

# **1.050 Engineering Mechanics I**

Fall 2007

# Notes and remarks

- Lecture Summary Slide
- Content Survey
- Lecture notes
- Homework assignments (weekly)
- Exams: 2 in-class quizzes, 1 final  
All exams are open-book
- Grading:  
**Two quizzes (25%)**  
**Final (25%)**  
**Homework assignment (50%)**

### Lecture 1 - summary

- Introduction to the engineering science approach
- Galileo problem: Could we simply 'upscale' an animal, human.. several times and could it still exist?
- Dimensional analysis shows: If same material is used, a monster can not exist
- Remedy: Change material (density) as the height is increased in order to create physical similarity

Express physical situation as function of nondimensional parameters (critical: find correct dependence on variables)

$$mg \leq F_{lim} = f(h, g, \rho, V, \sigma_0)$$

Galileo's Problem:

$$\Pi_0 = \frac{F_{lim}}{h^3 \sigma_0} = f\left(\Pi_1 = \frac{hg\rho}{\sigma_0}, \Pi_2 = \frac{V}{h^3}\right)$$

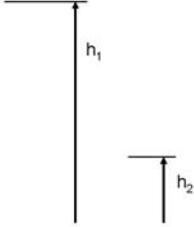
$$\rho g \Pi_2 h^3 \leq \Pi_0 \sigma_0 h^2$$

Robustness:  $\gamma = \frac{F_{lim}}{mg} = \frac{\Pi_0(\Pi_1, \Pi_2)}{\Pi_2 \Pi_1} \geq 1$

Thus, for a monster to exist need material with higher strength OR material with lower density.

Definition of Galileo number:  $N_{Gal} = \frac{hg\rho}{\sigma_0}$

Two events are similar if the invariants are the same, here the Galileo Number:

$$\Pi_1^{(1)} = \Pi_1^{(2)} = \frac{h^{(1)} \rho^{(1)} g}{\sigma_0^{(1)}} \quad \lambda = \frac{h_1}{h_2} = \frac{\sigma_0^{(1)}}{\sigma_0^{(2)}} \frac{\rho^{(2)}}{\rho^{(1)}}$$


### Lecture 1 - questions

- Explain the steps in the engineering science approach.
- Do you know how to solve a linear system of equations...
  - on paper
  - using Matlab
  - using Excel
- Is the concept "rank of a matrix" clear?
- Is there an physical reason why there are no monsters on earth?
- Using scaling relationships, explain the reason why there are no monsters on earth.
- Explain how to obtain dimensionless parameters for a given physical problem.
- Give possible reasons how it is possible that large dinosaurs have been able to live on earth.

# Assignments

- **Homework / Problem Sets (50%)**
  - Assigned weekly on Wednesday, evaluated and returned to you (ASAP)
  - Build *homework teams* of three students:
    - Engineering is team work. We expect a true team work, in which everybody contributes equally to the result. This is testified by the team members signing a declaration that “the signature confirms that all have equally contributed to the homework”.
    - Typical teamwork:
      - Each student works individually through the homework set.
      - The team meets and discusses questions, difficulties and solutions.
      - Possibly, meet with TA or instructor.
- You must reference your sources and collaborators, whether other students, sources on the web, archived solutions from previous years etc...

# A few things we'd like you to remember...

- **We teach the class for you!** At any time please let us know if you have concerns or suggestions, or if you have difficulties. We'll do the best to cater to your needs!
- The goal is that you will have an excellent basis for engineering science in many other applications – aside from the mechanics topic covered here...
- Our goal: **Discover Engineering Mechanics with you** – starting at fundamental concepts (Newton's laws) to be able to apply the knowledge to complex engineering problems.

# 1.050: Engineering Mechanics

## Why are there no monsters on Earth?

Images removed due to copyright restrictions.

Normandy Bridge 900m (1990ies)

**Can we build bridges  
Between continents?**

# Hurricane Katrina

- What caused major flooding in the city?  
Why did the levees break?

## Geotechnical Design

- Load < strength capacity
- Failure (plasticity or fracture)
- Mechanism

Photograph of floodwaters removed due to copyright restrictions.

## Impact

- 2 million people
- Nationwide Life Line interruption

## What caused this to happen?

- Global warming?
- Policy: Role of the federal government?

# Minnesota bridge collapse

## Aging infrastructure

- What caused the bridge to collapse?
- Are our bridges safe?
- Can we detect failure before tragedy happens?

Photographs of collapsed bridge removed due to copyright restrictions.

## Fixing the problems

- Retrofitting?
- Rebuilding new bridges?
- Funding? -- Policy change to allocate more funding to fix unfit infrastructure

# Earthquake disasters

## Earthquake in Peru (August 2007)

Map of Peru showing epicenter location removed  
due to copyright restrictions.

Photographs of collapsed roads removed due to copyright restrictions.

### Structural Design

- Service State (Elasticity)
- Failure (Plasticity or Fracture)
- Mechanism

### Impact

- Millions of people
- Nationwide Life Line interruption
- Economy

# 9-11: The Fall of the Towers

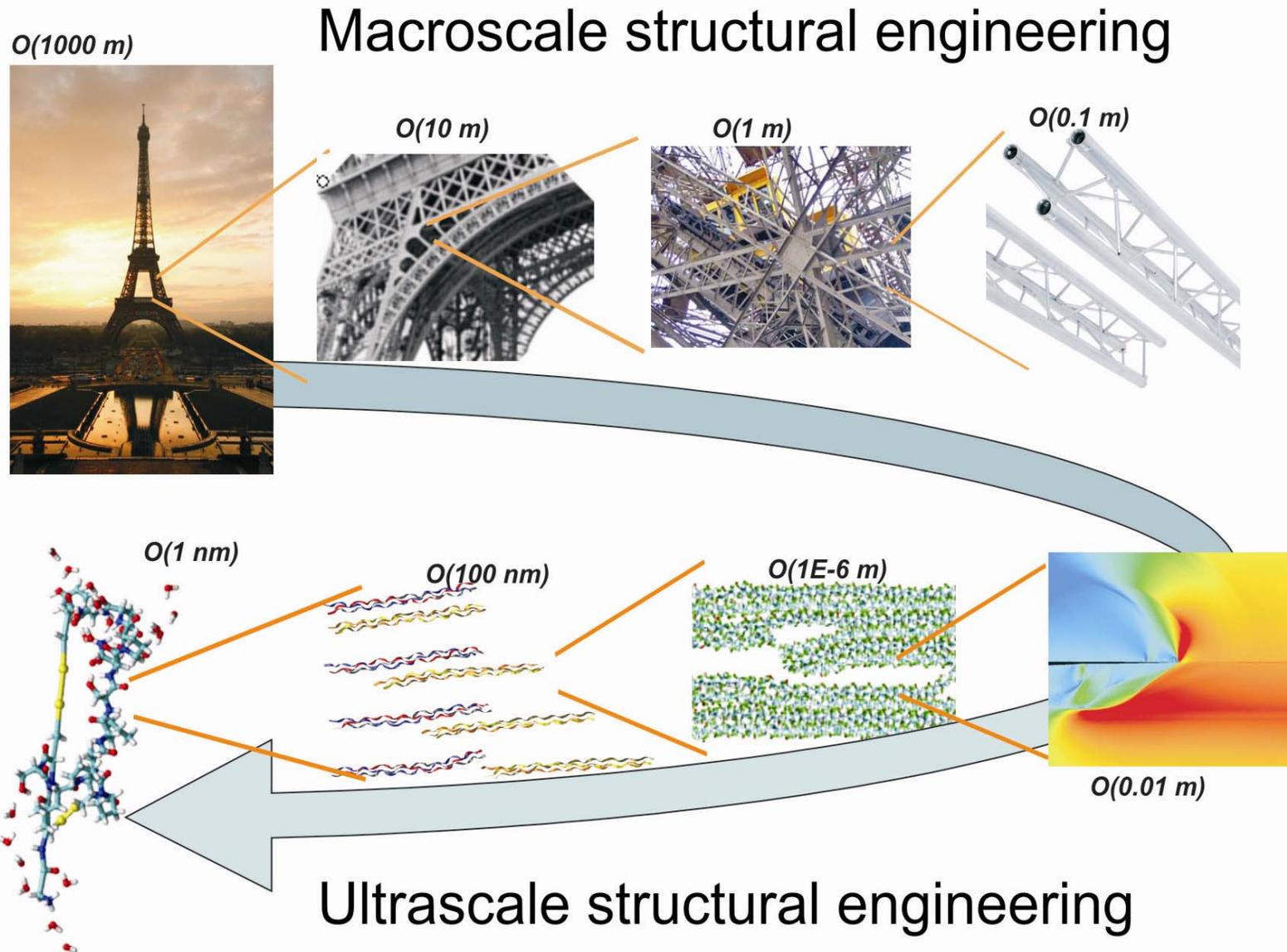
North Tower: 8:46 am above 96<sup>th</sup> floor, failed at 10:28 am

South Tower: 9:03 am above 80<sup>th</sup> floor, failed at 9:59 am

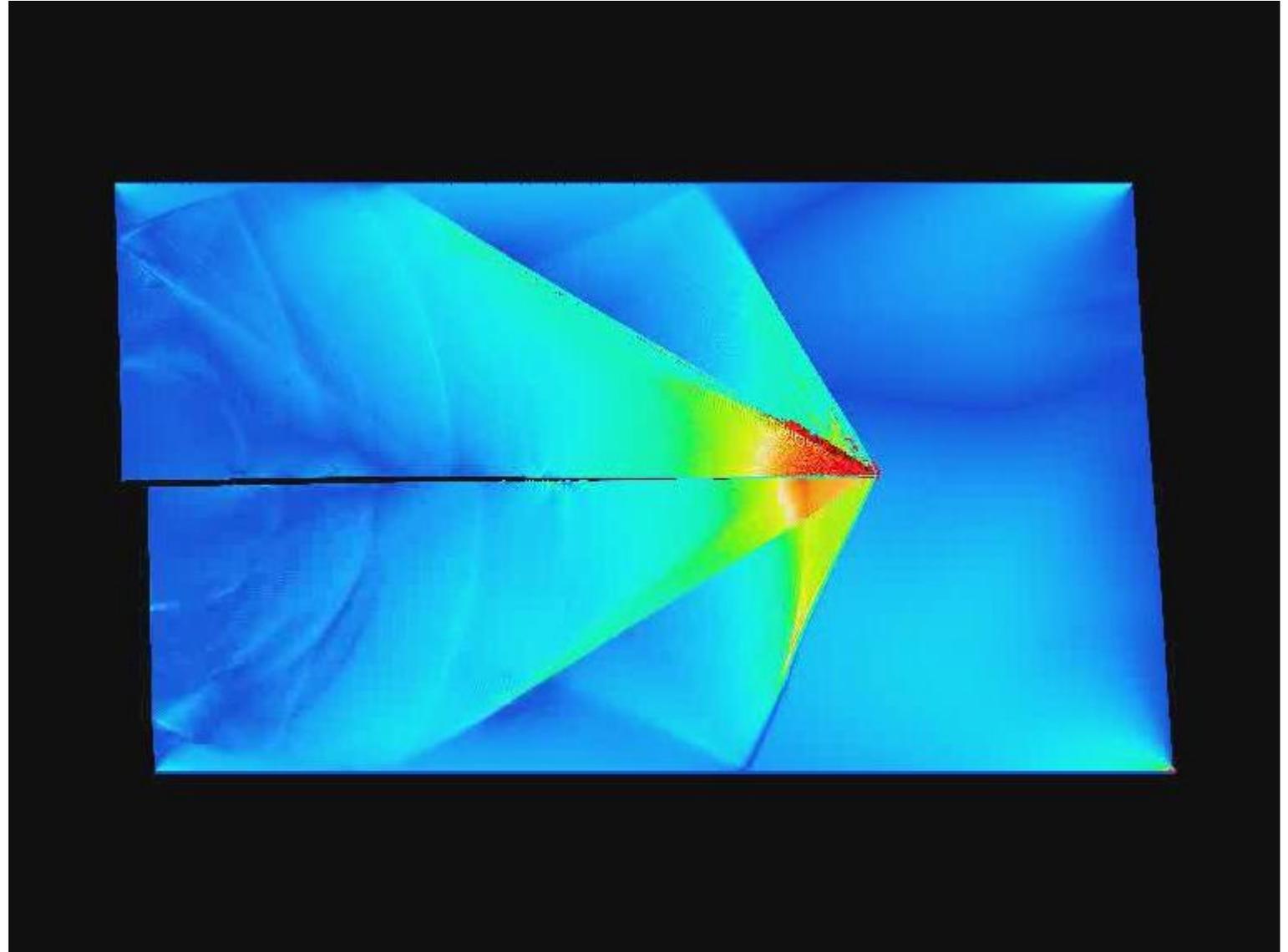
**Immediate Question:** How did the towers fail? - Mechanism – Lecture 4

Three sequential photographs of tower collapse removed due to copyright restrictions.

# Engineering science paradigm: Multi-scale view of materials



# Atomistic mechanisms of fracture



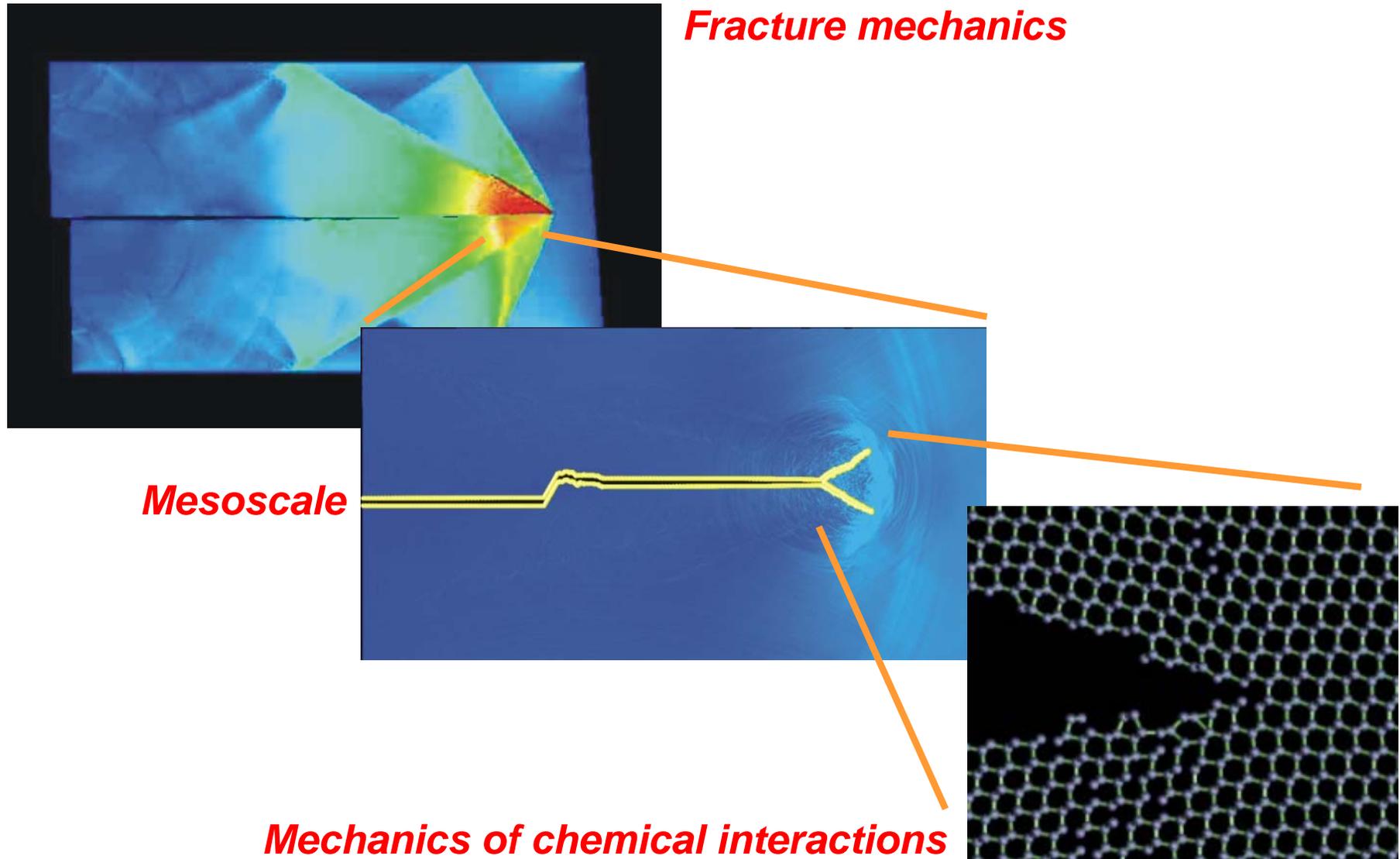
**Simulations of  
atomistic  
fracture  
mechanisms**

**Reveals new  
fracture  
mechanism:  
Supersonic  
fracture**

View the complete movie at:

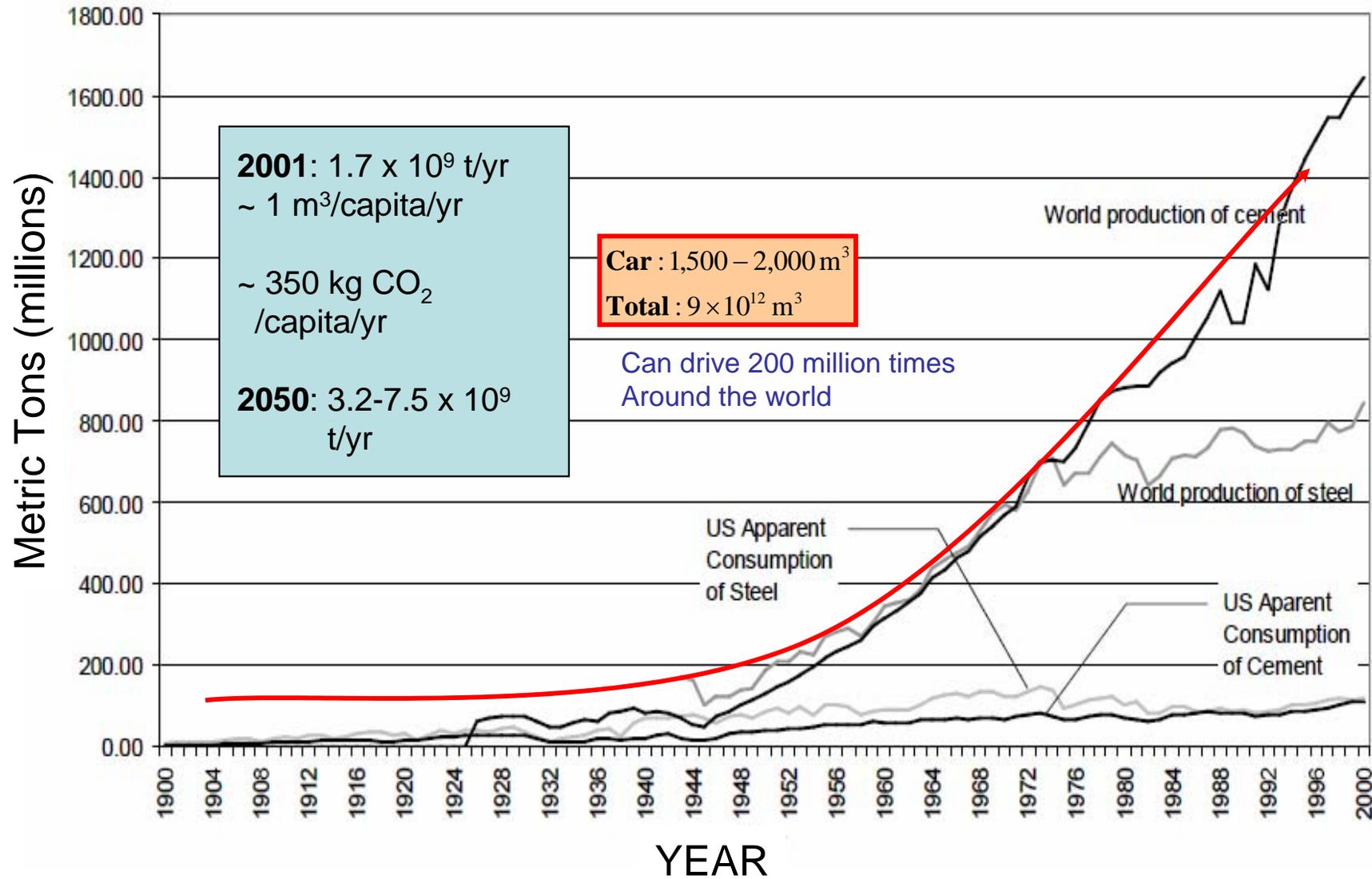
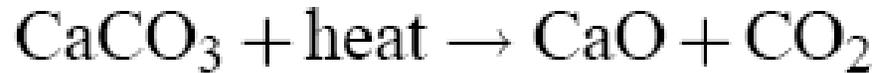
[http://web.mit.edu/mbuehler/www/research/supersonic\\_fracture.mpeg](http://web.mit.edu/mbuehler/www/research/supersonic_fracture.mpeg).

# Fracture is linked to the mechanics of chemical bond breaking



# Impact of cement on worldwide CO2 production

Worldwide Cement Consumption



**Worldwide Cement Consumption equates to 10% of worldwide CO2 Emission**

Chaturvedi, S. and Ochsendorf, J., "Global Environmental Impacts Due to Concrete and Steel," *Structural Engineering International*, 14/3, Zurich, Intl. Assoc. of Bridge and Structural Engineers, August 2004, 198-200.

Courtesy of John Ochsendorf. Used with permission.

# Concrete: A complex multi-scale material

New materials for construction industry?

Ti, Mg... based cement?

New production pathways?

**Mortar**  
few mm

**Cement paste**  
< 0.1 mm

Images of concrete from the nanometer to centimeter scale removed due to copyright restrictions.

**C-S-H**  
<  $\mu\text{m}$

**Platelets**  
few 10 nm

**Molecular mechanics**

**Chemistry**  
Angstrom-nm

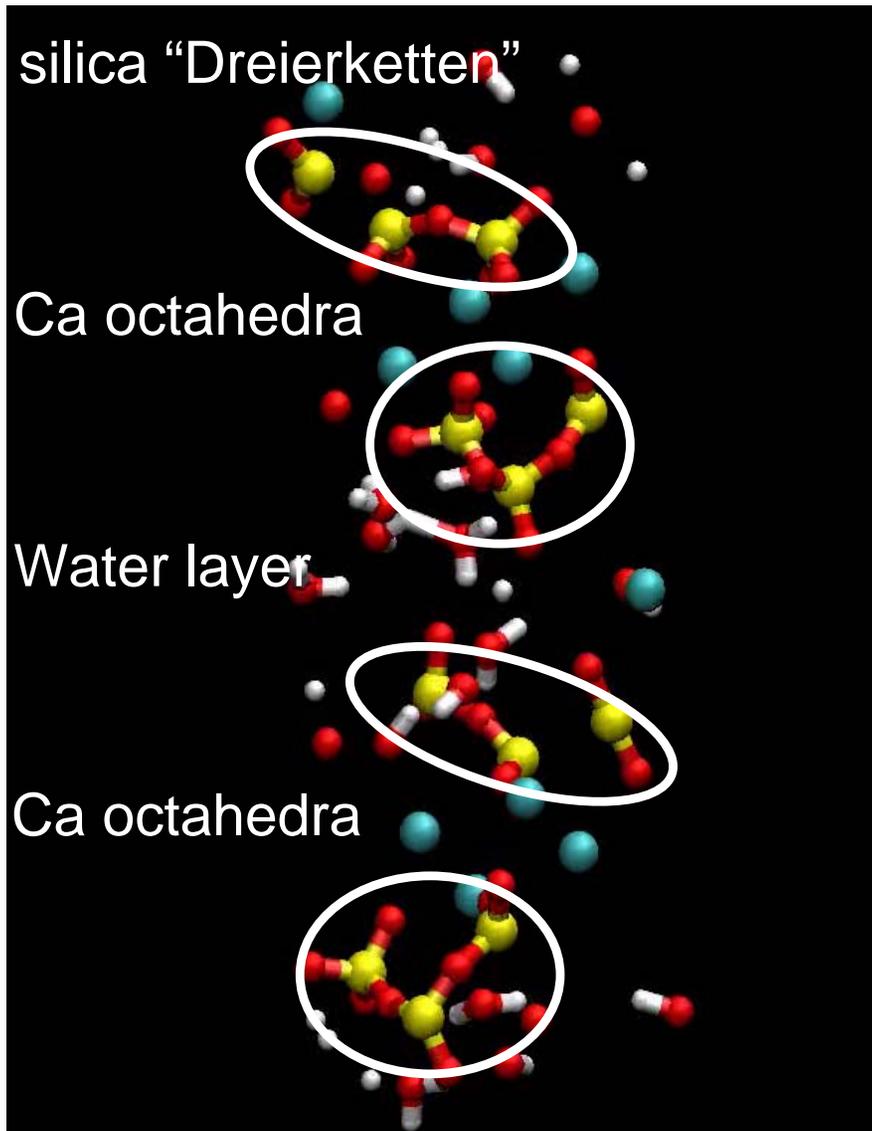
**Concrete**  
1 cm

↓  
Enables structures

↓  
Kilometers

Image of suspension bridge removed due to copyright restrictions.

# Opening molecular-nanoscale for engineering design



## Production of 'green concrete'

Reduce CO<sub>2</sub> emission during production

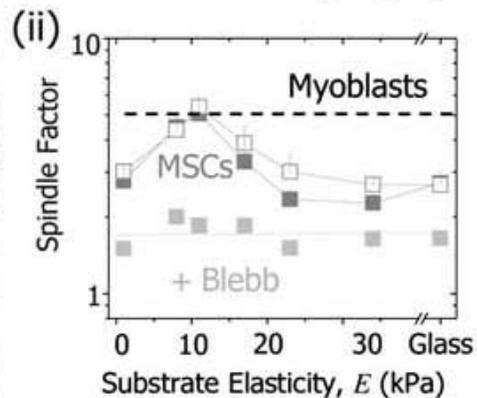
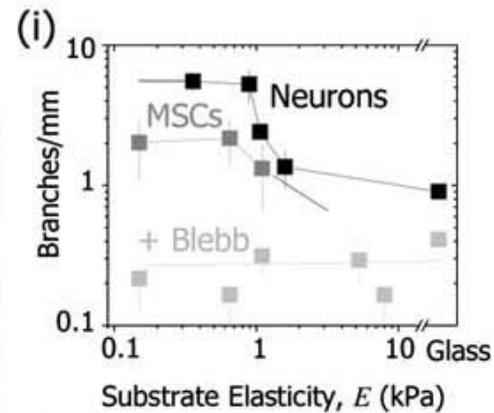
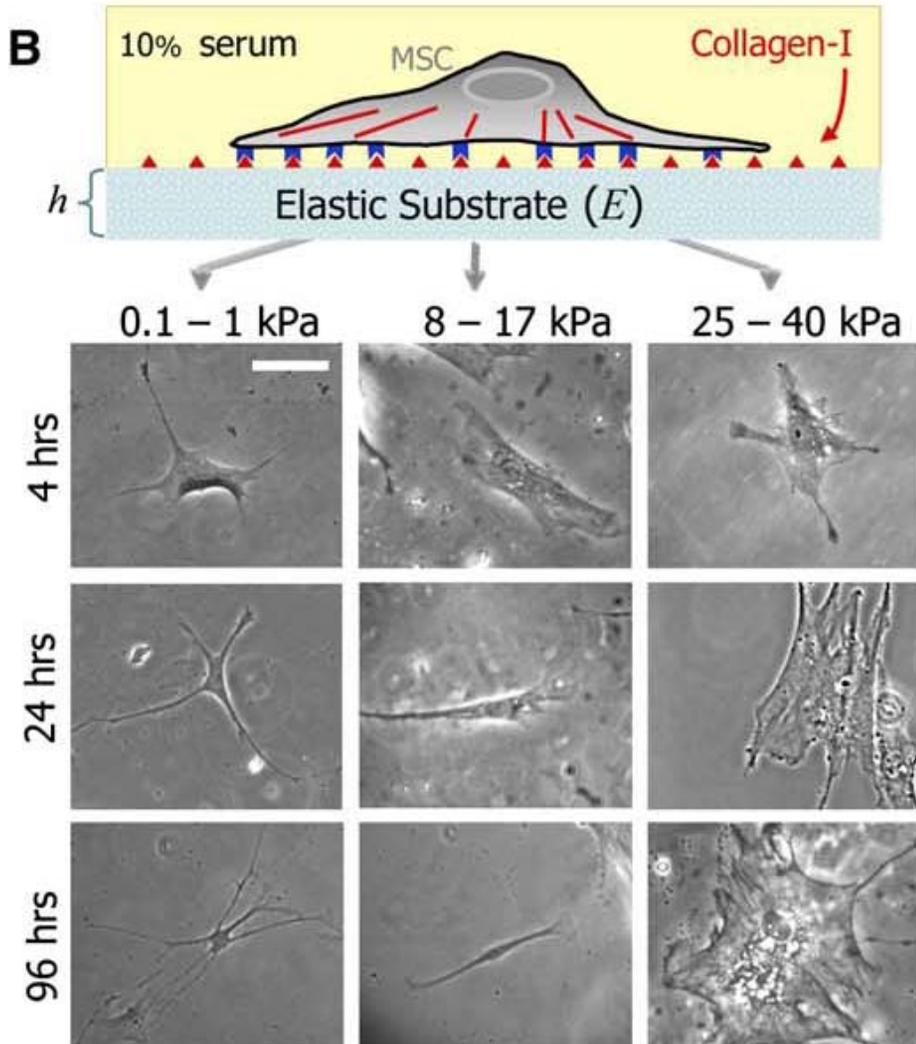
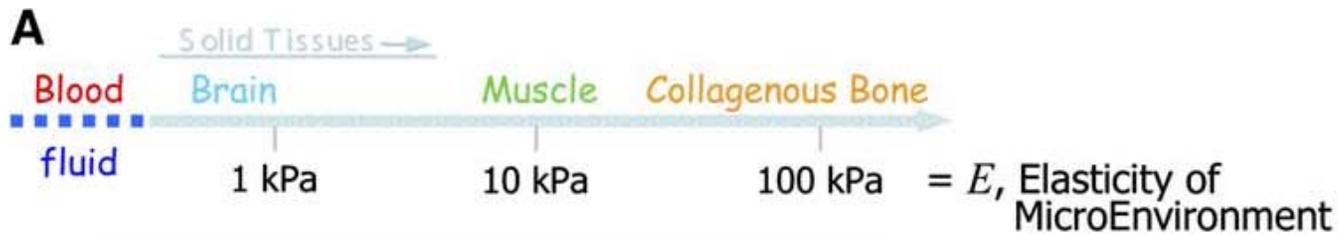
Understand diffusion of radioactive waste through concrete

Long-term stability/durability → avoid disasters

Environmental effects (chemicals, moisture,...)

Mechanical stability

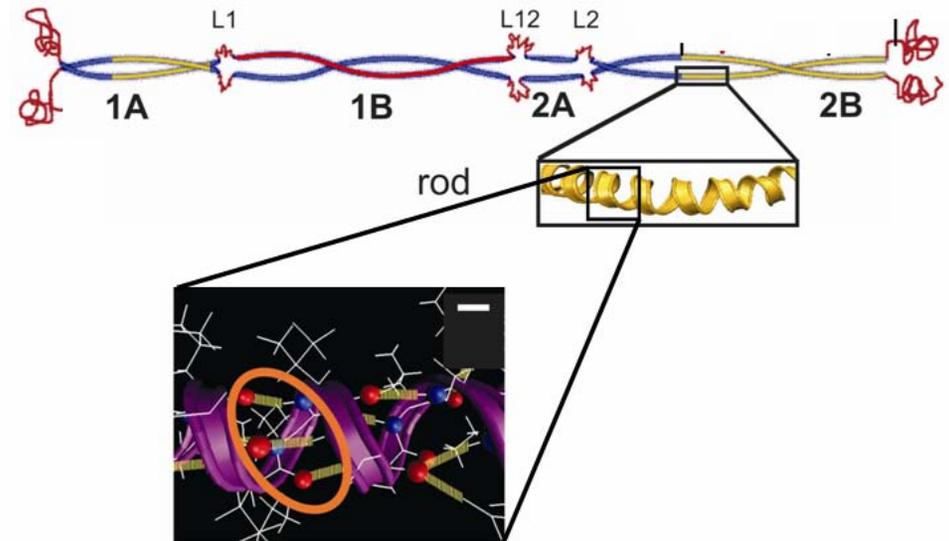
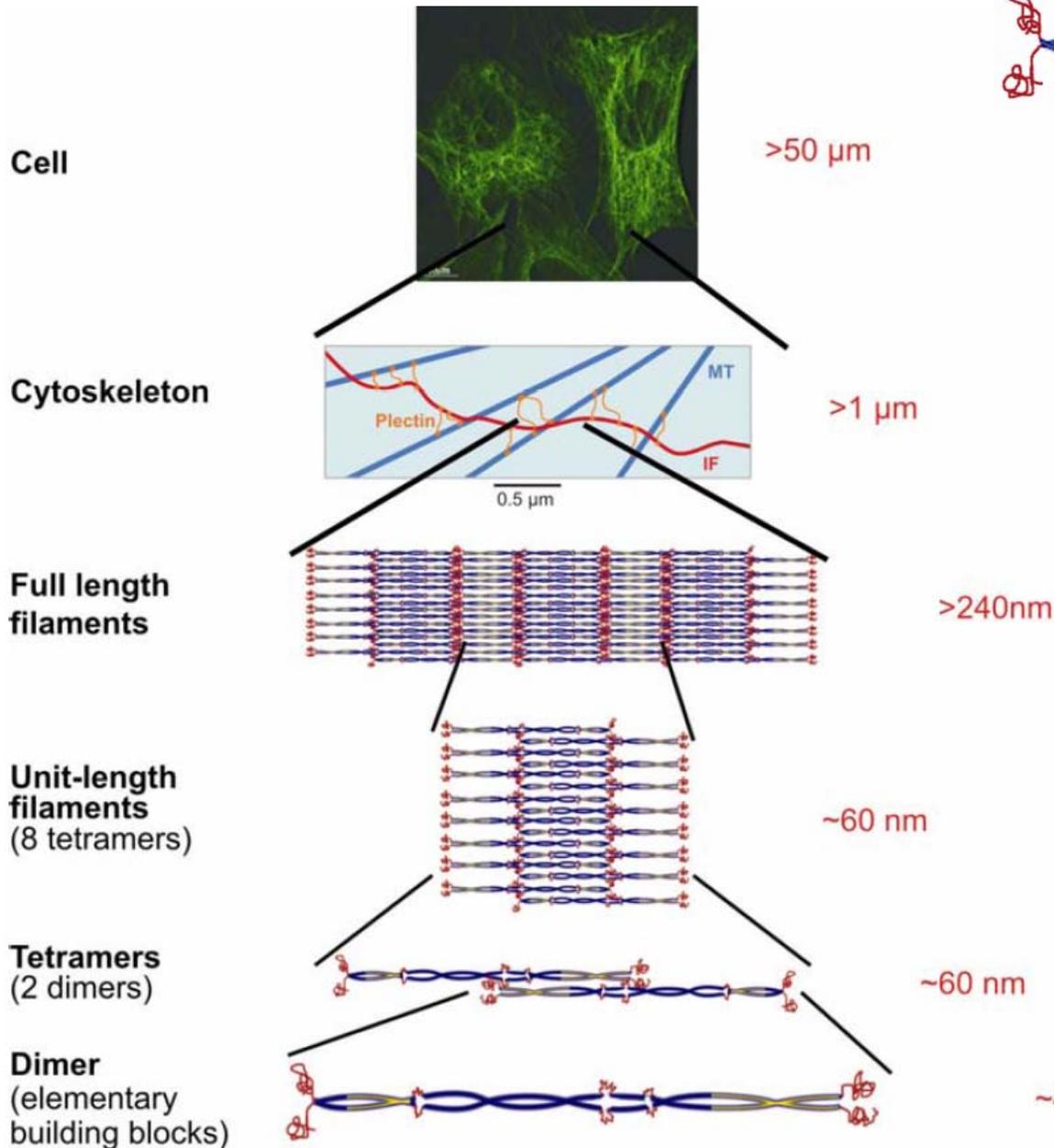
# Mechanics in life sciences



Elasticity of environment directs stem cell differentiation

- Brain tissue
- Muscle
- Bone

# Mechanics in life sciences



Courtesy Elsevier, Inc., <http://www.sciencedirect.com>.  
Used with permission.

- Change of mechanics in diseases?
- How can we use self-assembly to synthesize new materials?

# Mechanics in life sciences

- Single point mutations in IF structure causes severe diseases such as **rapid aging disease progeria – HGPS** (*Nature*, 2003; *Nature*, 2006, *PNAS*, 2006)
- Cell nucleus loses stability under cyclic loading
- Failure occurs at heart (fatigue)

Substitution of a single DNA base: Amino acid guanine is switched to adenine

Experiment suggests that mechanical properties of nucleus change (Dahl *et al.*, *PNAS*, 2006)

Images from the organismal to cell to molecular scales removed due to copyright restrictions.

# 1.050 – Content overview

## I. Dimensional analysis

1. On monsters, mice and mushrooms
2. Similarity relations: Important engineering tools

Lectures 1-3  
Sept.

## II. Stresses and strength

2. Stresses and equilibrium
3. Strength models (how to design structures, foundations.. against mechanical failure)

Lectures 4-15  
Sept./Oct.

## III. Deformation and strain

4. How strain gages work?
5. How to measure deformation in a 3D structure/material?

Lectures 16-19  
Oct.

## IV. Elasticity

5. Elasticity model – link stresses and deformation
6. Variational methods in elasticity

Lectures 20-31  
Nov.

## V. How things fail – and how to avoid it

7. Elastic instabilities
8. Plasticity (permanent deformation)
9. Fracture mechanics

Lectures 32-37  
Dec.

# 1.050 – Content

- The contents of 1.050 will be important in several subjects
- Spring: 1.060 Engineering Mechanics II –
  - Fluid Mechanics
    - Hydrostatics
    - Hydrodynamics
    - Open Channel Flow
- Application in many engineering applications and in engineering science
  - Biomechanics
  - Molecular mechanics & molecular dynamics
  - Microfluidics
  - Environmental science and application
  - Earthquake engineering
  - Structural engineering
  - Materials science
  - ...

# 1.050 – Content overview

## **I. Dimensional analysis**

Lecture 1: Introduction & Galileo's problem

Lecture 2: Dimensional Analysis and Atomic Explosion

Lecture 3: Dimension analysis and application to engineering structures

## **II. Stresses and strength**

## **III. Deformation and strain**

## **IV. Elasticity**

## **V. How things fail – and how to avoid it**