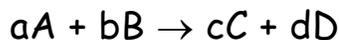


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5.60 Thermodynamics & Kinetics
Spring 2008

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Kinetics: Reaction Rates, Orders, Half Lives



Rate of Reaction:

$$\text{Rate} = -\frac{1}{a} \frac{d[A]}{dt} = -\frac{1}{b} \frac{d[B]}{dt} = \frac{1}{c} \frac{d[C]}{dt} = \frac{1}{d} \frac{d[D]}{dt}$$

$$\text{Experimentally} \Rightarrow \text{Rate} = k \prod_{i=1}^N C_i^{\gamma_i}$$

Where

k = rate constant

C_i = Concentration of Reactant "i"

γ_i = Order of reaction with respect to reactant "i"

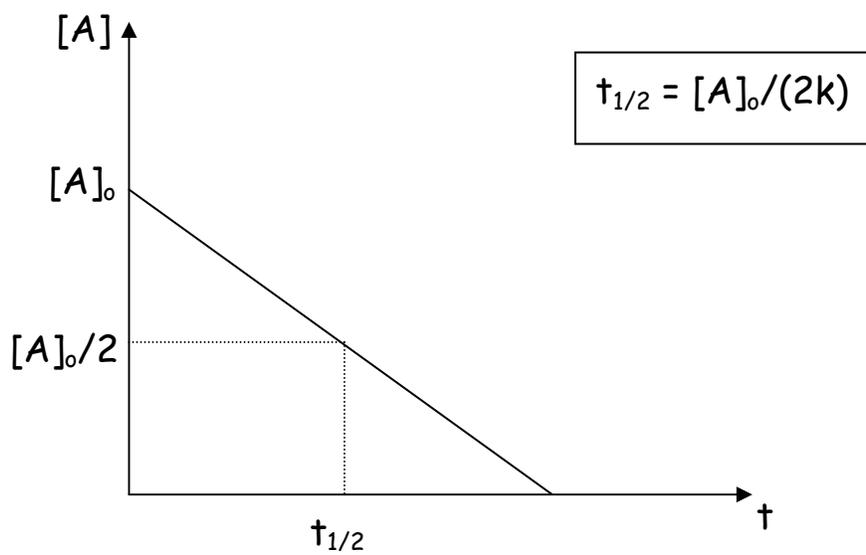
$$\sum_i \gamma_i = \text{Overall rate of reaction}$$

I) Zero Order Reactions (rare)

$$-\frac{d[A]}{dt} = k$$

{k is in [moles/(liter sec)]}

$$[A] = -kt + [A]_0$$



II) First Order Reactions

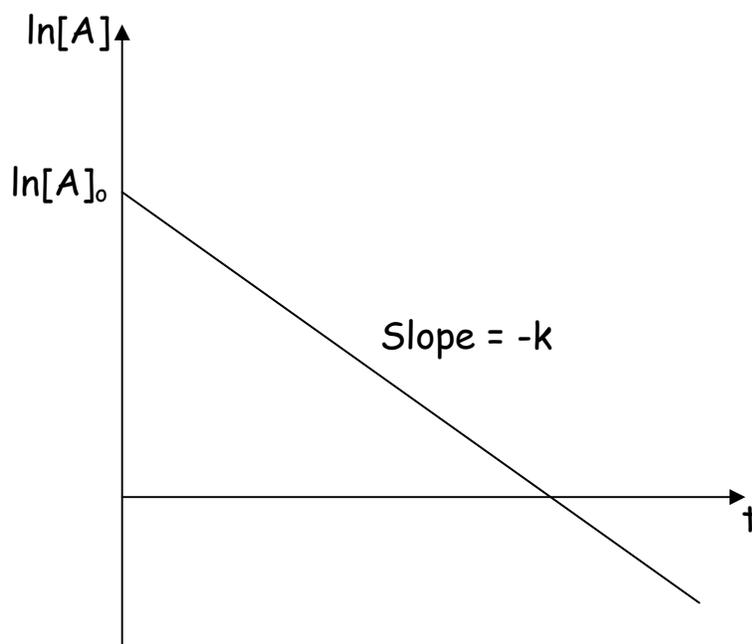


$$-\frac{d[A]}{dt} = k[A]$$

{k is in [1/sec]}

$$[A] = [A]_0 e^{-kt}$$

$$\ln[A] = -kt + \ln[A]_0$$



$$t_{1/2} = (\ln 2) / k = 0.693/k$$

$$k = (0.693)/(t_{1/2})$$

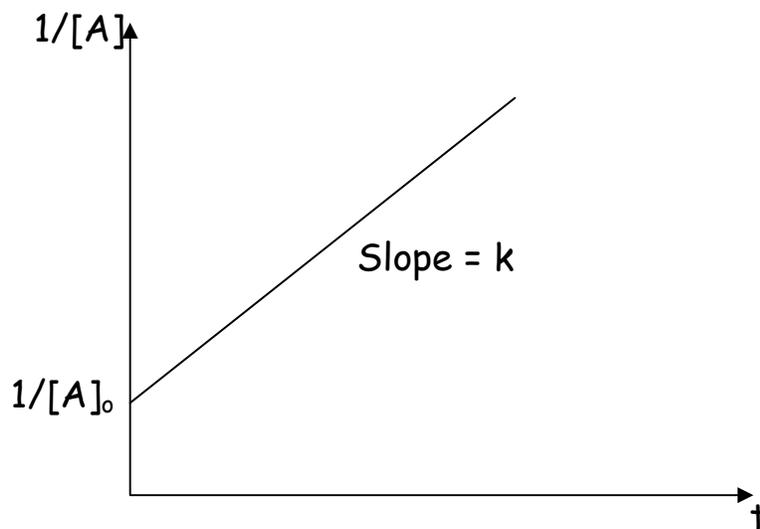
III) Second Order Reactions

a) Second order in one component

$A \rightarrow \text{products}$

$$-\frac{d[A]}{dt} = k[A]^2$$

$$\boxed{\frac{1}{[A]} = \frac{1}{[A]_0} + kt}$$



$$\boxed{t_{1/2} = 1/(k[A]_0)}$$

b) First order in each of two components

A + B → products

$$-\frac{d[A]}{dt} = k[A][B]$$

$$kt = \frac{1}{[A]_0 - [B]_0} \ln \frac{[A][B]_0}{[A]_0[B]} \quad [A]_0 \neq [B]_0$$

Special cases:

$$\text{i) } [A]_0 = [B]_0 \Rightarrow \begin{array}{l} \frac{1}{[A]} = \frac{1}{[A]_0} + kt \\ [A] = [B] \end{array}$$

This is like 2nd order in one component

$$\text{ii) } [B]_0 \ll [A]_0 \Rightarrow [B] = [B]_0 e^{-k't}$$

$$\text{where } k' = [A]_0 k$$

This is pseudo 1st order

Determining Orders of Reactions

I) Getting the data

- a) Quench the reaction, measure concentrations
- b) For gas phase, measure pressure vs. time
- c) Spectroscopically follow reactants/products

Etc...

II) Analyzing the data

A) Reactions with one reactant:



- a) Plot or analyze $[A]$ vs. t
- $\ln[A]$ vs. t
- $1/[A]$ vs. t

...

and find which gives a straight line.

b) Half-life method: measure $t_{1/2}$ vs. $[A]_0$

$$1^{\text{st}} \text{ order} \rightarrow t_{1/2} \propto [A]_0^0$$

$$2^{\text{nd}} \text{ order} \rightarrow t_{1/2} \propto [A]_0^{-1}$$

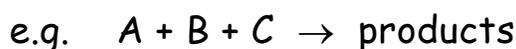
etc....

c) Multiple lifetimes ($t_{3/4}$ and $t_{1/2}$) (at $t_{3/4}$, $[A]=[A]_0/4$)

$$1^{\text{st}} \text{ order} \rightarrow t_{3/4} = (2\ln 2)/k \Rightarrow \frac{t_{3/4}}{t_{1/2}} = 2$$

$$2^{\text{nd}} \text{ order} \rightarrow t_{3/4} = 3/([A]_0 k) \Rightarrow \frac{t_{3/4}}{t_{1/2}} = 3$$

B) Reactions with more than one reactant:



a) Initial Rate Method

$$\text{For } [A]_0 \quad \left. \frac{\Delta[A]}{\Delta t} \right|_{t=0} = R_0 \approx k[A]_0^\alpha [B]_0^\beta [C]_0^\gamma$$

$$\text{For } [A]'_0 \quad \left. \frac{\Delta[A]'}{\Delta t} \right|_{t=0} = R'_0 \approx k[A]'_0^\alpha [B]_0^\beta [C]_0^\gamma$$

$$\text{Experimentally determine } \frac{R_0}{R'_0} = \left(\frac{[A]_0}{[A]'_0} \right)^\alpha$$

$$\text{If } 2[A]'_0 = [A]_0 \text{ then, if } \frac{R_0}{R'_0} = 1 \Rightarrow \alpha = 1$$

$$\text{if } \frac{R_0}{R'_0} = \sqrt{2} \Rightarrow \alpha = 1/2$$

$$\text{if } \frac{R_0}{R'_0} = 2 \Rightarrow \alpha = 1$$

$$\text{if } \frac{R_0}{R'_0} = 4 \Rightarrow \alpha = 2$$

etc...

b) Flooding or Isolation (goal is to try to make problem look like a one-reactant system)

take $[A]_0 \ll [B]_0, [C]_0$

e.g. flood system with B and C

Then $[B] \sim [B]_0$ and $[C] \sim [C]_0$

$$\text{So that } -\frac{d[A]}{dt} \approx k'[A]^\alpha$$

$$\text{Where } k' = k[B]_0^\beta [C]_0^\gamma$$

The reaction then becomes pseudo α -order with one reactant.