

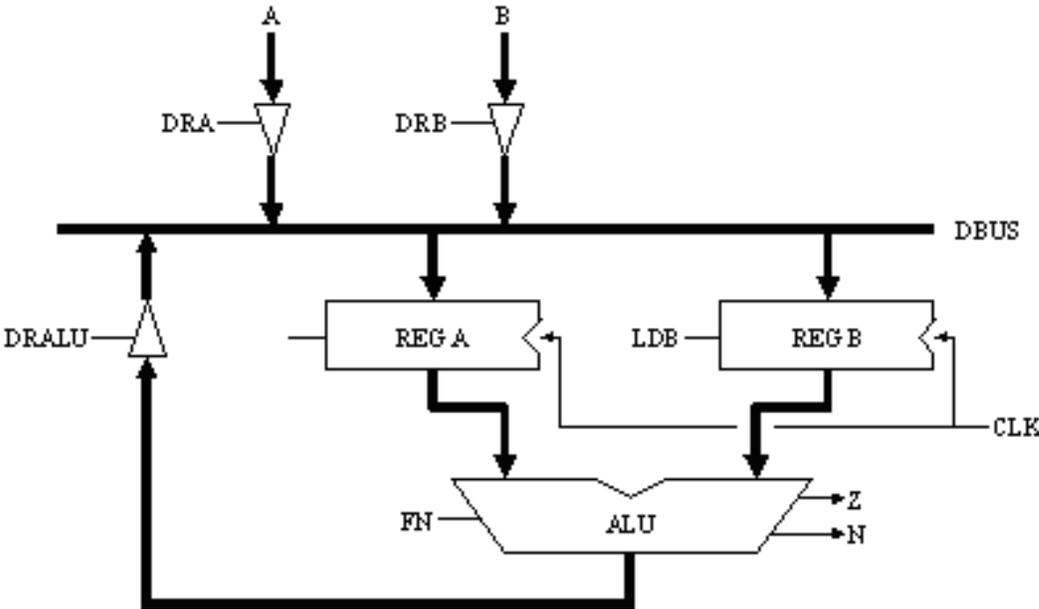
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6.004 Computation Structures  
Spring 2009

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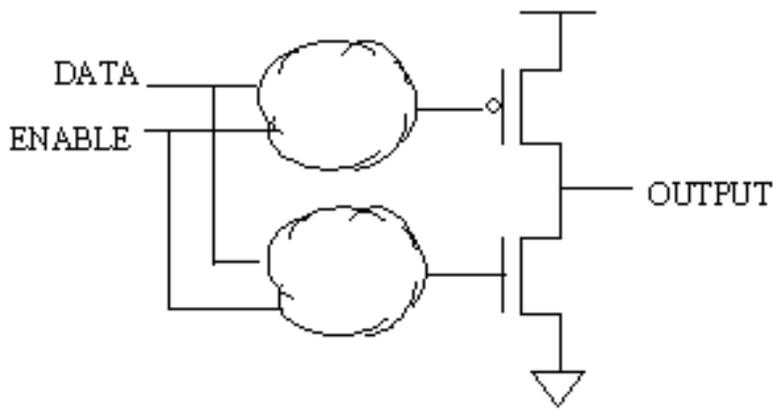
# Programmable machines

Problem 1. Consider the following circuit:



The heavy lines represent busses, which are many signals grouped together, e.g., an eight-bit bus is eight separate signal wires that are treated as a group. When a bus connects to one or more components, it's just shorthand for drawing the individual signal wires between those components.

- A. The components with triangular schematic symbols are tristate drivers that operate like buffers except that they have an additional control input called an enable. When the enable is high, the buffer is on and the input value is driven onto the output. When the enable is low, the buffer is off and doesn't drive anything onto its output (i.e., the output pin is in a high-impedance state). What rules should the designer follow when designing the logic that generates DRA, DRB and DRALU in order to ensure that the DBUS signals always have legitimate values?
  
- B. ★ Draw a schematic showing how a tristate driver might be implemented using mosfets. Hint: The following schematic shows one way of implementing a tristate driver.



You just have to fill in the logic inside each of the clouds—think about for what values of DATA, ENABLE you want the pullup to be on and replace the upper cloud with one or more logic gates that implement that equation. Ditto for the pulldown and lower cloud.

- C. ★ The register-like symbols labeled "Reg A" and "Reg B" also have an additional enable input and are called load-enabled registers. When the enable is high, the register will be loaded from the incoming data. When the enable is low, the register reloads itself with its previous value. Show how to implement a load-enabled register from a regular D-register and a 2-way multiplexer.
- D. It's considered bad practice to control the loading of a register by "gating" its clock, i.e., by adding some logic that controls whether or not the register sees a rising clock edge. Briefly explain why "gating the clock" is discouraged. Hint: consider the effects of clock skew and logic hazards.
- E. The arithmetic-logic unit (ALU) has two data inputs (A and B) and, in this circuit, can perform only two operations, based on the single control signal FN:
- when  $FN = 0$ , the ALU output is  $A - B$
  - when  $FN = 1$ , the ALU output is  $B - A$

The ALU also generates two condition codes which give us some additional information about the ALU output:

- Z = 1 when the ALU output is the number "0"
- N = 1 when the ALU output is a negative number

Assuming that we have 8-bit data values and use a two's complement representation for the data values processed by the ALU, draw gate-level schematics for the logic that generates the Z and N signals from the ALU output value.

- F. ★ Your job is to build a controller that will cause the circuit above to execute the following algorithm which computes the greatest common divisor of two inputs:

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while (a != b)
```

```
if (a > b) a = a - b;
else b = b - a;
```

The controller will be a state machine that takes 2 bits of input (Z and N) and produces control signals for the data paths (DRA, DRB, DRALU, LDA, LDB, FN).

Draw a state diagram for the controller. Outputs from your FSM should depend only on the current state. Indicate which are the initial and final states of your FSM on the diagram.

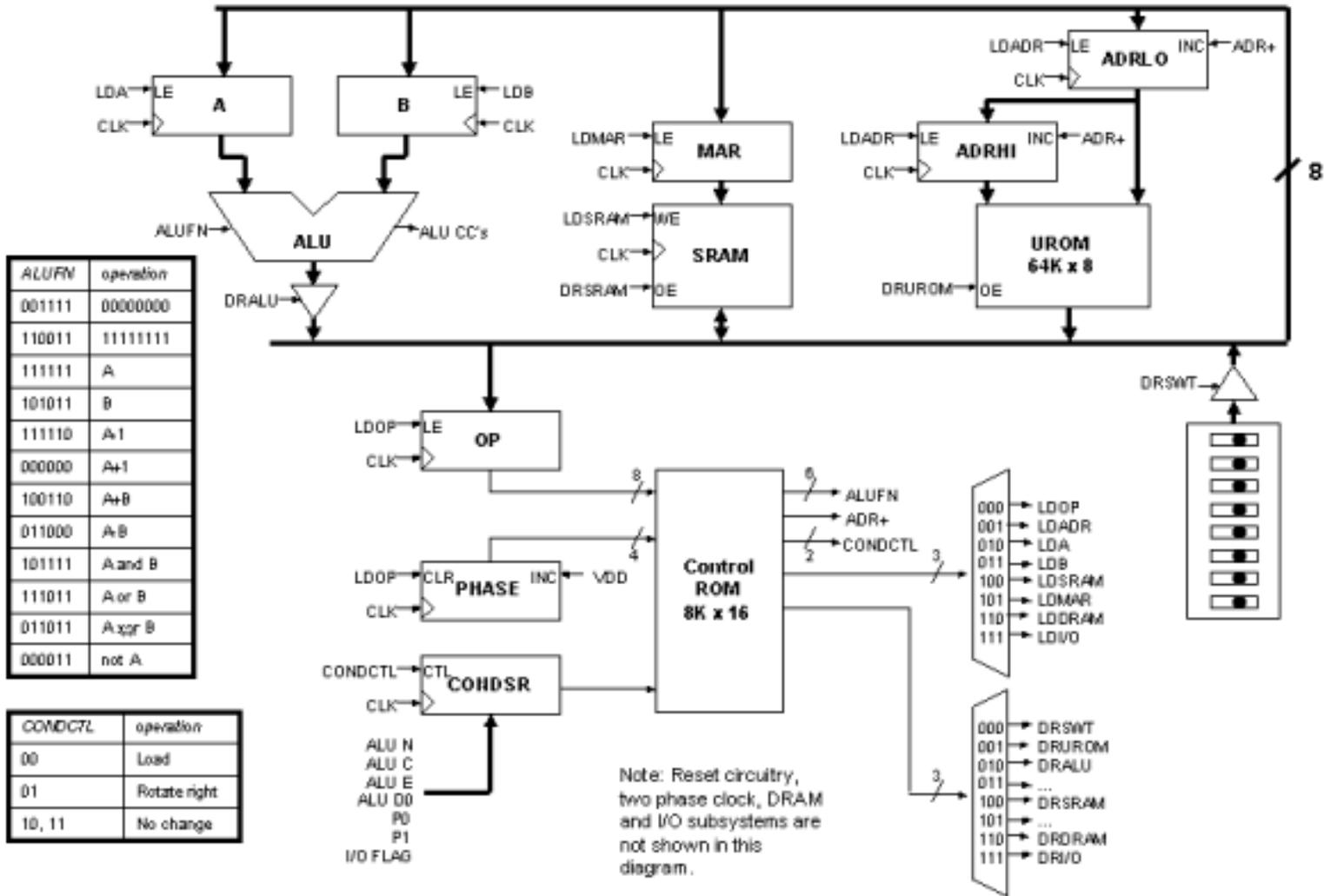
G. ★ Supply a truth table for the logic that generates the control signals.

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Problem 2. **The material in this question will not covered by any quizzes.** It's presented here as an extended example of a programmable datapath.

The following diagram shows the datapath and control circuitry for a nifty little microprogrammed architecture the students used to build in the 6.004 lab:

(portions of) the MAYBE datapath (see Chap. 11 & Appendix A in Ward & Halstead)



Some features of the MAYBE:

- The datapath is 8 bits wide. All the subsystems connect to a common 8-bit bus which routes data between the subsystems. In a particular cycle, one of the subsystems is selected to drive data onto the bus (chosen by the DR signals) which can then be loaded into the selected destination (chosen by the LD signals).
- The Control ROM is programmed as a nanointerpreter that executes one of 256 microinstructions selected by the contents of the OP register. Each microinstruction consists of up to 16 nanoinstruction; the nanoPC is generated by the PHASE counter which is reset to 0 each time the OP register is loaded.
- The Control ROM is programmed using the following template:

Opcode	Phase	COND	=	ADR+	ALU	CC	DRSEL	LDSEL	Comment
--------	-------	------	---	------	-----	----	-------	-------	---------

*****	****	*	=	1	111111	11	001	000	Opcode = uROM; ADR+
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"\*" is used to match either "0" or "1" on the corresponding address line. The template above initializes every nanoinstruction in the Control ROM to an operation that reads the next byte from the UROM (DRSEL = 001), places it in the OP register (LDSEL = 000), and then increments the ADRHI/ADRLO registers (ADR+ = 1).

- The UROM contains a microprogram that is executed by the nanointerpreter. Each microinstruction in the UROM begins with an 8-bit opcode; microinstruction execution begins by loading the opcode into the OP register. As the nanointerpreter executes the nanocode associated with that opcode, additional operand bytes may be fetched from the UROM. The final step in executing a microinstruction is to load the OP register with the opcode of the next microinstruction.
  - The ADRHI/ADRLO registers form a 16-bit program counter for the UROM program. These registers can be loaded from the data bus (eg, when doing a branch) or simply incremented by asserting ADR+. Note that the ADRHI/ADRLO registers are incremented at the end of the cycle after they have been used as the address for the UROM in the current cycle.
- A. If we inadvertently switch connections on two of the wires that run from the MAR register to the address inputs of the SRAM will operation be affected? Is your answer the same if we switch two wires running between ADRHI/ADRLO and the address inputs to the UROM? If the answers are not the same, what constitutes the difference between the SRAM and UROM?
  - B. What, if anything, prevents two drivers from putting conflicting data on the data bus of the MAYBE (ignore transients during propagation delays of the control circuitry)? Can such conflicts happen if there are programming errors in the Control ROM?
  - C. Given a big enough Control ROM, could the LDSEL and DRSEL decoders be eliminated (producing the load and drive signals directly as Control ROM outputs)? If so, what advantage might this have?
  - D. Execution of a nanoprogram can be influenced by information for the datapath? Explain how a nanoprogram can make data-dependent decisions.
  - E. Given a big enough Control ROM, could the condition shift register be eliminated (using the condition bits directly as Control ROM inputs)? If so, what advantage might this have? How many more (or fewer) outputs and inputs would the Control ROM need to have to implement this? What would be the size (in bits) of the Control ROM?
  - F. The nanoinstruction shown above selects the UROM as the data source and asserts ADR+ during the same clock cycle. How does this work, i.e., is the original or incremented address used when accessing the UROM?

G. What does the following nanocode program do?

Opcode	Phase	COND	=	ADR+	ALU	CC	DRSEL	LDSEL	Comment
00001010	0000	*	=	1	111111	11	001	101	MAR = uROM; ADR+
00001010	0001	*	=	0	111111	11	100	010	A = SRAM
00001010	0010	*	=	1	111111	11	001	101	MAR = uROM; ADR+
00001010	0011	*	=	0	111111	11	100	011	B = SRAM
00001010	0100	*	=	1	111111	11	001	101	MAR = uROM; ADR+
00001010	0101	*	=	0	100110	00	010	100	SRAM = A + B; latch CCs
00001010	0110	*	=	1	111111	11	001	000	OP = uROM; ADR+

H. What does the following nanocode program do?

Opcode	Phase	COND	=	ADR+	ALU	CC	DRSEL	LDSEL	Comment
00001011	0000	*	=	1	111111	11	001	010	A = uROM; ADR+
00001011	0001	*	=	1	111111	11	001	101	MAR = uROM; ADR+
00001011	0010	*	=	0	111111	11	100	011	B = SRAM
00001011	0011	*	=	1	111111	11	001	101	MAR = uROM; ADR+
00001011	0100	*	=	0	100110	00	010	100	SRAM = A + B; latch CCs
00001011	0101	*	=	1	111111	11	001	000	OP = uROM; ADR+

I. What does the following nanocode program do?

Opcode	Phase	COND	=	ADR+	ALU	CC	DRSEL	LDSEL	Comment
00001100	0000	*	=	1	111111	11	001	010	A = uROM; ADR+
00001100	0001	*	=	0	111111	11	001	001	ADR = uROM
00001100	0010	*	=	0	111111	11	010	001	ADR = A
00001100	0011	*	=	1	111111	11	001	000	OP = uROM; ADR+

J. What does the following nanocode program do?

Opcode	Phase	COND	=	ADR+	ALU	CC	DRSEL	LDSEL	Comment
00010111	0000	*	=	1	111111	11	001	010	A = uROM; ADR+

00010111	0001	*	=	0	111111	01	010	010	Shift CC's
00010111	0010	1	=	0	111111	11	001	001	ADR = uROM
00010111	0011	1	=	0	111111	11	010	001	ADR = A
00010111	0100	1	=	1	111111	11	001	000	OP = uROM; ADR+
00010111	0010	0	=	1	111111	11	001	010	A = uROM; ADR+
00010111	0011	0	=	1	111111	11	001	000	OP = uROM; ADR+

K. What does the following nanocode program do?

Opcode	Phase	COND	=	ADR+	ALU	CC	DRSEL	LDSEL	Comment
00000011	0000	*	=	0	110011	11	010	101	MAR = 11111111
00000011	0001	*	=	0	111111	11	100	010	A = SRAM
00000011	0010	*	=	0	111110	11	010	100	SRAM = A - 1
00000011	0011	*	=	1	111111	11	001	101	MAR = uROM; ADR+
00000011	0100	*	=	0	111111	11	100	011	B = SRAM
00000011	0101	*	=	0	111111	11	010	101	MAR = A
00000011	0110	*	=	0	101011	11	010	100	SRAM = B
00000011	0111	*	=	1	111111	11	001	000	OP = uROM; ADR+