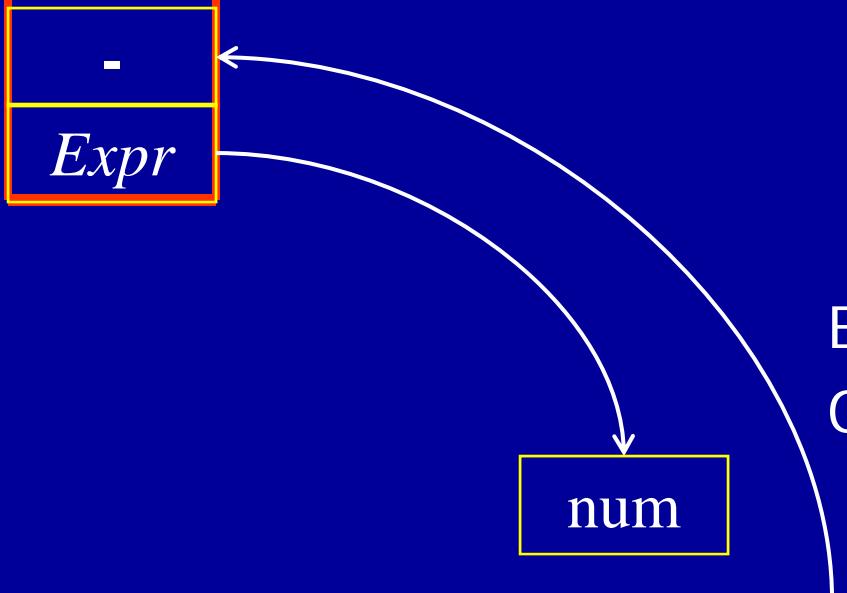
Shift/Reduce/Reduce Conflict

This Shift/Reduce Conflict
Reflects Ambiguity in
Grammar


$$\begin{aligned} Expr &\rightarrow Expr \text{ } Op \text{ } Expr \\ Expr &\rightarrow Expr \text{ } - \text{ } Expr \\ Expr &\rightarrow (Expr) \\ Expr &\rightarrow Expr \text{ } - \\ Expr &\rightarrow \text{num} \\ Op &\rightarrow + \\ Op &\rightarrow - \\ Op &\rightarrow * \end{aligned}$$

Shift/Reduce/Reduce Conflict

This Shift/Reduce Conflict
Reflects Ambiguity in
Grammar

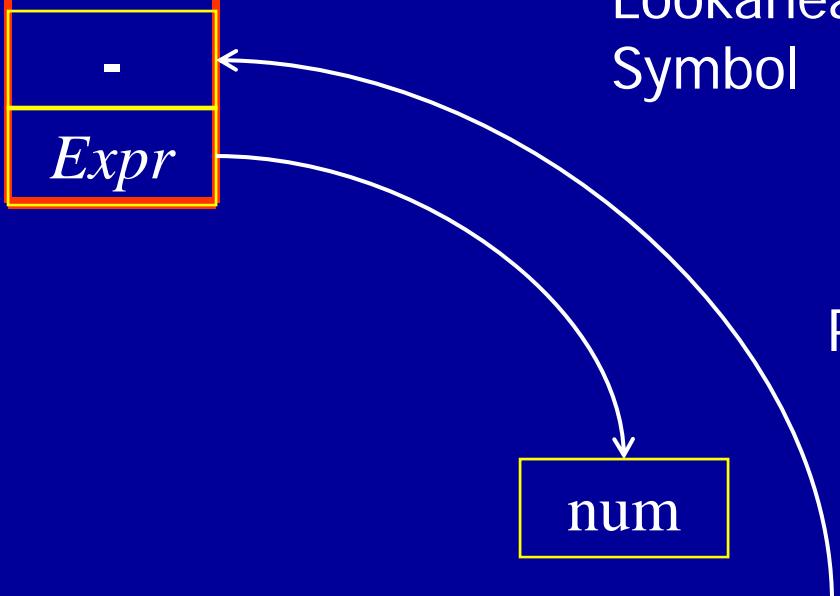


Eliminate by Hacking
Grammar

$Expr \rightarrow Expr \text{ } Op \text{ } Expr$
 ~~$Expr \Rightarrow Expr \text{ } Expr$~~
 $Expr \rightarrow (Expr)$
 $Expr \rightarrow Expr -$
 $Expr \rightarrow num$
 $Op \rightarrow +$
 $Op \rightarrow -$
 $Op \rightarrow *$

Shift/Reduce/Reduce Conflict

This Shift/Reduce
Conflict Can Be
Eliminated By
Lookahead of One
Symbol



$Expr \rightarrow Expr \text{ } Op \text{ } Expr$
 $Expr \rightarrow Expr \text{ - } Expr$
 $Expr \rightarrow (Expr)$
 $Expr \rightarrow Expr \text{ - }$
 $Expr \rightarrow num$
 $Op \rightarrow +$
 $Op \rightarrow -$
 $Op \rightarrow *$

Parser Generator Should
Handle It

num

Constructing a Parser

- We will construct version with no lookahead
- Key Decisions
 - Shift or Reduce
 - Which Production to Reduce
- Basic Idea
 - Build a DFA to control shift and reduce actions
 - In effect, convert grammar to pushdown automaton
 - Encode finite state control in parse table

Parser State

- Input Token Sequence (\$ for end of input)
- Current State from Finite State Automaton
- Two Stacks
 - State Stack (implements finite state automaton)
 - Symbol Stack (terminals from input and nonterminals from reductions)

Integrating Finite State Control

- Actions
 - Push Symbols and States Onto Stacks
 - Reduce According to a Given Production
 - Accept
- Selected action is a function of
 - Current input symbol
 - Current state of finite state control
- Each action specifies next state
- Implement control using parse table

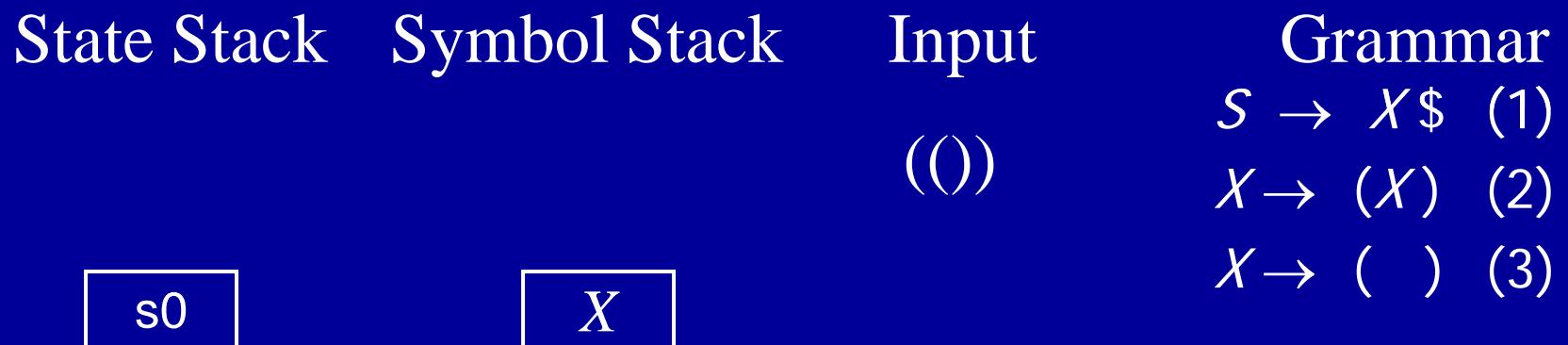
Parse Tables

State	ACTION			Goto
	()	\$	
s0	shift to s2	error	error	goto s1
s1	error	error	accept	
s2	shift to s2	shift to s5	error	goto s3
s3	error	shift to s4	error	
s4	reduce (2)	reduce (2)	reduce (2)	
s5	reduce (3)	reduce (3)	reduce (3)	

- Implements finite state control
- At each step, look up
 - Table[top of state stack] [input symbol]
- Then carry out the action

Parse Table Example

State	ACTION			Goto X
	()	\$	
s0	shift to s2	error	error	goto s1
s1	error	error	accept	
s2	shift to s2	shift to s5	error	goto s3
s3	error	shift to s4	error	
s4	reduce (2)	reduce (2)	reduce (2)	
s5	reduce (3)	reduce (3)	reduce (3)	



Parser Tables

State	()	\$	Goto
s0	shift to s2	error	error	goto s1
s1	error	error	accept	
s2	shift to s2	shift to s5	error	goto s3
s3	error	shift to s4	error	
s4	reduce (2)	reduce (2)	reduce (2)	
s5	reduce (3)	reduce (3)	reduce (3)	

- Shift to s_n
 - Push input token into the symbol stack
 - Push s_n into state stack
 - Advance to next input symbol

Parser Tables

State	()	\$	Goto X
s0	shift to s2	error	error	goto s1
s1	error	error	accept	
s2	shift to s2	shift to s5	error	goto s3
s3	error	shift to s4	error	
s4	reduce (2)	reduce (2)	reduce (2)	
s5	reduce (3)	reduce (3)	reduce (3)	

- Reduce (n)
 - Pop both stacks as many times as the number of symbols on the RHS of rule n
 - Push LHS of rule n into symbol stack

Parser Tables

State	()	\$	Goto
s0	shift to s2	error	error	goto s1
s1	error	error	accept	
s2	shift to s2	shift to s5	error	goto s3
s3	error	shift to s4	error	
s4	reduce (2)	reduce (2)	reduce (2)	
s5	reduce (3)	reduce (3)	reduce (3)	

- Reduce (n) (continued)
 - Look up
 - Table[top of the state stack][top of symbol stack]
 - Push that state (in goto part of table) onto state stack

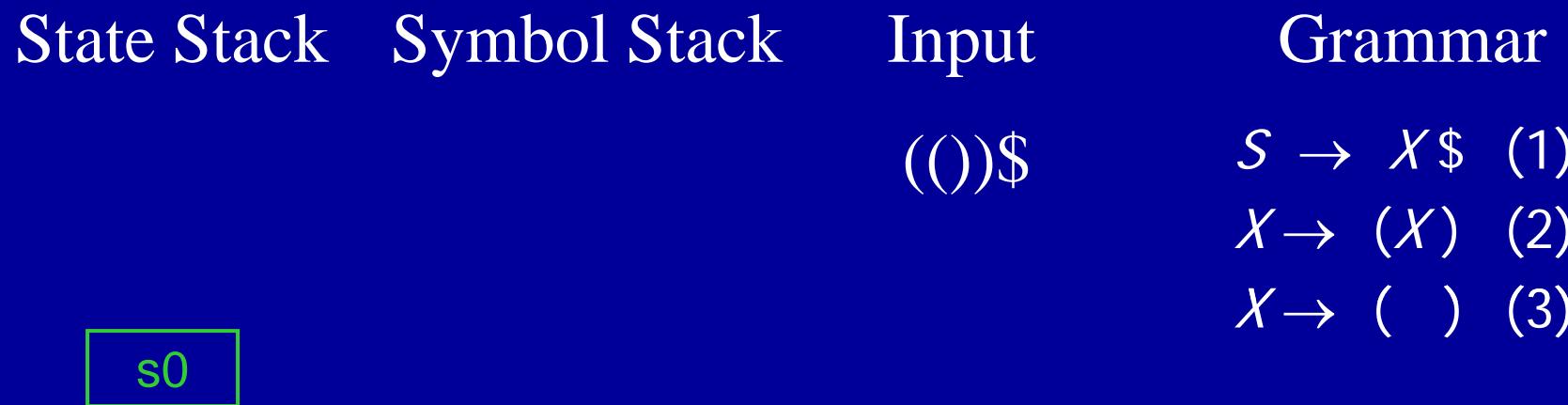
Parser Tables

State	()	\$	Goto X
s0	shift to s2	error	error	goto s1
s1	error	error	accept	
s2	shift to s2	shift to s5	error	goto s3
s3	error	shift to s4	error	
s4	reduce (2)	reduce (2)	reduce (2)	
s5	reduce (3)	reduce (3)	reduce (3)	

- Accept
 - Stop parsing and report success

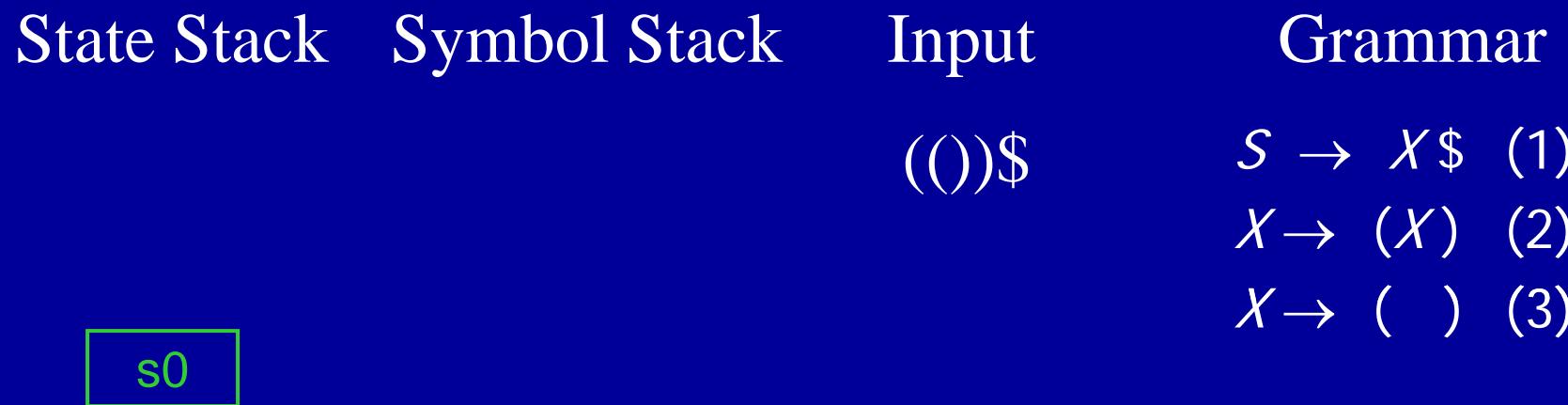
Parse Table In Action

State	ACTION			Goto X
	()	\$	
s0	shift to s2	error	error	goto s1
s1	error	error	accept	
s2	shift to s2	shift to s5	error	goto s3
s3	error	shift to s4	error	
s4	reduce (2)	reduce (2)	reduce (2)	
s5	reduce (3)	reduce (3)	reduce (3)	



Parse Table In Action

State	ACTION			Goto X
	()	\$	
s0	shift to s2	error	error	goto s1
s1	error	error	accept	
s2	shift to s2	shift to s5	error	goto s3
s3	error	shift to s4	error	
s4	reduce (2)	reduce (2)	reduce (2)	
s5	reduce (3)	reduce (3)	reduce (3)	



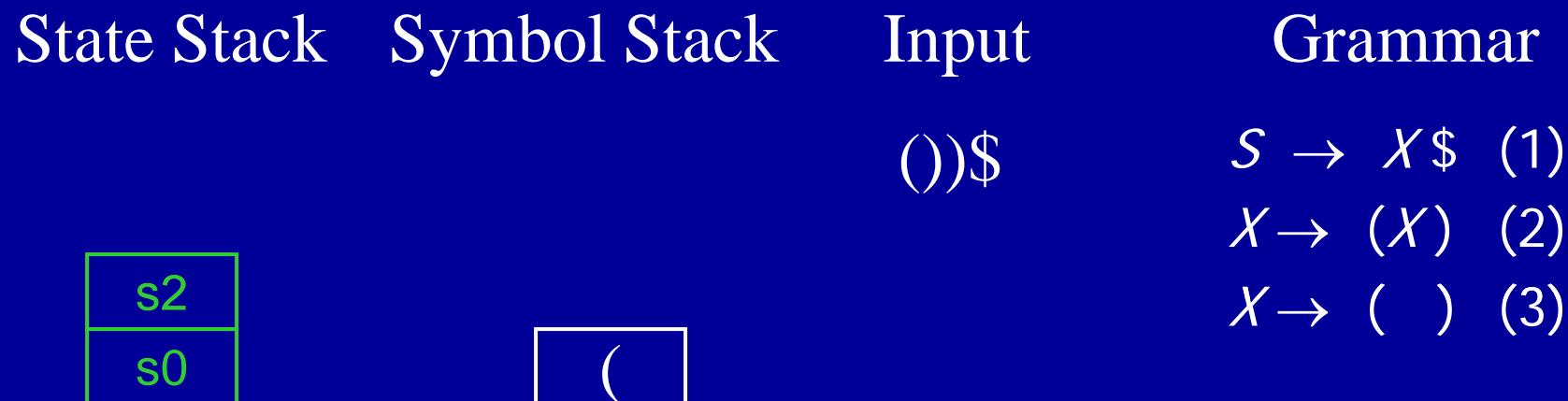
Parse Table In Action

State	ACTION			Goto X
	()	\$	
s0	shift to s2	error	error	goto s1
s1	error	error	accept	
s2	shift to s2	shift to s5	error	goto s3
s3	error	shift to s4	error	
s4	reduce (2)	reduce (2)	reduce (2)	
s5	reduce (3)	reduce (3)	reduce (3)	



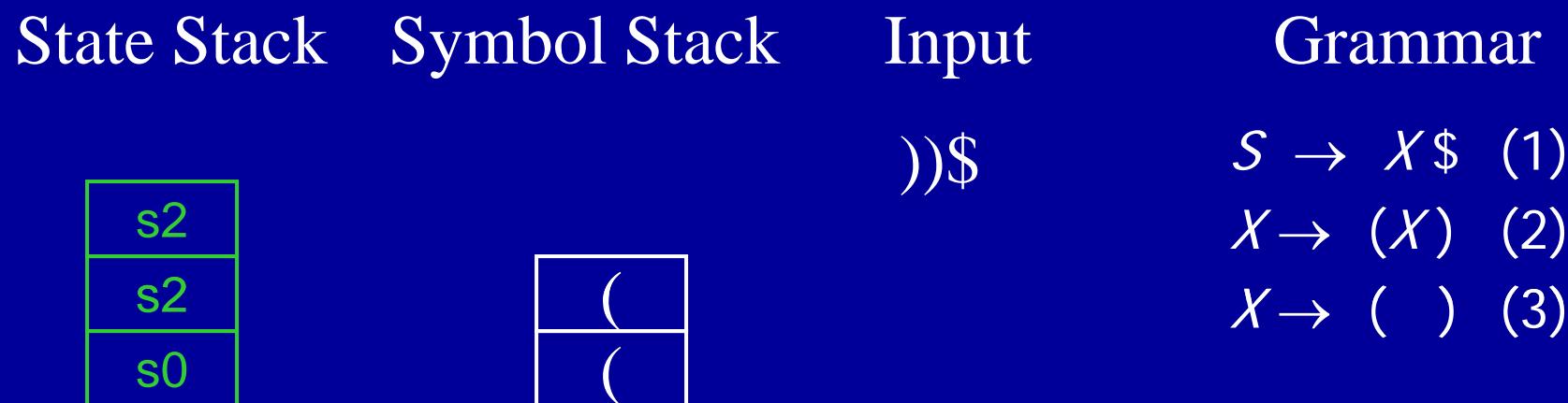
Parse Table In Action

State	ACTION			Goto X
	()	\$	
s0	shift to s2	error	error	goto s1
s1	error	error	accept	
s2	shift to s2	shift to s5	error	goto s3
s3	error	shift to s4	error	
s4	reduce (2)	reduce (2)	reduce (2)	
s5	reduce (3)	reduce (3)	reduce (3)	



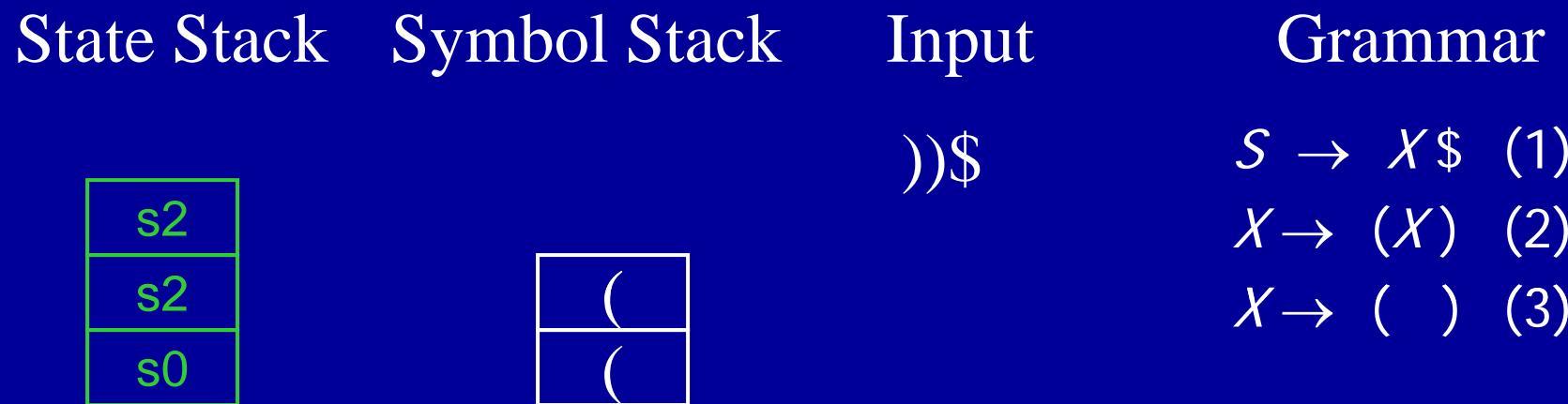
Parse Table In Action

State	()	\$	X
s0	shift to s2	error	error	goto s1
s1	error	error	accept	
s2	shift to s2	shift to s5	error	goto s3
s3	error	shift to s4	error	
s4	reduce (2)	reduce (2)	reduce (2)	
s5	reduce (3)	reduce (3)	reduce (3)	



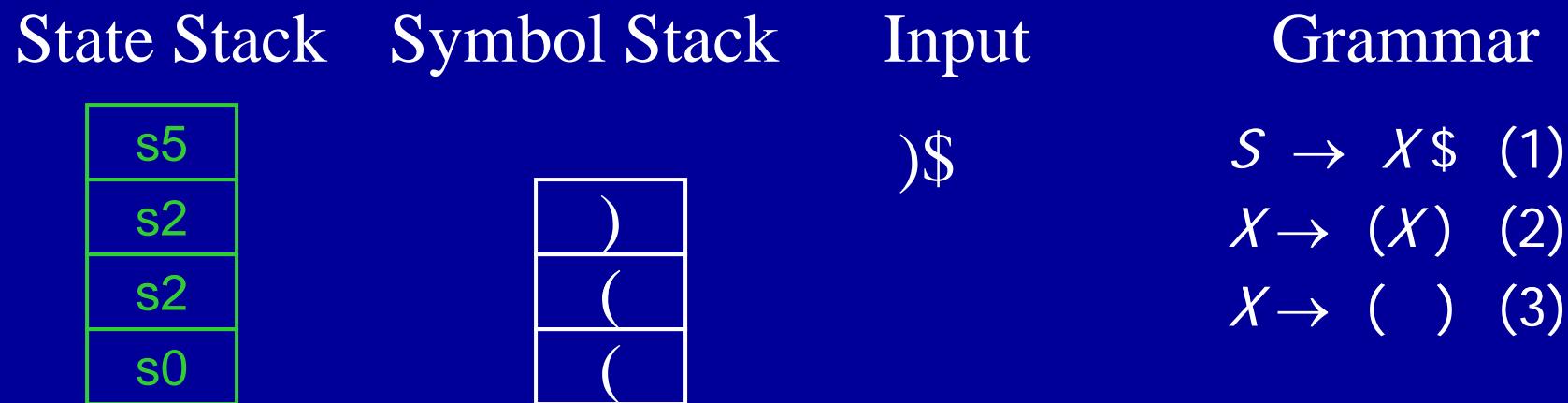
Parse Table In Action

State	ACTION			Goto X
	()	\$	
s0	shift to s2	error	error	goto s1
s1	error	error	accept	
s2	shift to s2	shift to s5	error	goto s3
s3	error	shift to s4	error	
s4	reduce (2)	reduce (2)	reduce (2)	
s5	reduce (3)	reduce (3)	reduce (3)	



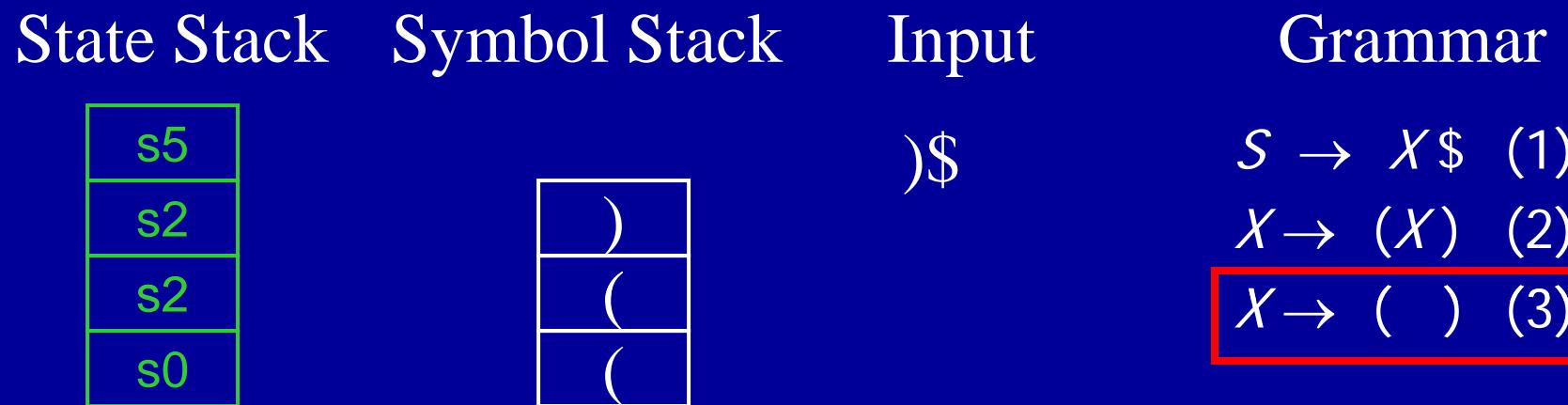
Parse Table In Action

State	ACTION			Goto X
	()	\$	
s0	shift to s2	error	error	goto s1
s1	error	error	accept	
s2	shift to s2	shift to s5	error	goto s3
s3	error	shift to s4	error	
s4	reduce (2)	reduce (2)	reduce (2)	
s5	reduce (3)	reduce (3)	reduce (3)	



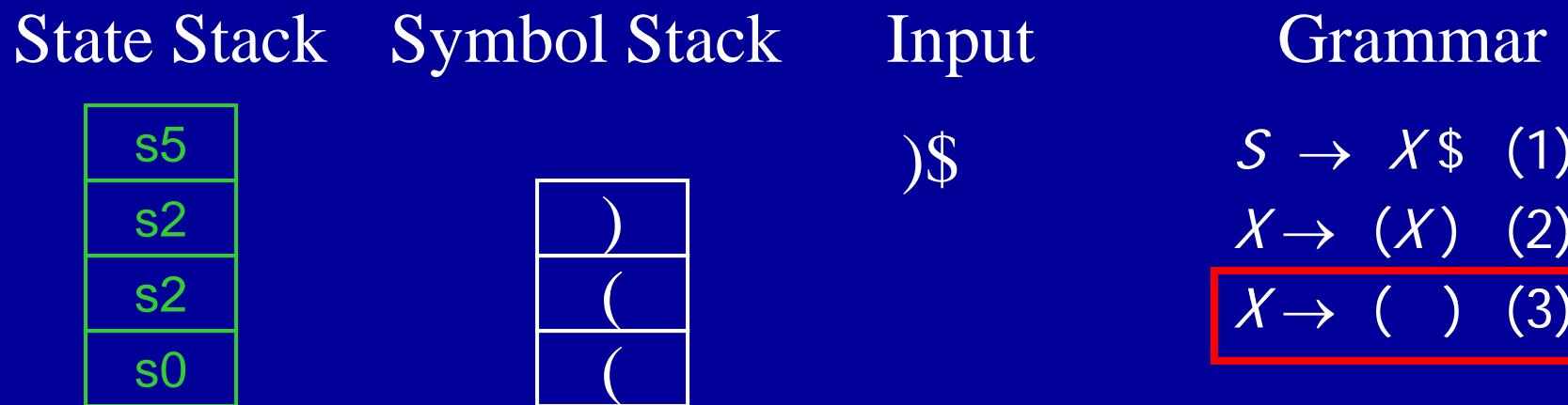
Parse Table In Action

State	ACTION			Goto X
	()	\$	
s0	shift to s2	error	error	goto s1
s1	error	error	accept	
s2	shift to s2	shift to s5	error	goto s3
s3	error	shift to s4	error	
s4	reduce (2)	reduce (2)	reduce (2)	
s5	reduce (3)	reduce (3)	reduce (3)	



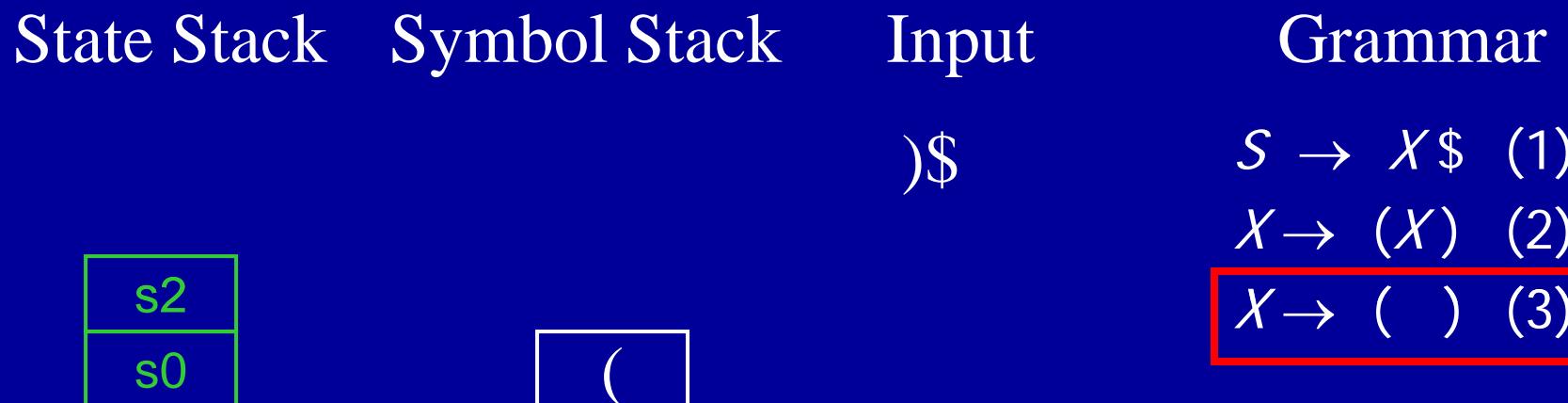
Step One: Pop Stacks

State	()	\$	X
s0	shift to s2	error	error	goto s1
s1	error	error	accept	
s2	shift to s2	shift to s5	error	goto s3
s3	error	shift to s4	error	
s4	reduce (2)	reduce (2)	reduce (2)	
s5	reduce (3)	reduce (3)	reduce (3)	



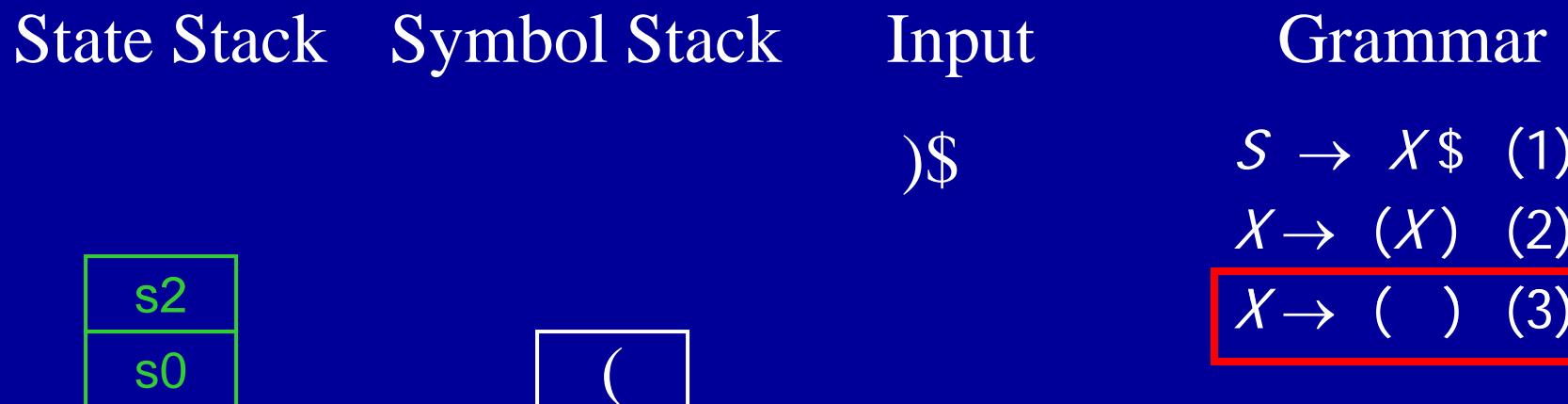
Step One: Pop Stacks

State	()	\$	Goto
s0	shift to s2	error	error	goto s1
s1	error	error	accept	
s2	shift to s2	shift to s5	error	goto s3
s3	error	shift to s4	error	
s4	reduce (2)	reduce (2)	reduce (2)	
s5	reduce (3)	reduce (3)	reduce (3)	



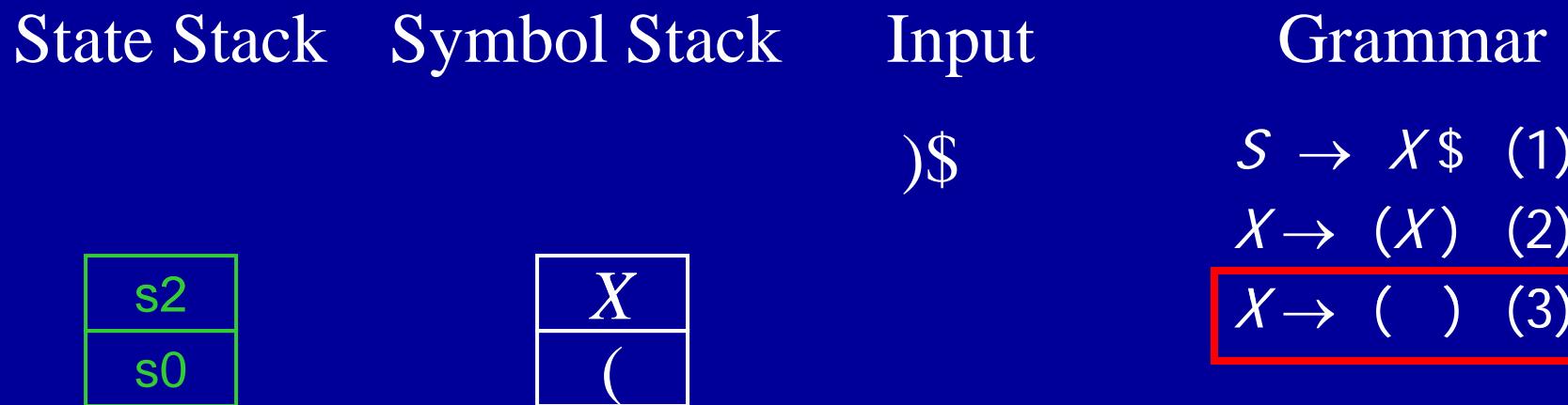
Step Two: Push Nonterminal

State	()	\$	Goto X
s0	shift to s2	error	error	goto s1
s1	error	error	accept	
s2	shift to s2	shift to s5	error	goto s3
s3	error	shift to s4	error	
s4	reduce (2)	reduce (2)	reduce (2)	
s5	reduce (3)	reduce (3)	reduce (3)	



Step Two: Push Nonterminal

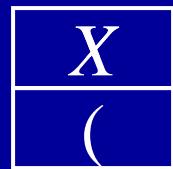
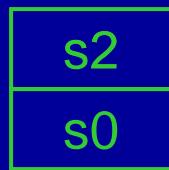
State	()	\$	Goto X
s0	shift to s2	error	error	goto s1
s1	error	error	accept	
s2	shift to s2	shift to s5	error	goto s3
s3	error	shift to s4	error	
s4	reduce (2)	reduce (2)	reduce (2)	
s5	reduce (3)	reduce (3)	reduce (3)	



Step Three: Use Goto, Push New State

State	()	\$	Goto
s0	shift to s2	error	error	goto s1
s1	error	error	accept	
s2	shift to s2	shift to s5	error	goto s3
s3	error	shift to s4	error	
s4	reduce (2)	reduce (2)	reduce (2)	
s5	reduce (3)	reduce (3)	reduce (3)	

State Stack Symbol Stack Input Grammar



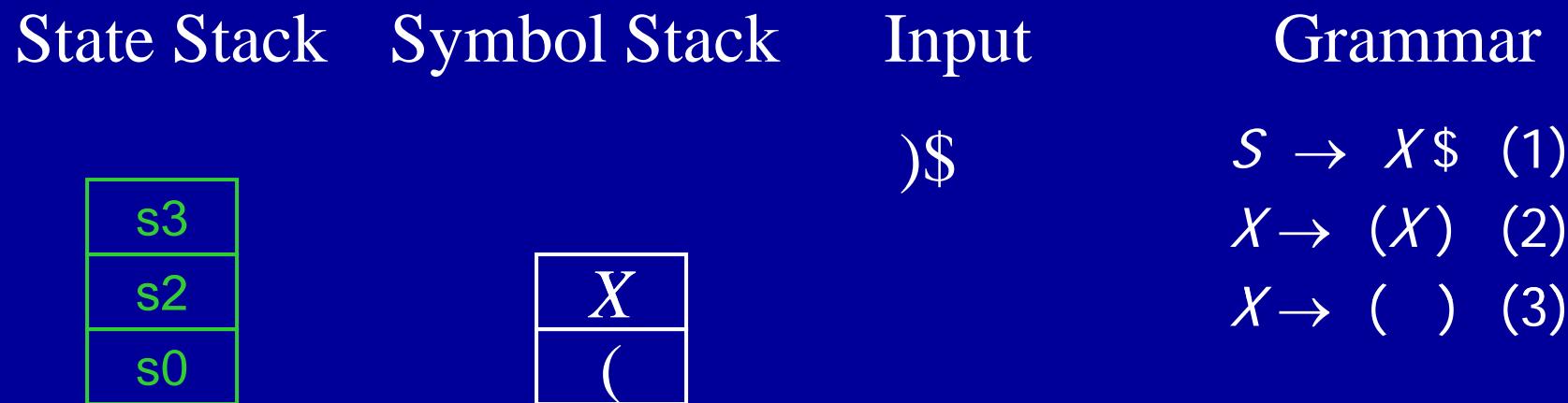
)\$ $S \rightarrow X\$ \quad (1)$

$X \rightarrow (X) \quad (2)$

$X \rightarrow () \quad (3)$

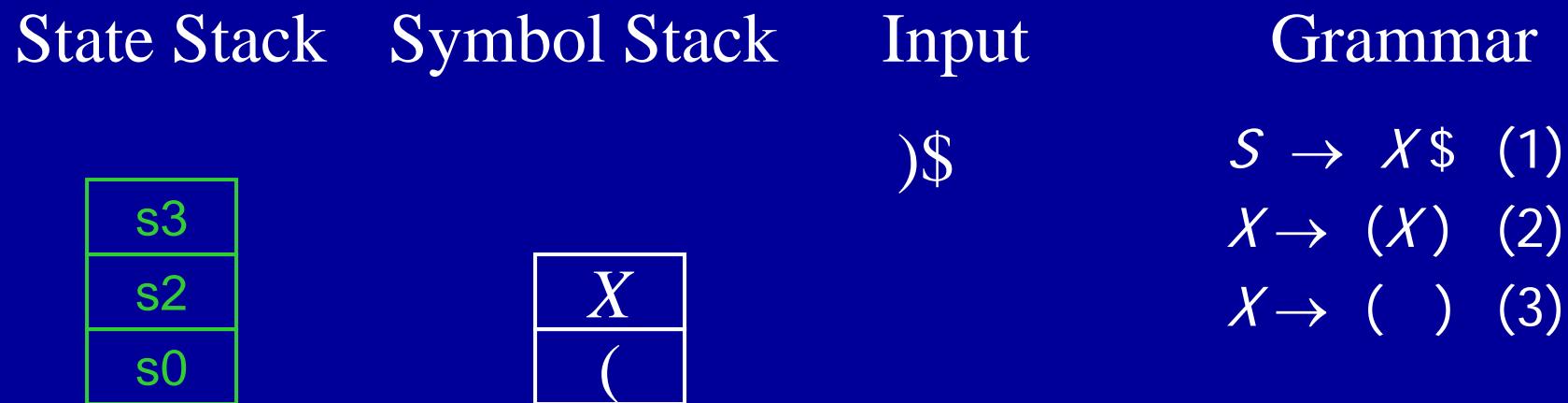
Step Three: Use Goto, Push New State

State	()	\$	Goto
s0	shift to s2	error	error	goto s1
s1	error	error	accept	
s2	shift to s2	shift to s5	error	goto s3
s3	error	shift to s4	error	
s4	reduce (2)	reduce (2)	reduce (2)	
s5	reduce (3)	reduce (3)	reduce (3)	



Parse Table In Action

State	ACTION			Goto X
	()	\$	
s0	shift to s2	error	error	goto s1
s1	error	error	accept	
s2	shift to s2	shift to s5	error	goto s3
s3	error	shift to s4	error	
s4	reduce (2)	reduce (2)	reduce (2)	
s5	reduce (3)	reduce (3)	reduce (3)	



Parse Table In Action

State	ACTION			Goto X
	()	\$	
s0	shift to s2	error	error	goto s1
s1	error	error	accept	
s2	shift to s2	shift to s5	error	goto s3
s3	error	shift to s4	error	
s4	reduce (2)	reduce (2)	reduce (2)	
s5	reduce (3)	reduce (3)	reduce (3)	

State Stack Symbol Stack Input Grammar

s4
s3
s2
s0

)
X
(

\$

$S \rightarrow X\$$ (1)

$X \rightarrow (X)$ (2)

$X \rightarrow ()$ (3)

Parse Table In Action

State	ACTION			Goto
	()	\$	
s0	shift to s2	error	error	goto s1
s1	error	error	accept	
s2	shift to s2	shift to s5	error	goto s3
s3	error	shift to s4	error	
s4	reduce (2)	reduce (2)	reduce (2)	
s5	reduce (3)	reduce (3)	reduce (3)	

State Stack Symbol Stack Input Grammar

s4
s3
s2
s0

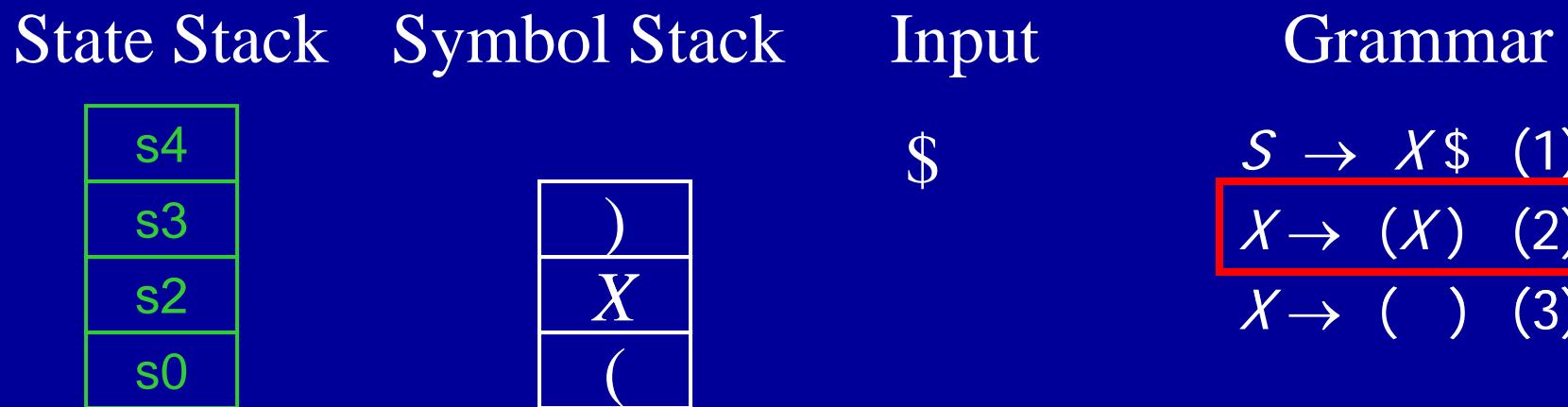
)
X
(

\$

$$\begin{aligned}
 S &\rightarrow X\$ \quad (1) \\
 X &\rightarrow (X) \quad (2) \\
 X &\rightarrow () \quad (3)
 \end{aligned}$$

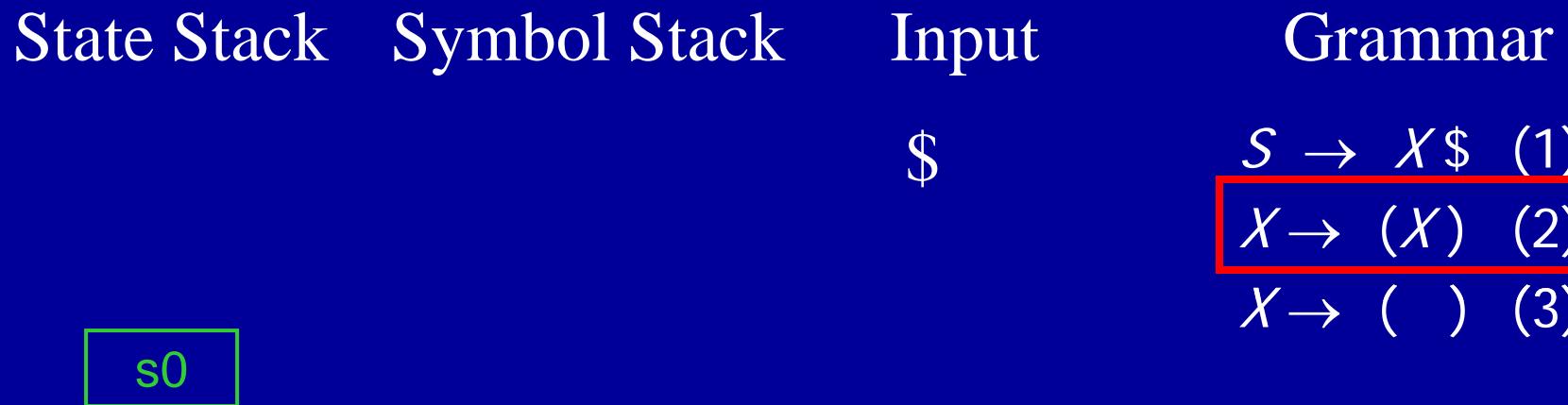
Step One: Pop Stacks

State	()	\$	Goto
s0	shift to s2	error	error	goto s1
s1	error	error	accept	
s2	shift to s2	shift to s5	error	goto s3
s3	error	shift to s4	error	
s4	reduce (2)	reduce (2)	reduce (2)	
s5	reduce (3)	reduce (3)	reduce (3)	



Step One: Pop Stacks

State	()	\$	Goto
s0	shift to s2	error	error	goto s1
s1	error	error	accept	
s2	shift to s2	shift to s5	error	goto s3
s3	error	shift to s4	error	
s4	reduce (2)	reduce (2)	reduce (2)	
s5	reduce (3)	reduce (3)	reduce (3)	



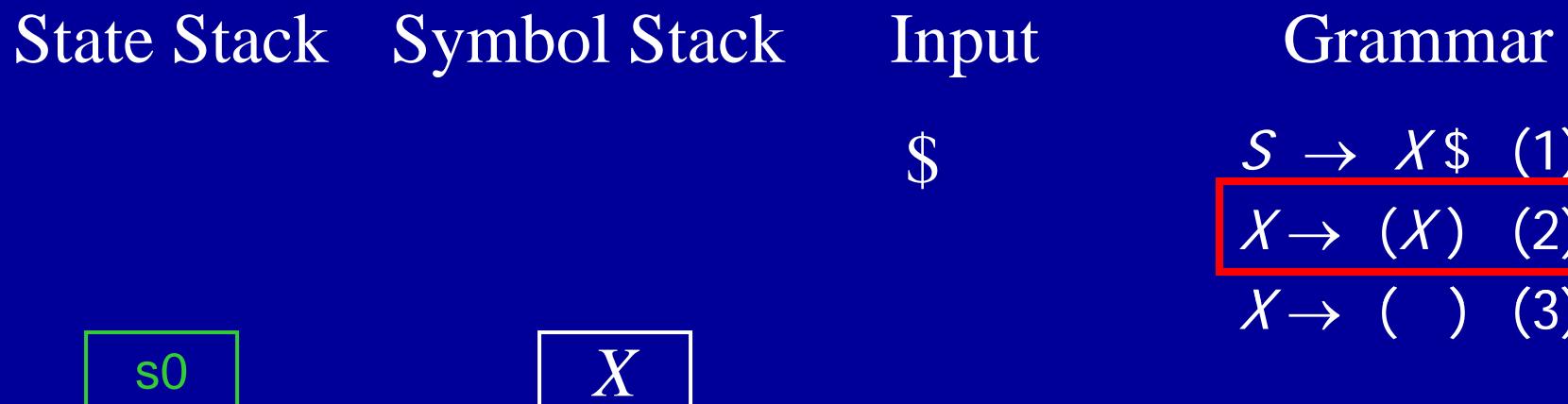
Step Two: Push Nonterminal

State	()	\$	Goto X
s0	shift to s2	error	error	goto s1
s1	error	error	accept	
s2	shift to s2	shift to s5	error	goto s3
s3	error	shift to s4	error	
s4	reduce (2)	reduce (2)	reduce (2)	
s5	reduce (3)	reduce (3)	reduce (3)	



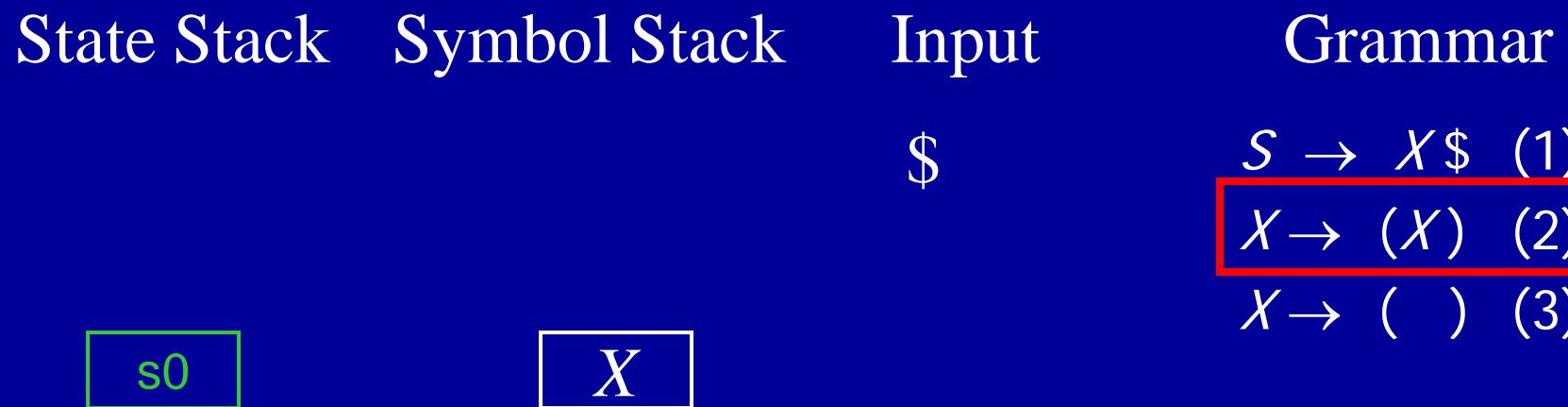
Step Two: Push Nonterminal

State	()	\$	Goto X
s0	shift to s2	error	error	goto s1
s1	error	error	accept	
s2	shift to s2	shift to s5	error	goto s3
s3	error	shift to s4	error	
s4	reduce (2)	reduce (2)	reduce (2)	
s5	reduce (3)	reduce (3)	reduce (3)	



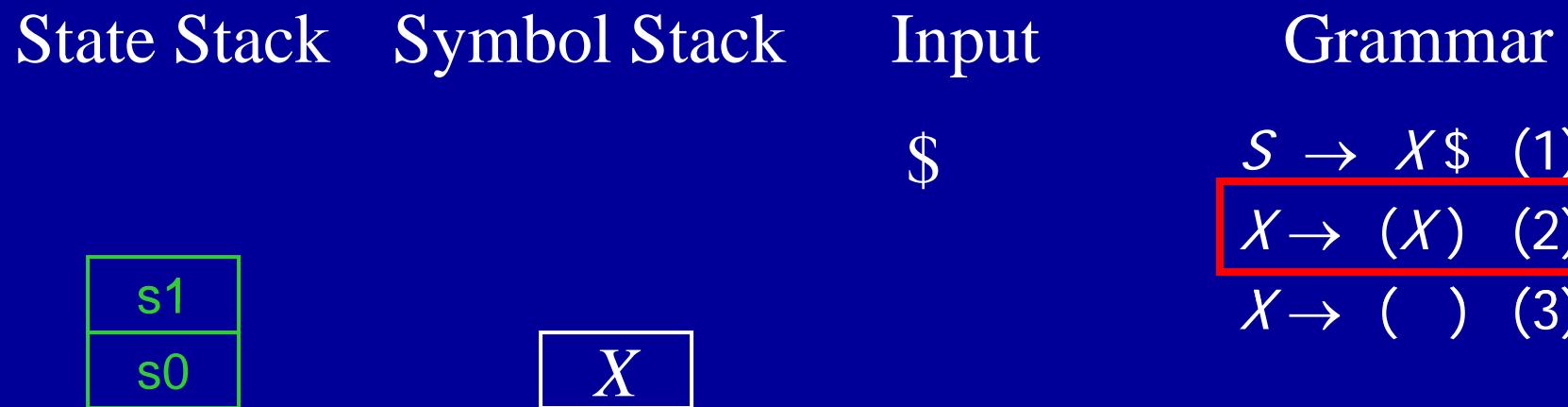
Step Three: Use Goto, Push New State

State	()	\$	Goto
s0	shift to s2	error	error	goto s1
s1	error	error	accept	
s2	shift to s2	shift to s5	error	goto s3
s3	error	shift to s4	error	
s4	reduce (2)	reduce (2)	reduce (2)	
s5	reduce (3)	reduce (3)	reduce (3)	



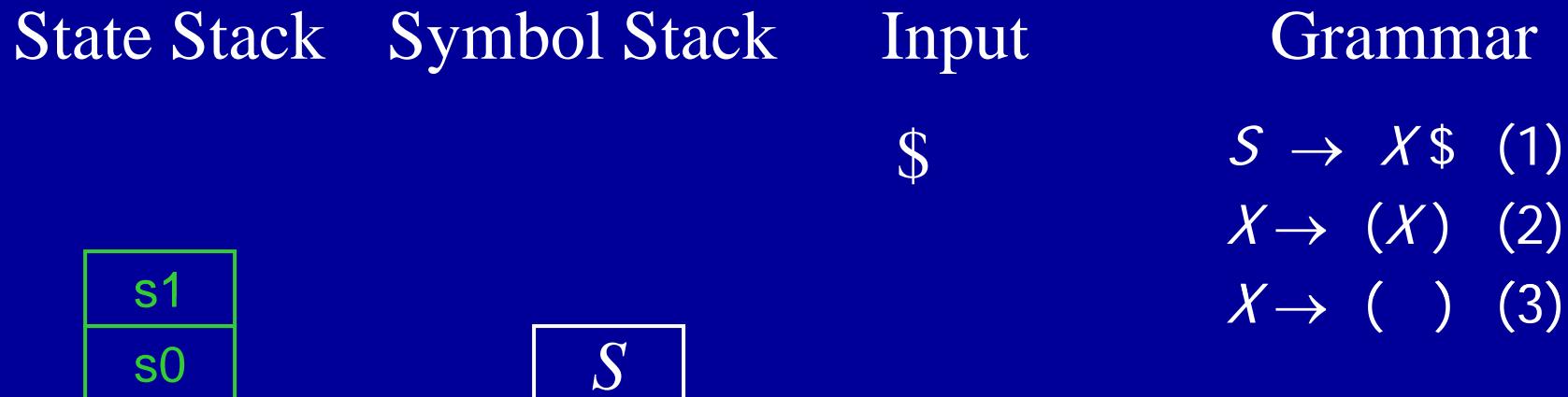
Step Three: Use Goto, Push New State

State	()	\$	Goto
s0	shift to s2	error	error	goto s1
s1	error	error	accept	
s2	shift to s2	shift to s5	error	goto s3
s3	error	shift to s4	error	
s4	reduce (2)	reduce (2)	reduce (2)	
s5	reduce (3)	reduce (3)	reduce (3)	



Accept the String!

State	()	\$	X
s0	shift to s2	error	error	goto s1
s1	error	error	accept	
s2	shift to s2	shift to s5	error	goto s3
s3	error	shift to s4	error	
s4	reduce (2)	reduce (2)	reduce (2)	
s5	reduce (3)	reduce (3)	reduce (3)	



Key Concepts

- Pushdown automaton for parsing
 - Stack, Finite state control
 - Parse actions: shift, reduce, accept

Parse table for controlling parser actions

- Indexed by parser state and input symbol
Entries specify action and next state
- Use state stack to help control
- Parse tree construction
 - Reads input from left to right
 - Bottom-up construction of parse tree

6.035 Computer Language Engineering
Spring 2010

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