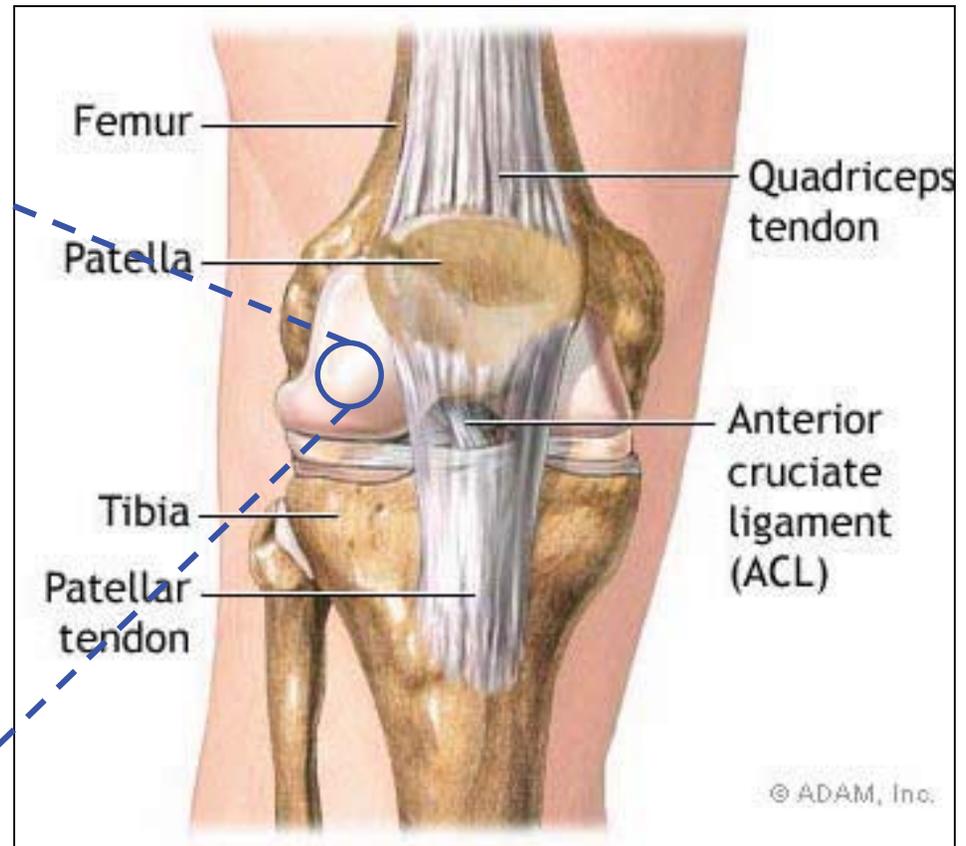
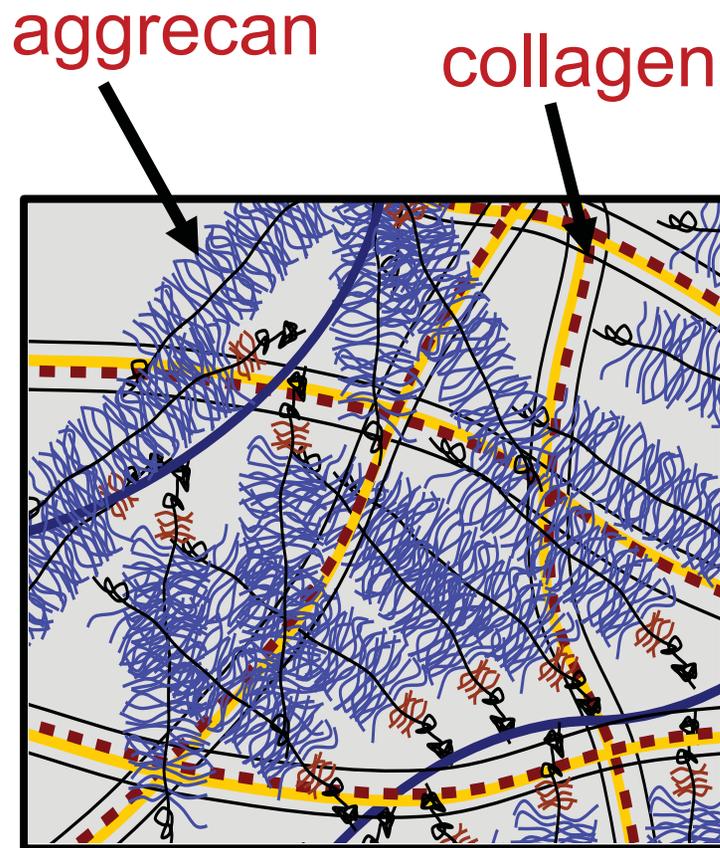


Aggrecan: Resists Compression (in tissues)

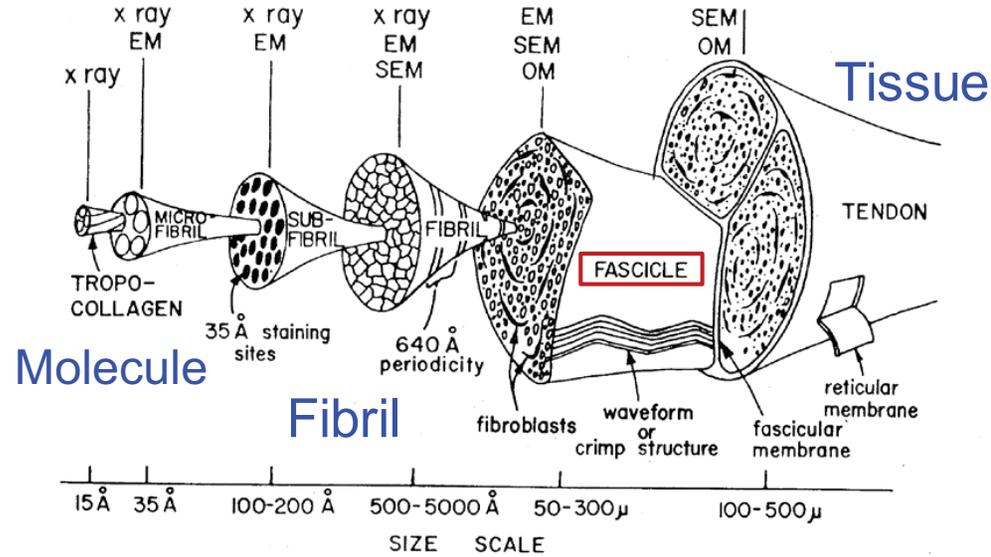
Collagen: Resists Tension (in tissues)



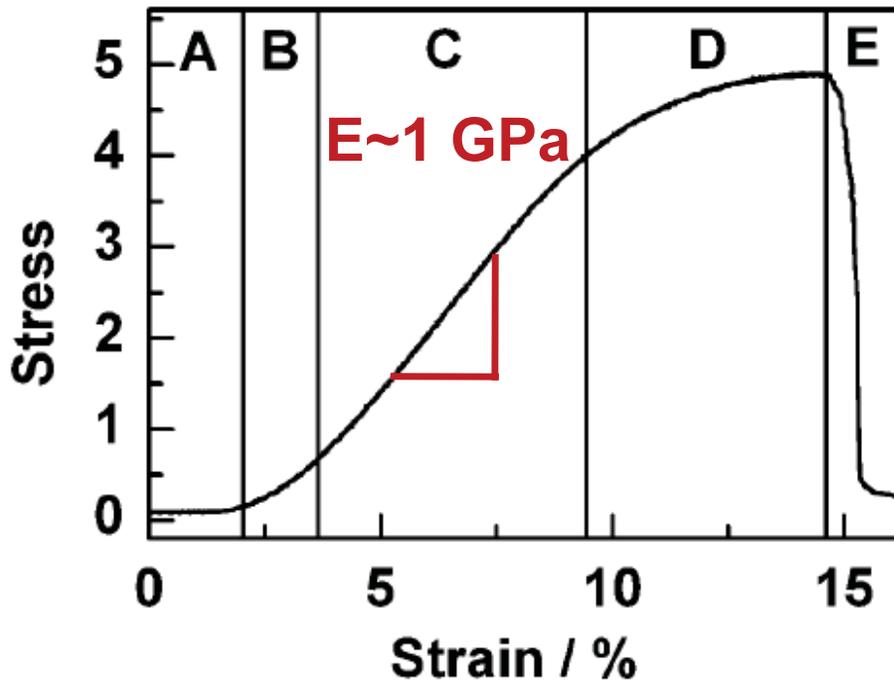
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Tendon



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 Source: Kastelic, J., A. Galeski, and E. Baer. "The Multicomposite Structure of Tendon." *Connective Tissue Research* 6, no. 1 (1978): 11-23.



~Equilibrium
 Stress vs strain curve of rat tail tendon:
 (A-B) "Toe" region,
(C) ~linear region (~HILE)
 (D) plateau,
 (E) rupture of the tendon.

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 Source: Gutschmann, Thomas et al. "Force Spectroscopy of Collagen Fibers to Investigate their Mechanical Properties and Structural Organization." *Biophysical Journal* 86, no. 5 (2004): 3186-93.

- Need 2 independent measurements (2 moduli), to completely characterize an elastic tissue
- Every elastic modulus can then be expressed in terms of those 2 moduli

	bulk	Young's	Lamé #2	Shear	Poisson	Longitudinal
	$K =$	$E =$	$\lambda =$	$G =$	$\nu =$	$M = H$
(K, E)	K	E	$\frac{3K(3K-E)}{9K-E}$	$\frac{3KE}{9K-E}$	$\frac{3K-E}{6K}$	$\frac{3K(3K+E)}{9K-E}$
(K, λ)	K	$\frac{9K(K-\lambda)}{3K-\lambda}$	λ	$\frac{3(K-\lambda)}{2}$	$\frac{\lambda}{3K-\lambda}$	$3K - 2\lambda$
(K, G)	K	$\frac{9KG}{3K+G}$	$K - \frac{2G}{3}$	G	$\frac{3K-2G}{2(3K+G)}$	$K + \frac{4G}{3}$
(K, ν)	K	$3K(1 - 2\nu)$	$\frac{3K\nu}{1+\nu}$	$\frac{3K(1-2\nu)}{2(1+\nu)}$	ν	$\frac{3K(1-\nu)}{1+\nu}$
(K, M)	K	$\frac{9K(M-K)}{3K+M}$	$\frac{3K-M}{2}$	$\frac{3(M-K)}{4}$	$\frac{3K-M}{3K+M}$	M
(E, λ)	$\frac{E+3\lambda+R}{6}$	E	λ	$\frac{E-3\lambda+R}{4}$	$\frac{2\lambda}{E+\lambda+R}$	$\frac{E-\lambda+R}{2}$
(E, G)	$\frac{EG}{3(3G-E)}$	E	$\frac{G(E-2G)}{3G-E}$	G	$\frac{E}{2G} - 1$	$\frac{G(4G-E)}{3G-E}$
(E, ν)	$\frac{E}{3(1-2\nu)}$	E	$\frac{E\nu}{(1+\nu)(1-2\nu)}$	$\frac{E}{2(1+\nu)}$	ν	$\frac{E(1-\nu)}{(1+\nu)(1-2\nu)}$
(λ, G)	$\lambda + \frac{2G}{3}$	$\frac{G(3\lambda+2G)}{\lambda+G}$	λ	G	$\frac{\lambda}{2(\lambda+G)}$	$\lambda + 2G$

Regulation of gene expression in intervertebral disc cells by low and high hydrostatic pressure

(Eur Spine J, 2006)

Cornelia Neidlinger-Wilke · Karin Würtz ·
Jill P. G. Urban · Wolfgang Börm · Markus Arand ·
Anita Ignatius · Hans-Joachim Wilke ·
Lutz E. Claes

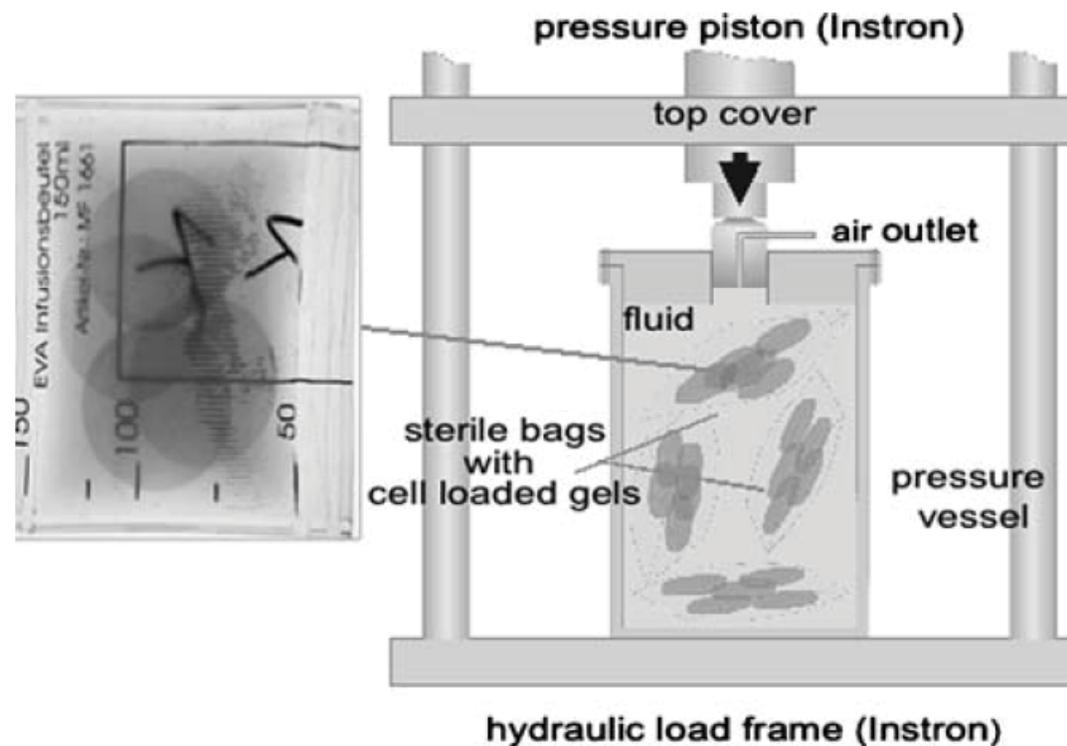
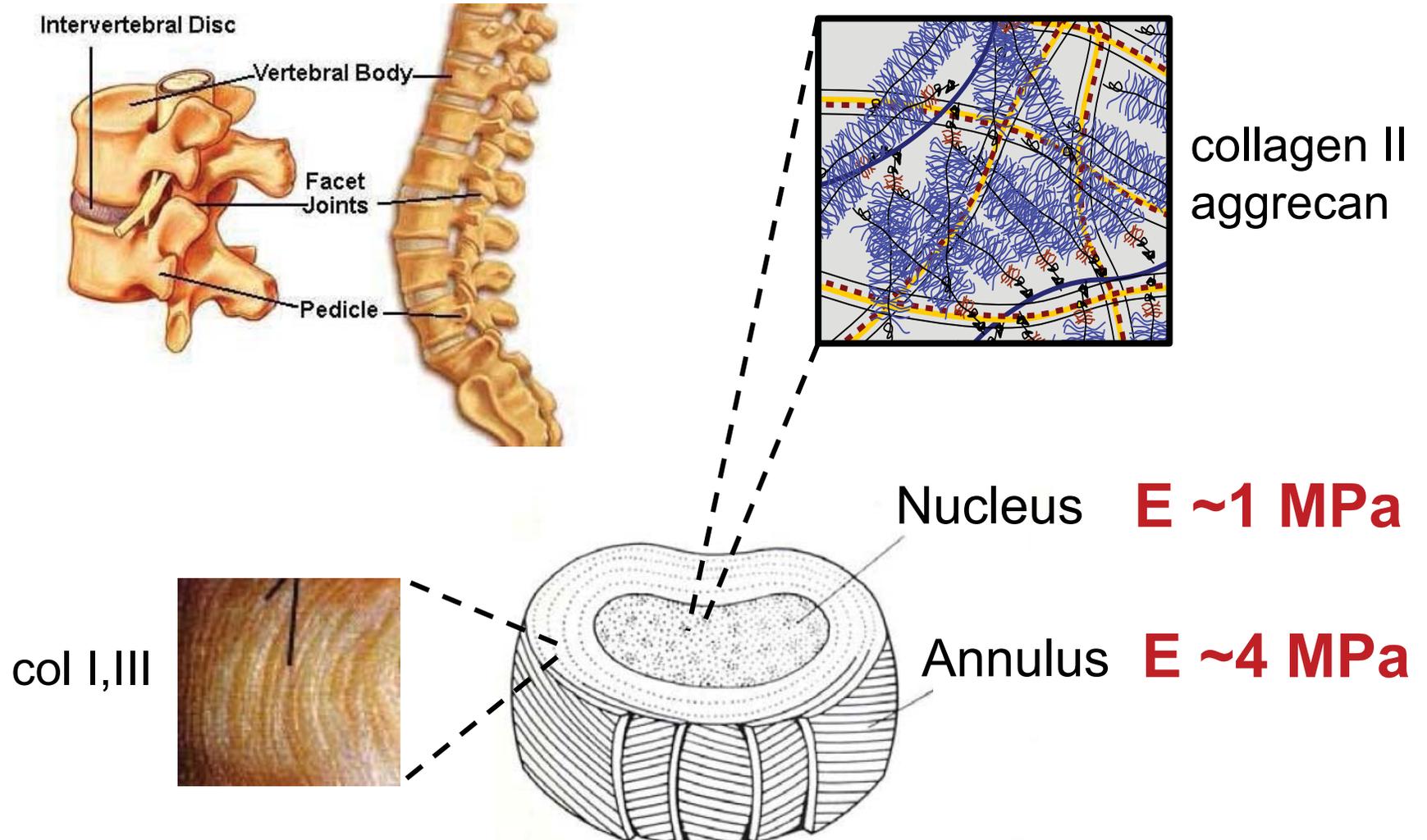


Fig. 1 Scheme of the stimulation device for the application of high hydrostatic pressure (2.5 MPa) and photo of a sterile bag with cell-seeded collagen gels

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Source: Neidlinger-Wilke, Cornelia, et al. "Regulation of Gene Expression in Intervertebral Disc Cells by Low and High Hydrostatic Pressure." *European Spine Journal* 15, no. 3 (2006): 372-8.

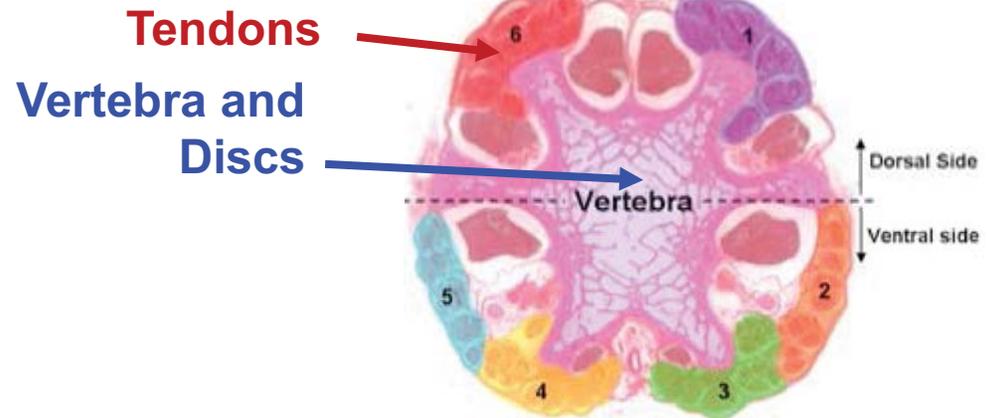
Intervertebral Disc

(Peter Roughley, Spine, 2004)



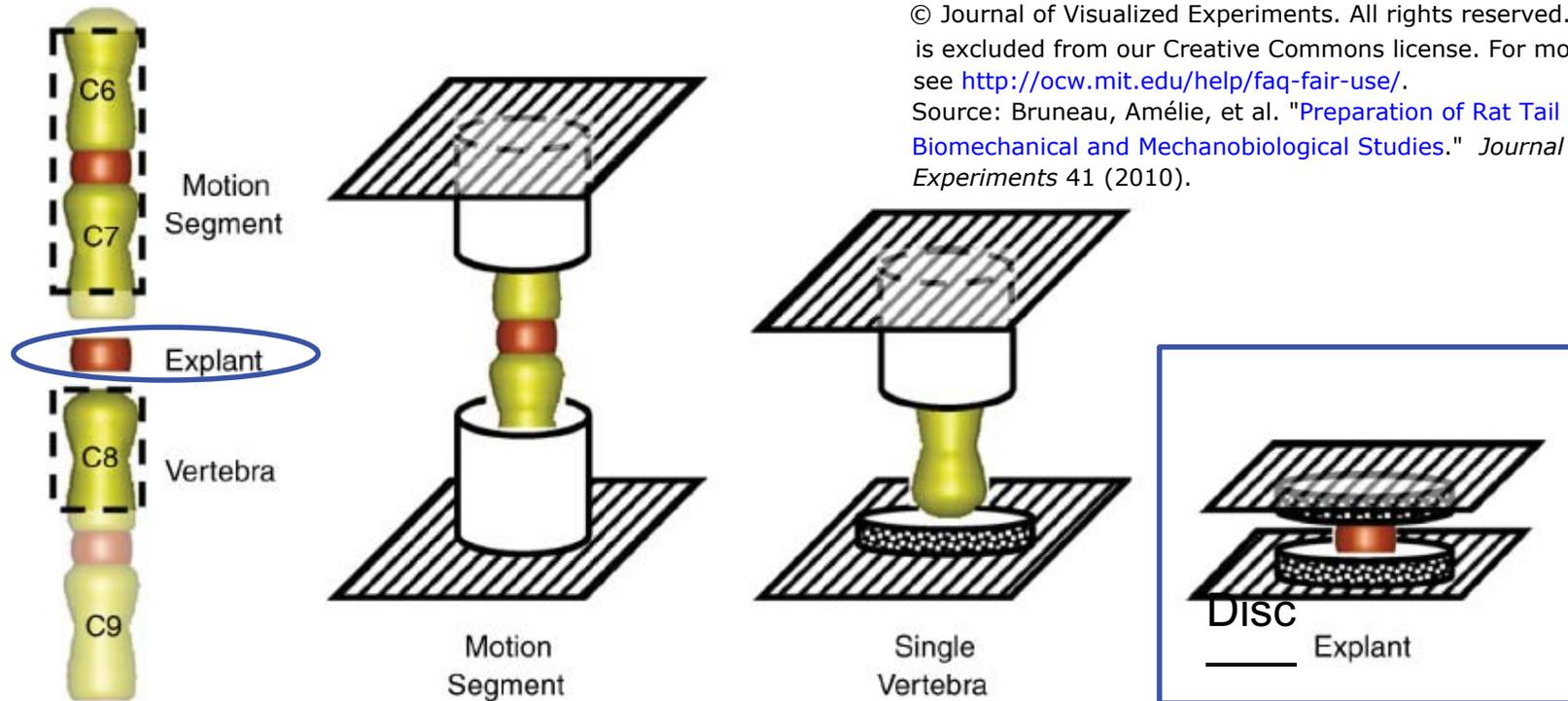
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“Creep-Compression” of intervertebral disc (rat tail)



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Source: Bruneau, Amélie, et al. "Preparation of Rat Tail Tendons for Biomechanical and Mechanobiological Studies." *Journal of Visualized Experiments* 41 (2010).

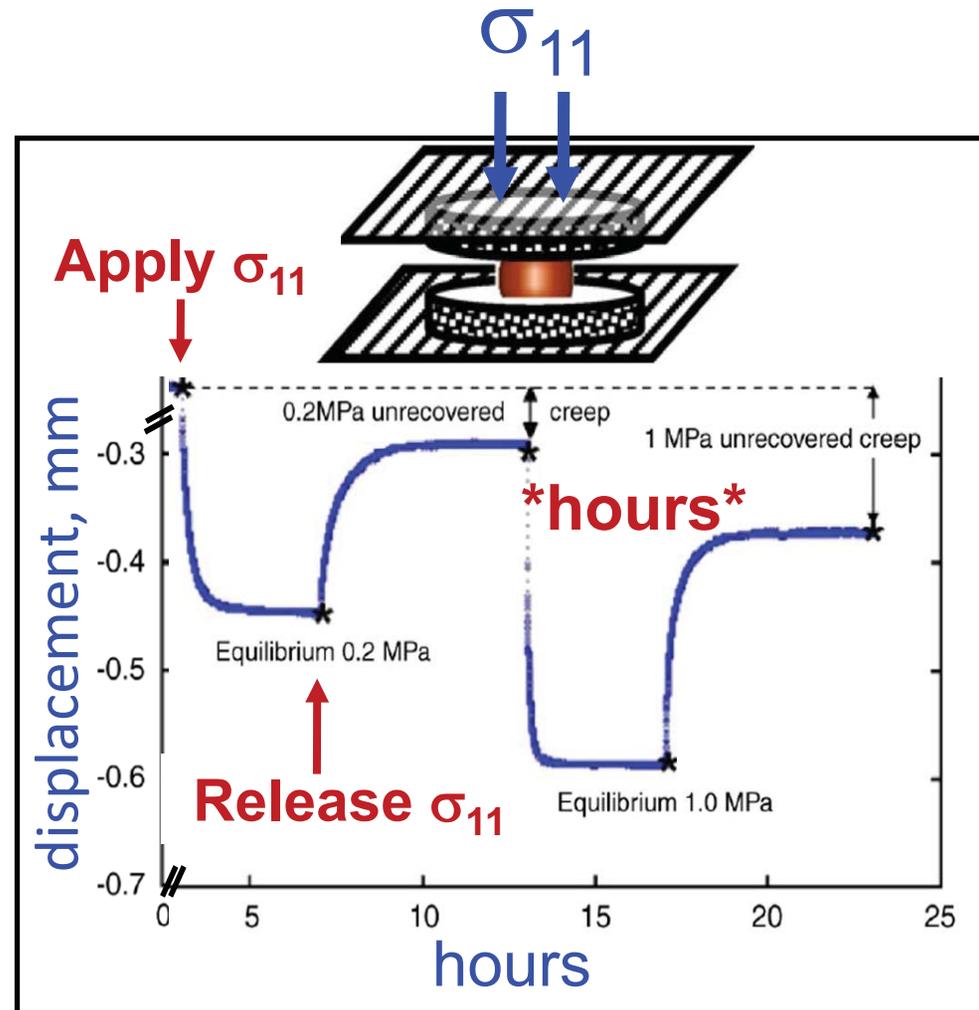


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Source: MacLean, Jeffrey J. "Role of Endplates in Contributing to Compression Behaviors of Motion Segments and Intervertebral Discs." *SPINE* 32, no. 1 (2007): 55-63.

(MacLean+, J Biomechanics, 2007)

“Creep-Compression” of intervertebral disc (rat tail):

Apply constant stress (σ_{11}) and measure displacement (strain) vs time



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Source: MacLean, Jeffrey J. "Role of Endplates in Contributing to Compression Behaviors of Motion Segments and Intervertebral Discs." *-RXUDDORI %LRP HFKDQLFV* 40, no. 1 (2007): 55-63.

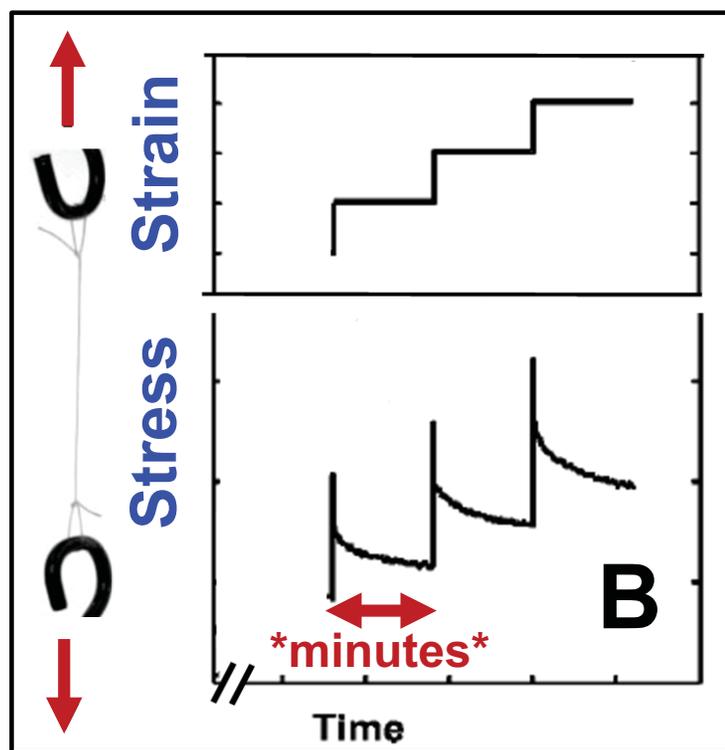
(MacLean+, J Biomechanics, 2007)

Influence of Decorin and Biglycan on Mechanical Properties of Multiple Tendons in Knockout Mice

“Stress Relaxation”

Apply step in strain (ϵ_{11}) and measure stress vs time

Mouse tendon fascicle



Tendon Hierarchy

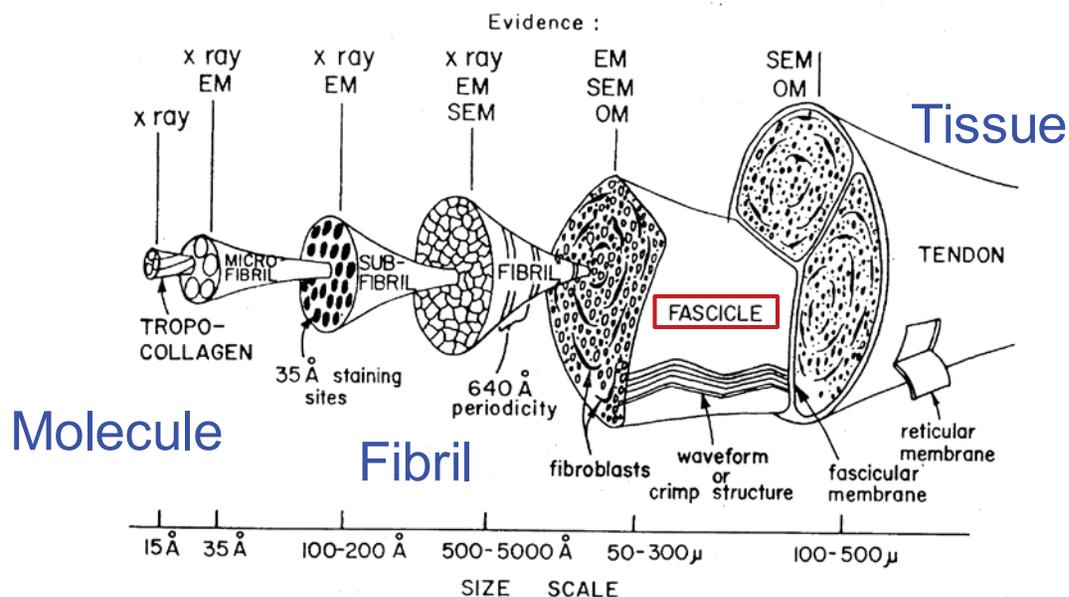


Figure 7.3:6 Hierarchy of structure of a tendon according to Kastelic et al. (1978). Reproduced by permission. Evidences are gathered from X ray, electron microscopy (EM), scanning electron microscopy (SEM), and optical microscopy (OM). (Y.C. Fung)

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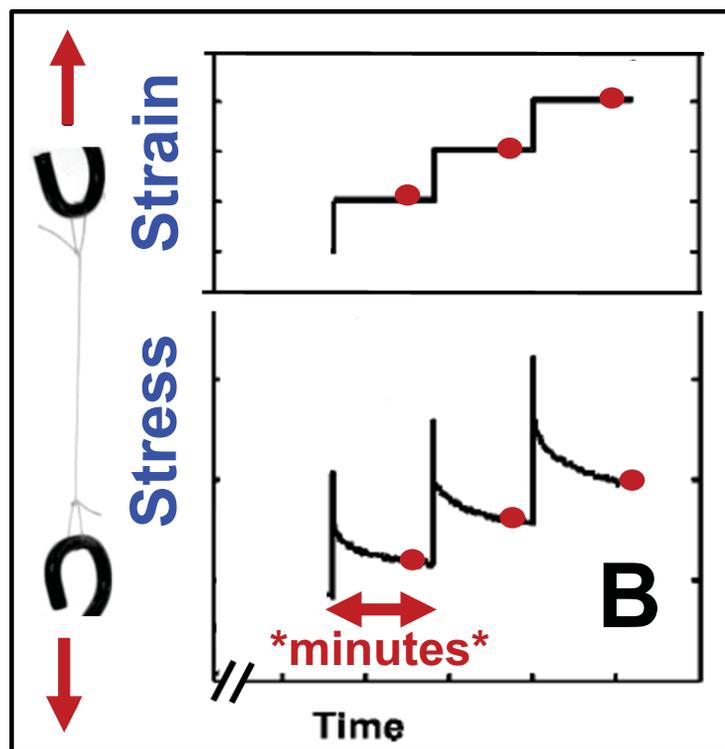
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Tendon Hierarchy

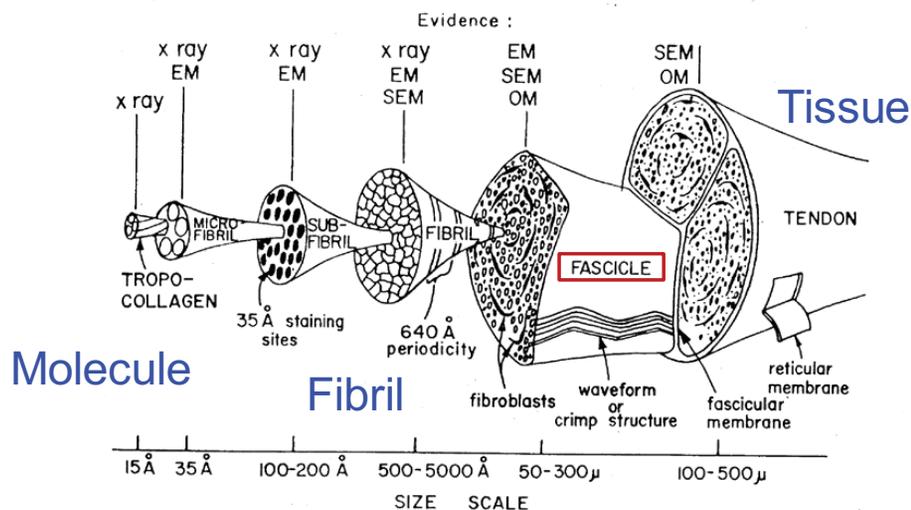
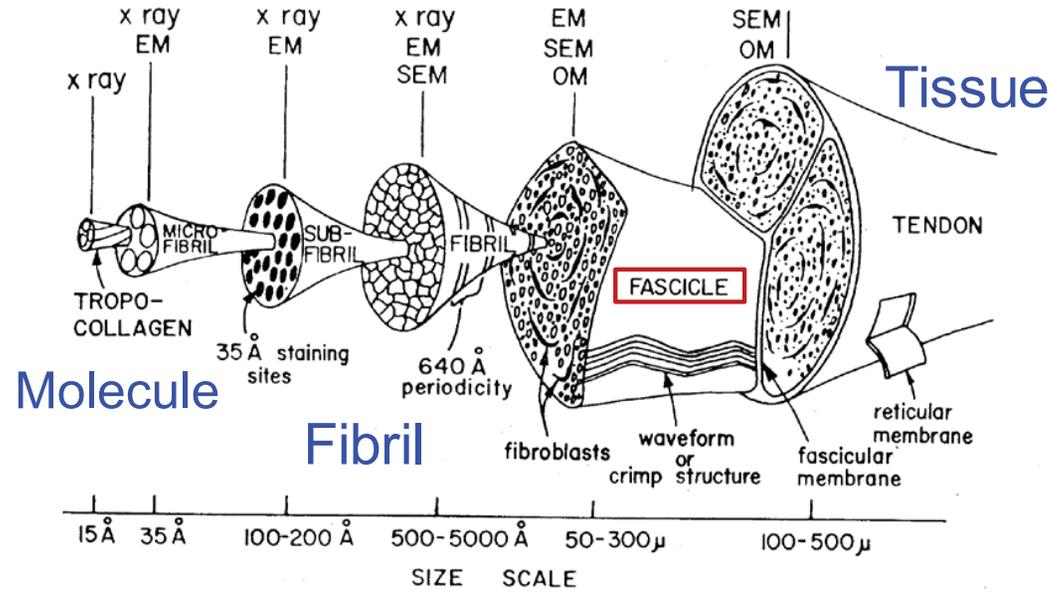


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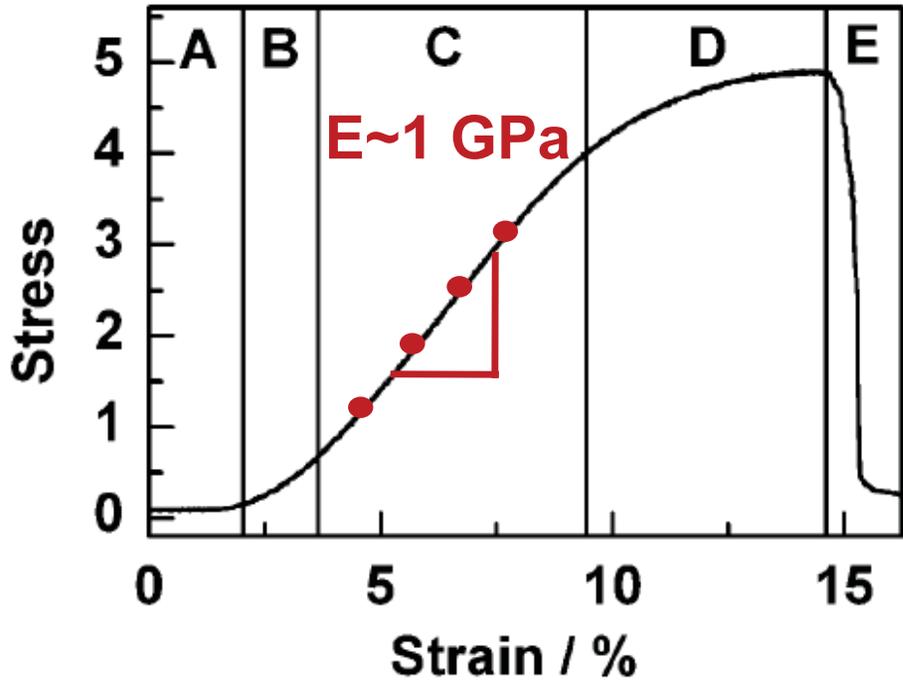
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Tendon



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~Equilibrium
 Stress vs strain curve of rat tail tendon:
 (A-B) "Toe" region,
(C) ~linear region (~HILE)
 (D) plateau,
 (E) rupture of the tendon.

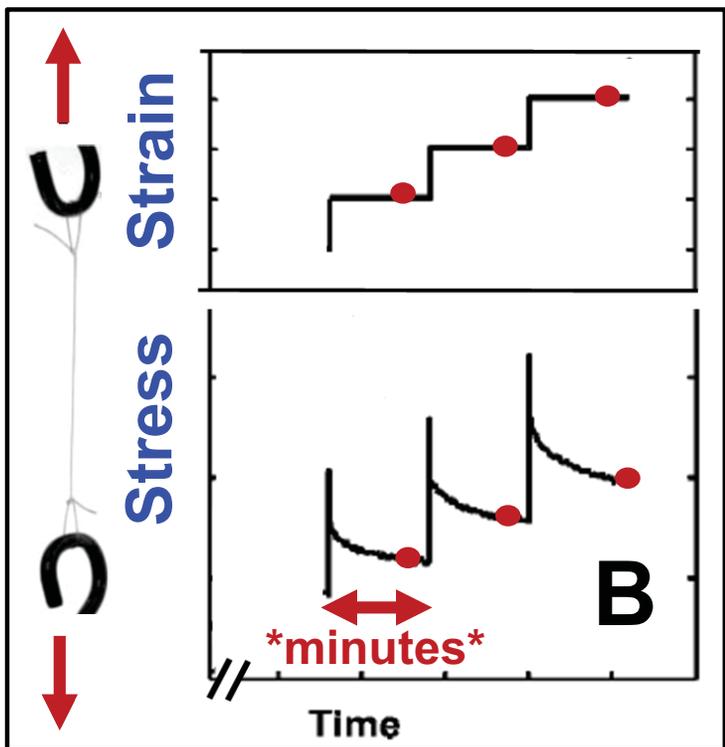
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Influence of **Decorin and Biglycan** on Mechanical Properties of Multiple Tendons in Knockout Mice

“Stress Relaxation”

Molecular- & Tissue-level Mechanisms??

Mouse tendon fascicle



Tendon Hierarchy

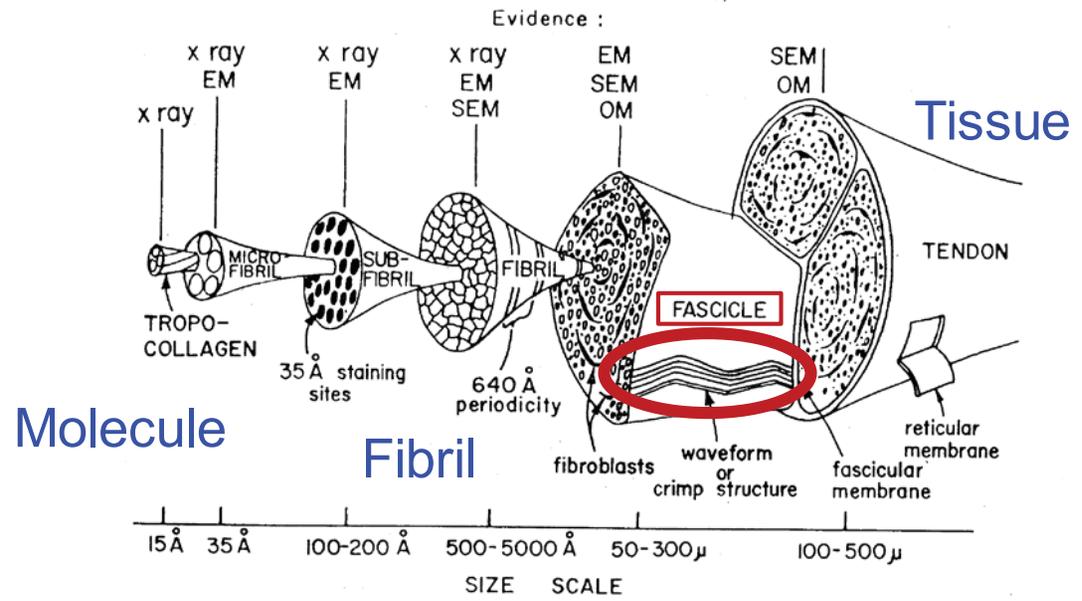


Figure 7.3:6 Hierarchy of structure of a tendon according to Kastelic et al. (1978). Reproduced by permission. Evidences are gathered from X ray, electron microscopy (EM), scanning electron microscopy (SEM), and optical microscopy (OM). (Y.C. Fung)

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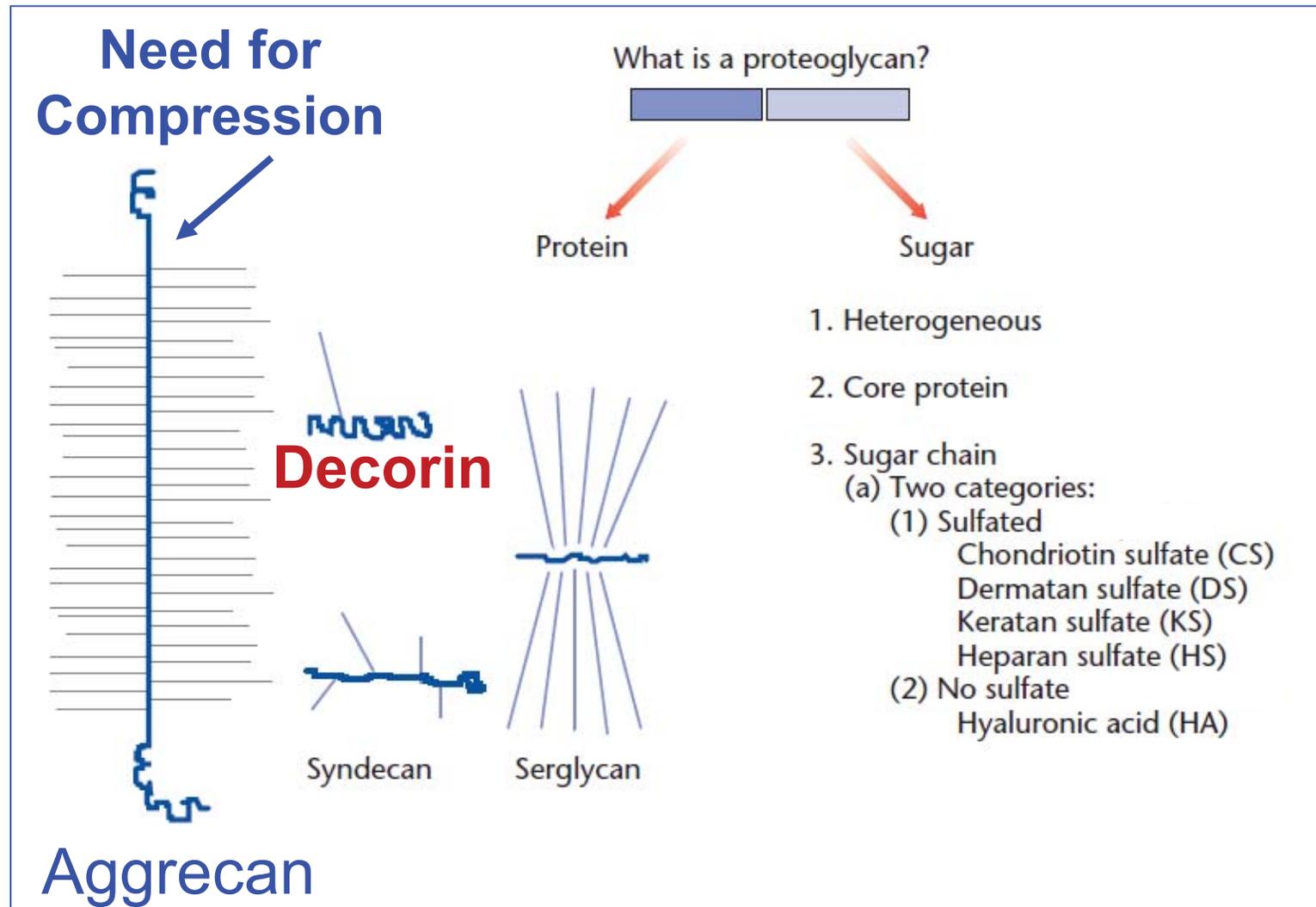
PROTEOGLYCAN SUPERFAMILY

- ECM molecules with (1) Core protein, and (2) Glycosaminoglycan (GAG) chains
 - “Sub-families” include
 - Extracellular • Large Aggregating (Aggrecan)
 - Small Leucine-Rich PG (SLRPs)
 - Cell Surface (e.g., glycocalyx HSPGs)
- 

Proteoglycans

Encyclop Life Sci, 2009

Nancy B Schwartz, *University of Chicago, Illinois, USA*



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Source: Schwartz, Nancy B. "Proteoglycans." eLS (2009).

Table 1. Extracellular matrix proteoglycans (Proteoglycan Superfamily)

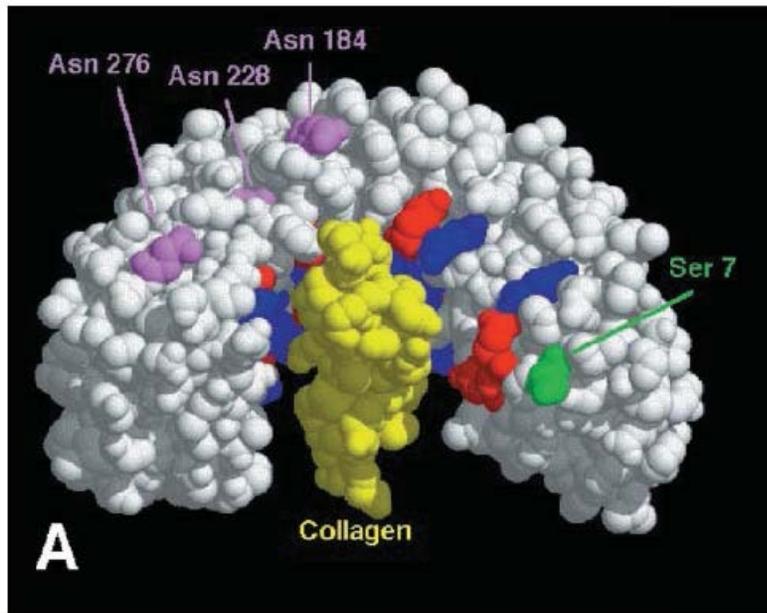
(36 - 42 or more)

GENE NAME	COMMON NAME(S)	DOMAINS	GAGs		
HSPG2	heparan sulfate proteoglycan 2/ perlecan	complex	HS/CS		
ASPN	asporin	LRR	maybe none		
BGN	biglycan		LRR		CS/DS
DCN	decorin		LRR		CS/DS
FMOD	fibromodulin	LRR	KS		
KERA	keratocan	LRR	KS		
LUM	lumican	LRR	KS		
OMD	osteo-modulin/costeo-adherin	LRR	KS		
PRELP	PRELP/prolagrin (pro/arg-end/leu-rich repeat protein)	LRR	KS ??		
EPYC	epiphycan	LRR	CS/DS		
OGN	osteo-glycin/mimecan	LRR	KS		
OPTC	opticin	LRR	??		
CHAD	chondroadherin	LRR	maybe none		
CHADL	chondroadherin-like	LRR	maybe none		
NYX	nyctalopin (probably GPI-linked)	LRR	maybe none		
NEPNP	nephroc (pseudogene in human)	LRR	maybe none		
PODN	podocan	LRR	maybe none		
PODNL1	podocan-like 1	LRR	maybe none		
ACAN	aggrecan	LINK/CLEC/CCP	CS/KS		
BCAN	brevican		LINK/CLEC/CCP	CS	
NCAN	neurocan		LINK/CLEC/CCP	CS	
VCAN	versican		LINK/CLEC/CCP	CS/DS	
HAPLN1	hyaluronan and proteoglycan link protein 1	LINK			
HAPLN2	hyaluronan and proteoglycan link protein 2	LINK			
HAPLN3	hyaluronan and proteoglycan link protein 3	LINK			
HAPLN4	hyaluronan and proteoglycan link protein 4	LINK			
PRG2	proteoglycan 2, bone marrow PG	CLEC			
PRG3	proteoglycan 3	CLEC			
SPOCK1	testican 1	SPARC, Kazal, TY	CS/KS		
SPOCK2	testican 2	SPARC, Kazal, TY	CS/KS		
SPOCK3	testican 3	SPARC, Kazal, TY	CS/KS		
PRG4	proteoglycan 4/lubricin	SO/HX	maybe none		
SRGN	serglycin	serglycin	HS/CS		
IMPG1	interphotoreceptor matrix proteoglycan 1	SEA domain	CS		
IMPG2	interphotoreceptor matrix proteoglycan 2	SEA domain	CS		
ESM1	endocan/endothelial cell-specific molecule 1	IB domain	CS/DS		

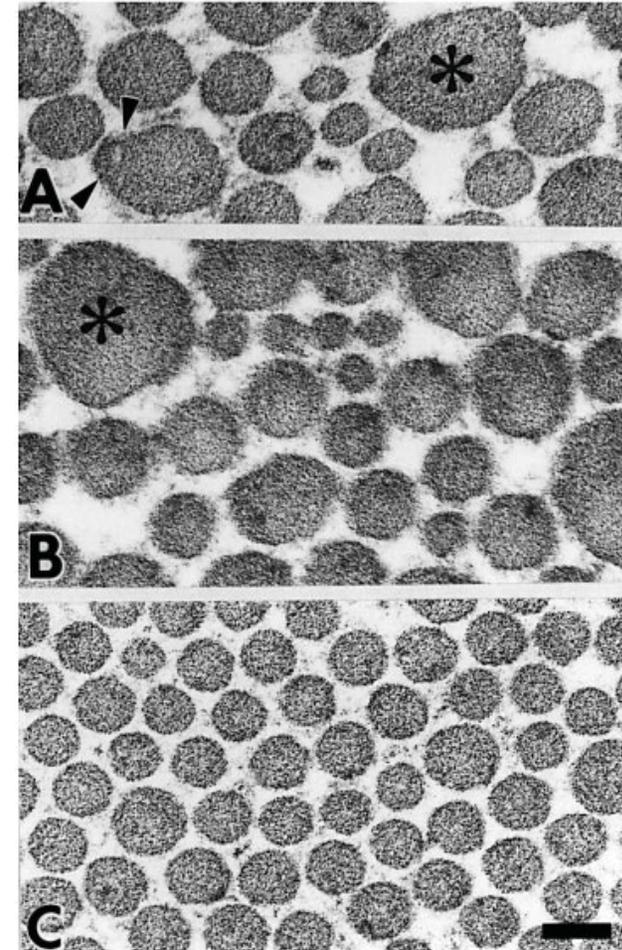
SLRPS

Large Aggregating PGs

Decorin & Collagen Fibrillogenesis



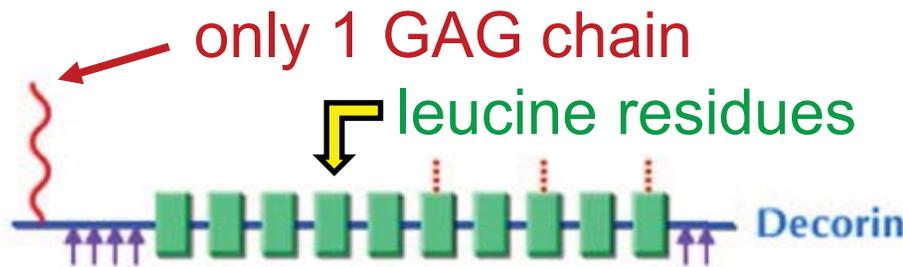
Courtesy of The Journal of Biological Chemistry. Used with permission.
Source: Iozzo, Renato V. "The Biology of the Small Leucine-rich Proteoglycans Functional Network of Interactive Proteins." *Journal of Biological Chemistry* 274, no. 27 (1999): 18843-6.



SKIN
decorin
KO

decorin
KO

Normal
(WT)

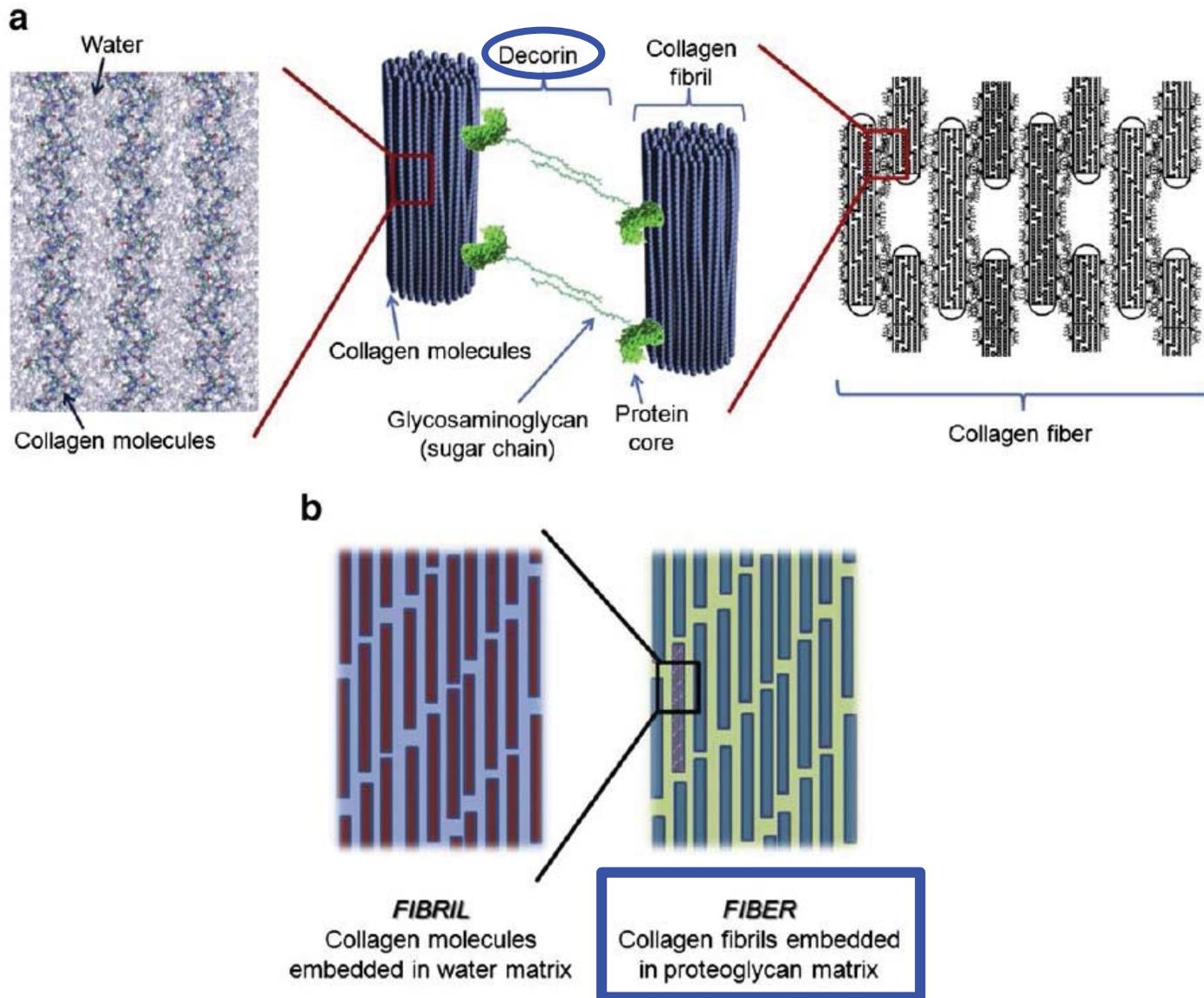


**Example of
Small-Leucine-Rich
Proteoglycans**

Figure 4 Ultrastructural appearance of dermal collagen from the skin of decorin null (*A* and *B*) and wild-type (*C*) mice. Notice the larger and irregular cross-sectional profiles in the decorin null collagen fibers (*asterisks*) with evidence of lateral fusion (*A*, *arrowheads*). Bar: 90 nm.

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Source: Iozzo, Renato V. "Matrix Proteoglycans: From Molecular Design to Cellular Function." *Annual Review of Biochemistry* 67, no. 1 (1998): 609-52.

(Iozzo +, Normal and decorin null mice, J Biol Chem 1999)



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 Source: Gautieri, Alfonso et al. "Viscoelastic Properties of Model Segments of Collagen Molecules." *Matrix Biology* 31, no. 2 (2012): 141-9.

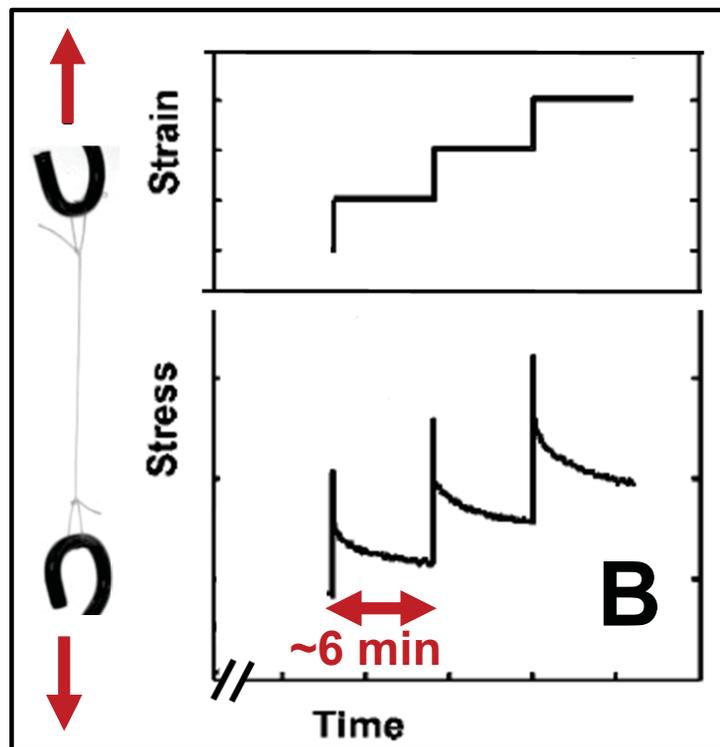
Gauteri, Buehler et al., *Matrix Biology*, 31:141-9, 2012

Influence of Decorin and Biglycan on Mechanical Properties of Multiple Tendons in Knockout Mice

“Stress Relaxation”

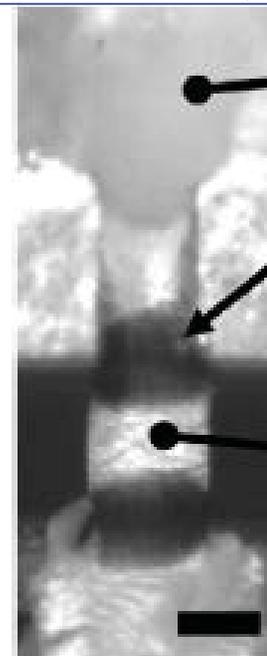
Apply step in strain (ϵ_{11}) and *measure stress vs time*

Mouse tendon fascicle



decorin k/o
Modulus ↓

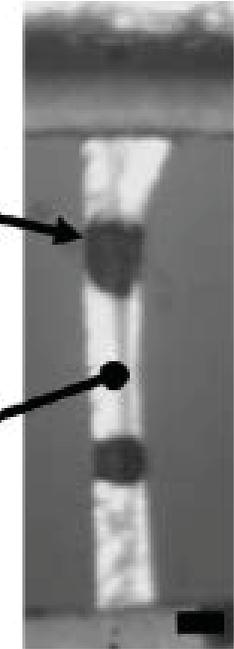
Biglycan k/o
Modulus ↑



Patella

Stain lines for
optical strain
measurement

Tendon



Patellar (left) and flexor digitorum longus (right)

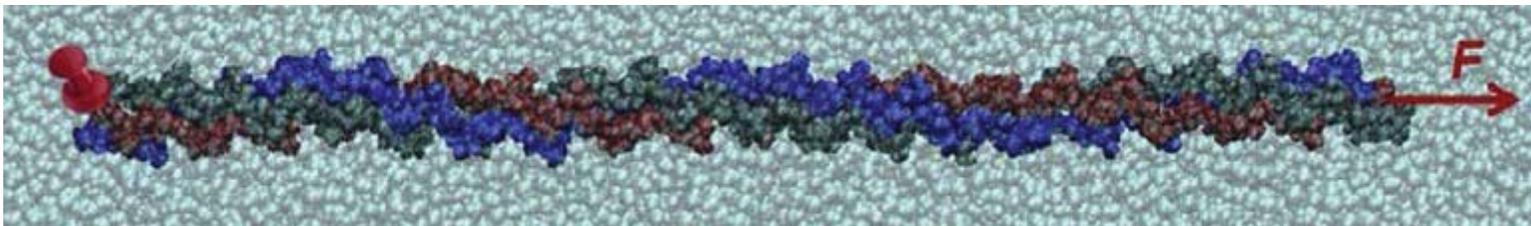
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Source: Robinson, Paul S., et al. "Influence of Decorin and Biglycan on Mechanical Properties of Multiple Tendons in Knockout Mice." *Journal of Biomechanical Engineering* 127, no. 1 (2005): 181-5.

“Lumped Element” Viscoelastic Models

Viscoelastic properties of model segments of collagen molecules

Alfonso Gautieri ^{a,b}, Simone Vesentini ^b, Alberto Redaelli ^b, Markus J. Buehler ^{a,c,*}

-a deep understanding of the relationship between molecular structure and mechanical properties remains elusive, hindered by the complex hierarchical structure of collagen-based tissues...
- Although extensive studies of viscoelastic properties have been pursued at the macroscopic (fiber/tissue) level, fewer investigations have been performed at the smaller scales, including collagen molecules and fibrils.
- Here, using atomistic modeling, we perform “in silico” creep tests of a collagen-like peptide.....relate time-dependence to molecular structure



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Source: Gautieri, Alfonso et al. "Viscoelastic Properties of Model Segments of Collagen Molecules." *Matrix Biology* 31, no. 2 (2012): 141-9.

“In silico” creep test of a **segment of a collagen molecule**

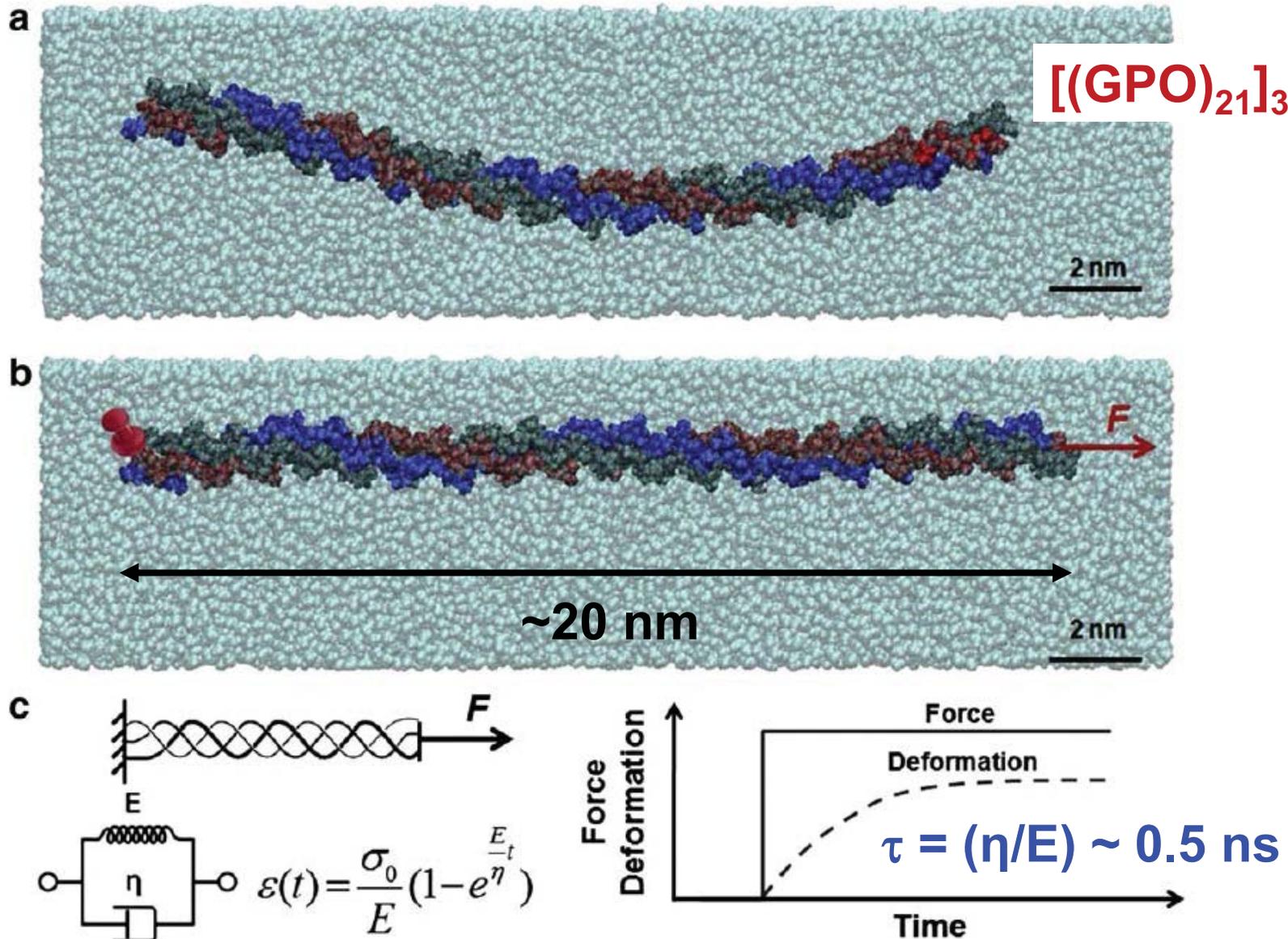
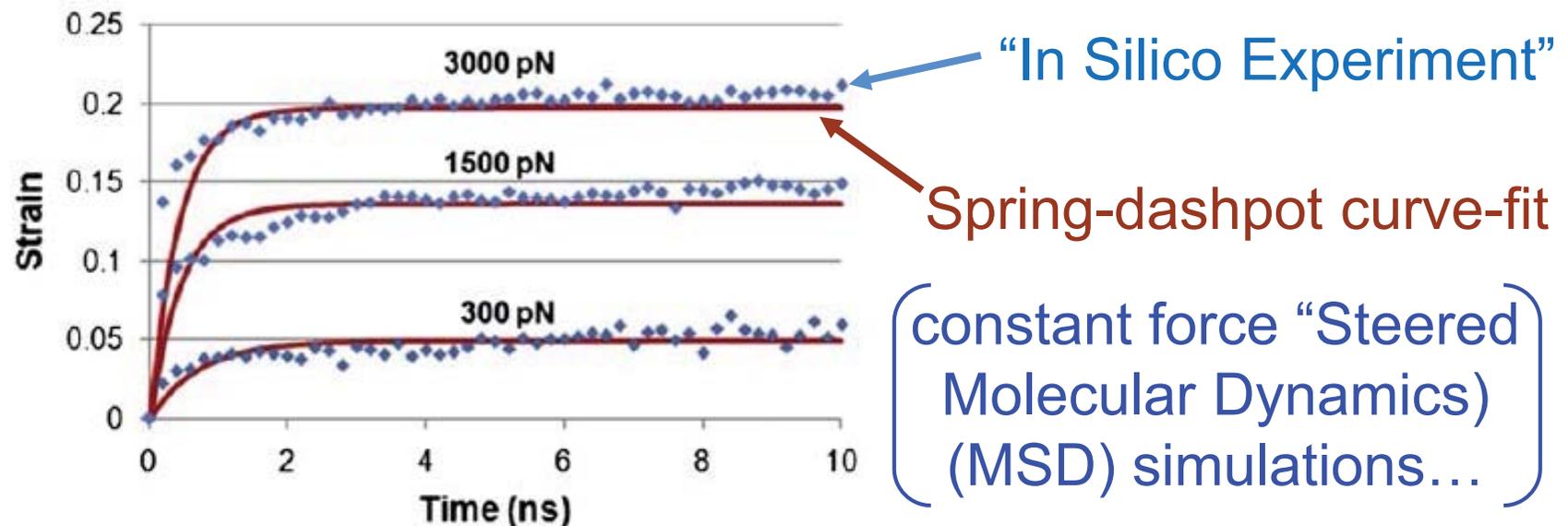


Fig. 1. Snapshots of the collagen peptide in water box. Panel a shows the conformation of the full atomistic model of a $[(GPO)_{21}]_3$ collagen peptide solvated in water box and equilibrated for 30 ns. After equilibration the molecule is subjected to virtual creep tests: one end of the collagen peptide is held fixed, whereas the other end is pulled with constant force (from 300 pN to 3000 pN) until end-to-end distance reaches equilibrium (Panel b). Panel c shows a schematic of the creep test; a constant force is applied instantaneously to the molecule and its response (deformation over time) is monitored. The mechanical response of collagen molecule is modeled using a KV model, from which molecular Young's modulus (E) and viscosity (η) are calculated.

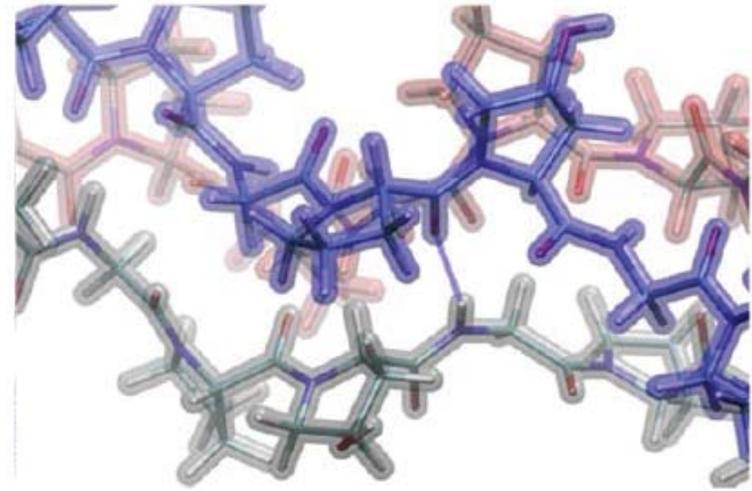
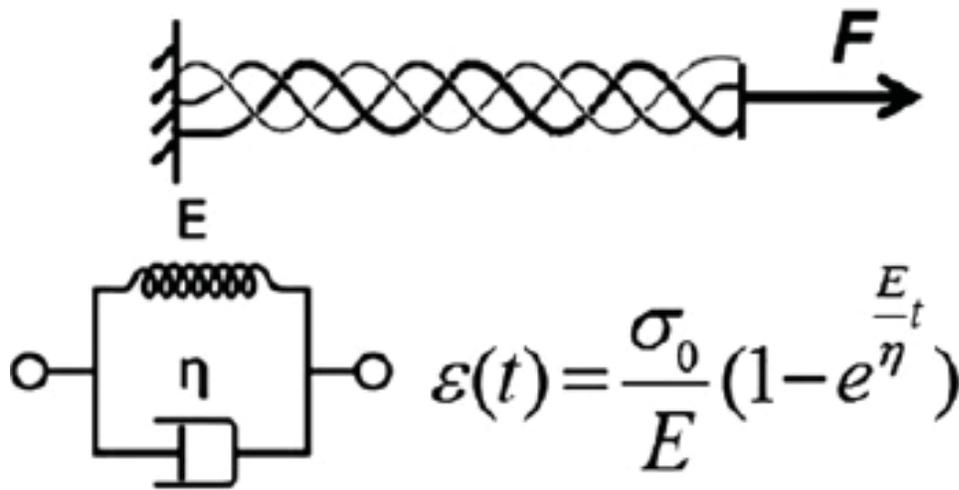
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 Source: Vesentini, Simone, et al. "Nanomechanics of Collagen Microfibrils." *Muscles, Ligaments and Tendons Journal* 3, no. 1 (2013): 23.

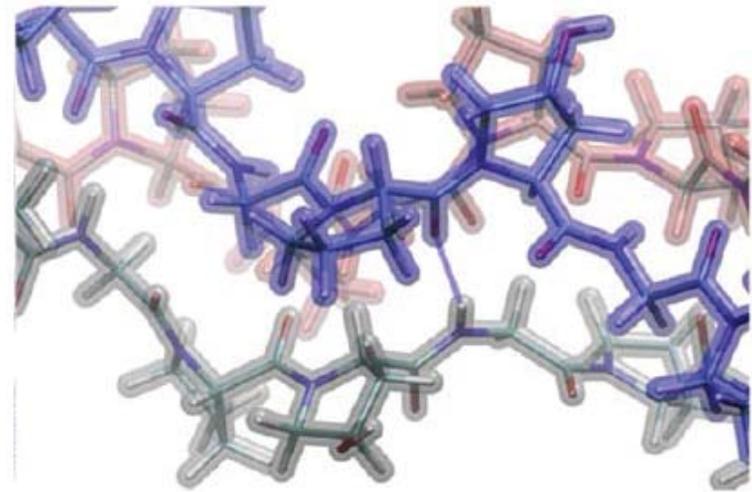
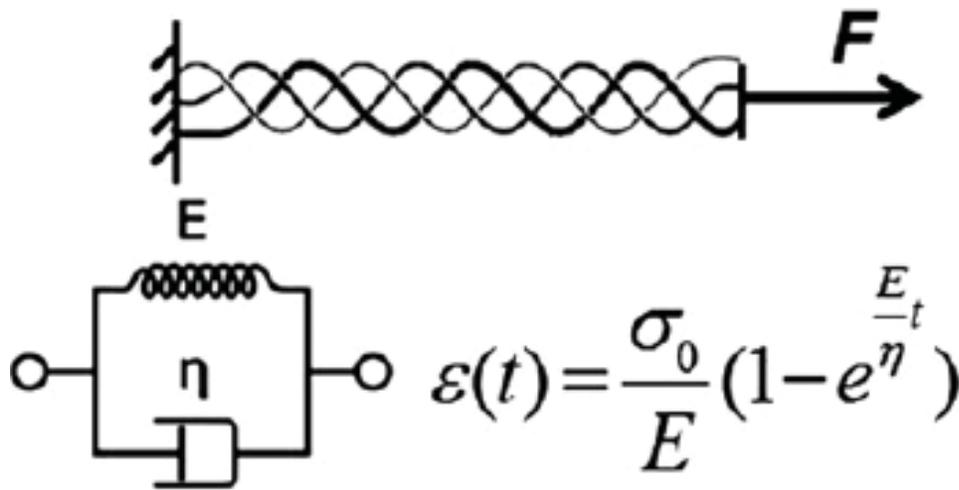
Fig. 2. Single molecule creep test. Mechanical response of solvated collagen molecule to creep tests for three cases with increasing value of external force. Dots represent the experimental data, whereas curves represent the fitted curves using a Kelvin–Voigt model.

$$\tau = (\eta/E) \sim 0.5 \text{ ns}$$



We use the KV model to fit the extension-time curves since this model is the most basic viscoelastic mechanical model available and it provides an excellent fit to the measured mechanical response. It

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 Source: Vesentini, Simone, et al. "Nanomechanics of Collagen Microfibrils." *Muscles, Ligaments and Tendons Journal* 3, no. 1 (2013): 23.

We use the KV model to fit the extension-time curves since this model is the most basic viscoelastic mechanical model available and it provides an excellent fit to the measured mechanical response. It is of great interest to discuss whether the two elements of the KV model, i.e. the purely elastic spring and the purely viscous dashpot, have an actual physical meaning. A likely explanation would be that the elastic spring corresponds to the protein backbone, while the damping effect could be attributed to the interchain H-bonds. The backbone deformation include dihedral, angle and bond deformation, which are terms expressed by harmonic (or similar) functions in the molecular dynamics force field, and thus result in an elastic response to stretching. On the other hand, the viscous behavior may be due to the breaking and reforming of H-bonds, in particular H-bonds between the three collagen chains.



“In silico” creep test of a **segment of a collagen molecule**

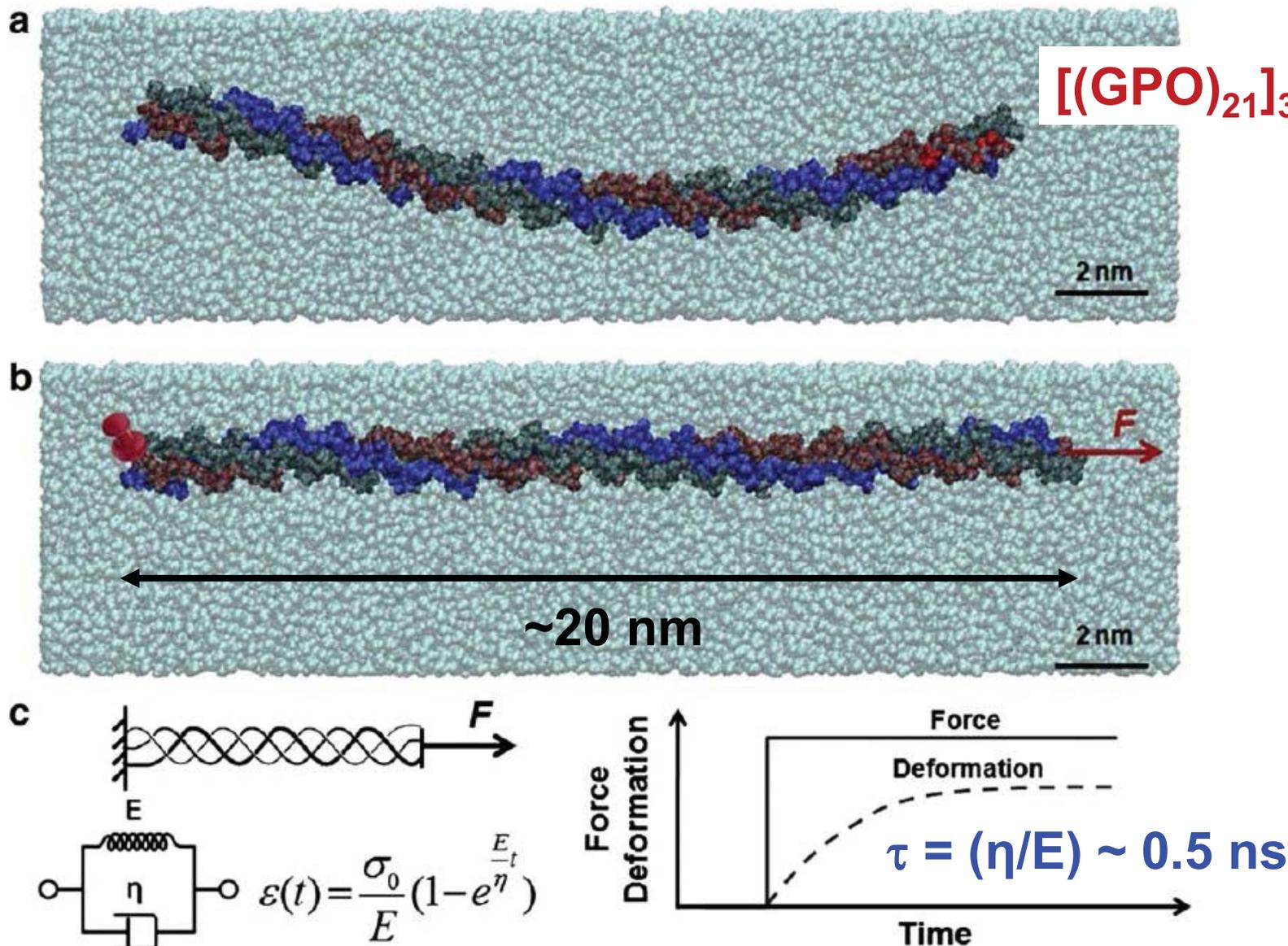


Fig. 1. Snapshots of the collagen peptide in water box. Panel a shows the conformation of the full atomistic model of a $[(\text{GPO})_{21}]_3$ collagen peptide solvated in water box and equilibrated for 30 ns. After equilibration the molecule is subjected to virtual creep tests: one end of the collagen peptide is held fixed, whereas the other end is pulled with constant force (from 300 pN to 3000 pN) until end-to-end distance reaches equilibrium (Panel b). Panel c shows a schematic of the creep test; a constant force is applied instantaneously to the molecule and its response (deformation over time) is monitored. The mechanical response of collagen molecule is modeled using a KV model, from which molecular Young's modulus (E) and viscosity (η) are calculated.

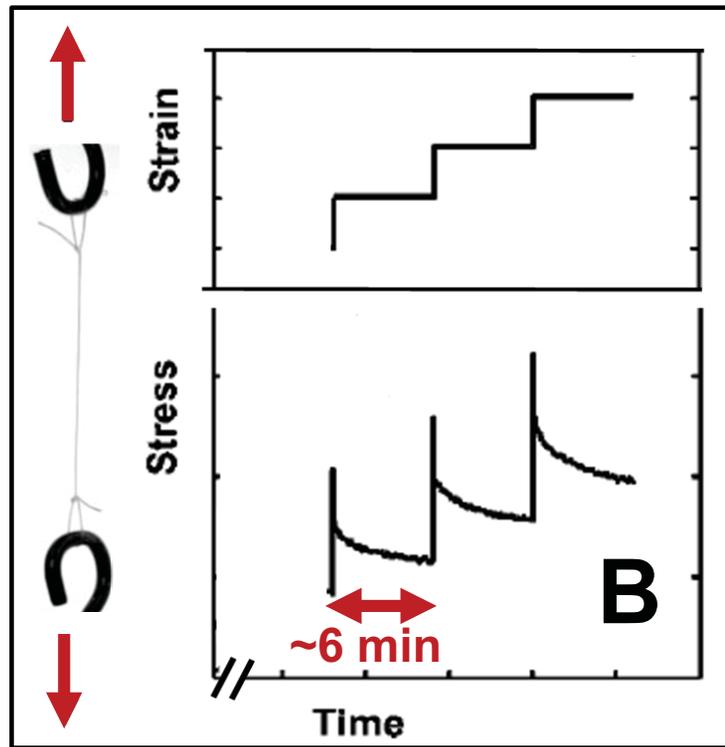
Courtesy of Elsevier, Inc., <http://www.sciencedirect.com>. Used with permission.
 Source: Gautieri, Alfonso et al. "Viscoelastic Properties of Model Segments of Collagen Molecules." *Matrix Biology* 31, no. 2 (2012): 141-9.

Influence of Decorin and Biglycan on Mechanical Properties of Multiple Tendons in Knockout Mice

“Stress Relaxation”

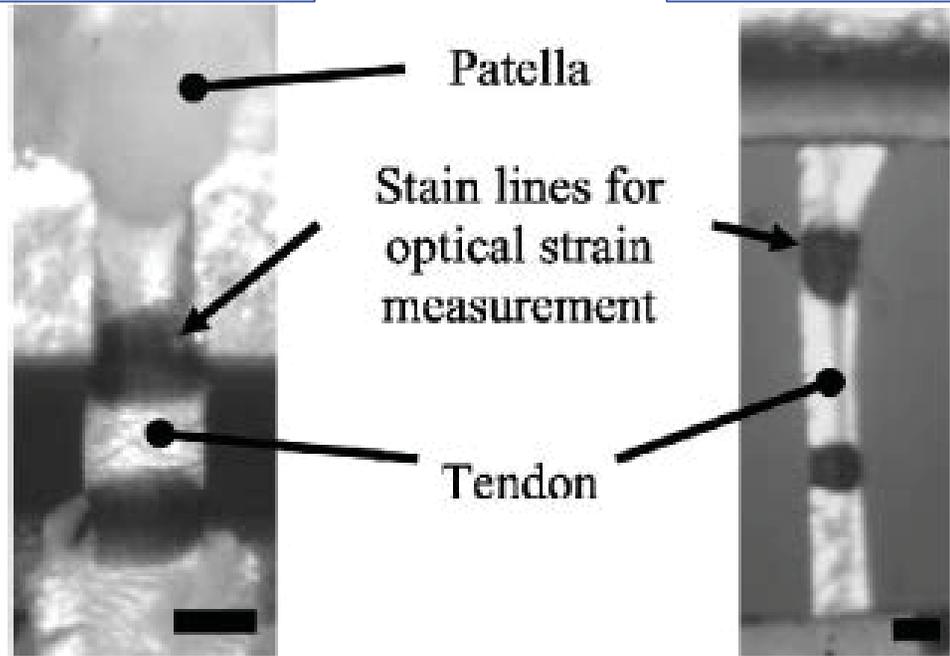
Apply constant strain (ϵ_{11}) and measure stress vs time

Mouse tendon fascicle



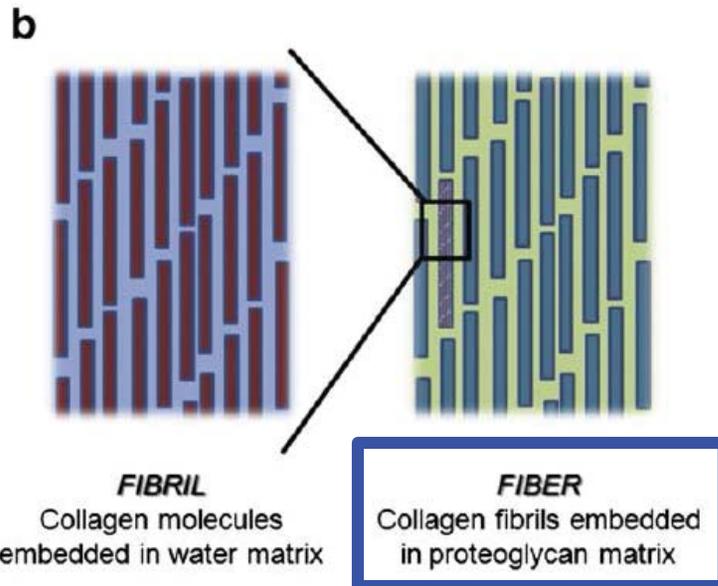
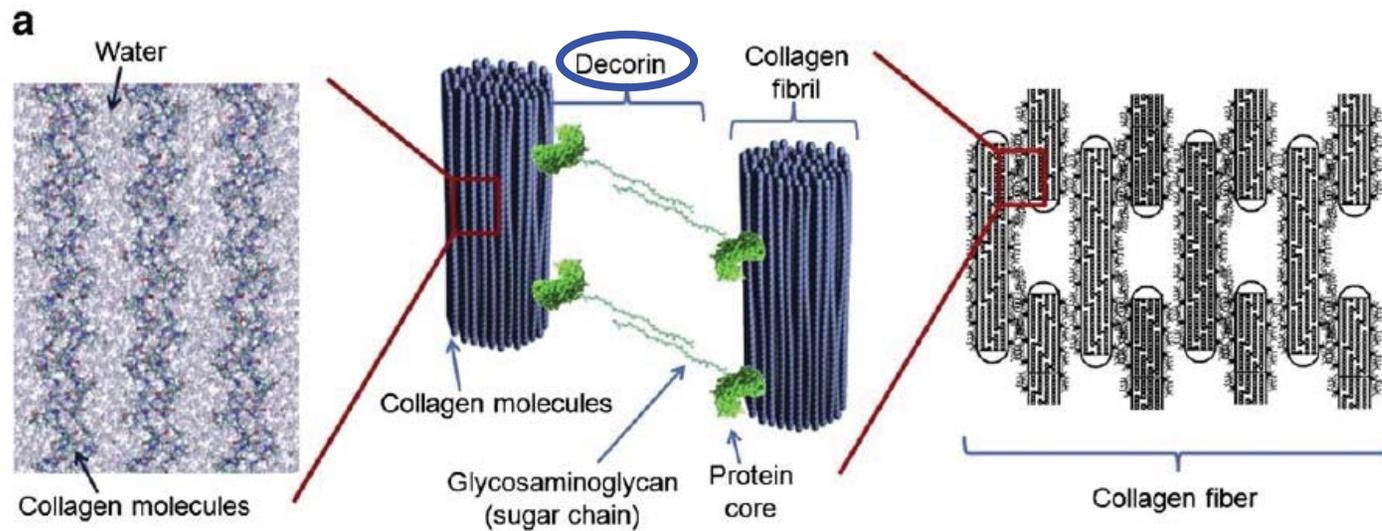
decorin k/o
Modulus

Biglycan k/o
Modulus ↑



Patellar (left) and flexor digitorum longus (right)

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 Source: Robinson, Paul S., et al. "Influence of Decorin and Biglycan on Mechanical Properties of Multiple Tendons in Knockout Mice." *Journal of Biomechanical Engineering* 127, no. 1 (2005): 181-5.



("poroelasticity")

$$\tau = (\eta/E)$$

-the viscous behavior of fibrils and fibers involves additional mechanisms, such as molecular sliding between collagen molecules within the fibril or effects of relaxation of larger volumes of solvent

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