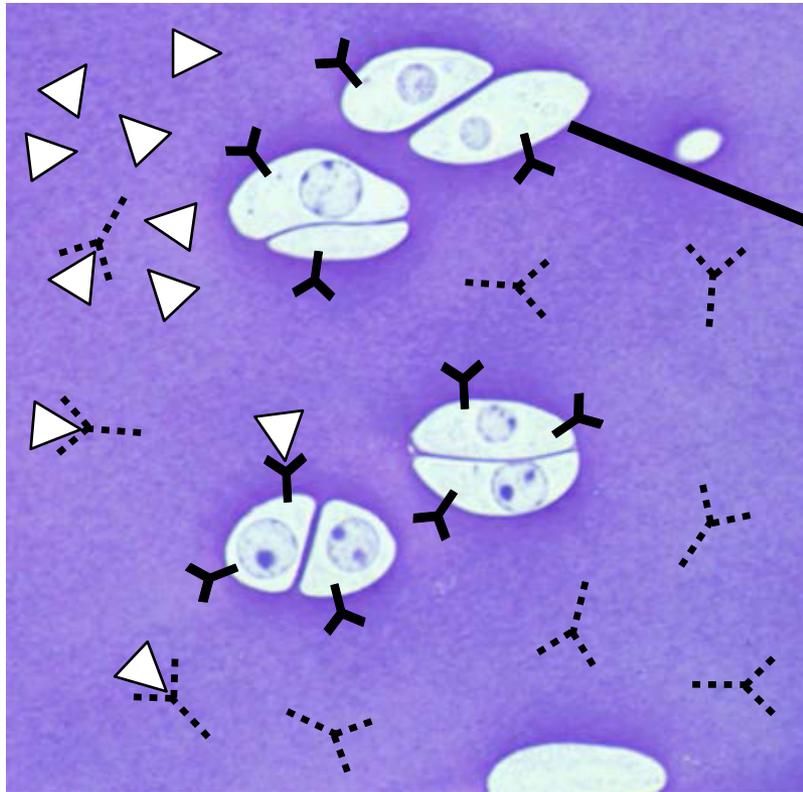
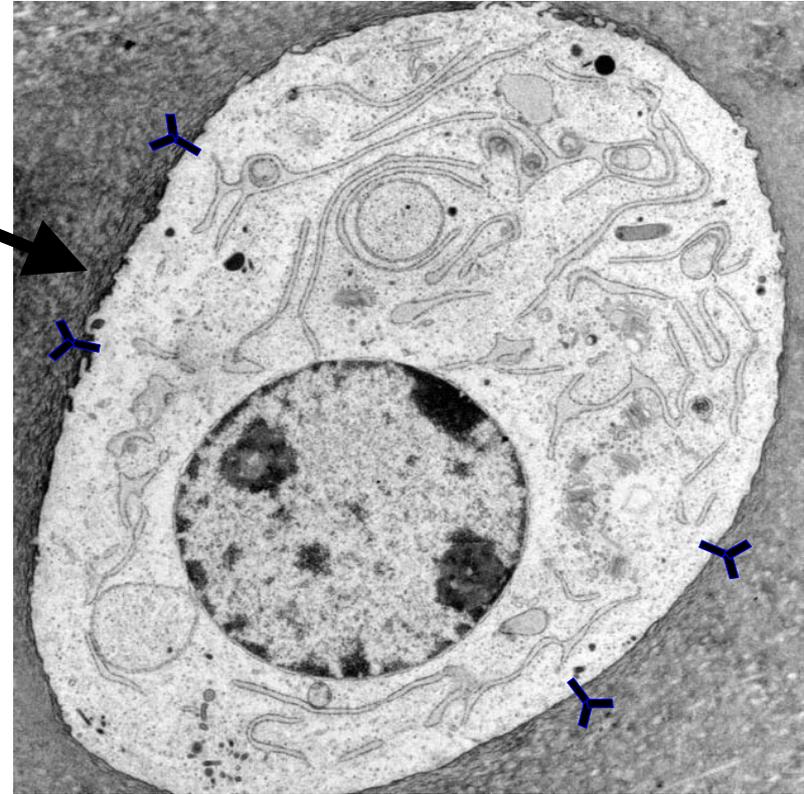


# IGF-1 Transport: stimulate anabolic response

(1) Through dense **tissue Extracellular Matrix (ECM)** of **collagens, proteoglycans, glycoproteins... to cell**



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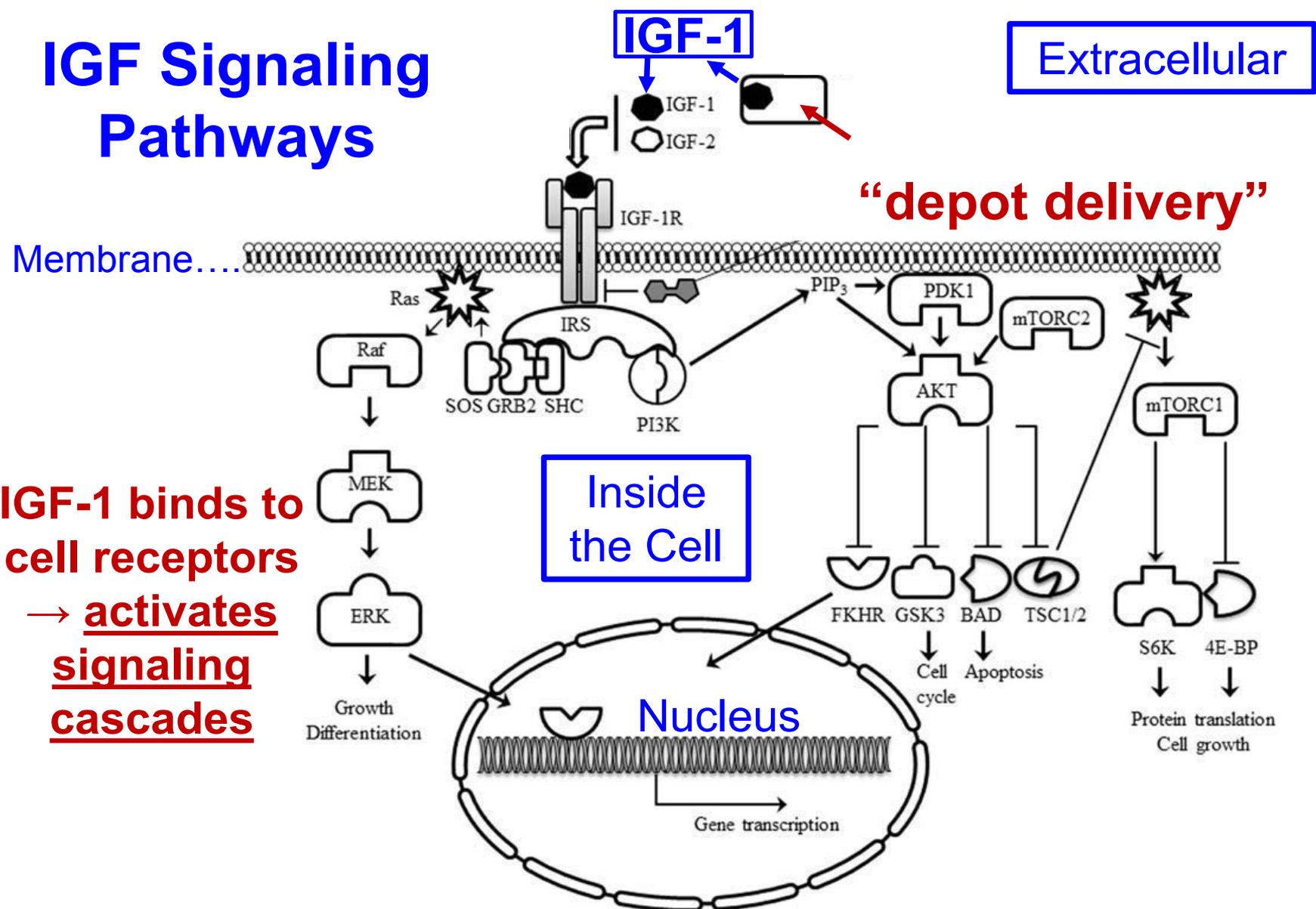


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(2) **Binding Sites:**

- **Cell surface receptors (10,000 / cell!)**
- **IGF binding proteins**

# IGF Signaling Pathways

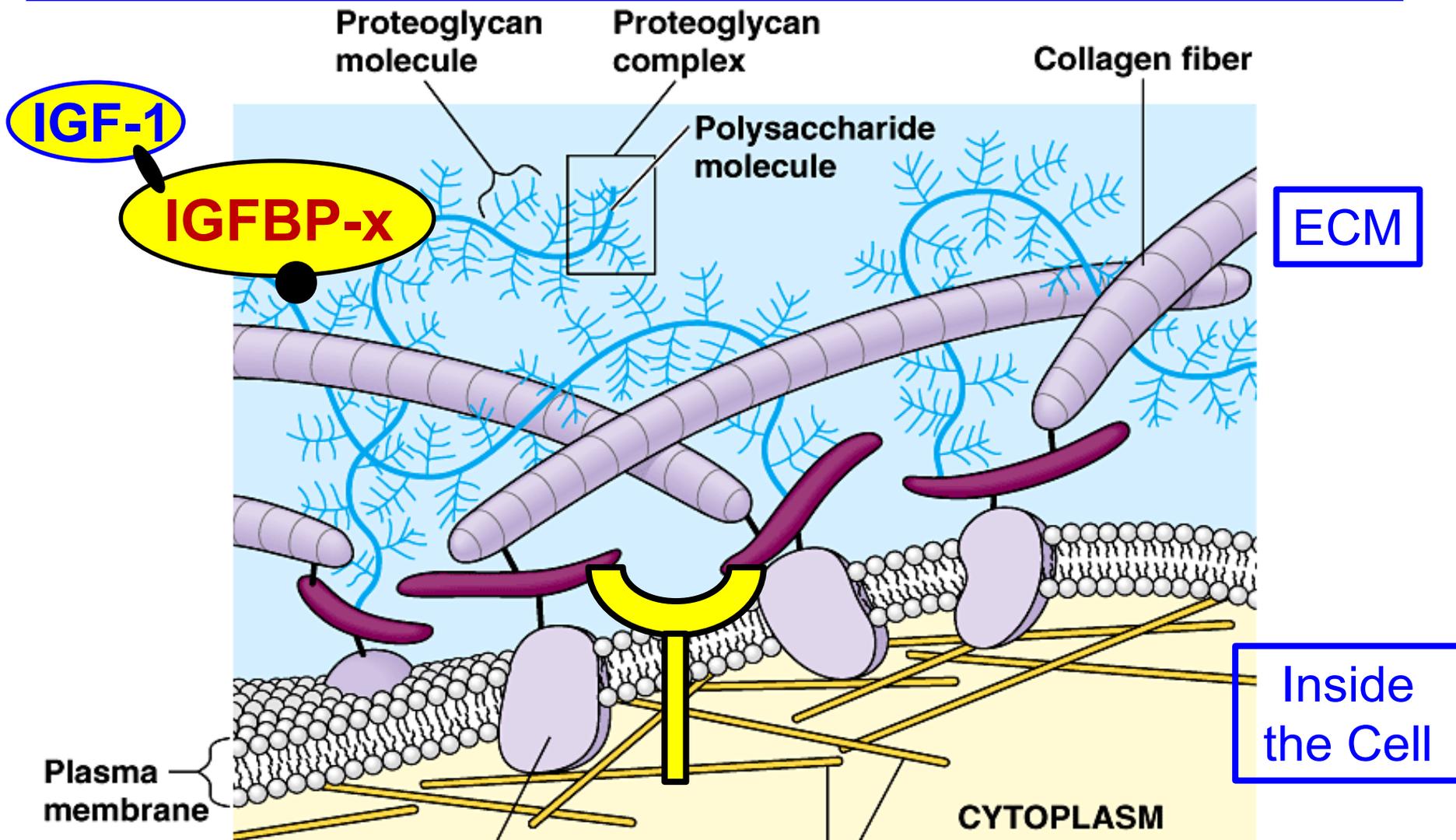


**IGF-1 binds to cell receptors → activates signaling cascades**

**→ stimulates transcription, protein translation, cell cycle progression, cell proliferation and growth, and inhibition of apoptosis.**

Courtesy of Alexandre Arcaro. License: CC BY.  
 Source: Arcaro, Alexandre. "Targeting the insulin-like growth factor-1 receptor in human cancer." Front Pharmacol 4, no. 30.10 (2013): 3389.

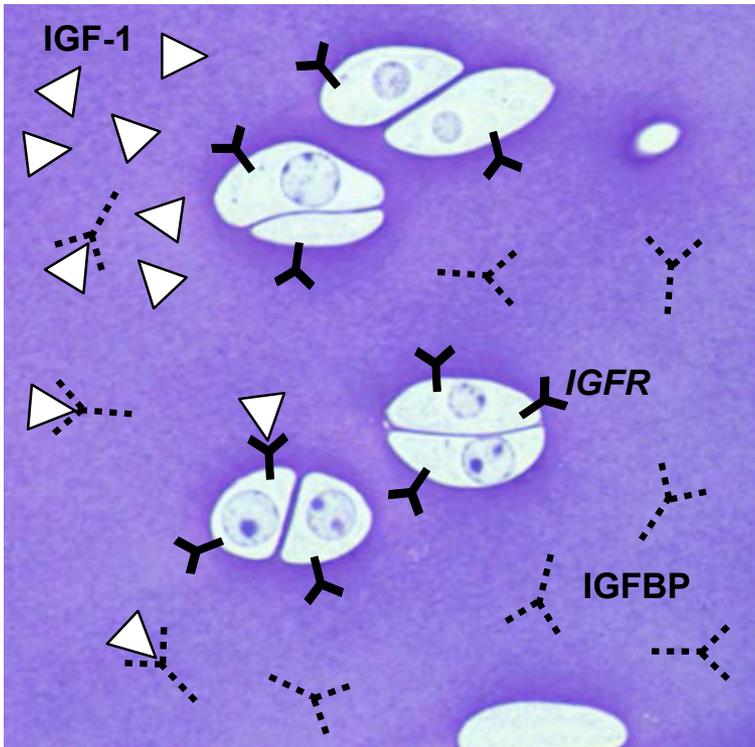
# Can IGFBPs bind to ECM macromolecules and inhibit IGF-1 transport, uptake, & cell signaling



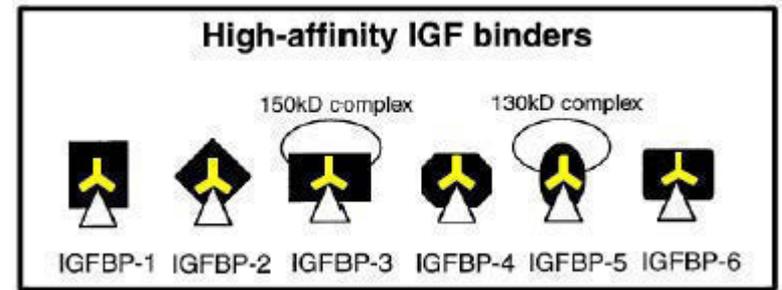
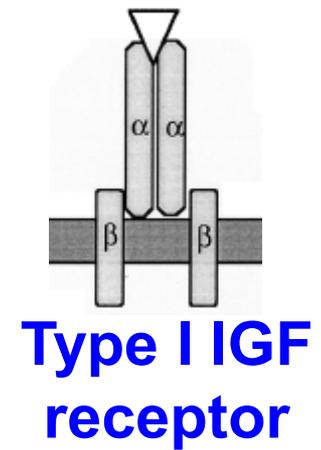
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**Implications for Drug Delivery: Dose and Timing**

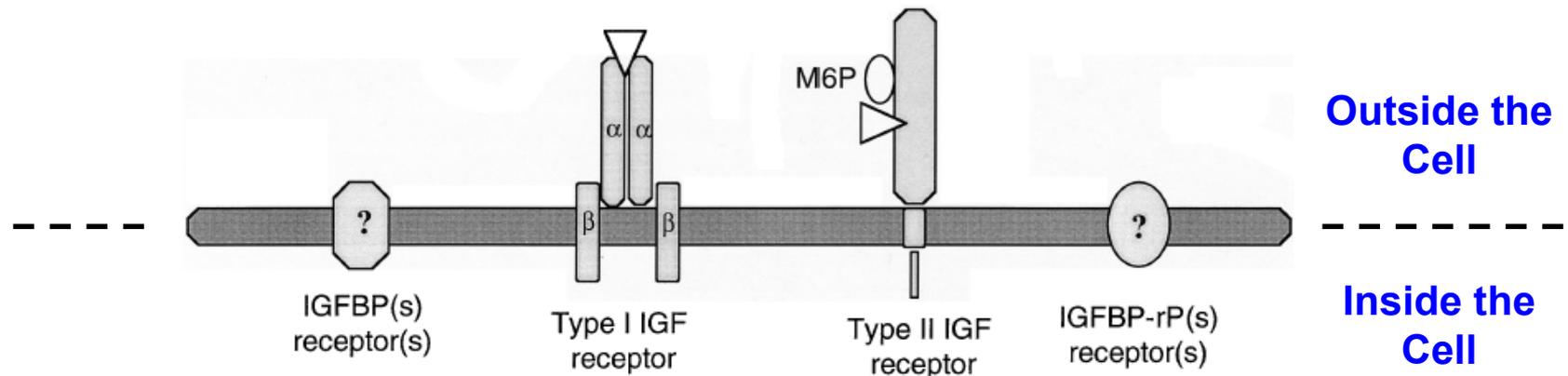
# IGF-1 System



△  
IGF-I/II

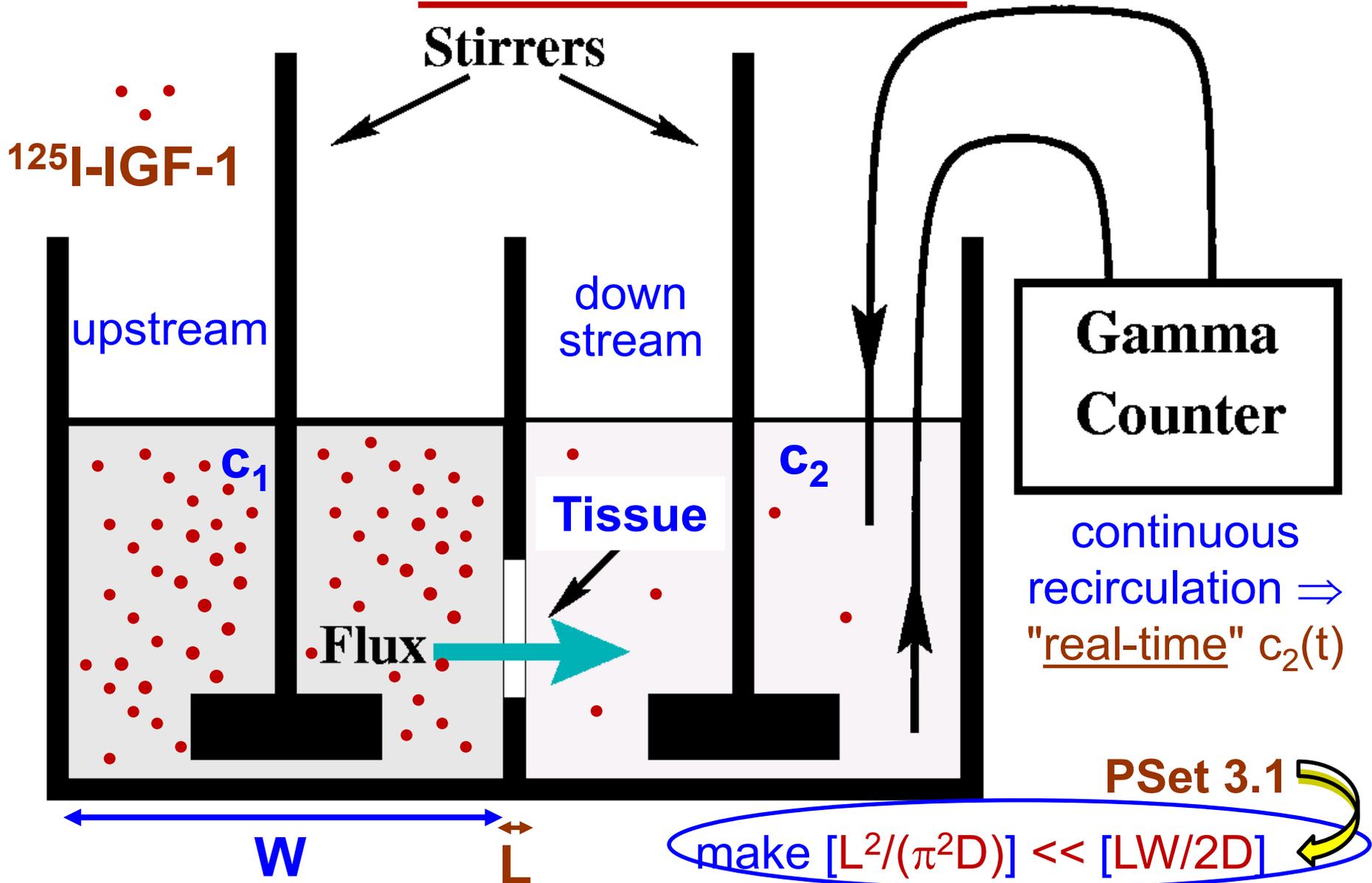


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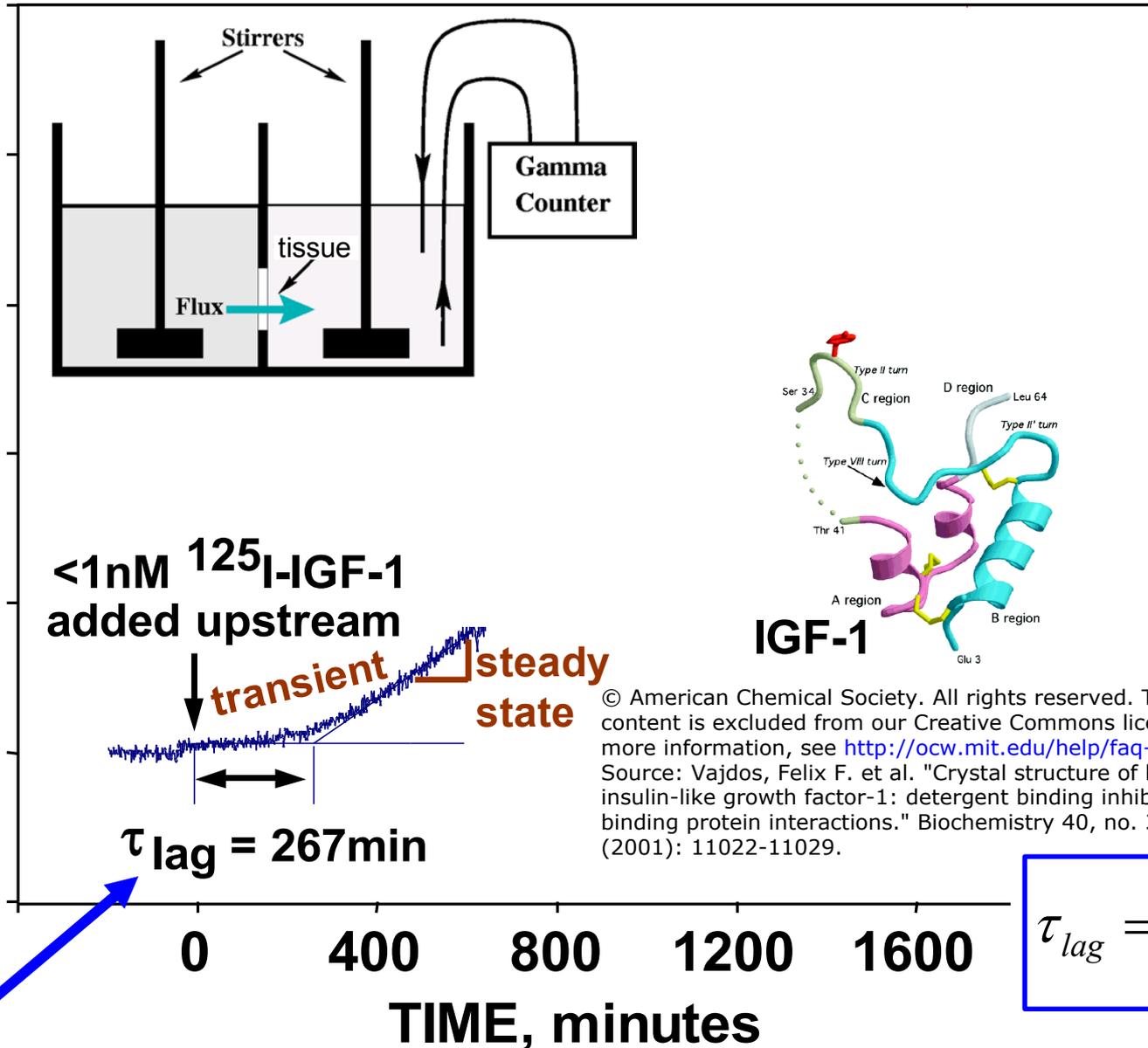
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# Transport & Binding within Native Tissue Microenvironment



# IGFBP-3 Binding Slows entry of IGF-1 into Tissue!

DOWNSTREAM / UPSTREAM RATIO, %



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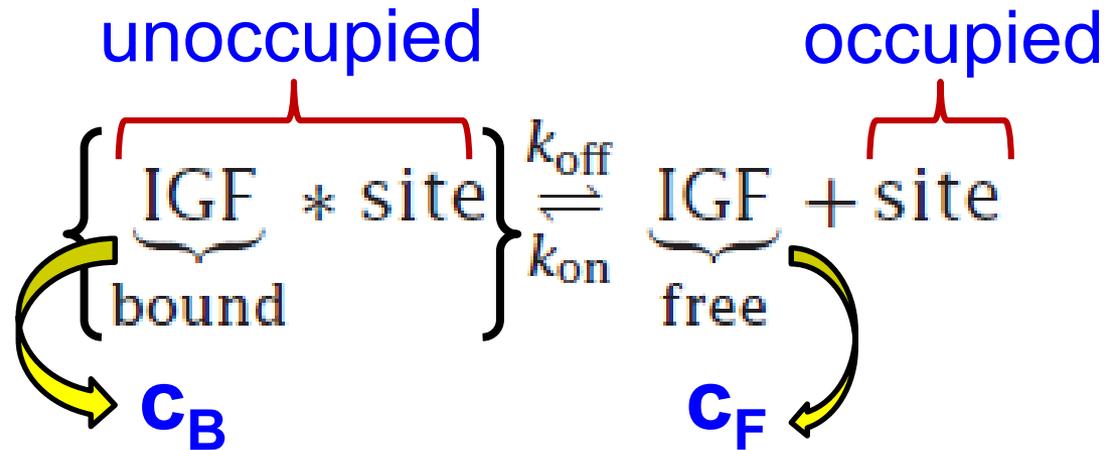
$$\tau_{lag} = \frac{L^2}{6D_{eff}}$$

slow reaction, or slow diffusion compared to reaction???

## Last Time:

Reaction

(1)



Rate Eqn

(2)

$$\frac{\partial C_B}{\partial t} = \left[ k_{on} C_F [\text{sites}] - k_{off} C_B \right]$$

binding site density "n"  
(definition)

(3)

$$n = \underbrace{[ \text{IGF} * \text{site} ]}_{\text{occupied}} + \underbrace{[ \text{site} ]}_{\text{unoccupied}}$$

Binding  
"Isotherm"

(4)

$$C_B = \frac{n C_F}{K_d + C_F}$$

**IGF-1**

**Diffusion  
thru ECM**

**Multiple Reactions in ECM**

$$\frac{\partial c_1^f}{\partial t} = D_{IGF} \nabla^2 c_1^f - k_{+11} c_1^f c_{BP1}^f + k_{-11} c_{SC11}^f +$$

$$k_{-1BP} c_{SC11}^f - k_{+11RC} c_1^f c_{IR} + k_{-11RC} c_{IR1}$$

$$- k_{+13RC} c_1^f c_R + k_{-13RC} c_{R1} - k_{-1IGF} c_1^f$$
(1)

(Coupled PDEs)  
( $\mathbf{x}, t$ )

**IGFBPs**

$$\frac{\partial c_2^f}{\partial t} = D_{IGF} \nabla^2 c_2^f - k_{+21} c_2^f c_{BP1}^f + k_{-21} c_{SC21}^f + k_{-1BP} c_{SC21}^f$$

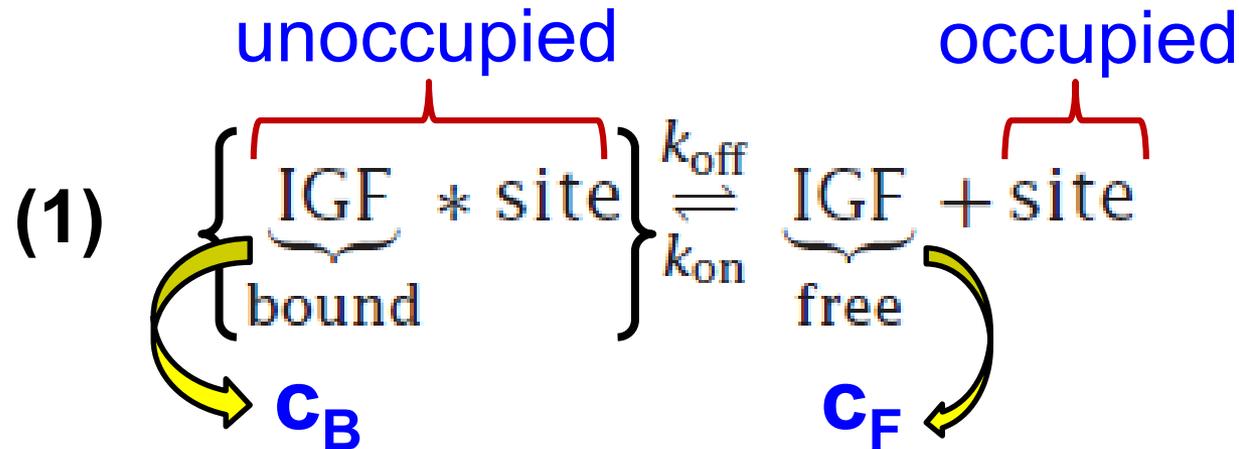
$$- k_{+22} c_2^f c_{BP2}^f + k_{-22} c_{SC22}^f + k_{-2BP} c_{SC22}^f$$

$$- k_{+21RC} c_2^f c_{IR} + k_{-21RC} c_{IR2} -$$

$$k_{+22RC} c_2^f c_{IIR} + k_{-22RC} c_{IIR2} - k_{-1IGF} c_2^f$$
(2)

## Last Time:

### Reaction



### Rate Eqn

(2) 
$$\frac{\partial C_B}{\partial t} = \left[ k_{on} C_F [\text{sites}] - k_{off} C_B \right] = 0 \text{ in equilibrium}$$

binding site density "n"  
(definition)

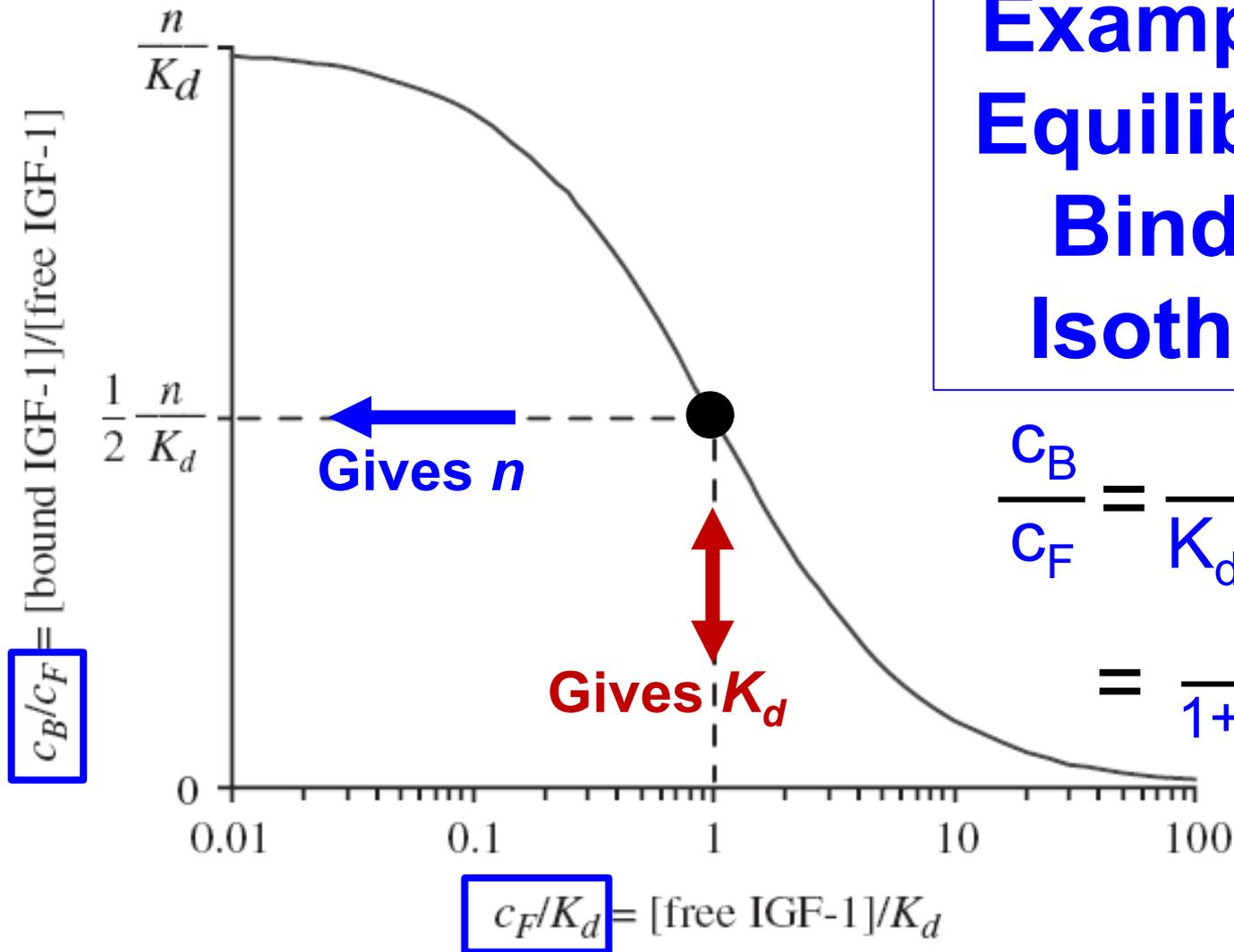
(3) 
$$n = \underbrace{[\text{IGF * site}]}_{\text{occupied}} + \underbrace{[\text{site}]}_{\text{unoccupied}}$$

### Binding "Isotherm"

(4)

$$C_B = \frac{n C_F}{K_d + C_F}$$

# Example of Equilibrium Binding Isotherm

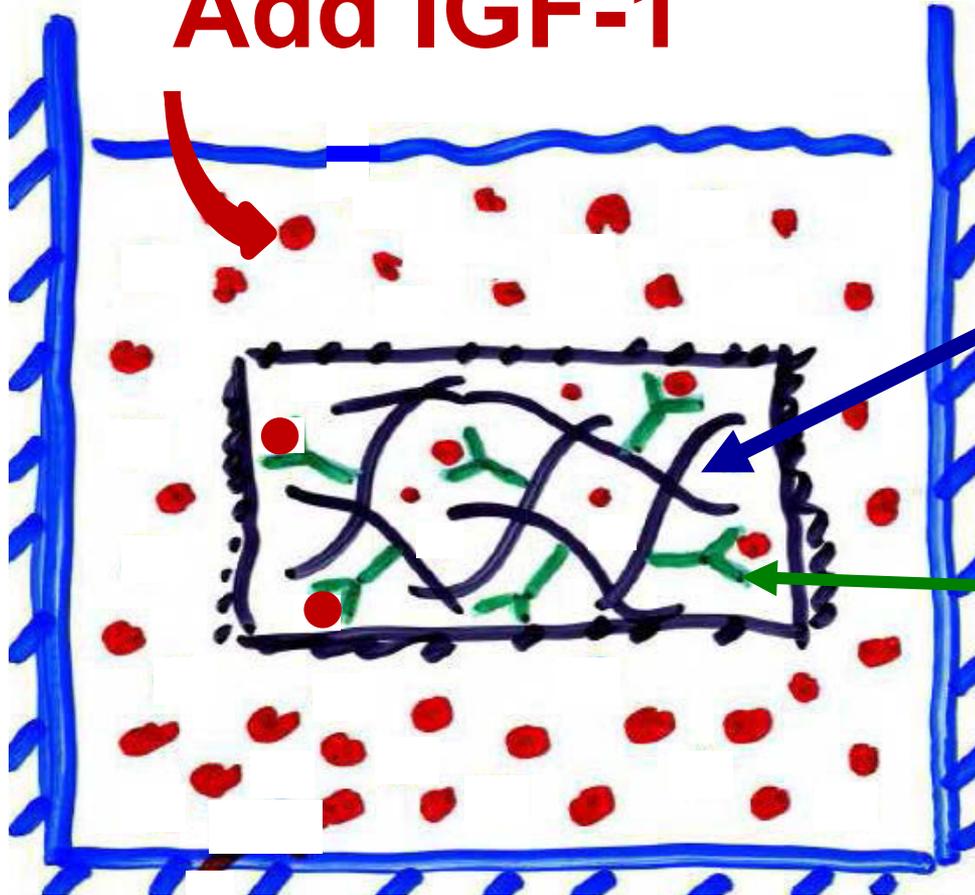


$$\frac{c_B}{c_F} = \frac{n}{K_d + c_F} = \frac{n/K_d}{1 + c_F/K_d}$$

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**(Bound IGF-1 / Free IGF-1) versus free IGF normalized to  $K_d$**

**Add IGF-1**

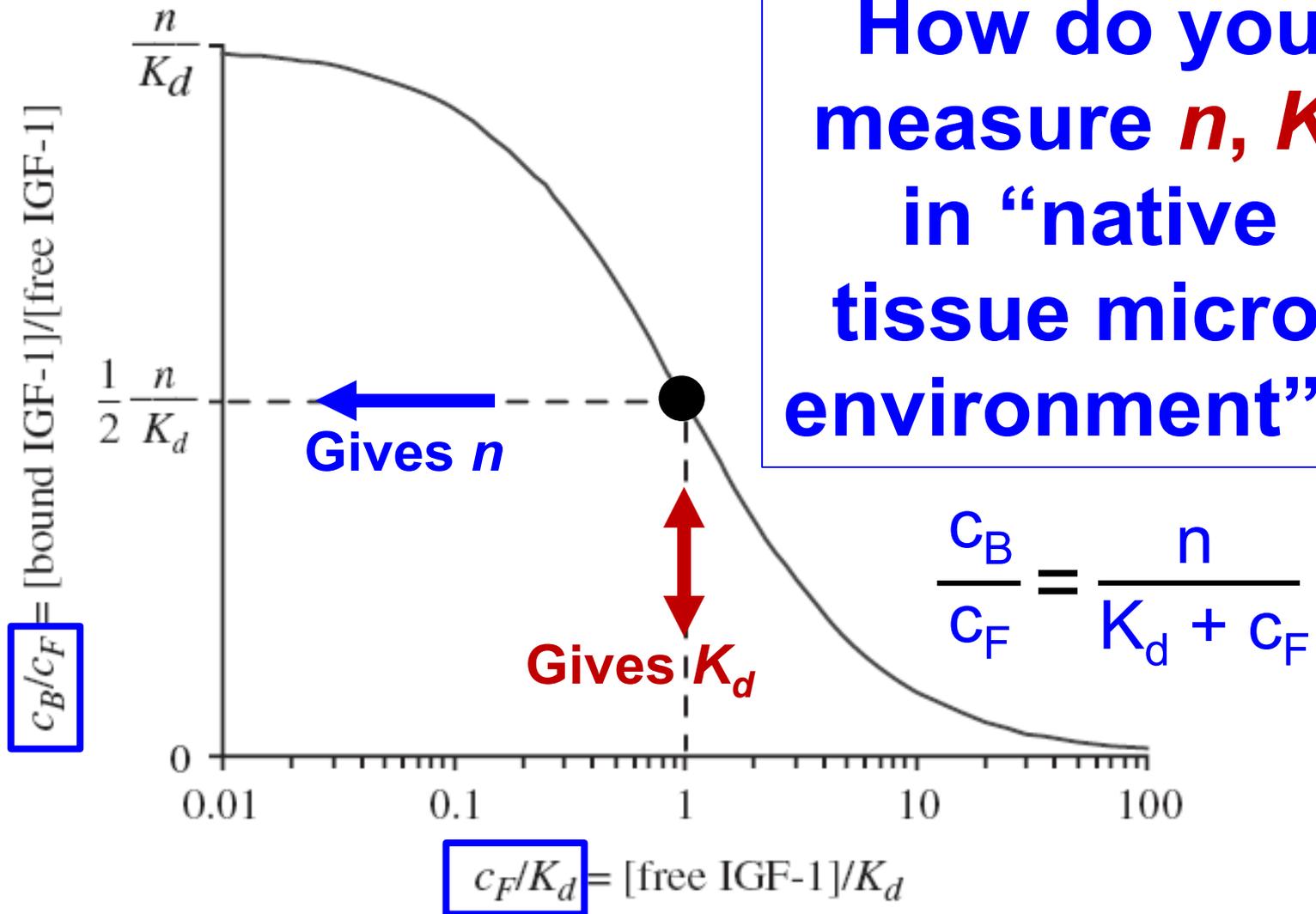


**Tissue** in medium at equilibrium  
(PBS or DMEM...)

IGFBP-''x''

Assuming:  
 $[IGFBP-x] \gg [IGF-R]$

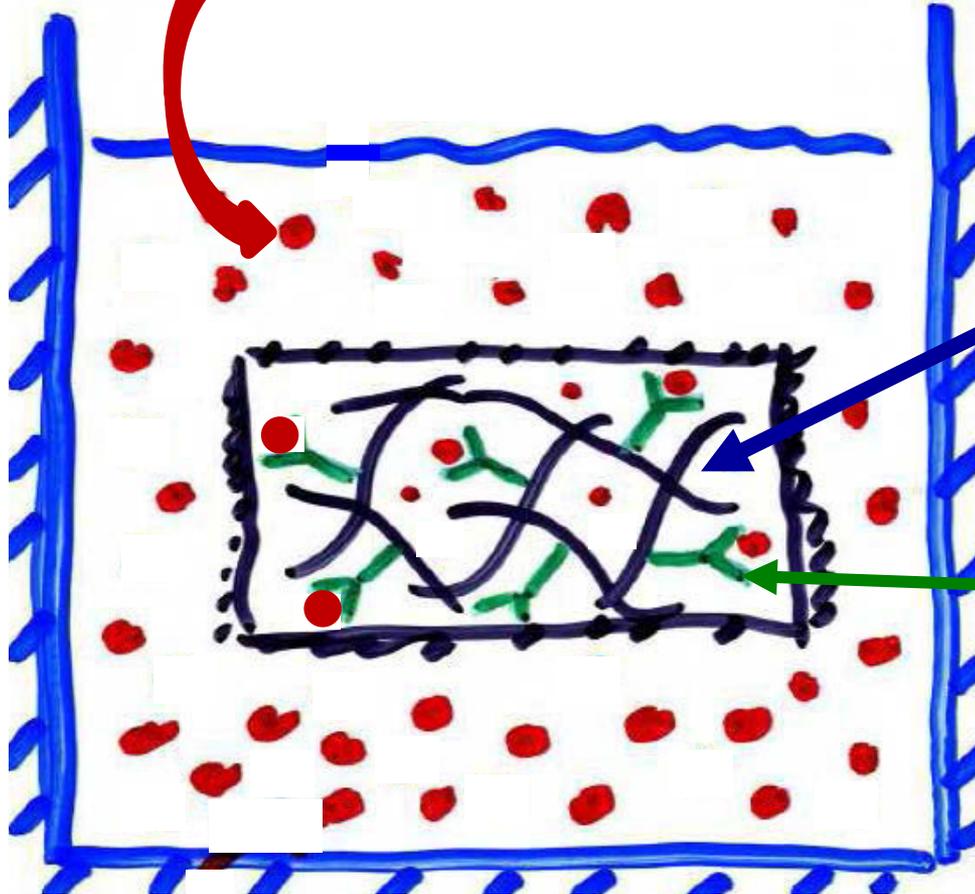
How do you measure  $n$ ,  $K_d$  in “native tissue micro-environment” ?



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**(Bound IGF-1 / Free IGF-1) versus free IGF normalized to  $K_d$**

First add  $^{125}\text{I}$ -IGF-1 ( $< 0.1 \text{ nM}$ )

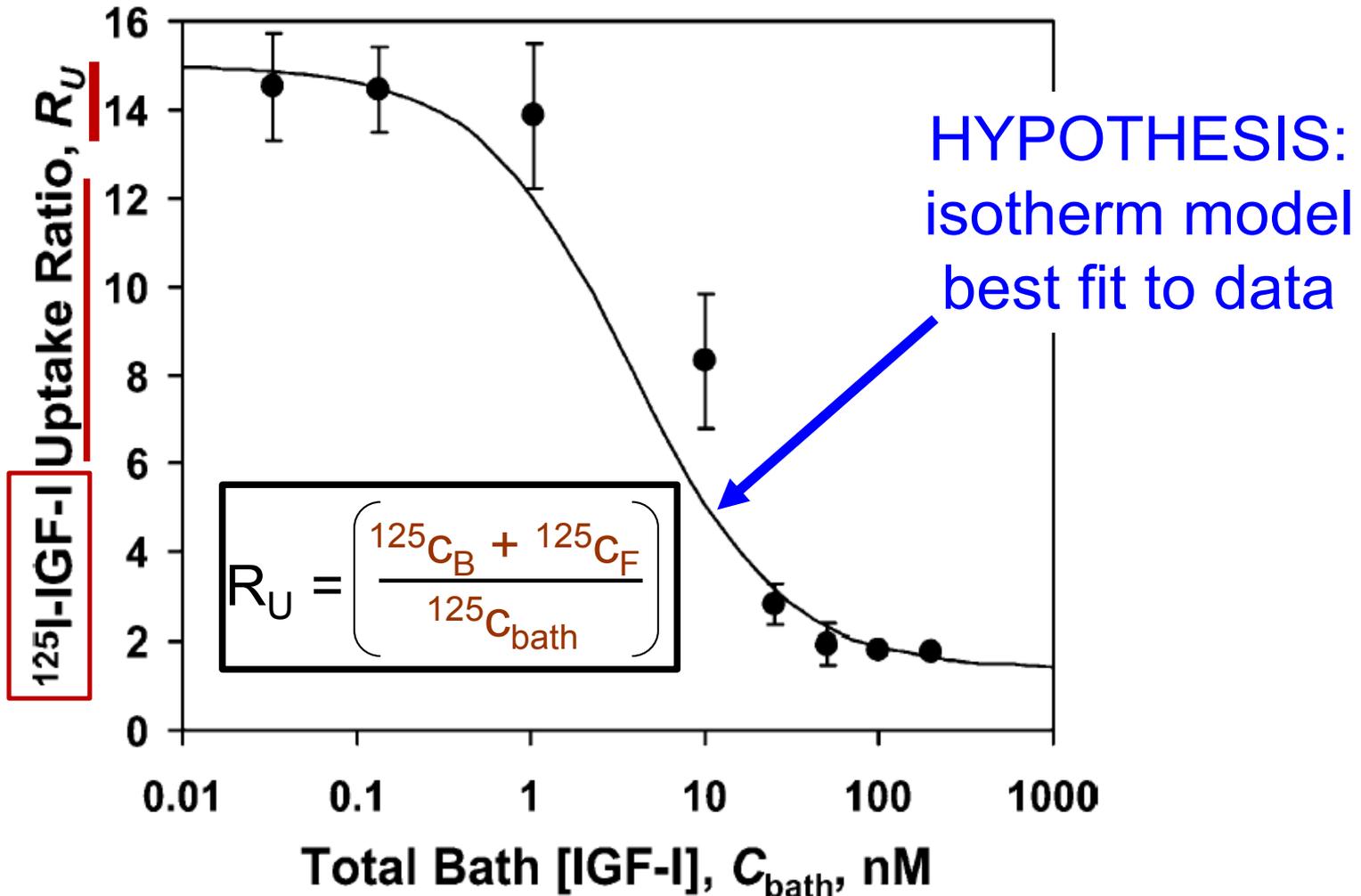


Tissue in medium at equilibrium  
(PBS or DMEM...)

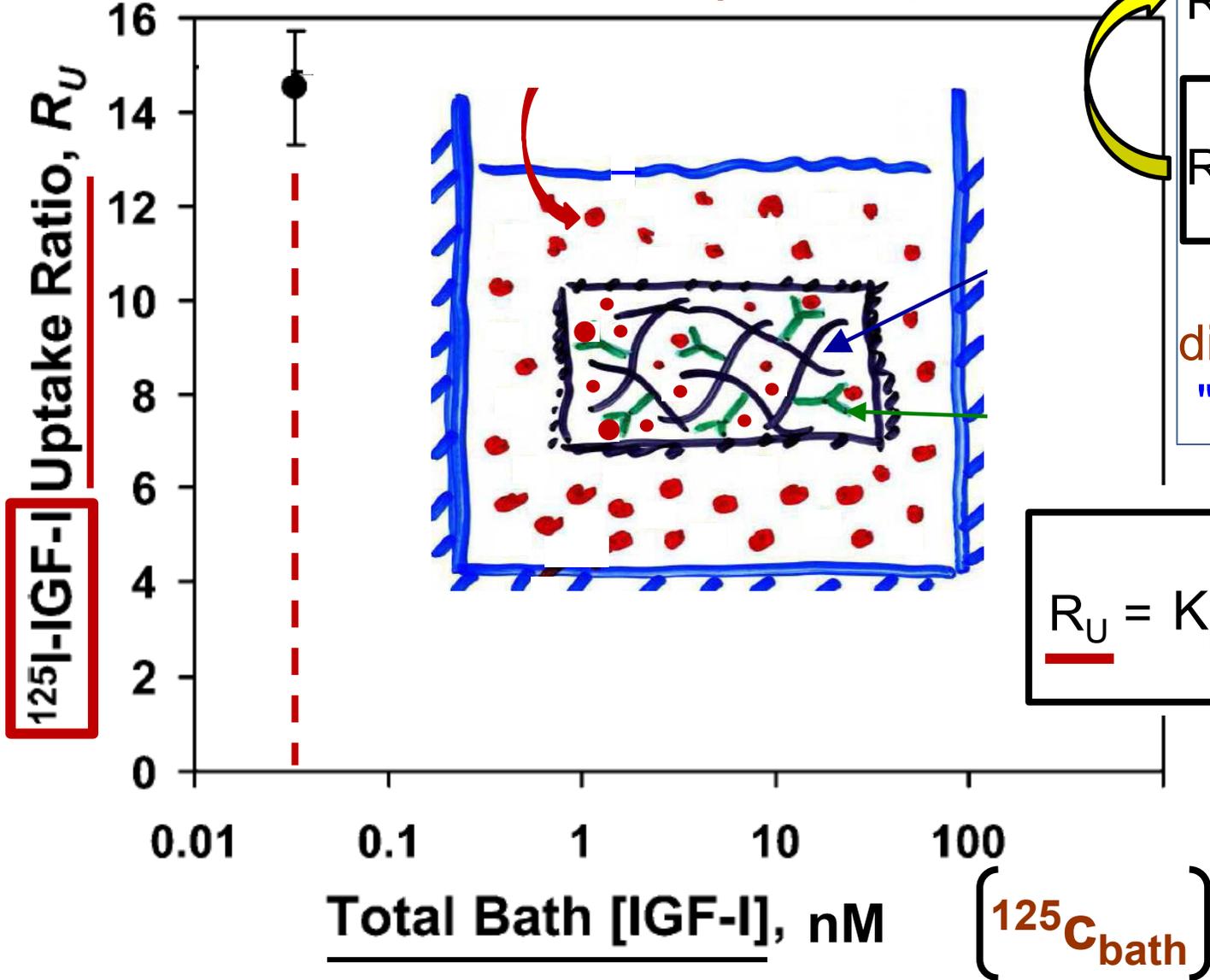
IGFBP-"x"

Assuming:  
[IGFBP-x]  $\gg$  [IGF-R]

# Competitive Binding Experiment to Measure Equilibrium Binding Isotherm



1st addition (hot):  
 $^{125}\text{I}$ -IGF-1 (< 0.1 nM)



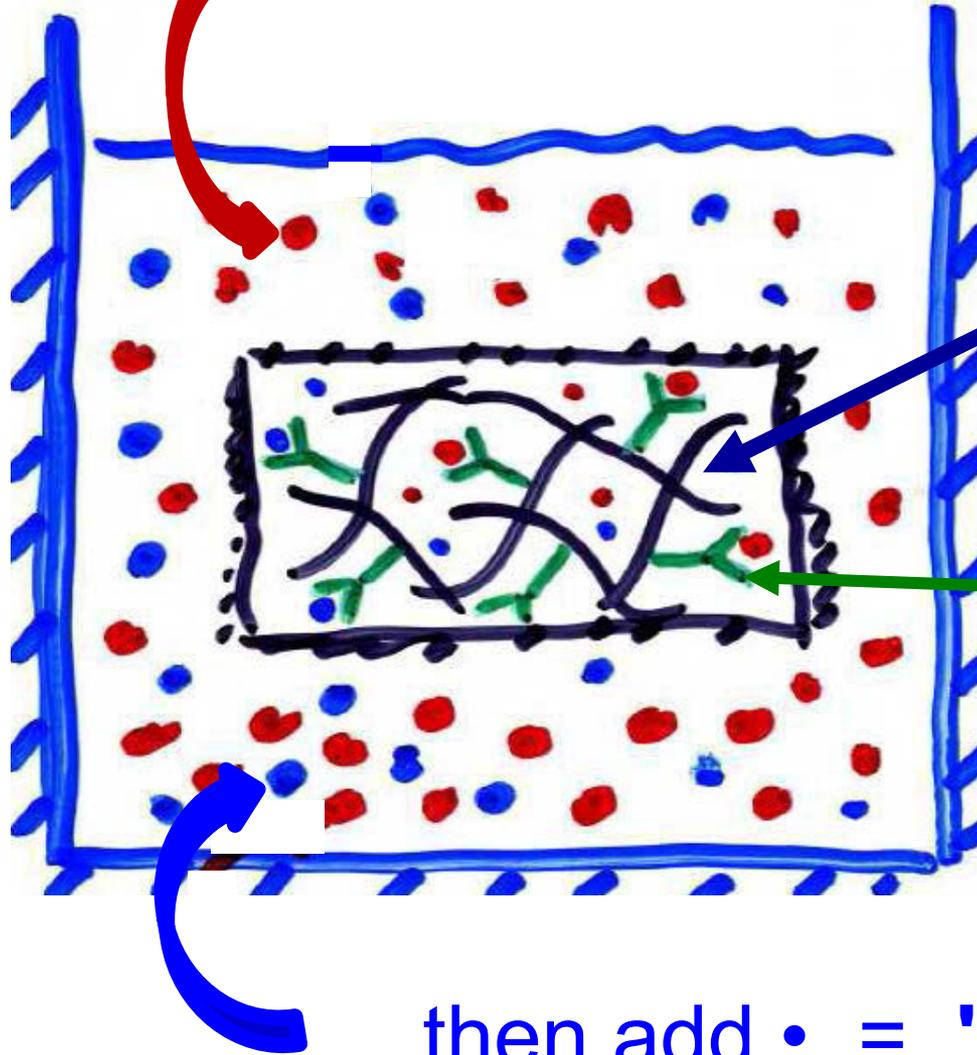
$$R_U = \left( \frac{C_B^{\text{tiss}} + C_F^{\text{tiss}}}{C_{\text{bath}}} \right)$$

$$R_U = \left( \frac{^{125}C_B + ^{125}C_F}{^{125}C_{\text{bath}}} \right)$$

since tracer  
distribution mimics  
"mother species"

$$R_U = K_{\text{part}} \left( 1 + \frac{n}{K_d + C_F} \right)$$

First add  $^{125}\text{I}$ -IGF-1 ( $< 0.1 \text{ nM}$ )

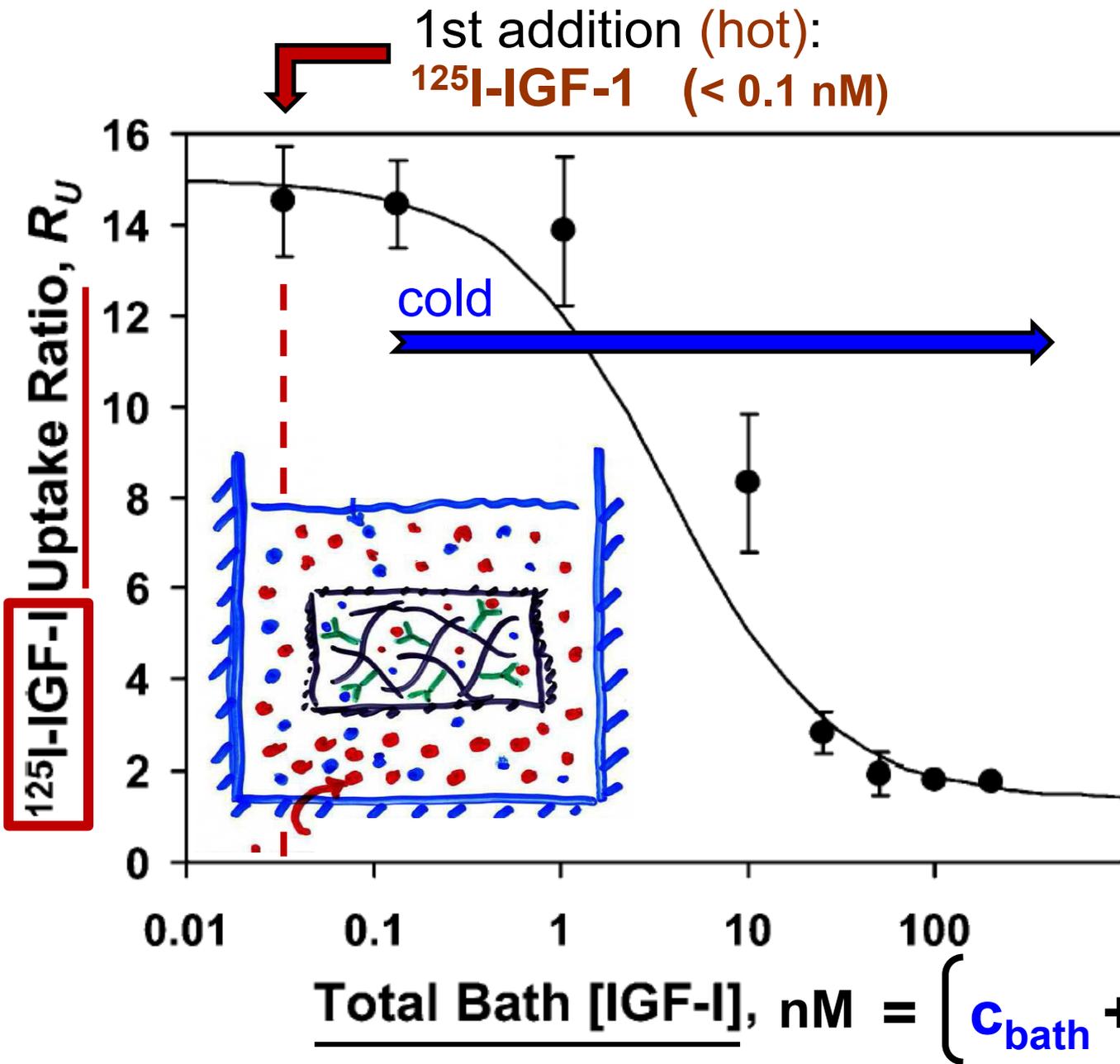


Tissue in medium at equilibrium (PBS; DMEM...)

IGFBP-"x"

Assuming:  
[IGFBP-x]  $\gg$  [IGF-R]

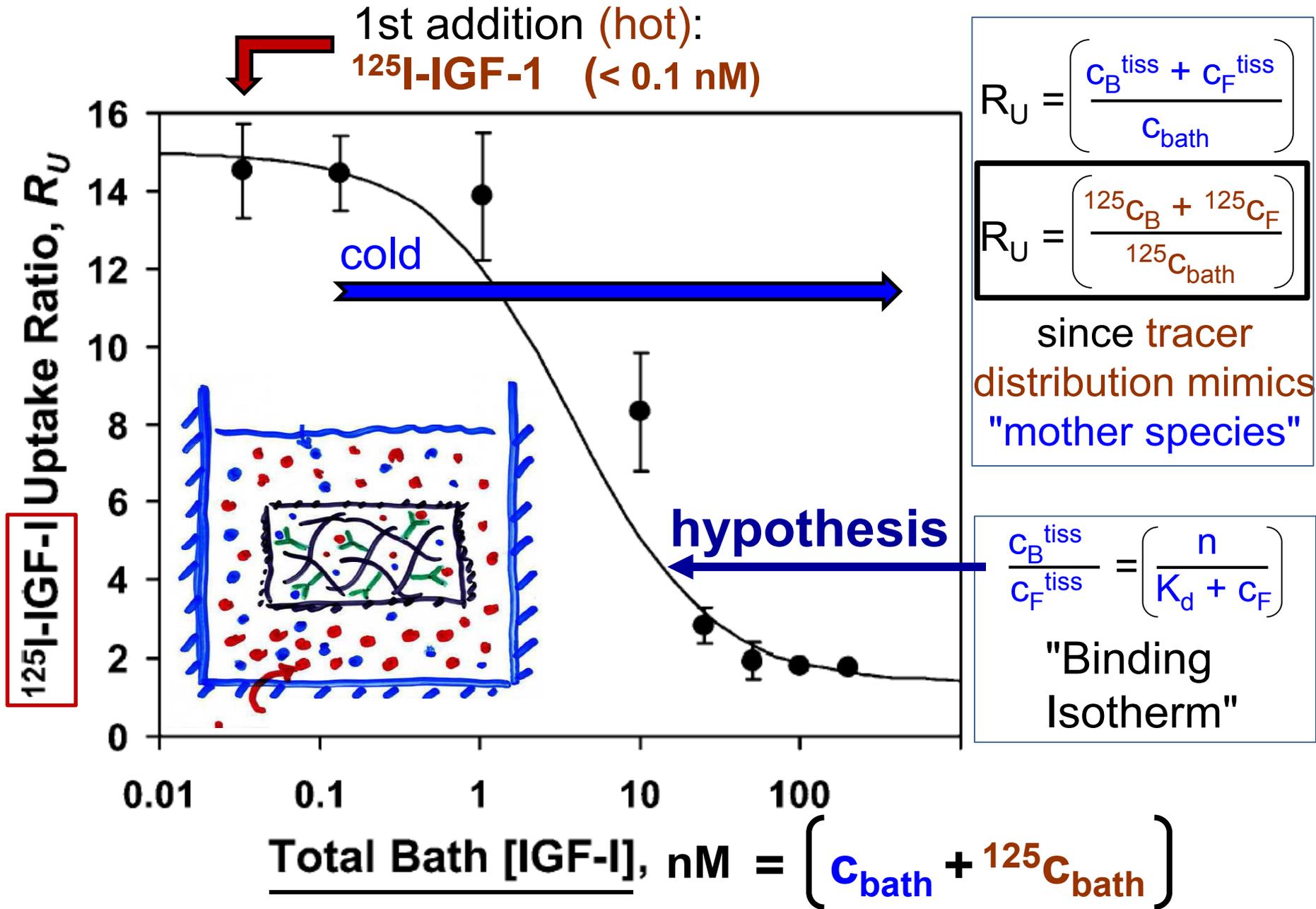
...then add  $\bullet$  = "cold" IGF-1



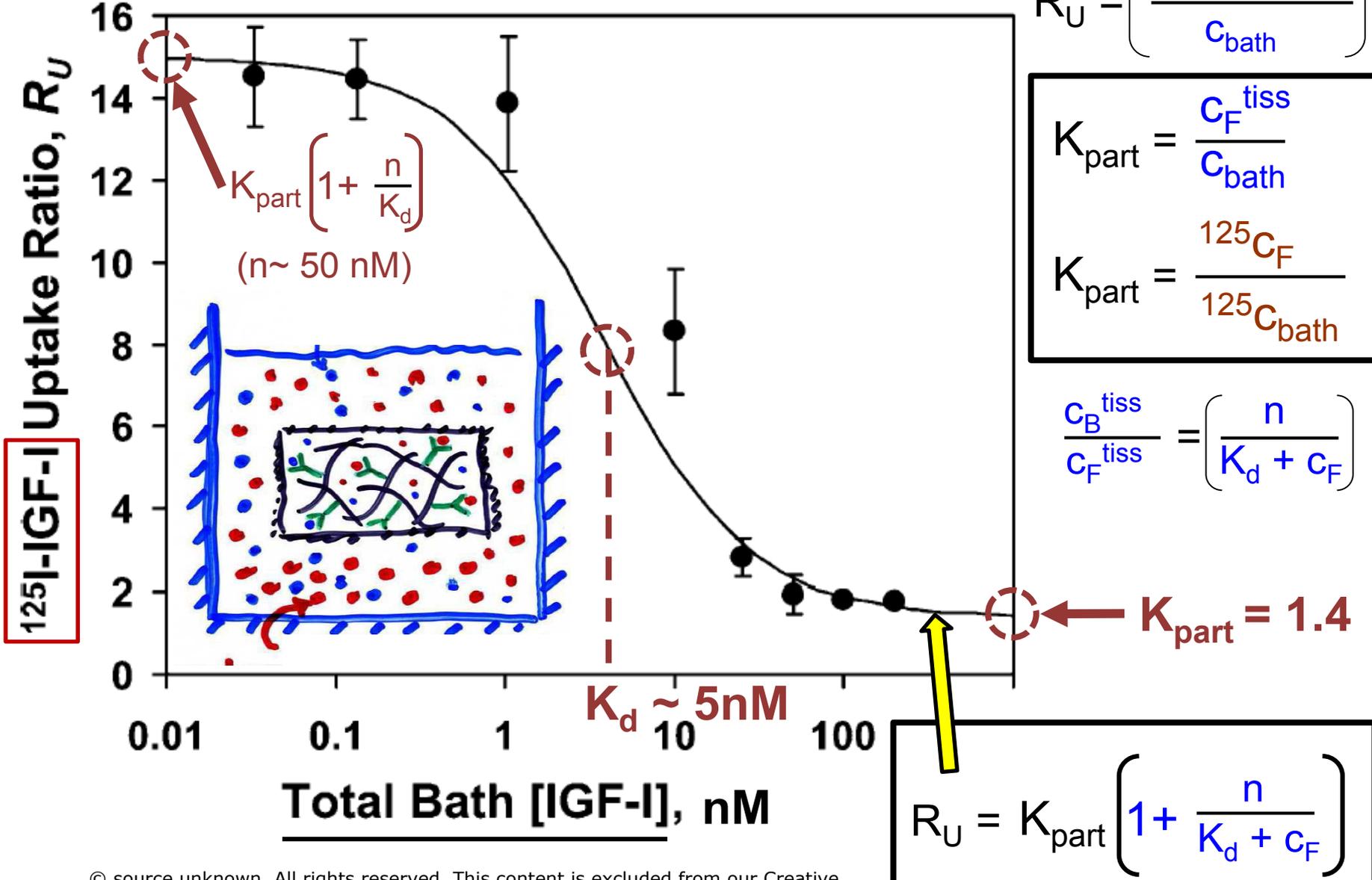
$$R_U = \left( \frac{C_B^{\text{tiss}} + C_F^{\text{tiss}}}{C_{\text{bath}}} \right)$$

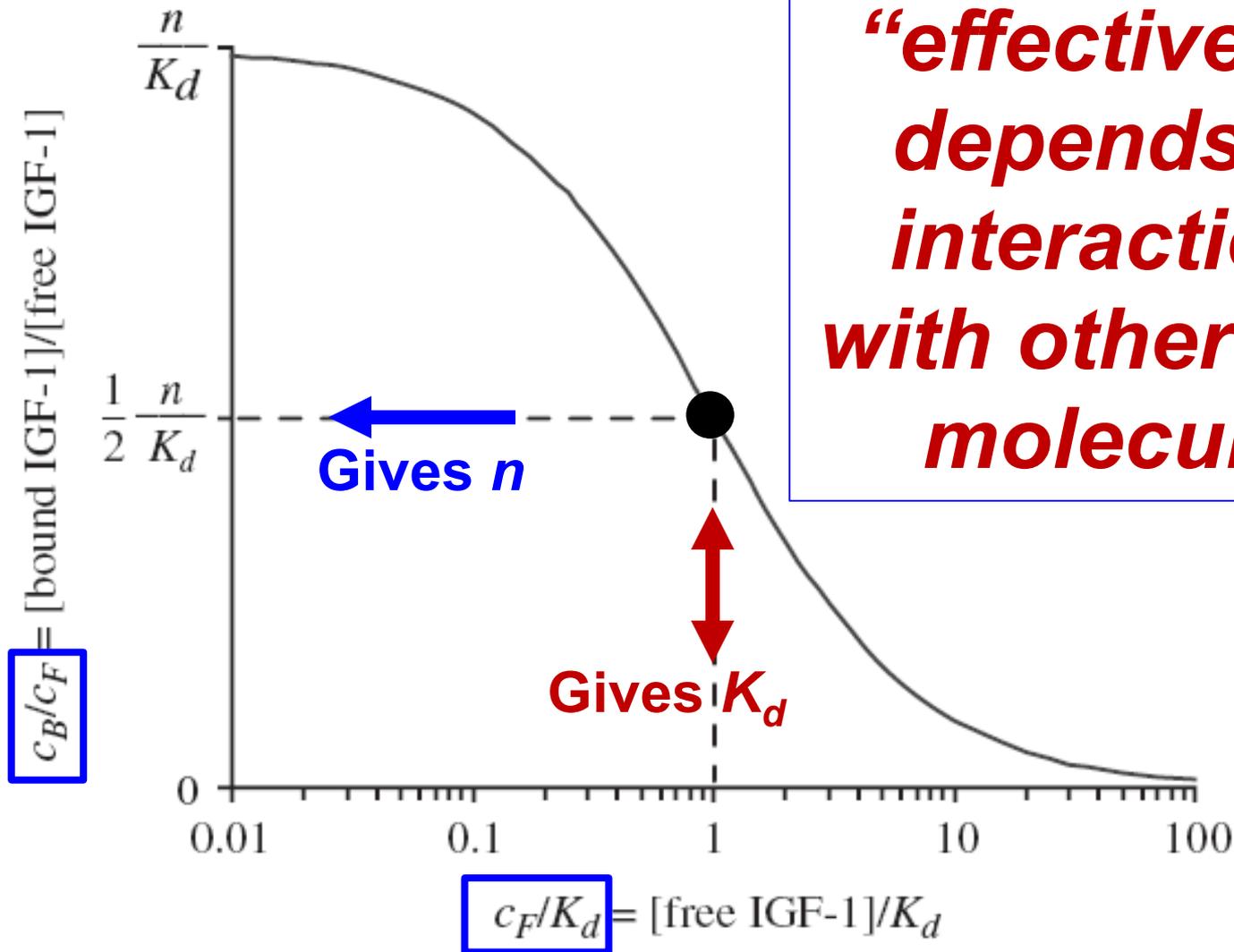
$$R_U = \left( \frac{{}^{125}C_B + {}^{125}C_F}{{}^{125}C_{\text{bath}}} \right)$$

since tracer distribution mimics "mother species"



# Equilibrium Binding



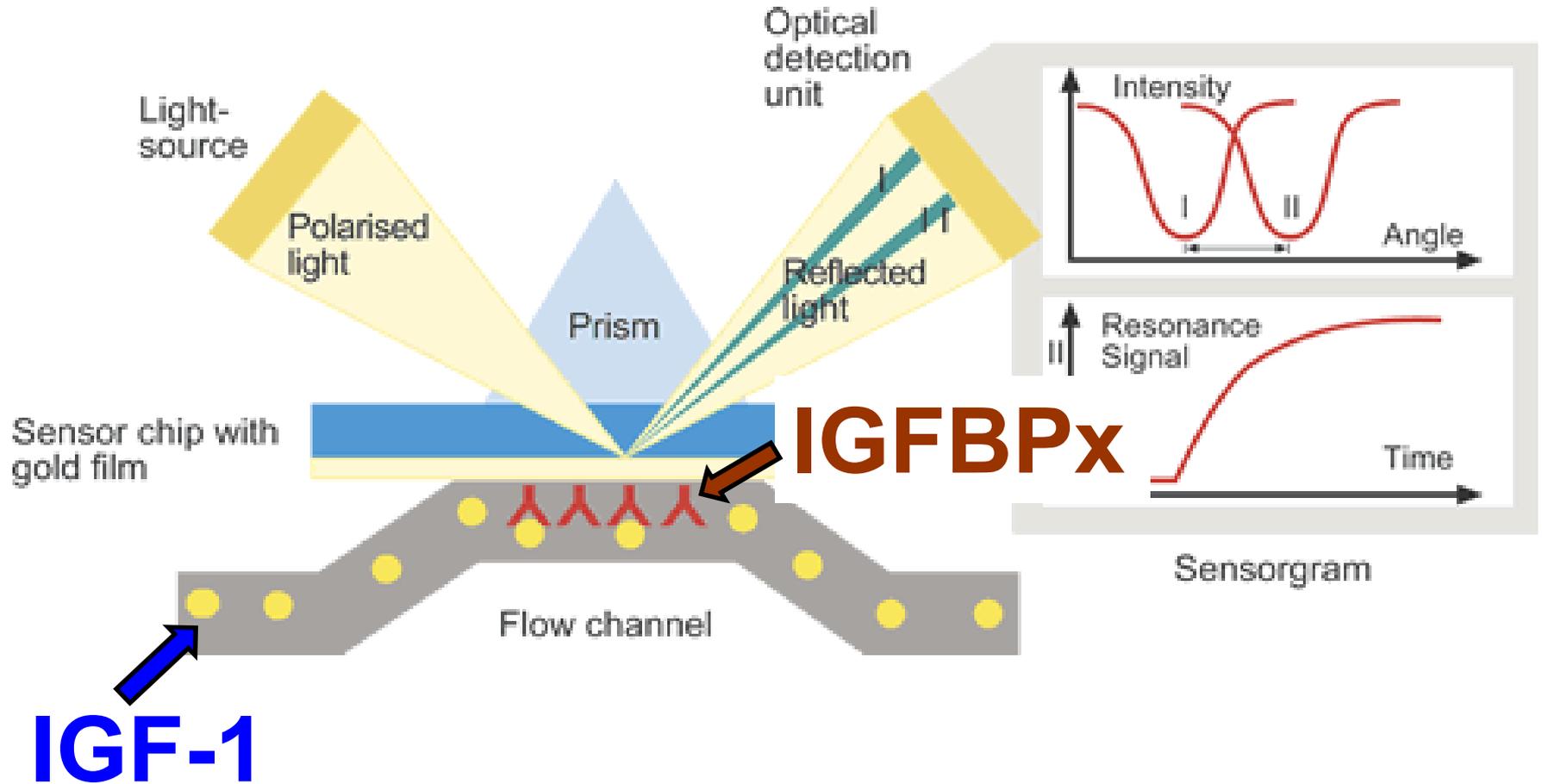


***“effective”  $K_d$  depends on interactions with other ECM molecules***

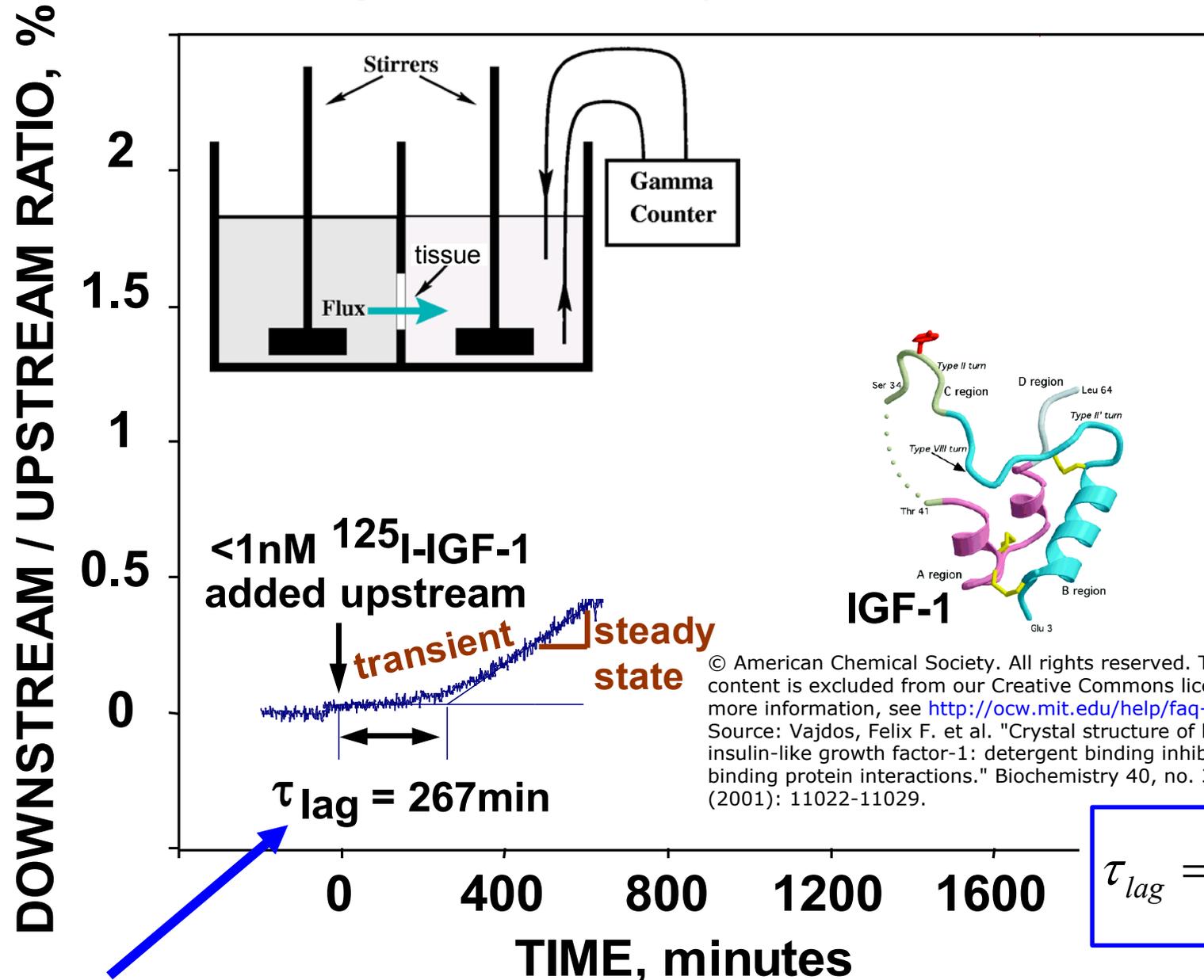
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**(Bound IGF-1 / Free IGF-1) versus free IGF normalized to  $K_d$**

# Surface Plasmon Resonance Instrument (“BiaCore”) to measure binding of ligand to specific target



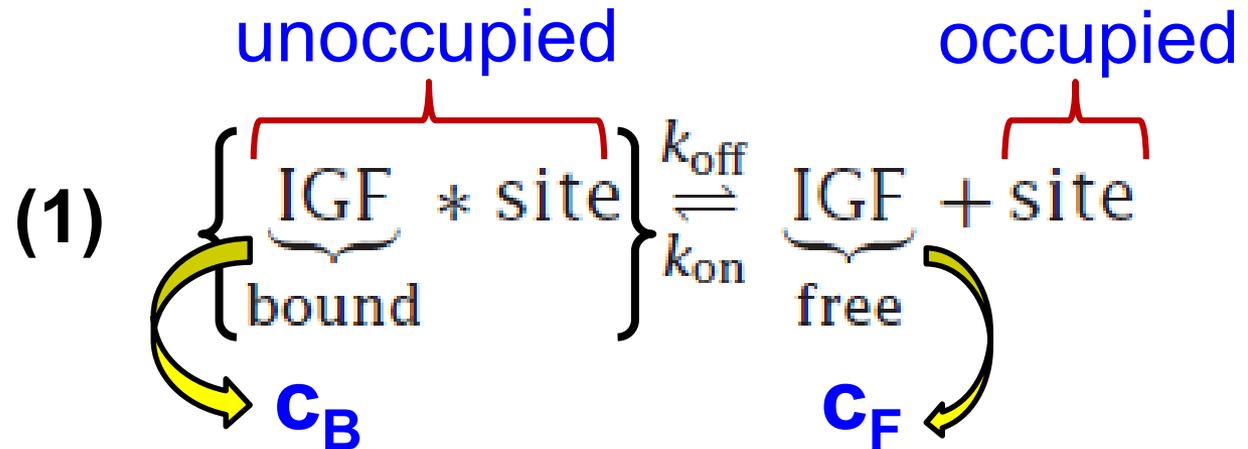
# IGFBP-3 Binding Slows entry of IGF-1 into Tissue!



slow reaction, or slow diffusion compared to reaction???

## Last Time:

### Reaction



### Rate Eqn

(2) 
$$\frac{\partial C_B}{\partial t} = \left[ k_{on} C_F [\text{sites}] - k_{off} C_B \right] = 0 \text{ in equilibrium}$$

binding site density "n"  
(definition)

(3) 
$$n = \underbrace{[IGF * site]}_{\text{occupied}} + \underbrace{[site]}_{\text{unoccupied}}$$

### Binding "Isotherm"

(4) 
$$C_B = \frac{n C_F}{K_d + C_F}$$

# HW Prob 3.1

The diffusion equation (1.65) then takes the form

$$\frac{\partial \bar{c}_F(x, t)}{\partial t} + \frac{\partial}{\partial t} \left( \frac{n \bar{c}_F(x, t)}{K_D + \bar{c}_F(x, t)} \right) = D_{\text{IGF}} \frac{\partial^2 \bar{c}_F}{\partial x^2} \quad (1.68)$$

By using the chain rule for differentiation, (1.68) can then be written as

$$\frac{\partial \bar{c}_F}{\partial t} \left( 1 + \frac{n K_d}{(K_d + \bar{c}_F)^2} \right) = D_{\text{IGF}} \frac{\partial^2 \bar{c}_F}{\partial x^2} \quad (1.69)$$

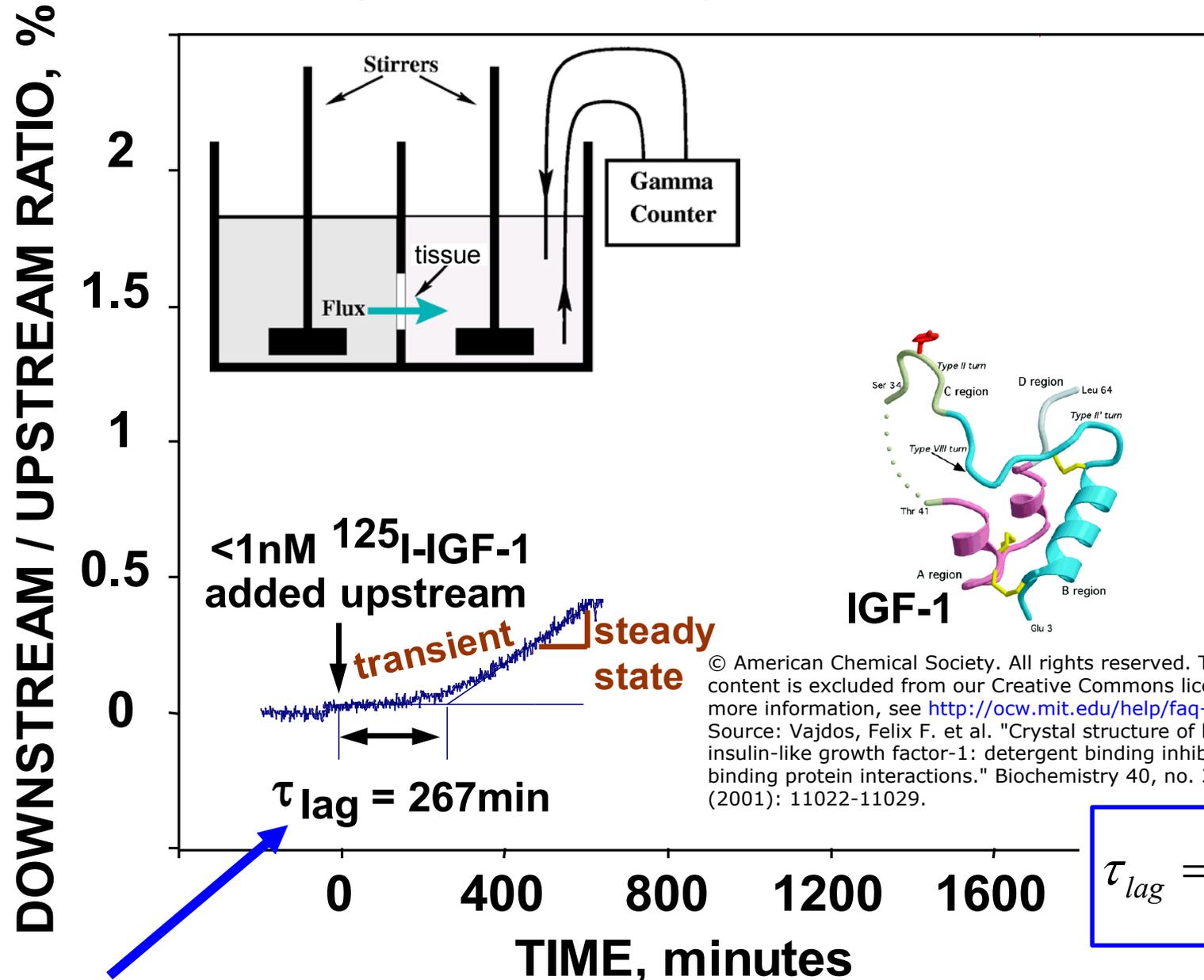
The diffusion–reaction equation (1.69) is nonlinear in  $c_F$ ; however, for small enough concentrations  $c_F \ll K_d$ , it can be written in the form

**Fast reaction,  
slow diffusion  
limit**

$$\frac{\partial \bar{c}_F}{\partial t} = D_{\text{eff}} \frac{\partial^2 \bar{c}_F}{\partial x^2} \quad (1.70)$$

$$D_{\text{eff}} = \frac{D_{\text{IGF}}}{1 + n/K_d} \quad (1.71)$$

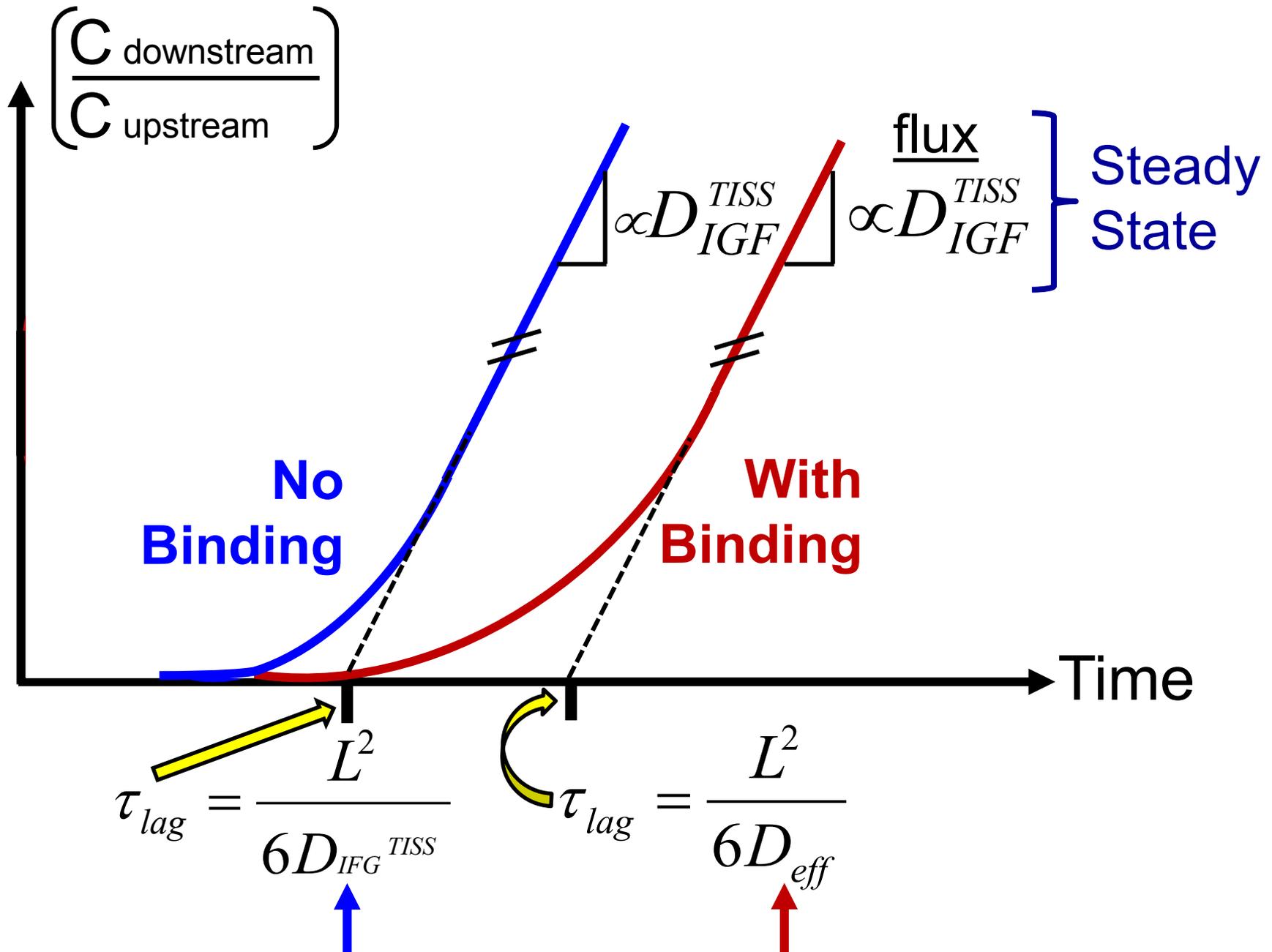
# IGFBP-3 Binding Slows entry of IGF-1 into Tissue!



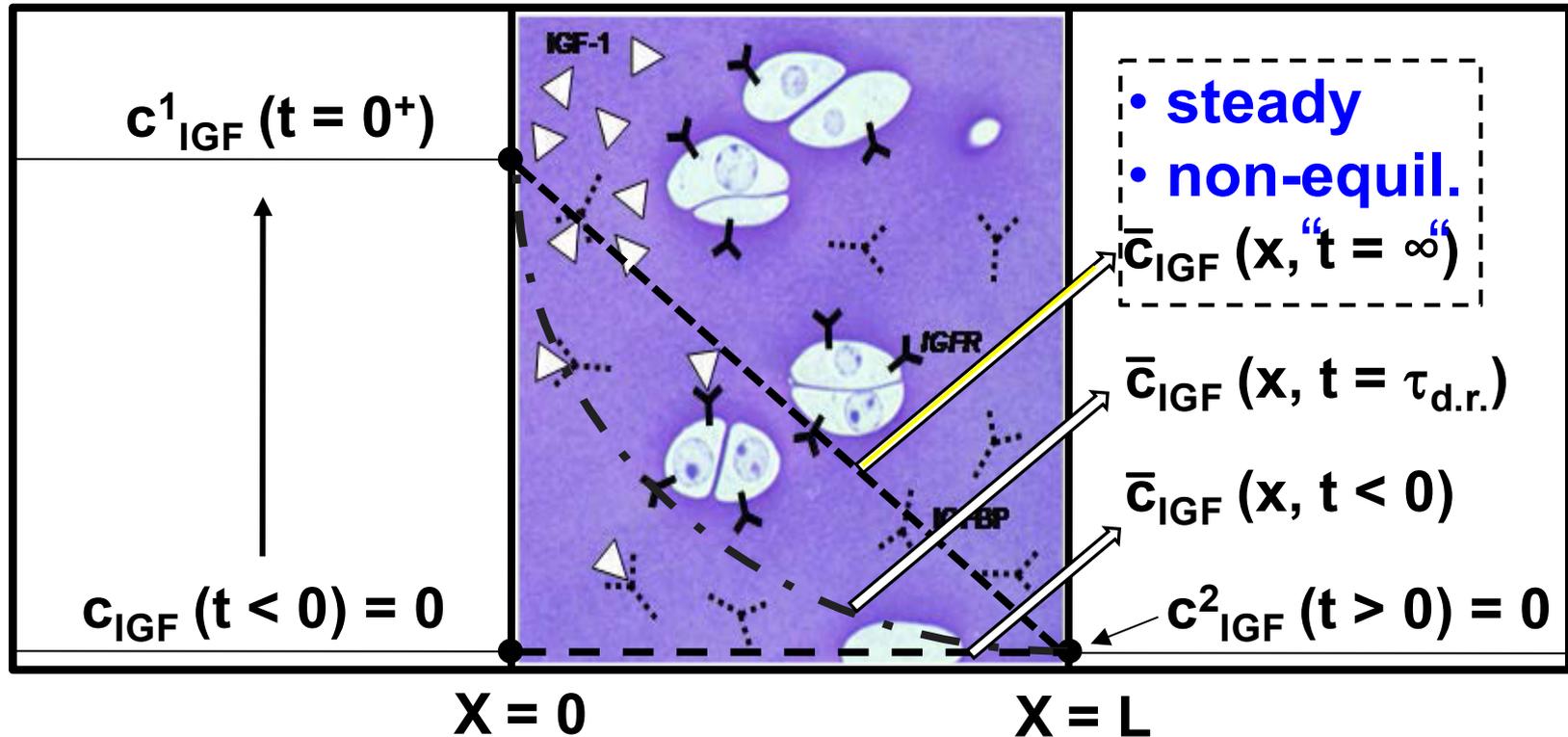
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$$\tau_{lag} = \frac{L^2}{6D_{eff}}$$

slow reaction, or slow diffusion compared to reaction???



Find  $c(x,t) \rightarrow$  Measure / Estimate  $D_{\text{eff}}$ ;  
 $\rightarrow$  relate  $D_{\text{eff}}$  to  $D_{\text{IGF}}$  and binding parameters ( $n, K_d$ )



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## "Transient"

- non-steady
- non-equil.

PSet 1.4

$$\bar{c}_F(x, t) = c_1 \left(1 - \frac{x}{L}\right) - \frac{2Kc_1}{\pi} \sum_{n=1}^{\infty} \left[\frac{1}{n}\right] \sin\left(\frac{n\pi x}{L}\right) e^{-t/\tau_n} \quad (1.72)$$

$$\tau_n = \frac{L^2}{n^2 \pi^2 D_{\text{eff}}} \quad \tau_1 = \frac{L^2}{\pi^2 D_{\text{eff}}} \quad (1.73)$$

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