

20.430 / 2.795 / 6.561 / 10.539

Fields Forces and Flows in Biological Systems

Fall 2015

Instructors: Mark Bathe, Alan Grodzinsky

Textbook:

Fields Forces and Flows in Biological Systems

Garland Science, March 2011

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Source: Grodzinsky, Alan. Field, Forces, and Flows
in Biological Systems. Garland Science, 2011.

Plus:

- Additional readings from primary (research) literature
- Supplementary materials throughout

20.430 Scope and Purpose

- Describes the fundamental driving forces for transport: chemical gradients, electrical interactions & fluid flow, applied to the biology and biophysics of molecules / cells / tissues

Philosophy of the Subject

- Primary objective: to integrate principles of coupling between chemical, electrical, & mechanical forces and flows intrinsic to tissues, membranes, macromolecules, and biomaterials.
- Focus: Topics in biology, biophysics & medicine motivate quantitative engineering approaches: molecular scale through complex structural organization of tissues and organs.
- Lectures focus on current problems in biology, biophysics, and medicine, and then use text material as the basis for understanding measurement, modeling, and analysis

FFF: Assignments and Grading

Homework: (~eight 1-week assignments during the term)

You are *encouraged to form teams* with other class members to discuss the underlying concepts and approaches.
(Of course, the work turned in must be your own.)

Term Paper Project:

- **Critical review** of a journal article from the literature
- Collaboration: **Teams of 3 people**

Two take home quizzes: (~ middle and end of term)

| | | |
|-----------------|--------------------|-----|
| Grading: | Homework | 30% |
| | Term Paper Project | 30% |
| | Take Home Quizzes | 40% |

Term Paper Project

Enzymatic Targeting of the Stroma Ablates Physical Barriers to Treatment of Pancreatic Ductal Adenocarcinoma

Cancer Cell
2012

Paolo P. Provenzano,¹ Carlos Cuevas,⁴ Amy E. Chang,¹ Vikas K. Goel,¹ Daniel D. Von Hoff,⁵ and Sunil R. Hingorani^{1,2,3,*}

¹Clinical Research Division

²Public Health Sciences Division

Fred Hutchinson Cancer Research Center, Seattle, WA 98109, USA

³Division of Medical Oncology, University of Washington School of Medicine, Seattle, WA 98195, USA

⁴Department of Radiology, University of Washington, Seattle, WA 98195, USA

⁵Clinical Translational Research Division, Translational Genomics Research Institute, Scottsdale, AZ 85259, USA

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DOI 10.1016/j.ccr.2012.01.007

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Source: [Prof. Paolo Provenzano's website](#).

Role of Extracellular Matrix Assembly in Interstitial Transport in Solid Tumors

Paolo A. Netti,² David A. Berk,³ Melody A. Swartz,⁴ Rakesh K. Jain⁵

Steele Laboratory for Tumor Biology, Department of Radiation Oncology, Massachusetts General Hospital and Harvard Medical School, Boston, Massachusetts 02114 [D. A. B., M. A. S., R. K. J.], and Department of Electrical Engineering, Massachusetts Institute of Technology, Cambridge, Massachusetts 02139 [A. J. G.]

ABSTRACT

- **The extracellular matrix may contribute to the drug resistance of a solid tumor by preventing the penetration of therapeutic agents. We measured differences in interstitial resistance to macromolecule (IgG) transport in 4 tumor types and found an unexpected correspondence between transport resistance and the mechanical stiffness.**
- **The interstitial diffusion coefficient of IgG was measured *in situ* by FRAP.....**

Term Paper Project

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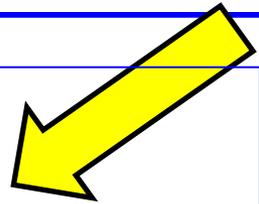
DOI 10.1016/j.ccr.2012.01.007

Hyaluronan, fluid pressure, and stromal resistance in pancreas cancer

British J of Cancer
2013

P P Provenzano^{1,4} and S R Hingorani^{*,1,2,3}

¹Clinical Research Division, Fred Hutchinson Cancer Research Center, Seattle, WA 98109, USA; ²Public Health Sciences Division, Fred Hutchinson Cancer Research Center, Seattle, WA 98109, USA; ³Division of Medical Oncology, University of Washington School of Medicine, Seattle, WA 98195, USA



Fields Forces & Flows: Syllabus

I. CHEMICAL SUBSYSTEM

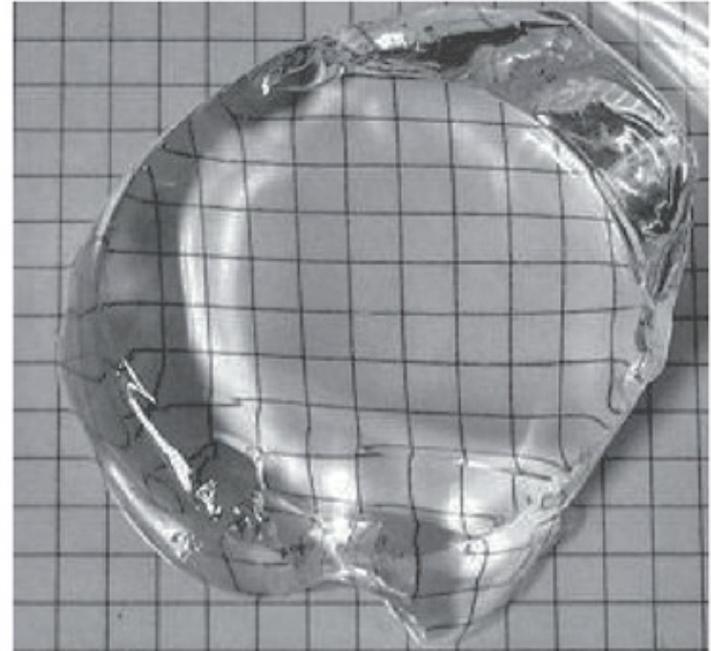
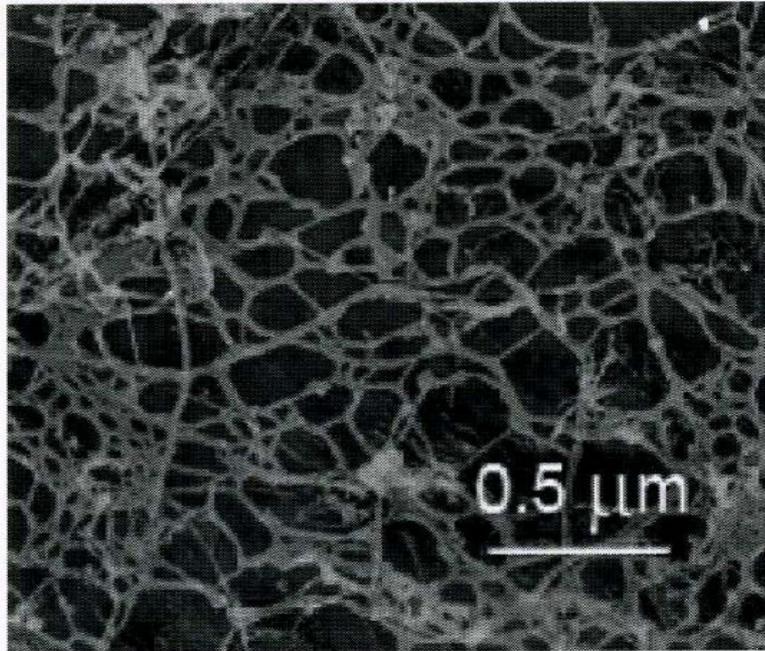
II. ELECTRICAL SUBSYSTEM

III. MECHANICAL SUBSYSTEM

IV. INTEGRATIVE CASE STUDIES: PHYSICOCHEMICAL, BIOPHYSICAL

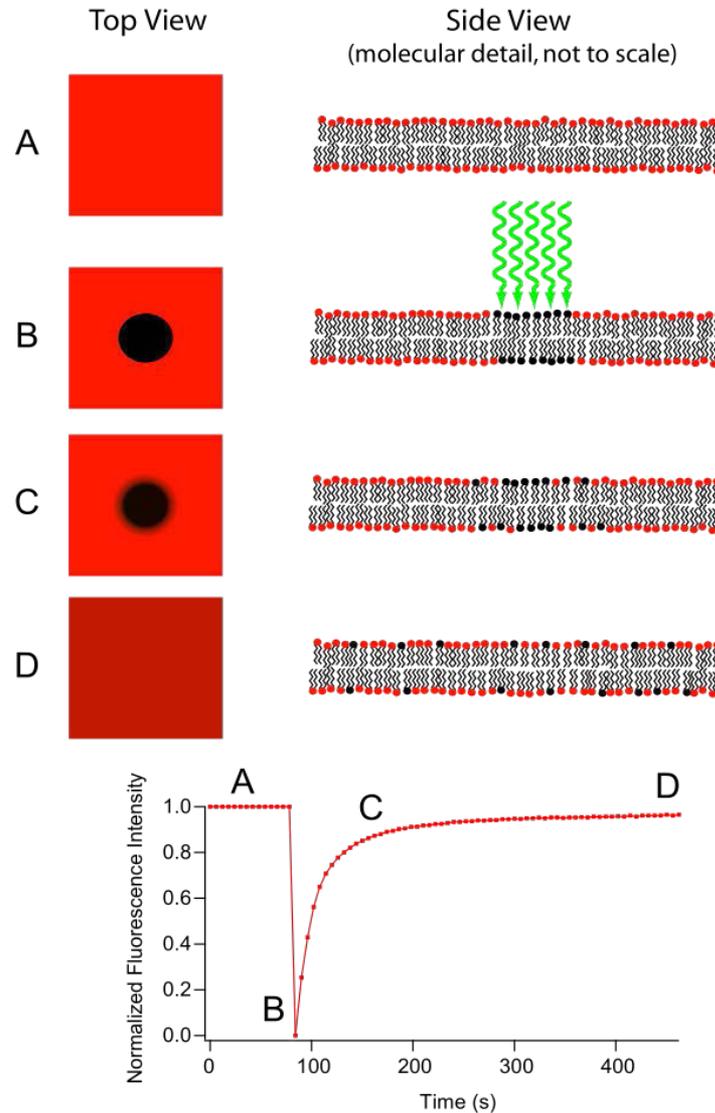
| Lect | Date | Topic |
|------------------------------|--------|---|
| 1 | Sep 9 | Course introduction, overview, and objectives |
| I. CHEMICAL SUBSYSTEM | | |
| 2 | Sep 14 | Diffusion as a random walk; Stokes-Einstein relation for diffusion coefficient; Examples of diffusion |
| 3 | Sep 16 | Constitutive equations for diffusion (Fick's Laws); Conservation of mass for a control volume; Differential form; Steady diffusion (1D); Boundary conditions |
| 4 | Sep 21 | Diffusion and reaction; Reaction rates, order, molecularity and mechanisms; Scaling and the Damköhler number; Solution procedures |
| 5 | Sep 23 | Examples of diffusion-reaction: Diffusion of a ligand through tissue with cell receptor-ligand interactions; Diffusion-reaction kinetics |
| 6 | Sep 28 | More examples of diffusion-reaction |
| 7 | Sep 30 | Case study: IGF-1 diffusion-reaction within tissues and cell seeded scaffolds; binding to IGF binding proteins & cell surface receptors; experimental methods |

Solute Flow in & across "Bio Porous Materials: Molecular Networks, Gels....



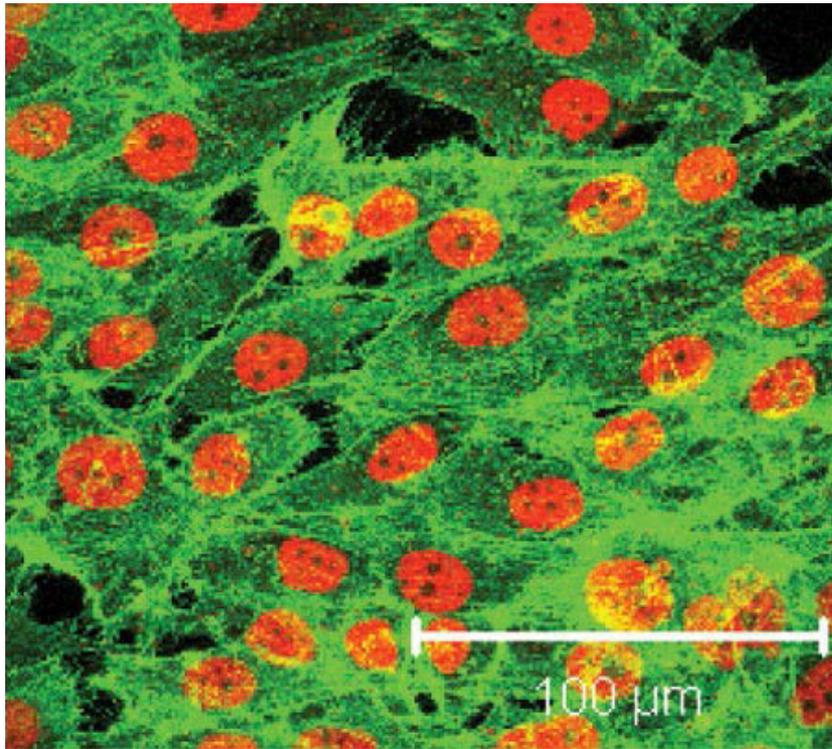
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"Measure and Model": Find Diffusivity D_i

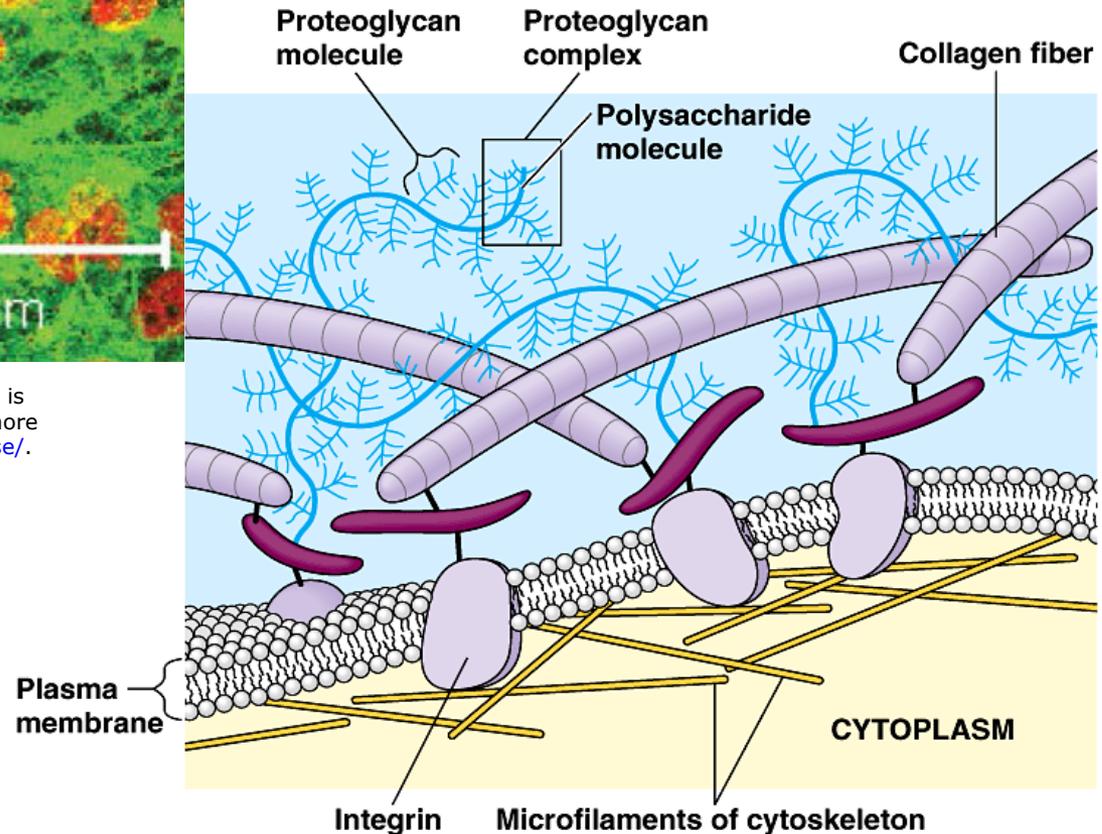


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Growth factors (e.g., IGF-1) and cytokines (e.g., TNF α) can bind to Extracellular Matrix molecules as well as cell receptors



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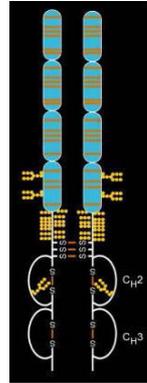


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“Biologic” TNF- α Blockers: >\$20 Billion/year



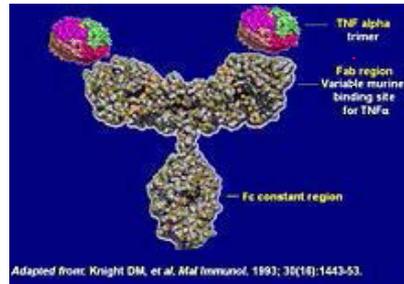
(Amgen / Pfizer)
(1998 RA)



Remicade

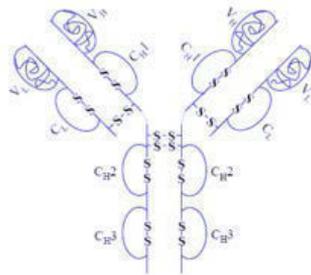
INFLIXIMAB

(Centocor / J&J)
(1998 Crohn's)



HUMIRA

adalimumab
(Abbott)
(2002 RA)

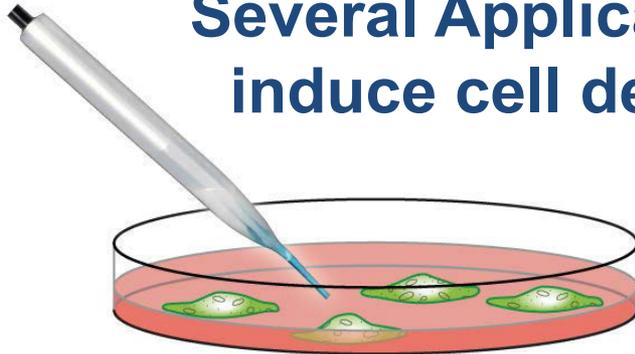


Autoimmune-Inflammatory Diseases

- Rheumatoid Arthritis
- Crohn's Disease (IBD)
- Ulcerative Colitis (IBD)
- Ankylosing Spondylitis
- Psoriatic Arthritis
- Psoriasis

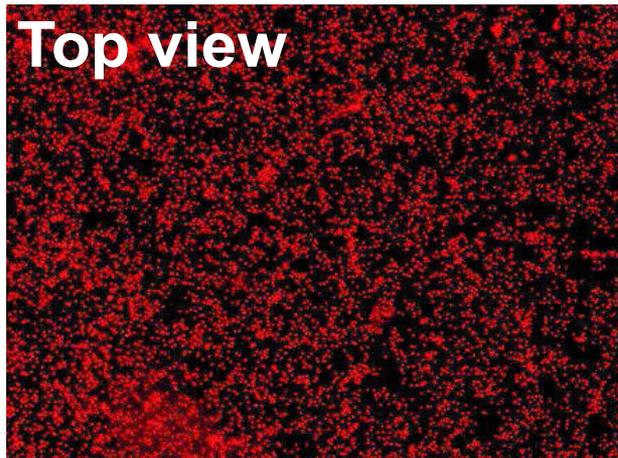
Effects of a cell signaling (kinase) blocker (Merck BI-78D)

Several Applications: diabetes; purposely induce cell death (apoptosis) in tumors



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Monolayer cell culture



Day 1 of culture

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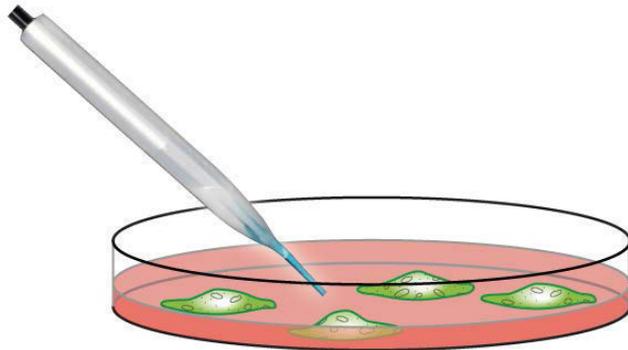
- Added kinase inhibitor on Day 0

- Use fluorescent markers to assess cell viability:

RED = Dead cells

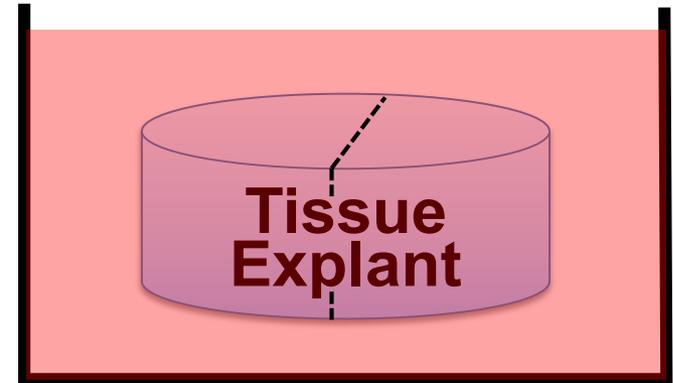
GREEN = Live cells

Effects of a cell signaling (kinase) blocker (Merck BI-78D)

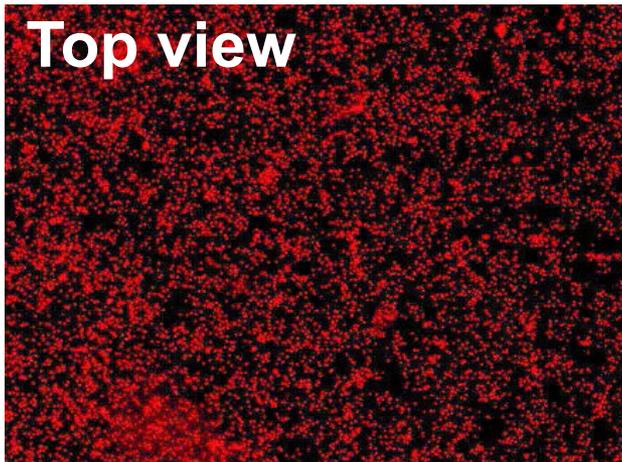


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Monolayer cell culture

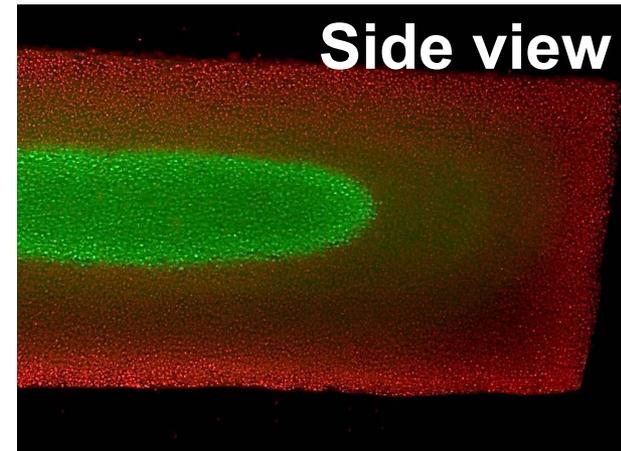


Tissue with same cells



Day 1 of culture

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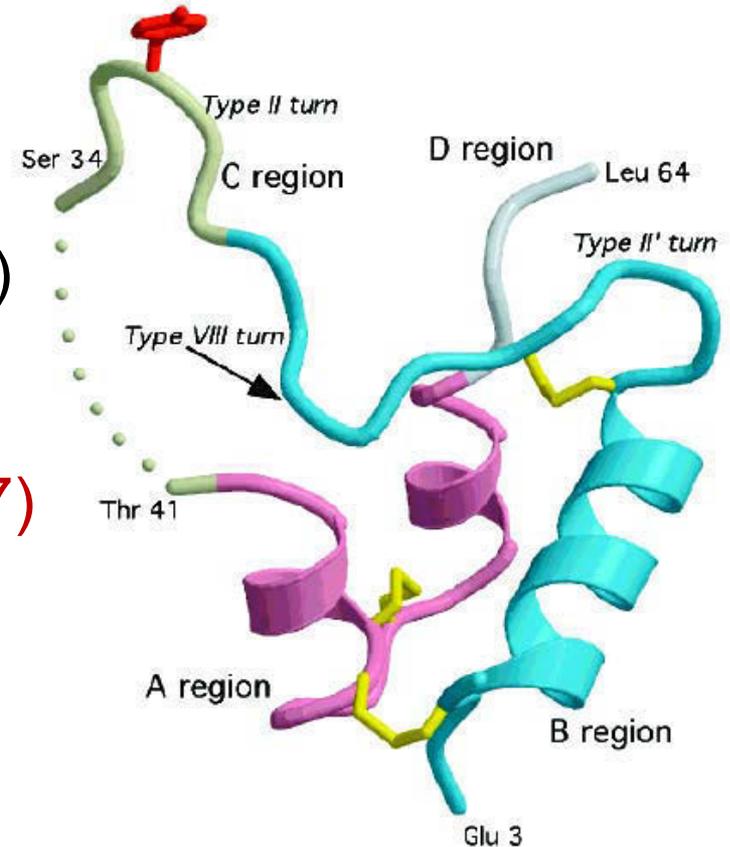


Day 6 of culture

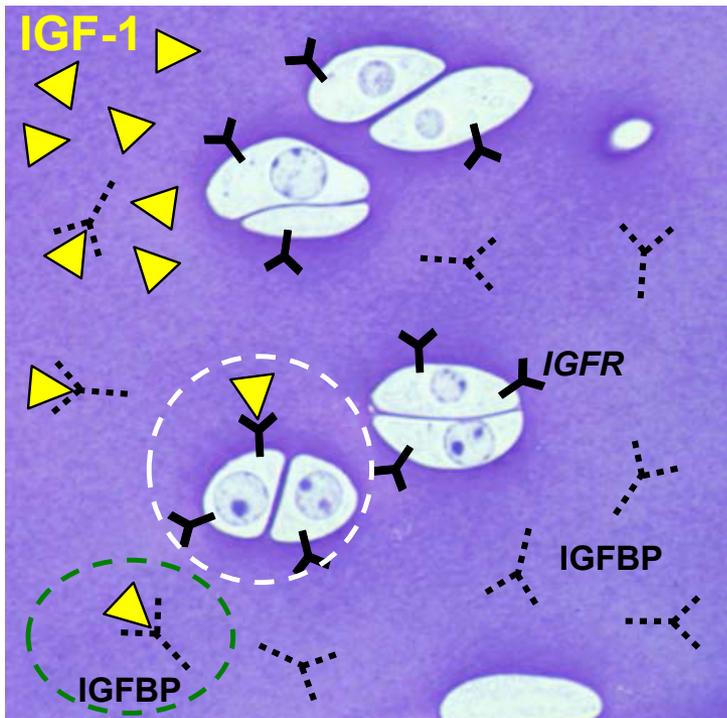
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Insulin-like Growth Factor-1 (IGF-1)

- Peptide Growth Factor:
 - ◆ Stimulates cellular biosynthesis;
 - ◆ Inhibits catabolic degradation of ECM
 - ◆ Anti-Apoptotic
- Protein: **7.6 kDa (70 amino acids)**
- “Folds” like Insulin in Aq. Solution
- **pI ~ 8.4 (“basic” + charged @ pH 7)**
- **Found in: Nerve, Muscle, Connective, & Epithelial Tissues**
 - ◆ Serum (50-200 ng/ml)
 - ◆ Joint Fluid (20-50 ng/ml)
 - ◆ Tissue (1-10 ng/ml)
 - ◆ CSF; Brain (~5 ng/ml; ~5 pg/mg)

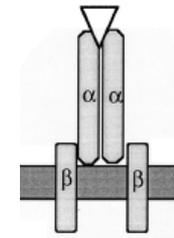


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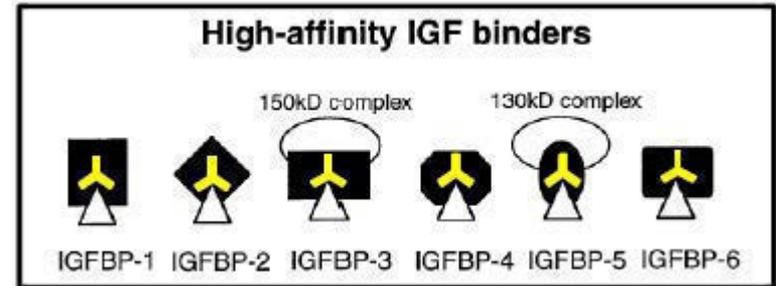


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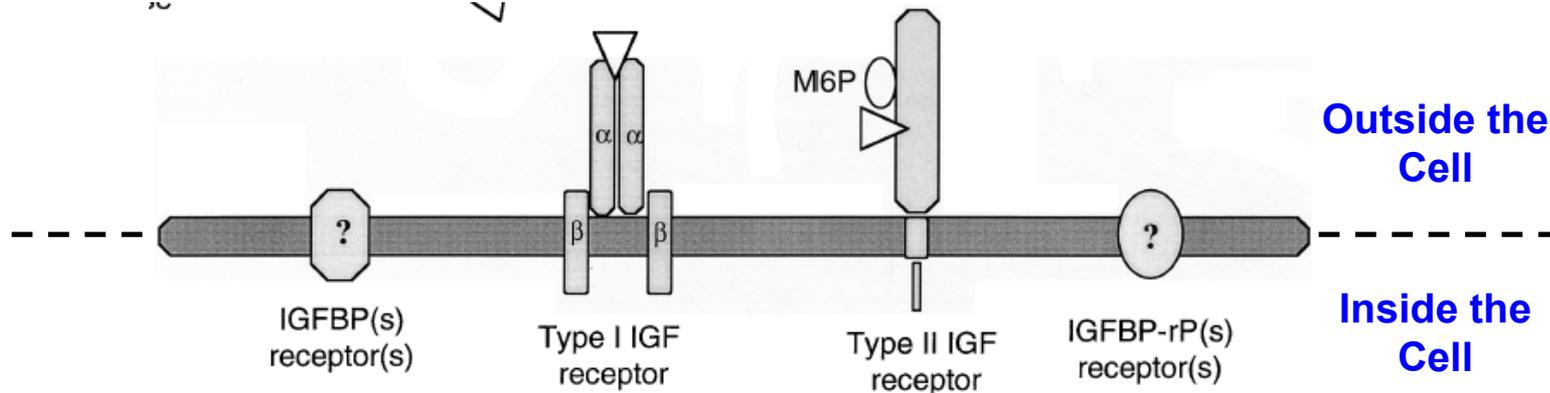
IGF-I/II



Type I IGF receptor



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Partial reversal of Rett Syndrome-like symptoms in MeCP2 mutant mice

PNAS 2009

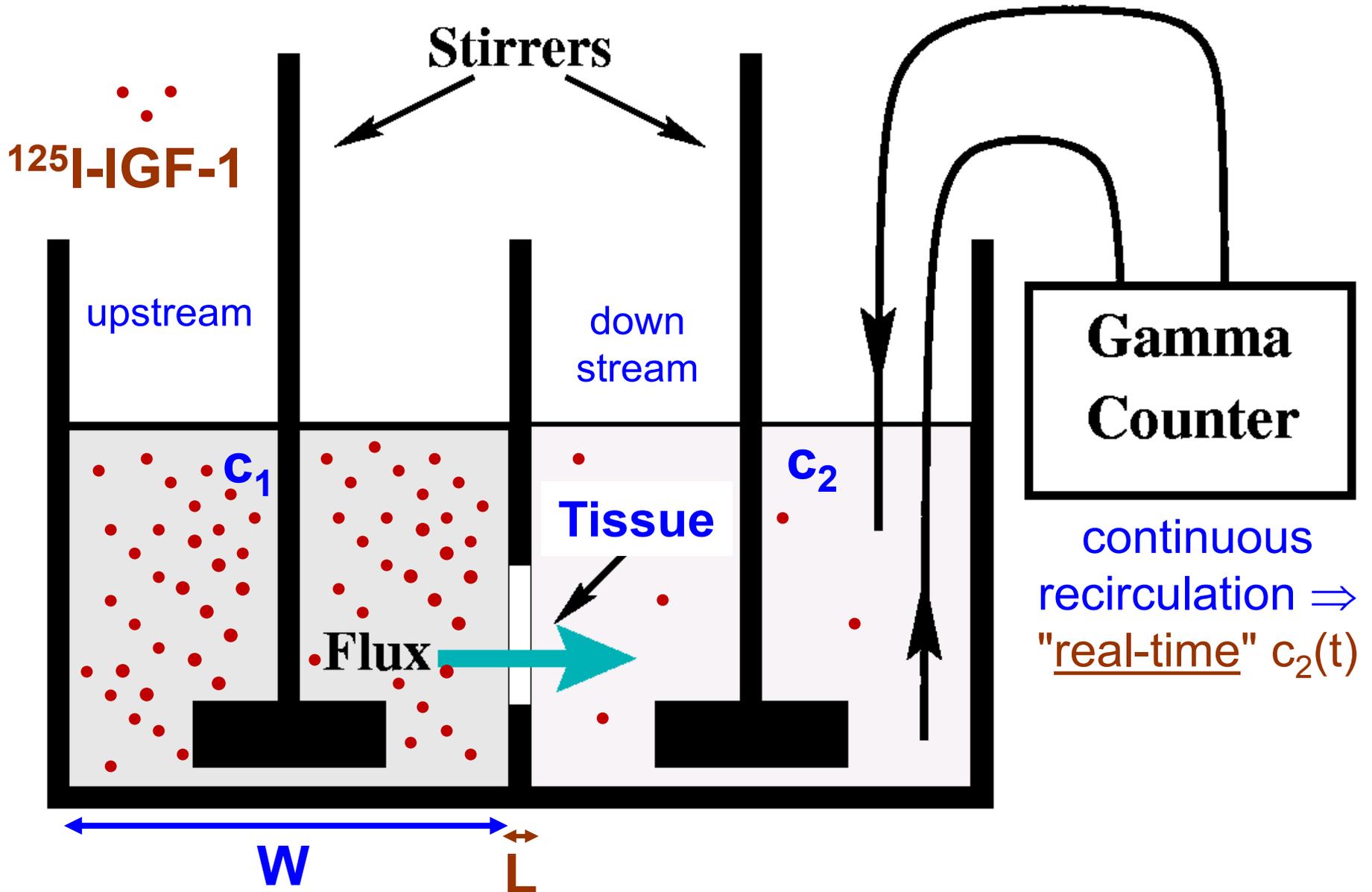
Daniela Tropea^{a,1}, Emanuela Giacometti^{b,1}, Nathan R. Wilson^{a,1}, Caroline Beard^b, Cortina McCurry^a, Dong Dong Fu^b, Ruth Flannery^b, Rudolf Jaenisch^{b,c,2}, and Mriganka Sur^{a,2} ←

^aPicower Institute for Learning and Memory and Department of Brain and Cognitive Sciences, Massachusetts Institute of Technology, Cambridge, MA 02139;

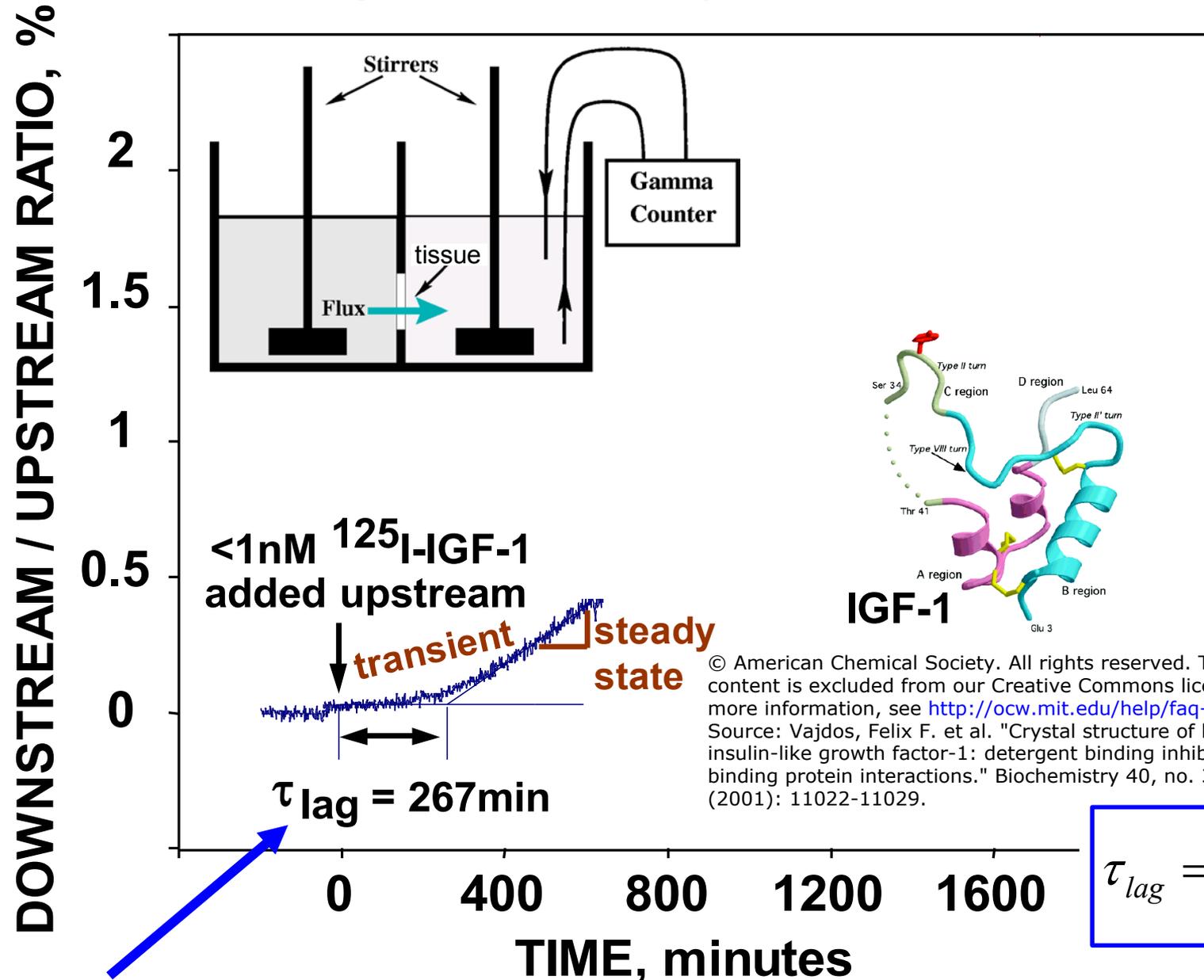
^bWhitehead Institute for Biomedical Research, Cambridge, MA 02142; and ^cDepartment of Biology, Massachusetts Institute of Technology, Cambridge, MA 02139

- **Rett patients express aberrantly high levels of IGFBP3, which inhibits IGF-1 signaling. Depressed IGF-1 signaling has indeed been implicated in autism spectrum disorder**

Experimental Setup: Transport



IGFBP-3 Binding Slows entry of IGF-1 into Tissue!



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$$\tau_{lag} = \frac{L^2}{6D_{eff}}$$

slow reaction, or slow diffusion compared to reaction???

| Lect | Date | II. ELECTRICAL SUBSYSTEM |
|------|--------|---|
| 8 | Oct 5 | E-fields and transport; Maxwell's equations for electric & magnetic fields |
| 9 | Oct 7 | Define electrical potential; conservation of charge; Electro-quasistatics |
| 10 | Oct 13 | Laplacian solutions via Separation of Variables; Electric field boundary conditions; Ohmic transport; Charge Relaxation; Electrical migration vs. chemical diffusive fluxes |
| 11 | Oct 14 | Electrochemical coupling; Electrical double layers; Poisson–Boltzmann Equation |
| 12 | Oct 19 | Donnan equilibrium in tissues, gels, polyelectrolyte networks |
| 13 | Oct 21 | Charge group ionization & electro-diffusion-reaction in molecular networks |
| 14 | Oct 26 | Case study: Insulin-like growth factor-1 transport in tissues & cell-seeded gels; IGF-1 binding to cell receptors vs. extracellular matrix; Experimental methods |

(Chap 2): E-fields

- What are sources of \underline{E} fields
- Where do they come from
- What can \underline{E} do (applications)

Table 2.7 Maxwell's equations for linear media.

| Name | Differential form |
|---------------------|---|
| Gauss' law | $\nabla \cdot \epsilon \mathbf{E} = \rho_e$ |
| Ampère's law | $\nabla \times \mathbf{H} = \mathbf{J} + \frac{\partial \epsilon \mathbf{E}}{\partial t}$ |
| EM Waves | |
| Faraday's law | $\nabla \times \mathbf{E} = -\frac{\partial \mu \mathbf{H}}{\partial t}$ |
| Magnetic flux | $\nabla \cdot \mu \mathbf{H} = 0$ |
| Charge conservation | $\nabla \cdot \mathbf{J} = -\frac{\partial \rho_e}{\partial t}$ |

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Source: Grodzinsky, Alan. Field, Forces and Flows in Biological Systems. Garland Science, 2011. [Preview with [Google Books](#)]

Table 2.8 Quasistatic laws for linear media.

Electroquasistatic (EQS)

$$\nabla \cdot \epsilon \mathbf{E} = \rho_e$$

$$\nabla \times \mathbf{E} = 0$$

$$\nabla \cdot \mathbf{J} = -\frac{\partial \rho_e}{\partial t}$$

Magnetoquasistatic (MQS)

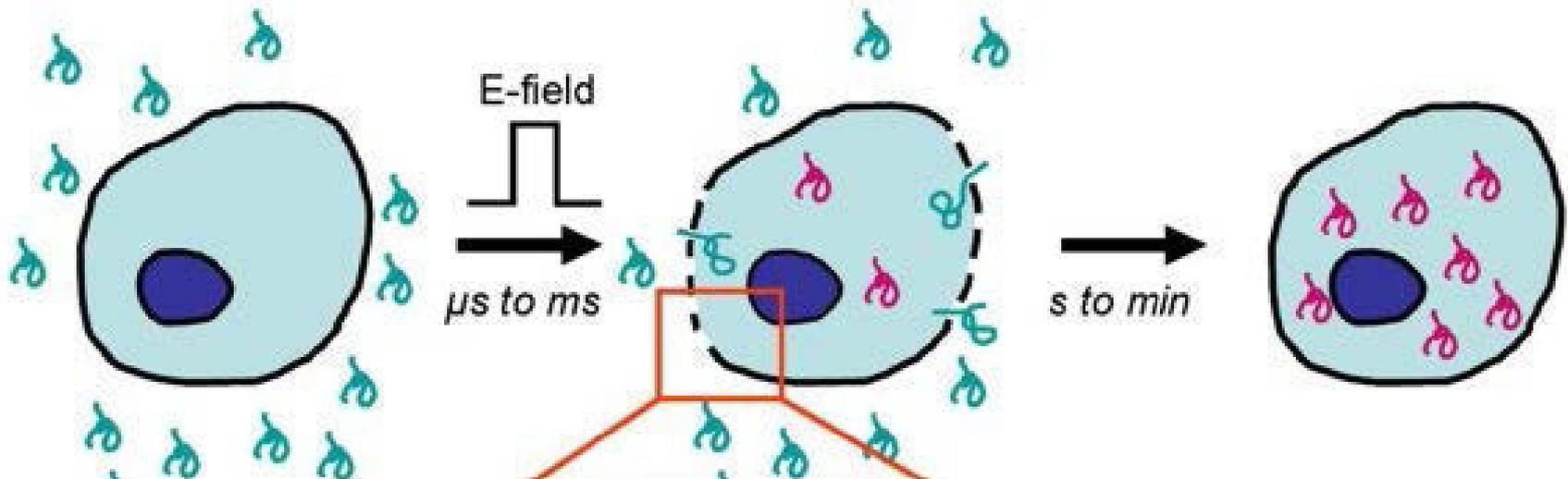
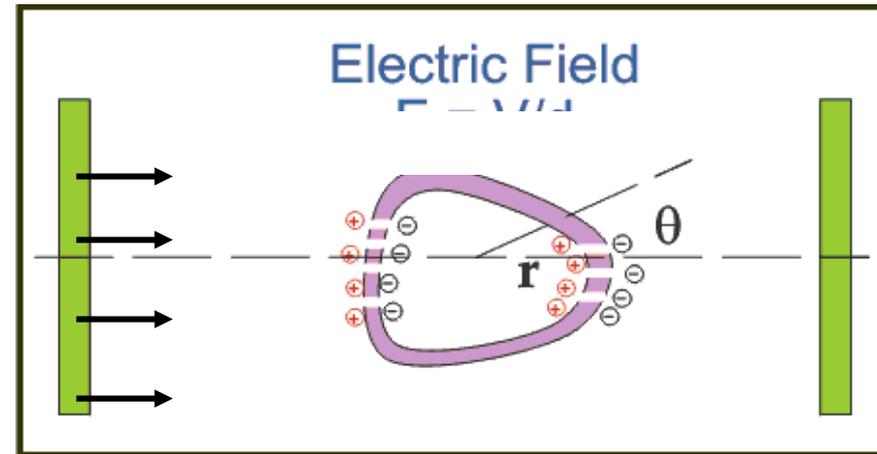
$$\nabla \times \mathbf{H} = \mathbf{J}, \nabla \cdot \mathbf{J} = 0$$

$$\nabla \cdot \mu \mathbf{H} = 0$$

$$\nabla \times \mathbf{E} = -\frac{\partial \mu \mathbf{H}}{\partial t}$$

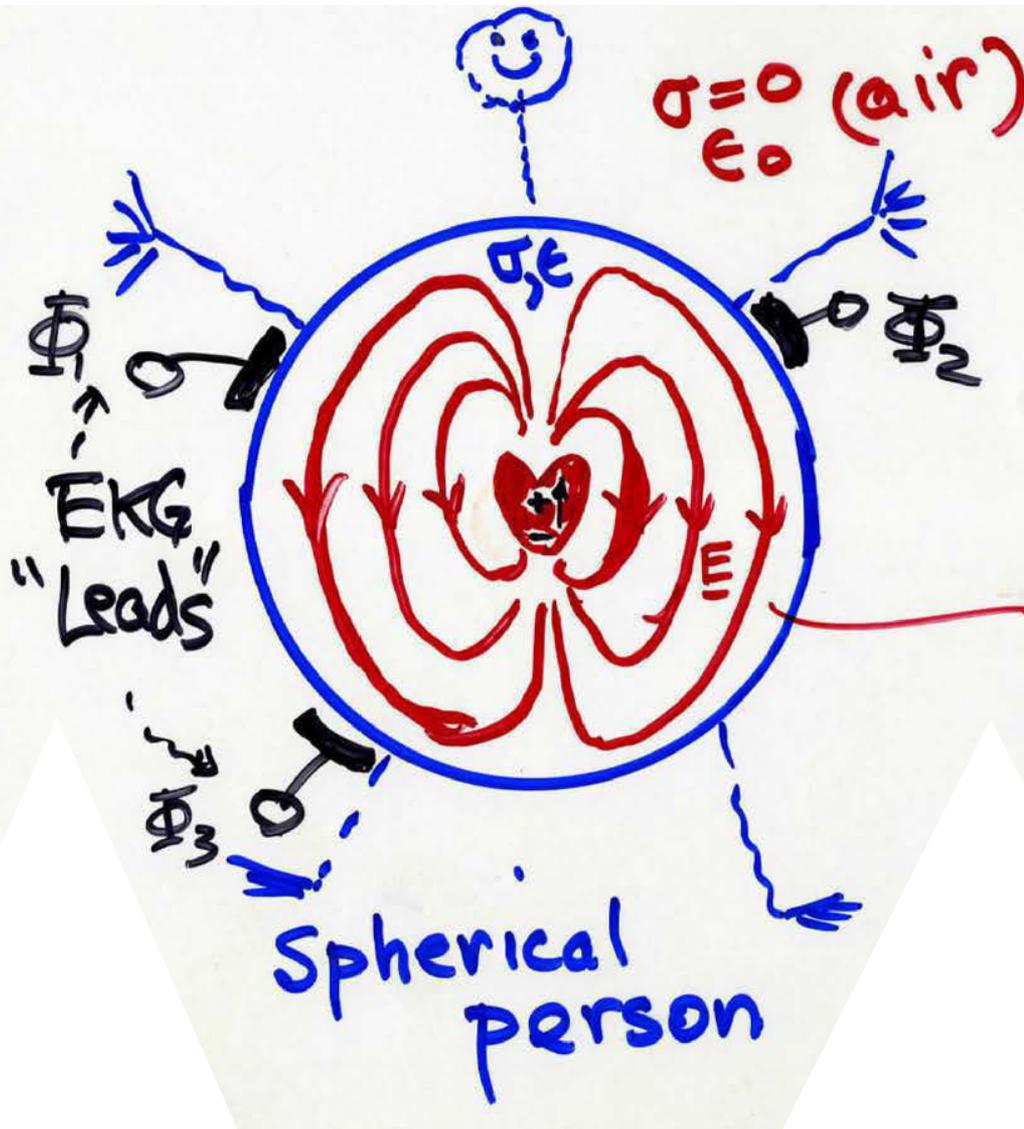
[+ Ohmic Constitutive Law ($\mathbf{J} = \sigma \mathbf{E}$)]

Electroporation: transient permeabilization of cell membrane for gene transfection/therapy; drug delivery; tumor treatment, and cell-based therapy



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EKG: Centric Dipole Model of the Heart



$f \sim 1 \text{ Hz}$
low enough
for EQS!

FIND \underline{E}_{in} ; $\Phi(r=R, t)$

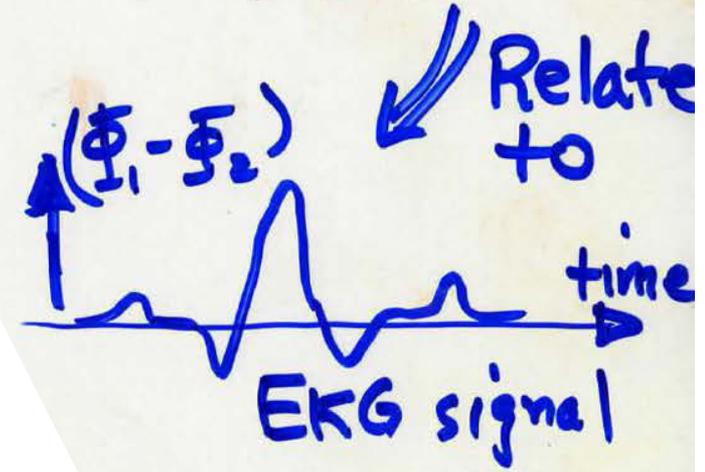


Table 2.8 Quasistatic laws for linear media.

Electroquasistatic (EQS)

$$\nabla \cdot \epsilon \mathbf{E} = \rho_e$$

$$\nabla \times \mathbf{E} = 0$$

$$\nabla \cdot \mathbf{J} = -\frac{\partial \rho_e}{\partial t}$$

Magnetoquasistatic (MQS)

$$\nabla \times \mathbf{H} = \mathbf{J}, \nabla \cdot \mathbf{J} = 0$$

$$\nabla \cdot \mu \mathbf{H} = 0$$

$$\nabla \times \mathbf{E} = -\frac{\partial \mu \mathbf{H}}{\partial t}$$

[+ Ohmic Constitutive Law ($\mathbf{J} = \sigma \mathbf{E}$)]

MRI

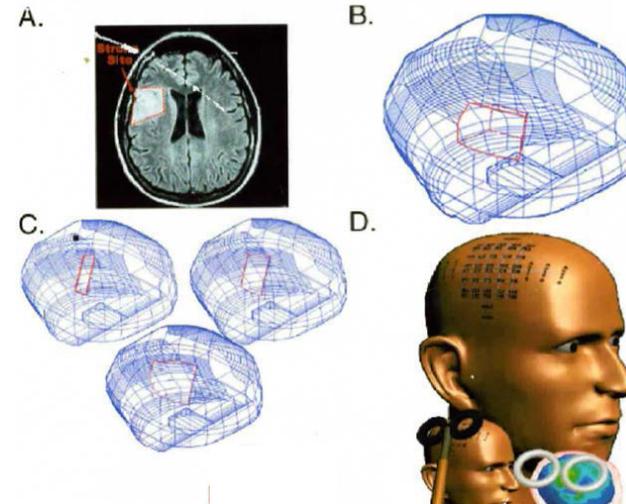


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Deep Brain Stimulation via B-fields

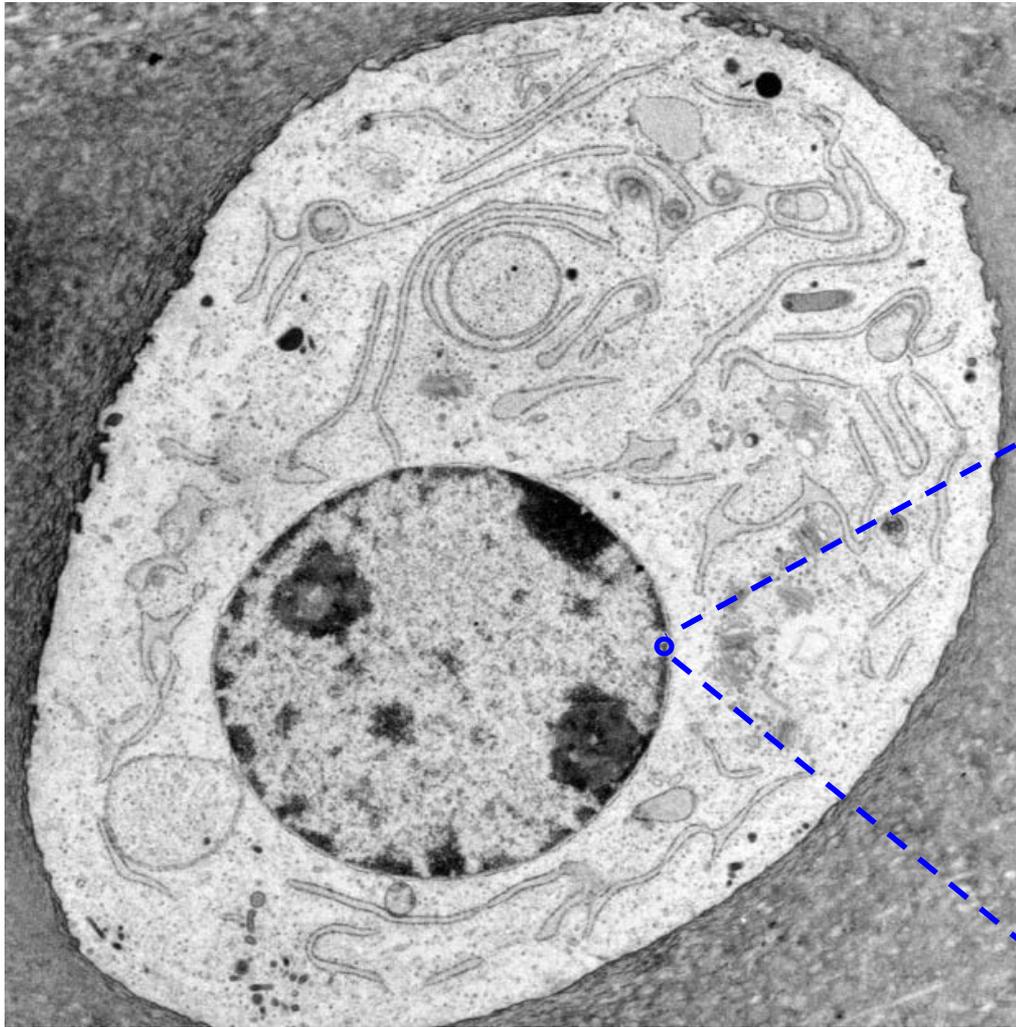


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Chap 3: Electrochemical Interactions & Transport

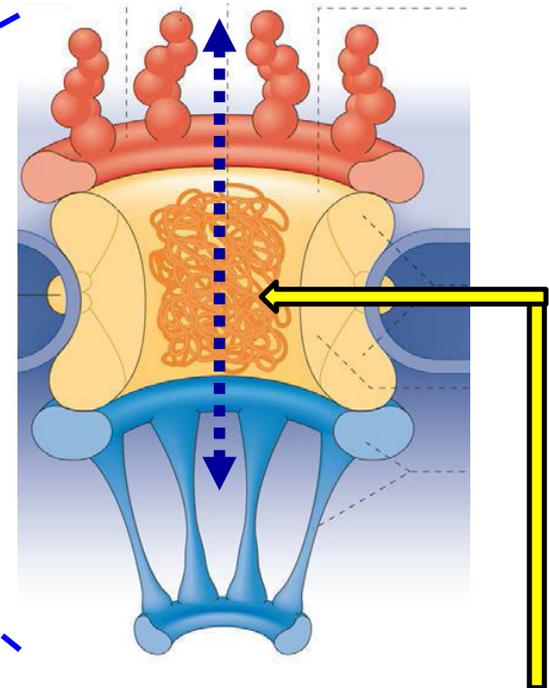
Effects of "Ligand" Molecular Charge on:

- Boltzmann Partitioning into charged tissues, gels
- Binding (to ECM / ICM, receptors.....)
- Non-Equil Diffusion (D_{eff}): do E-effects speed up or slow down transport?
- "Donnan" Osmotic Pressure in tissues/gels/cells



~2,000 nuclear pores
per nucleus

per second
(e.g., tRNA, mRNA)



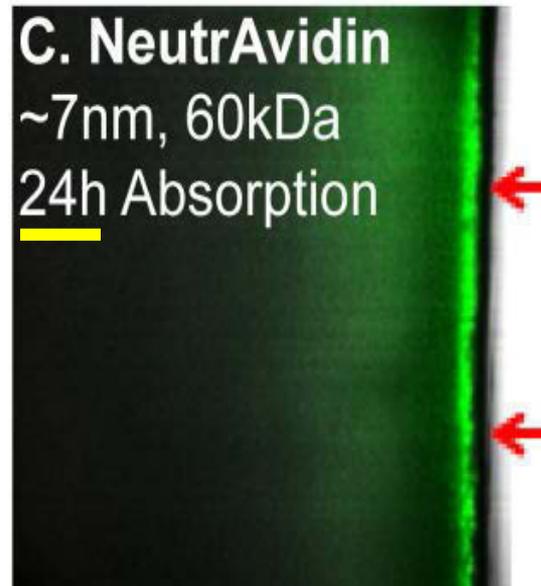
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Source: Raices, Marcela, and Maximiliano A. D'Angelo.
"Nuclear pore complex composition: a new regulator of tissue-specific and developmental functions." Nature Reviews Molecular Cell Biology 13, no. 11 (2012): 687-699.

"Hydrophilic" : lots of lysines (+ charge)

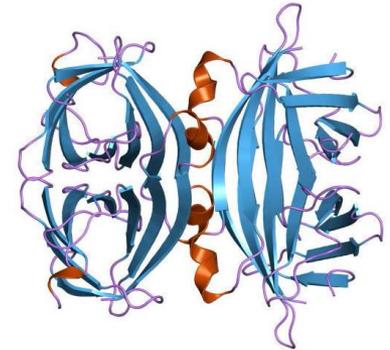
Avidin uptake into dense negative extracellular matrix:

- **Electrostatic & binding interactions: uptake \uparrow by 400-fold**
- **Functionalize drugs to (+) nanoparticles, to target tissues**



**Negatively Charged
Connective Tissue**

Courtesy of Alan Grodzinsky. Used with permission.



Courtesy of [Jawahar Swaminathan](#) and [MSD staff](#) at the European Bioinformatics Institute; image in the public domain.

Avidin

pl ~ 10.5; 66 kDa

9 lysine (+);

8 Arginine (+)

7 Glutamic (-)

5 Aspartic (-)

+5 per chain; 4 chains

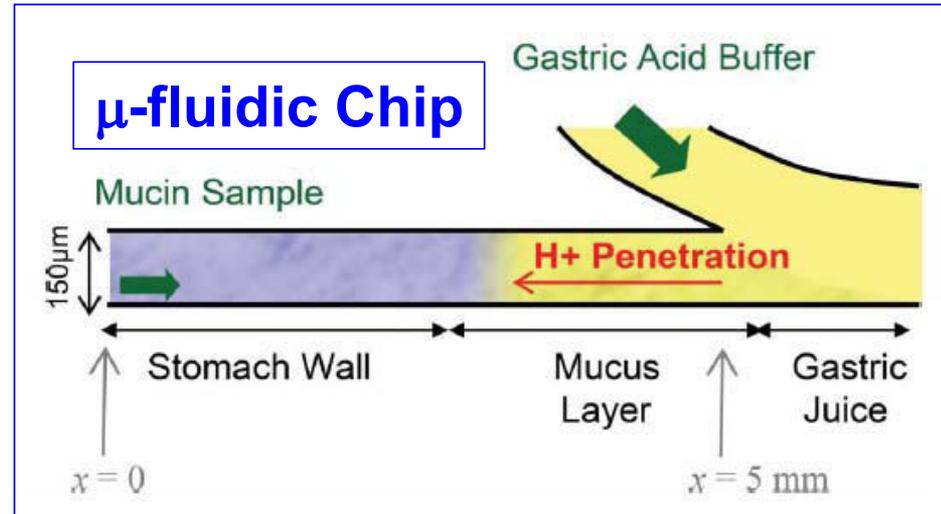
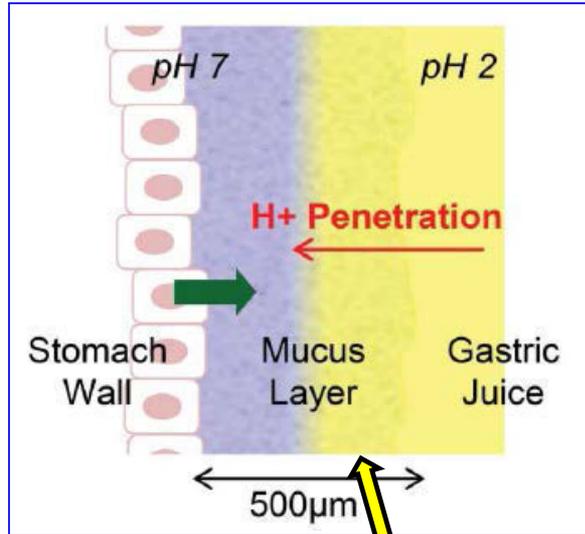
Total Charge +20

| Lect | Date | III. MECHANICAL SUBSYSTEM |
|------|--------|--|
| 15 | Oct 28 | Conservation of mass and momentum in fluids |
| 16 | Nov 2 | Viscous stress-strain rate relations; Navier–Stokes equations; examples |
| 17 | Nov 4 | Low Reynolds number flows; Stokes equation; Scaling and dimensional analysis; examples |
| 18 | Nov 9 | Newtonian, fully developed low Reynolds number flows; Stokes drag on sphere |
| 19 | Nov 16 | Diffusion and convection; The Peclet number; Convection-diffusion-reaction and boundary layers |
| 20 | Nov 18 | Concentration boundary layers: fully-developed flow and transport |

A microfluidic *in vitro* system for the quantitative study of the stomach mucus barrier function

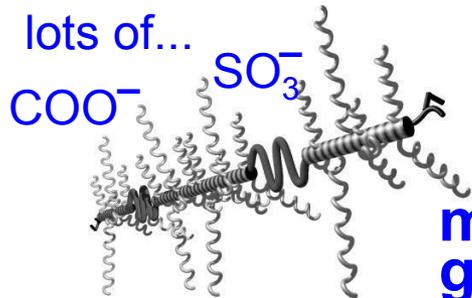
Leon Li,^{ab} Oliver Lieleg,^{†c} Sae Jang,^d Katharina Ribbeck^{*c} and Jongyoon Han^{*bc}

2012 Lab on a Chip



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Source: Li, Leon et al. "A microfluidic *in vitro* system for the quantitative study of the stomach mucus barrier function." *Lab on a Chip* 12, no. 20 (2012): 4071-4079.



mucin glycoprotein

$$v \frac{\partial [\text{H}^+]}{\partial x} = D_{\text{H}^+} \frac{\partial^2 [\text{H}^+]}{\partial x^2} - k_{\text{on_B1}} [\text{H}^+] [\text{B1}] + k_{\text{off_B1}} [\text{H}_{\text{B1}}] \dots$$

"...continuously secreted mucin layer hinders acid diffusion..."

IV. INTEGRATIVE CASE STUDIES: PHYSICOCHEMICAL, BIOPHYSICAL INTERACTIONS

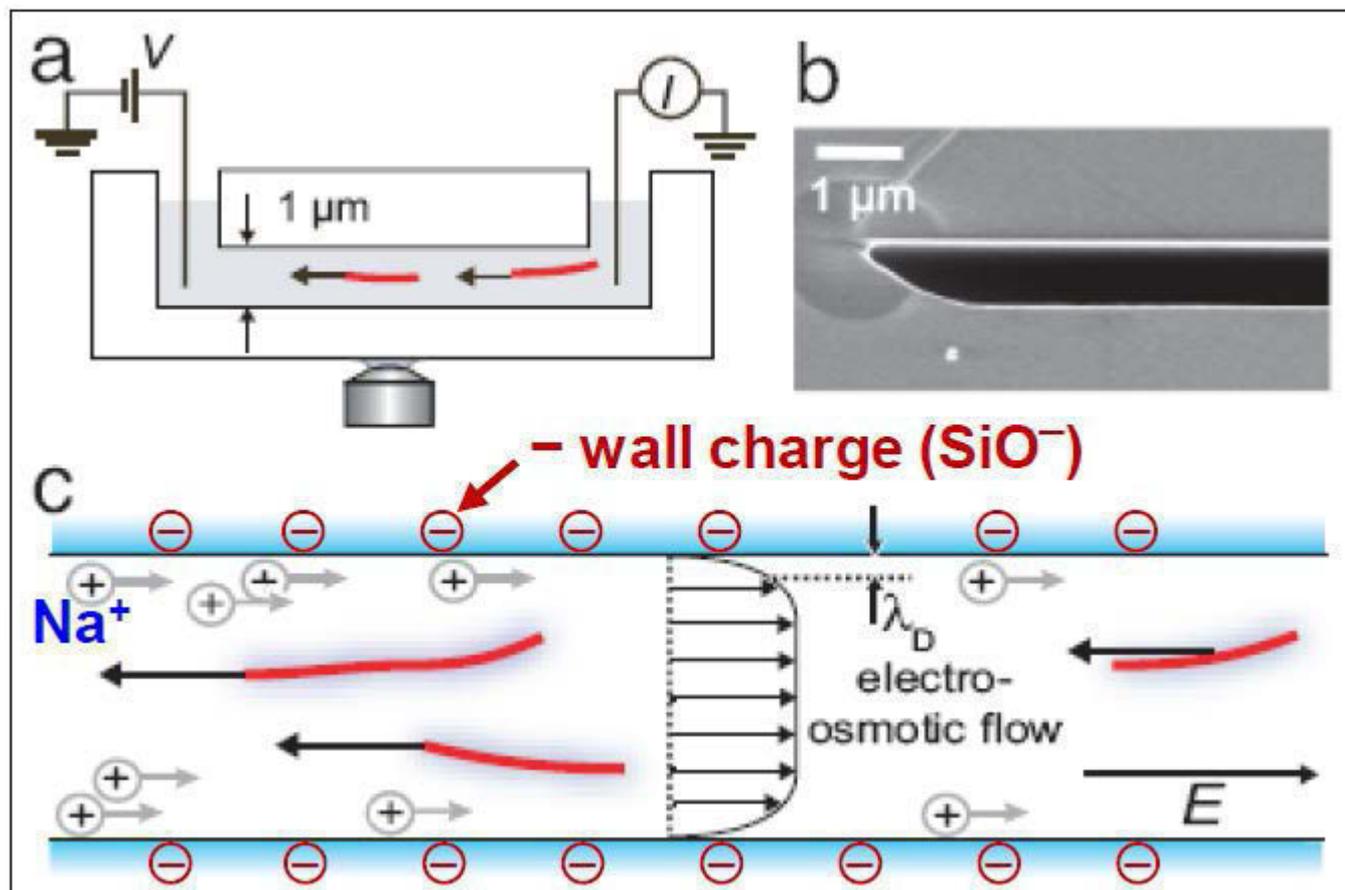
| Lect | Date | Topic |
|-------------|-------------|---|
| 21 | Nov 23 | Electrokinetics: Capillary electroosmosis: theory and experiments |
| 22 | Nov 25 | MEMs, microfluidics, cell membranes and hydrogels |
| 23 | Nov 30 | Electrophoretic motion: proteins in gels, tissues, molecular networks, & membranes; zeta potential |
| 24 | Dec 2 | DLVO theory: double layer repulsion and Van der Waals interactions (DNA, RNA, proteins, glycoproteins, GAGs: macromolecular interactions) |
| 25 | Dec 7 | Porous media flows: extracellular and intracellular |
| 26 | Dec 9 | Cell/molecular electrokinetics; review of term paper project |

Electrophoresis of individual microtubules in microchannels

PNAS 2007

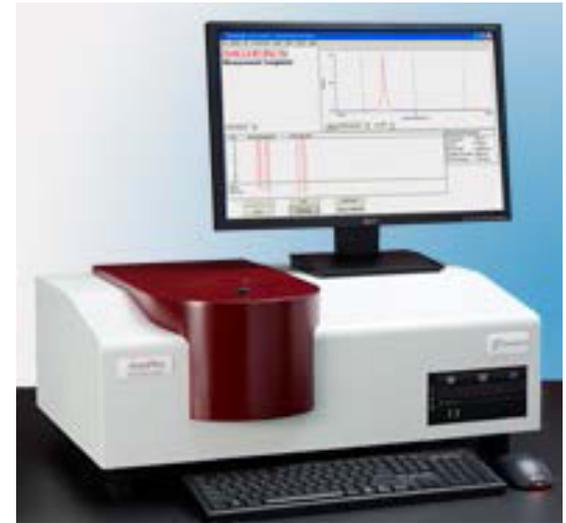
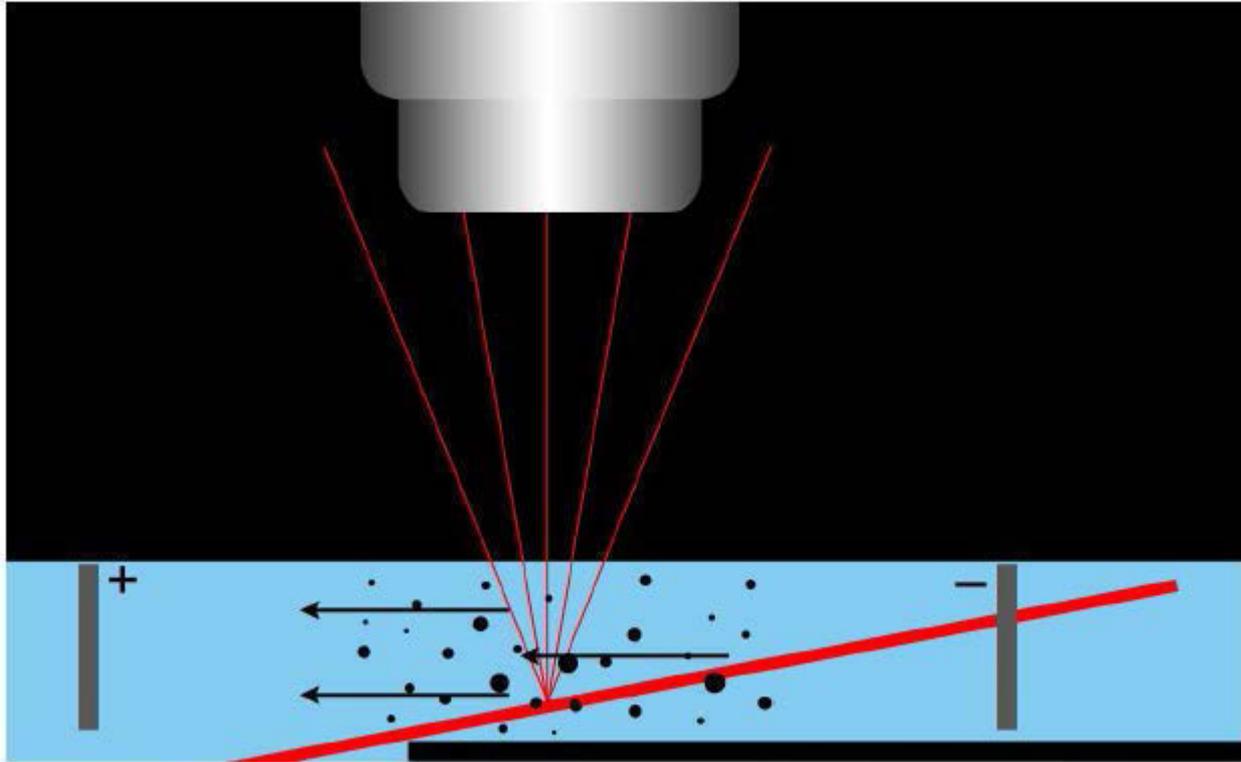
M. G. L. van den Heuvel, M. P. de Graaff, S. G. Lemay, and C. Dekker*

Kavli Institute of Nanoscience, Delft University of Technology, Lorentzweg 1, 2628 CJ, Delft, The Netherlands



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Source: Van den Heuvel, M. G. L. et al. "Electrophoresis of individual microtubules in microchannels." Proceedings of the National Academy of Sciences 104, no. 19 (2007): 7770-7775.

Zeta Potential (particle charge) Instruments



+ (applied electric field) **-**

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Measure “ ζ ” → Infer effective particle charge

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Source: Gelbert, William M. et al. "[DNA-Inspired Electrostatics](#)." Physics Today. 53:9 (2000): 38.

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Fall 2015

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