

Curvature

Position | Tangency | Curvature - Continuity

In Defense of the Curve

A Story of the Organic

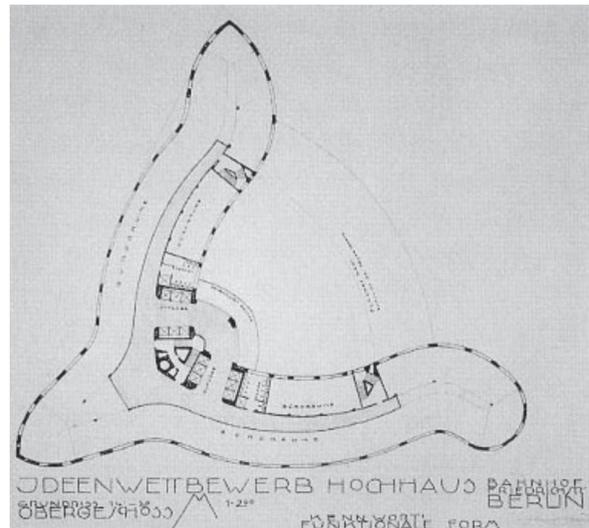
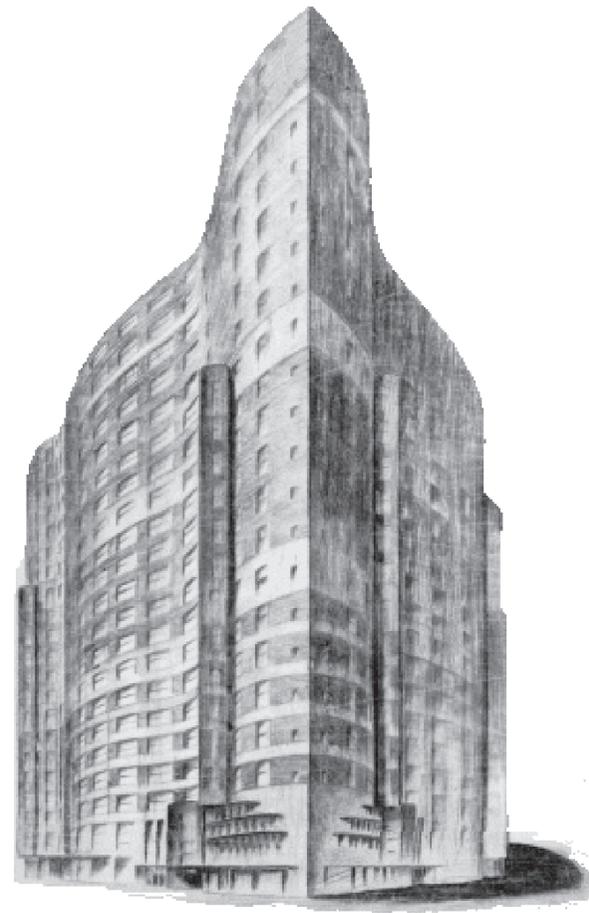
HUGO HÄRING

VS

LUDWIG MIES VAN DER ROHE

In a conversation between Mies van der Rohe and Hugo Häring, Mies inquires, “our steel beams, they have been born straight haven’t they?” he then argues, “It takes a great deal of effort to bend them”.

MIES VAN DER ROHE “MIES SPEAKS: I DO NOT DESIGN BUILDINGS.”
ARCHITECTURAL REVIEW, NO. 862, DECEMBER 1968: 452.



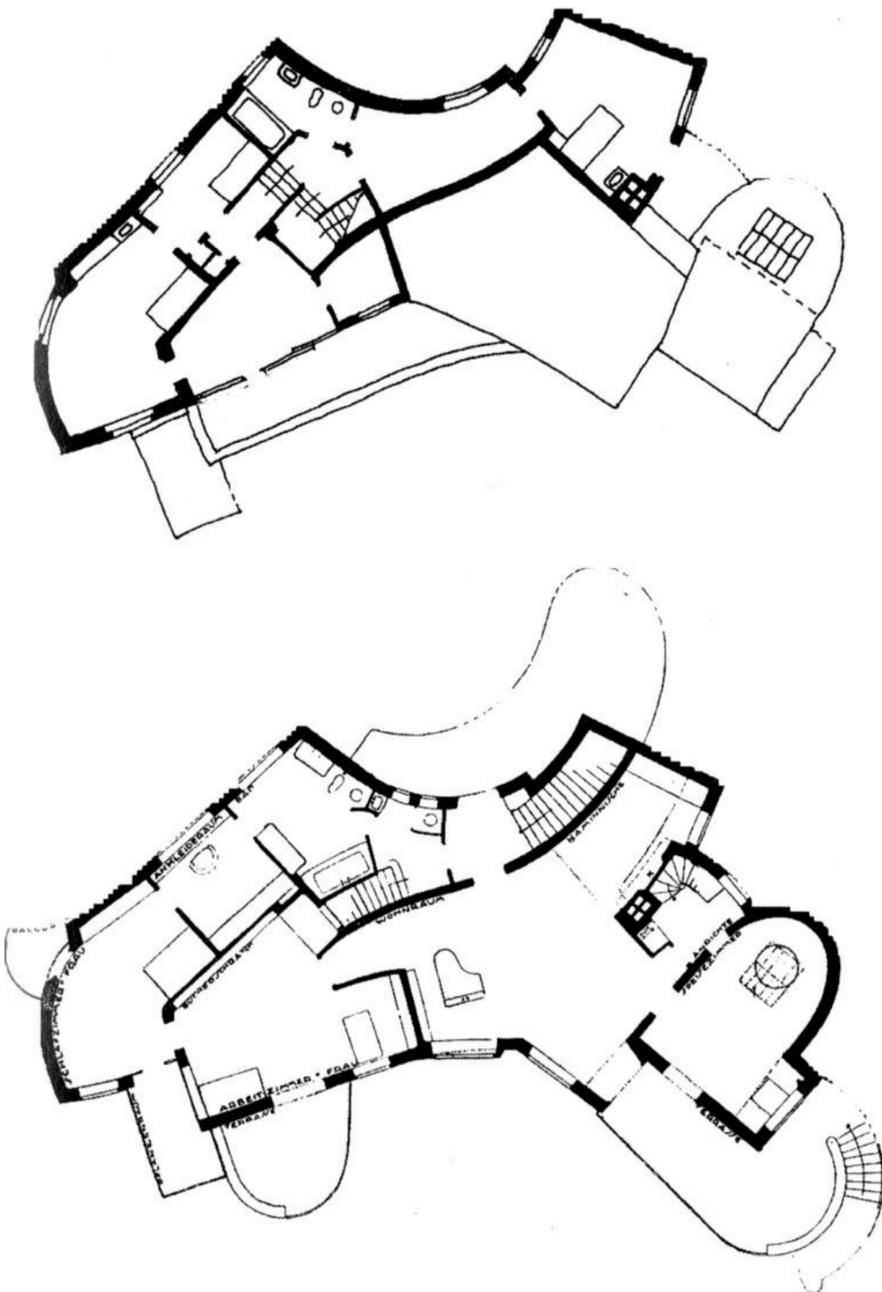
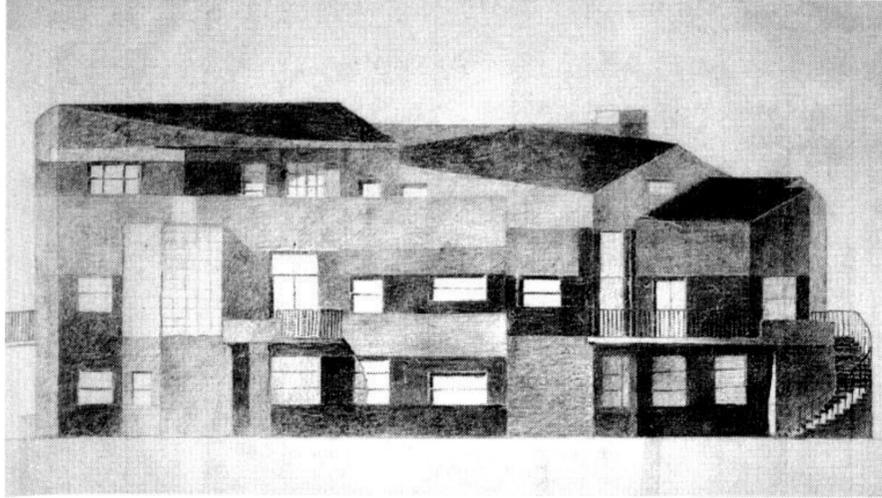
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Hugo Häring, Friedrichstrasse Office Building, 1922, Competition Entry (left)

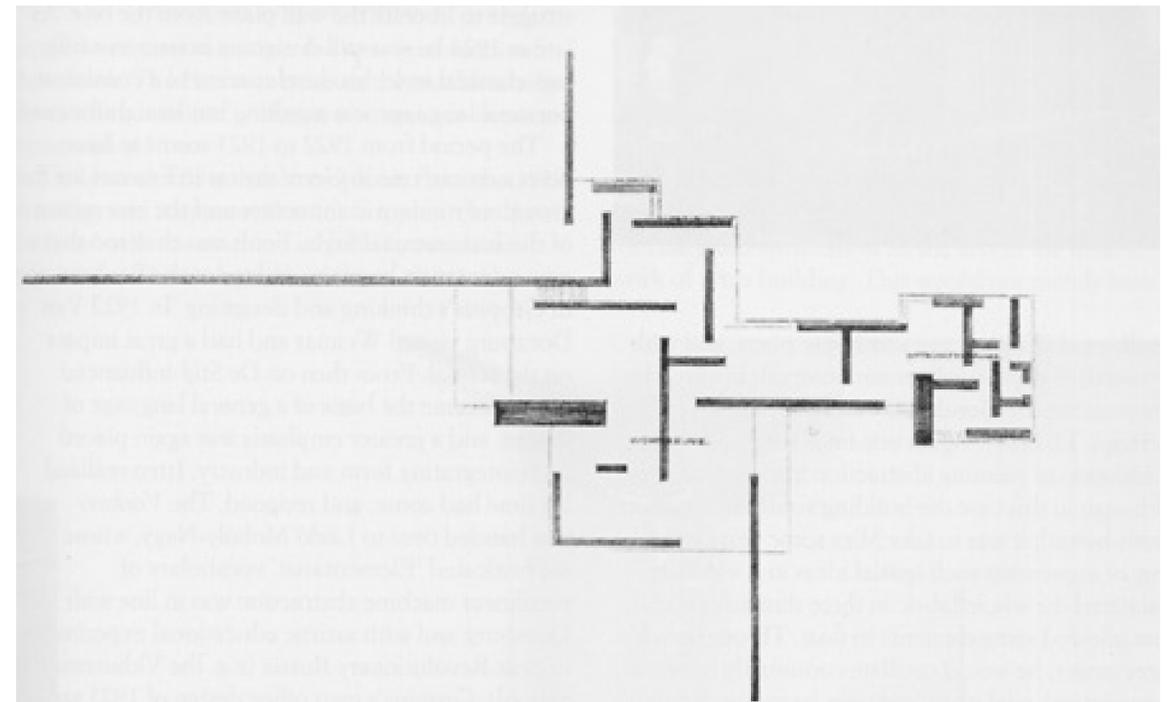


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Ludwig Mies van der Rohe, Friedrichstrasse Office Building, 1922, Competition Entry (right)



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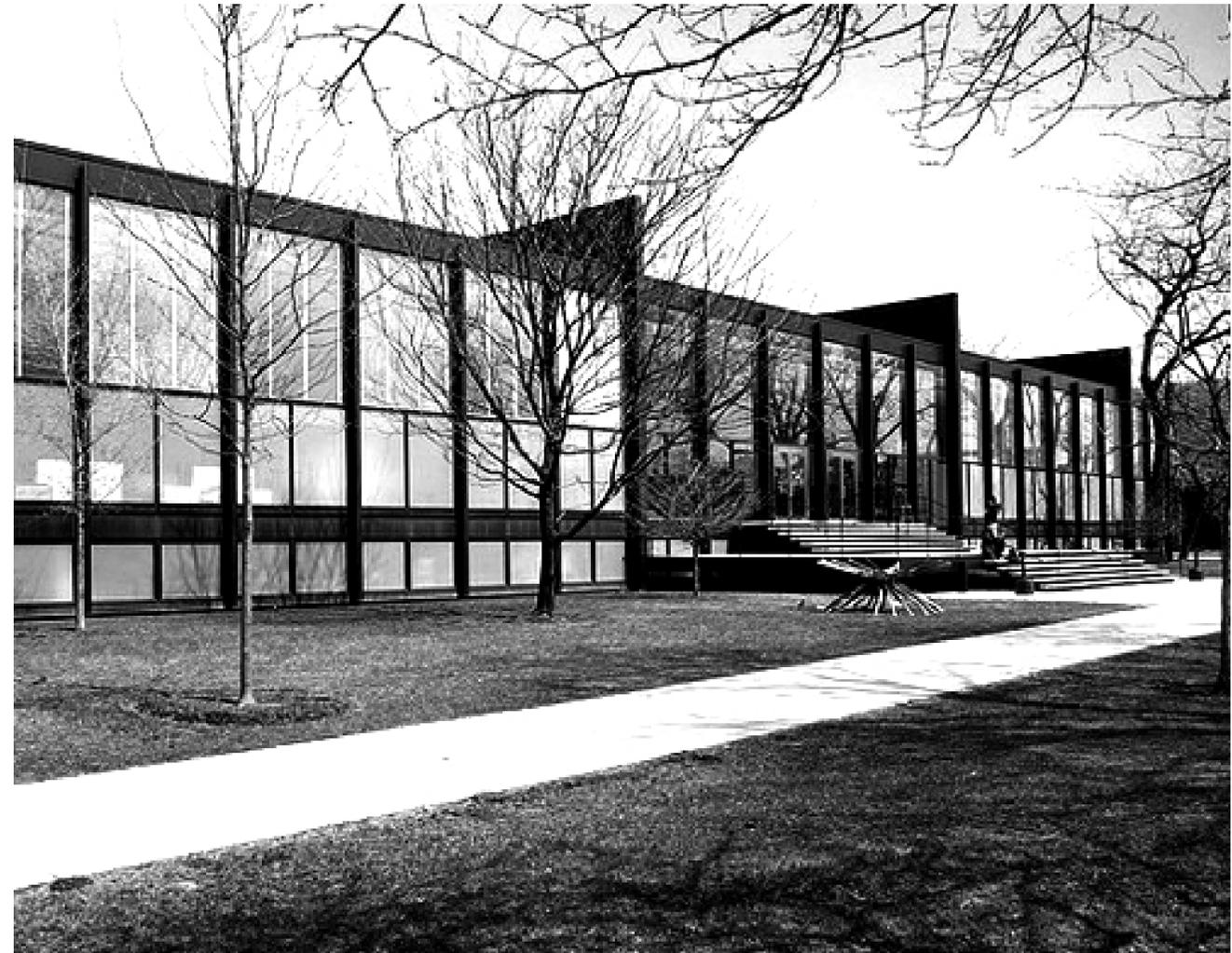
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Hugo Häring, Country House, 1923/24, Elevation and Plans (left)
Ludwig Mies van der Rohe, Brick Country House, 1923, Plan (above)



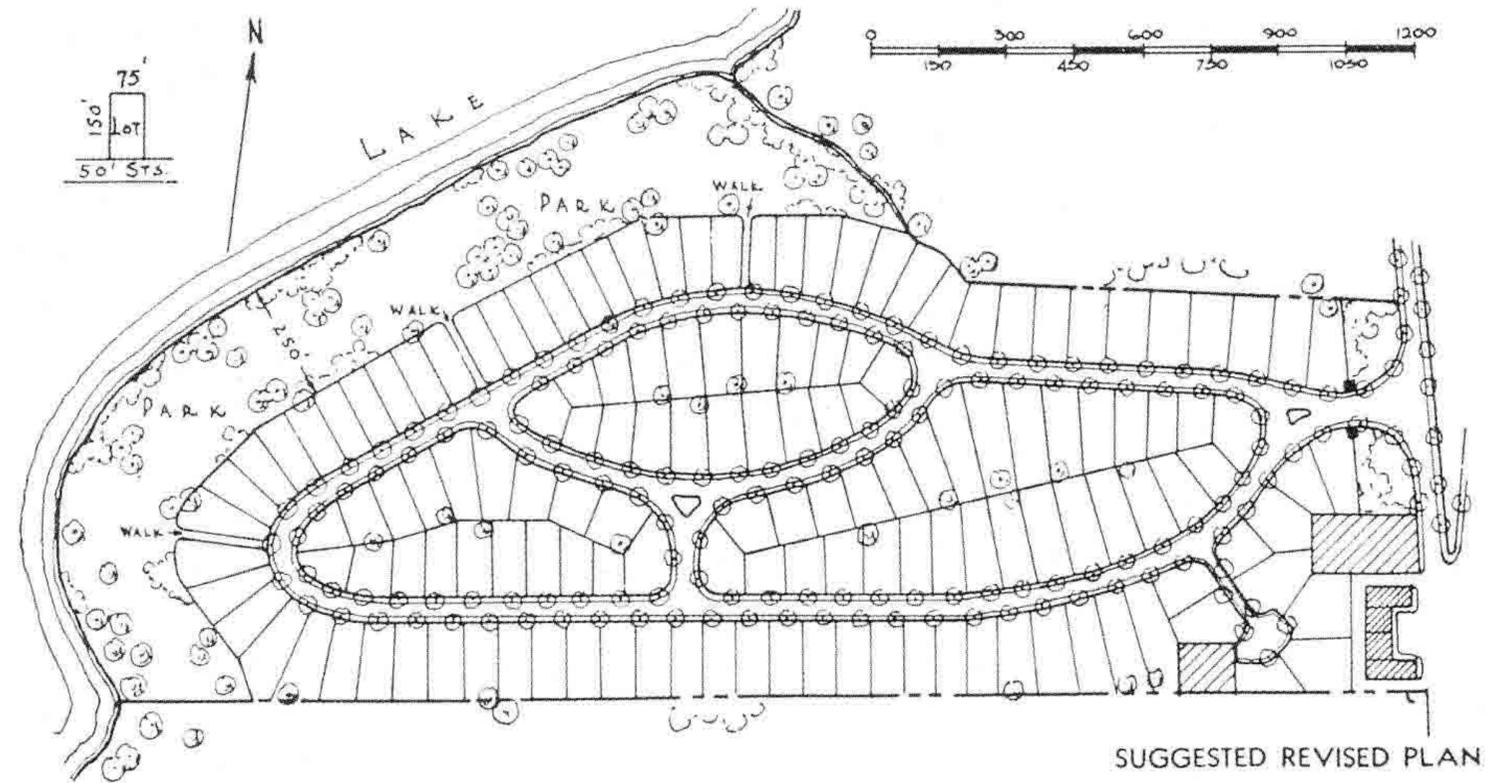
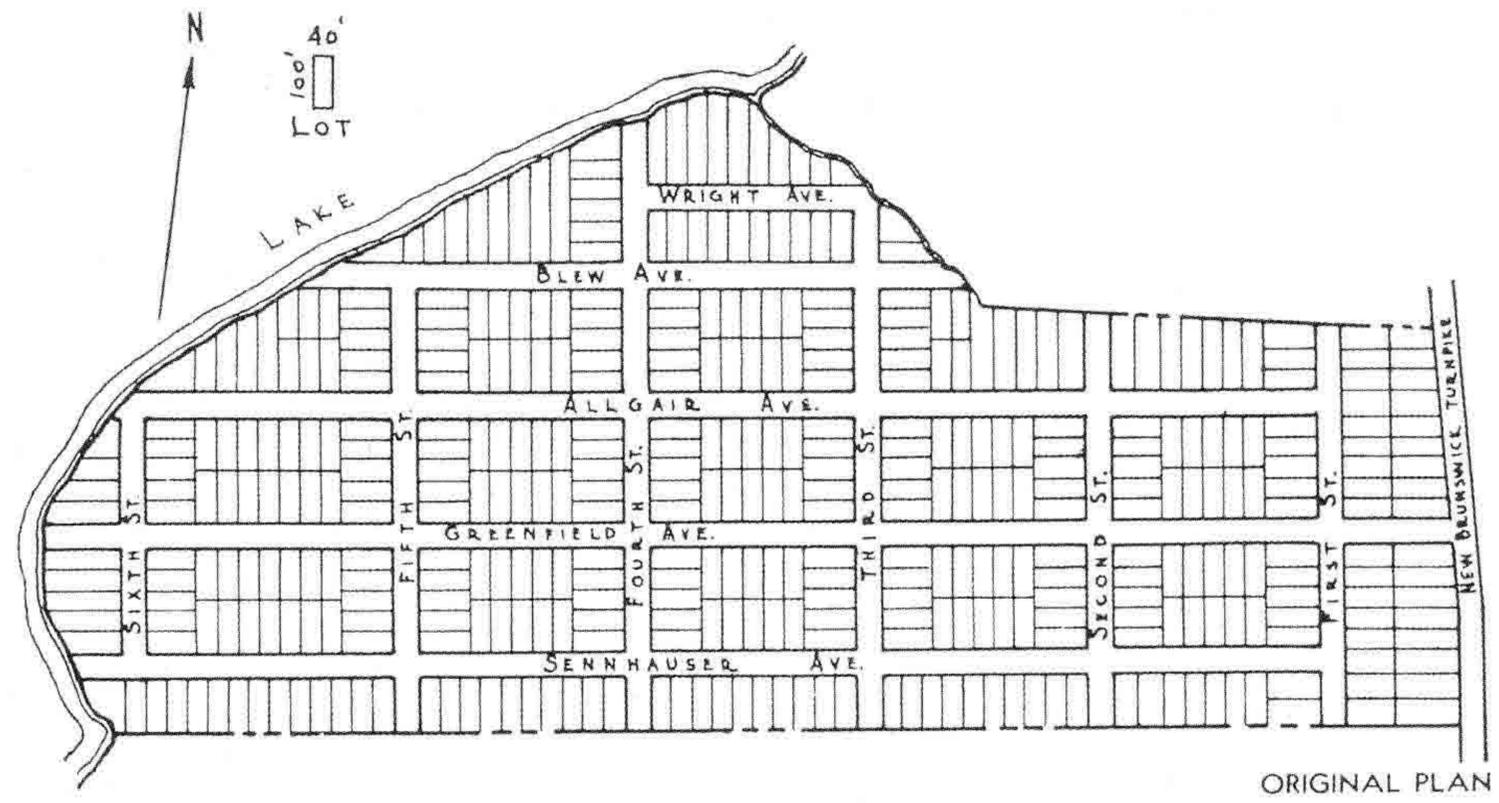
Courtesy of Vicente del Amo Hernández. Used with permission.

Eladio Dieste, Church of Christ the Worker, 1958-60 (left)



Photograph courtesy of [Charles MacEachen](#) on Flickr.

Ludwig Mies van der Rohe, S. R. Crown Hall, 1956 (right)



These images are in the public domain.

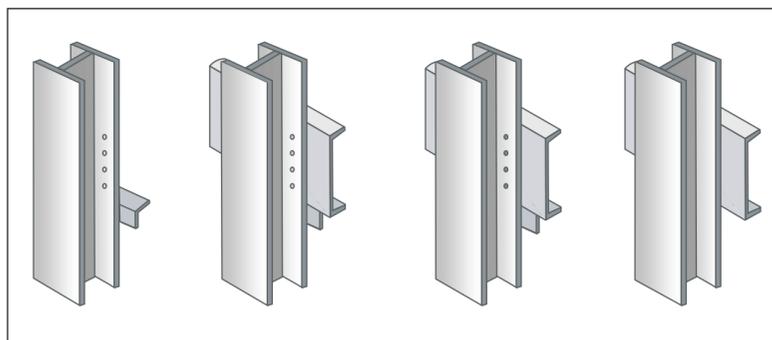
Source: Federal Housing Administration. [Planning Profitable Neighborhoods](#), Technical Bulletin No. 7. Washington, D.C., Government Printing Office, 1938.



Gerrit Rietveld, Red-Blue Chair, 1917–19.

Photograph courtesy of [defining Design](#) on Flickr.

Drawing of Gerrit Rietveld, Detail Connection, Red-Blue Chair, 1917-19 removed due to copyright restrictions.
 Source: Kuper, M., and I. Van Zijl. *Gerrit Rietveld 1888–1964: The Complete Works*. Princeton Architectural Press, 1993.
 See page 10 of "[In Defense of the Curve: Provoked by Reason](#)" for a reference image.



Drawing of Mies van der Rohe, Plug weld procedure: connection prepared, beam placed, plug weld, connection finished.

Image by MIT OpenCourseWare.

Photograph of Thonet bending forms incorporating a metal strip removed due to copyright restrictions.
 Source: Von Vegesack, Alexander. *Thonet: Classic Furniture in Bent Wood and Tubular Steel*. Rizzoli, 1997.
 See page 11 of "[In Defense of the Curve: Provoked by Reason](#)" for a reference image.



Michael Thonet, No. 14 Chair, 1859–60.

Photograph courtesy of [Holger.Ellgaard](#) on Wikimedia Commons.

Photograph of Adolf Loos, Café Museum Chair, 1908 removed due to copyright restrictions.
 See page 12 of "[In Defense of the Curve: Provoked by Reason](#)" for a reference image.

Photographs of Charles and Ray Eames, Leg Splint, 1941 (left);
Charles and Ray Eames, Body Splint, 1941 (upper right);
Leg Splint Demonstration, 1941 (lower right)

removed due to copyright restrictions.

Source: Neuhart, John, and Marilyn Neuhart. *Eames Design*. 1st ed. Abrams, 1989.

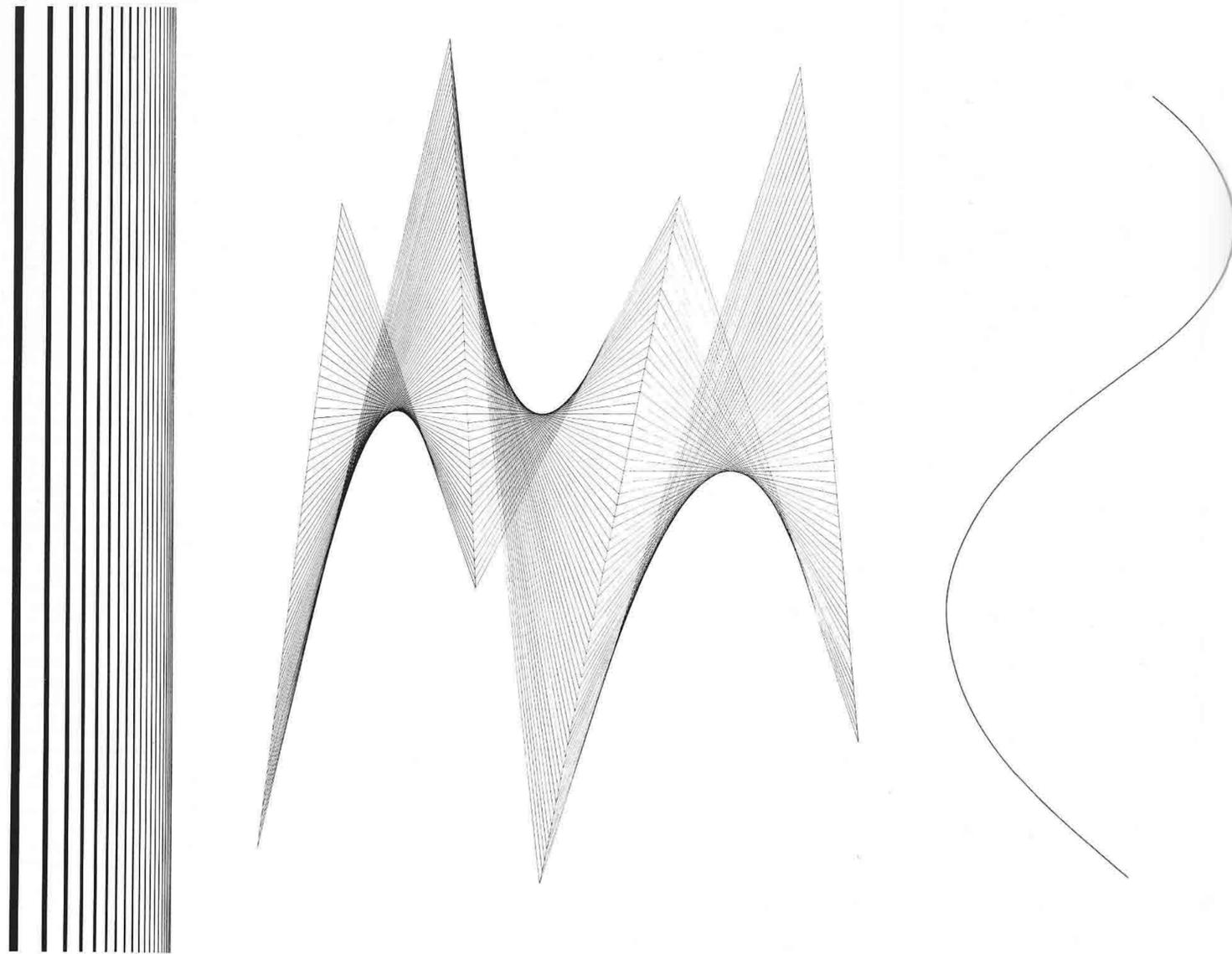
See page 13 of "[In Defense of the Curve: Provoked by Reason](#)" for a reference image.

Photographs of Charles Eames casting fiberglass (left);
Charles and Ray Eames, LCW Chair, 1945, Plywood Process (upper right);
Charles and Ray Eames, Plastic Armchair, 1950–53, Fiberglass Process (lower right)

removed due to copyright restrictions.

Source: Neuhart, John, and Marilyn Neuhart. *Eames Design*. 1st ed. Abrams, 1989.

See page 14 of "[In Defense of the Curve: Provoked by Reason](#)" for a reference image.



Ludwig Mies van der Rohe, Drafting exercise for first-year students at the Armour Institute, 1938

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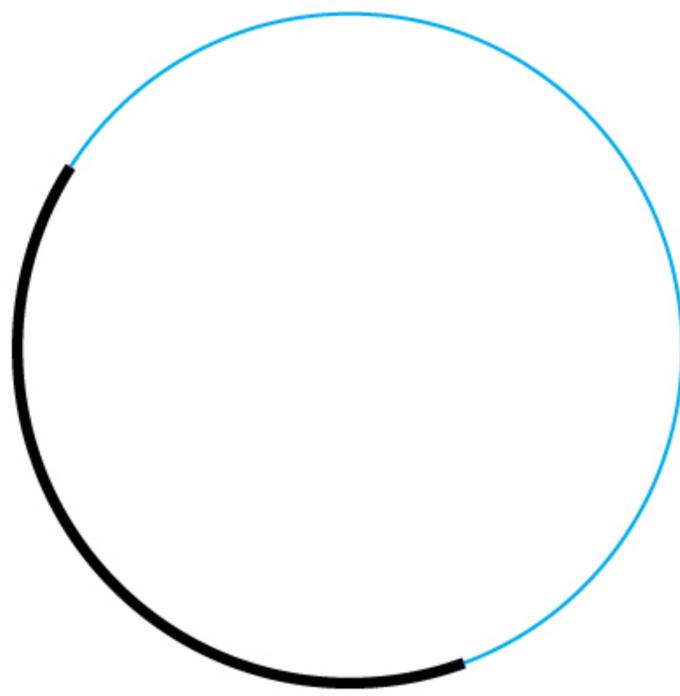
Curvature Calculations / Calculus

CURVATURE

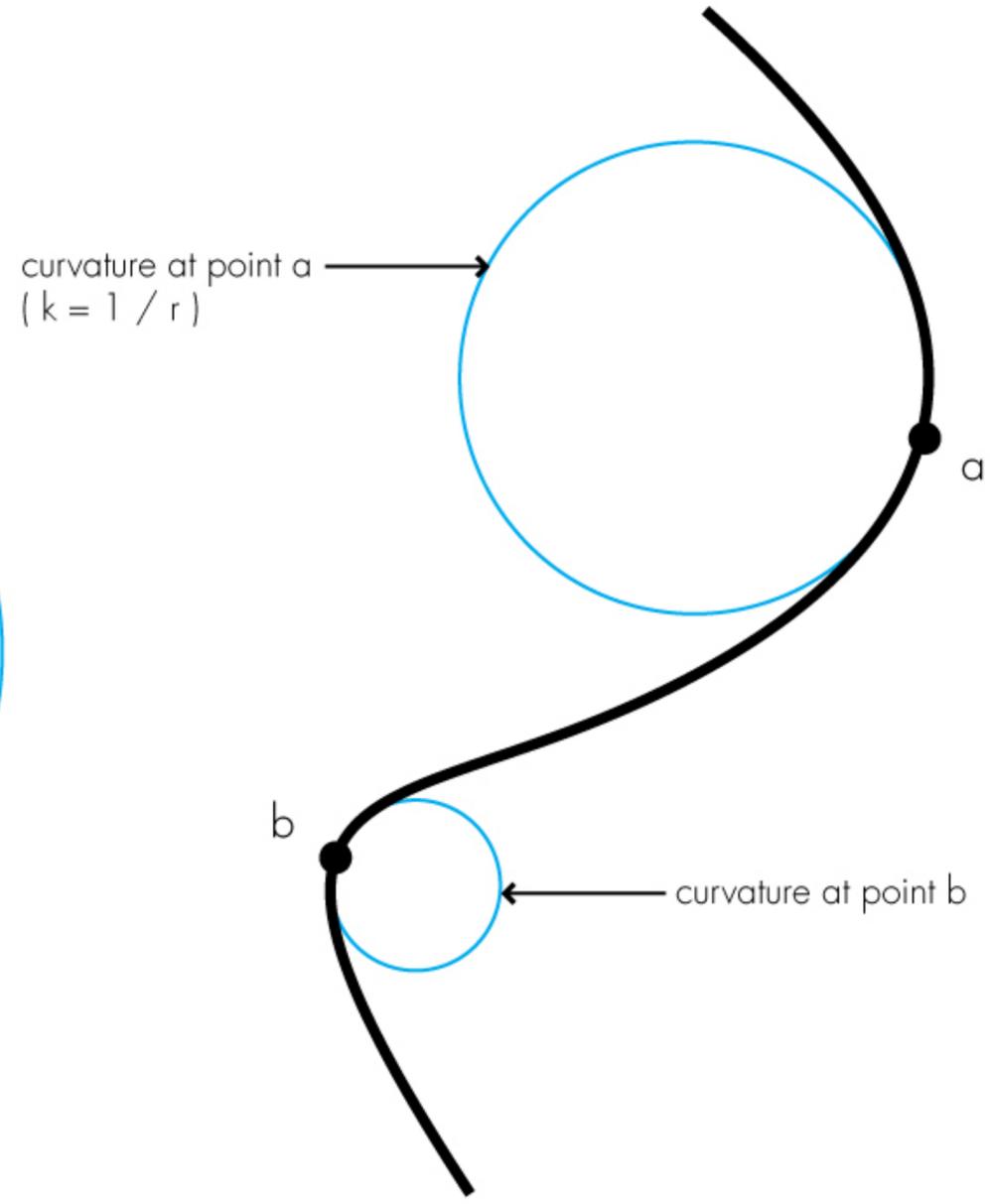
curvature in planar curves



ZERO



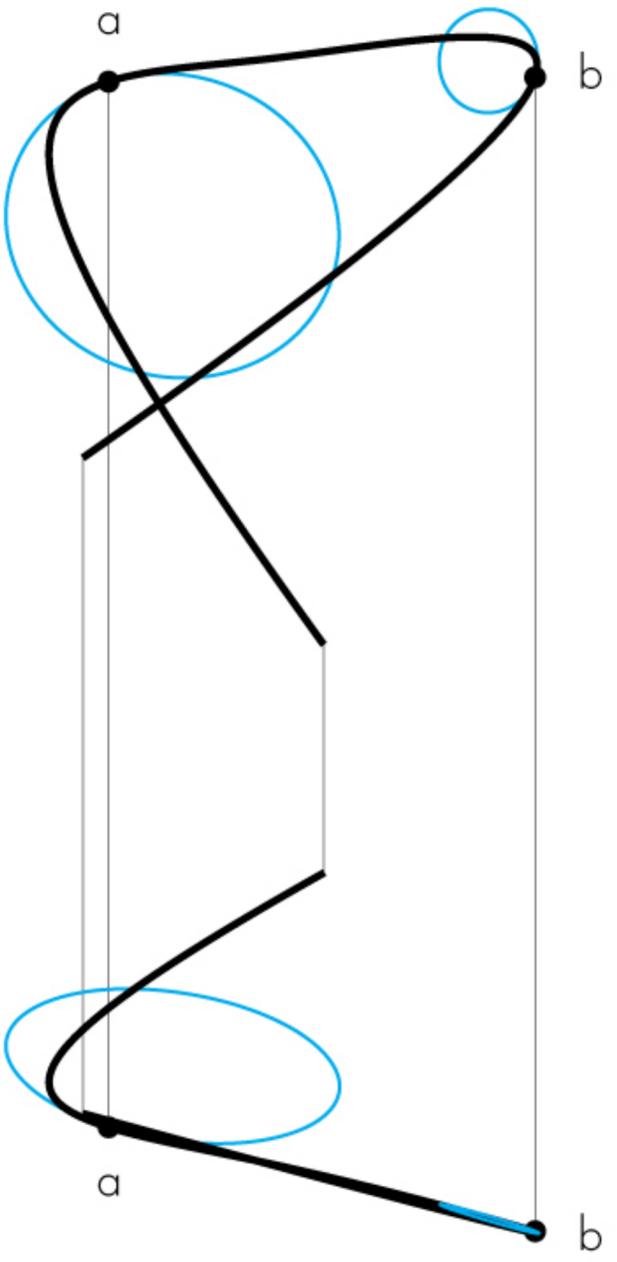
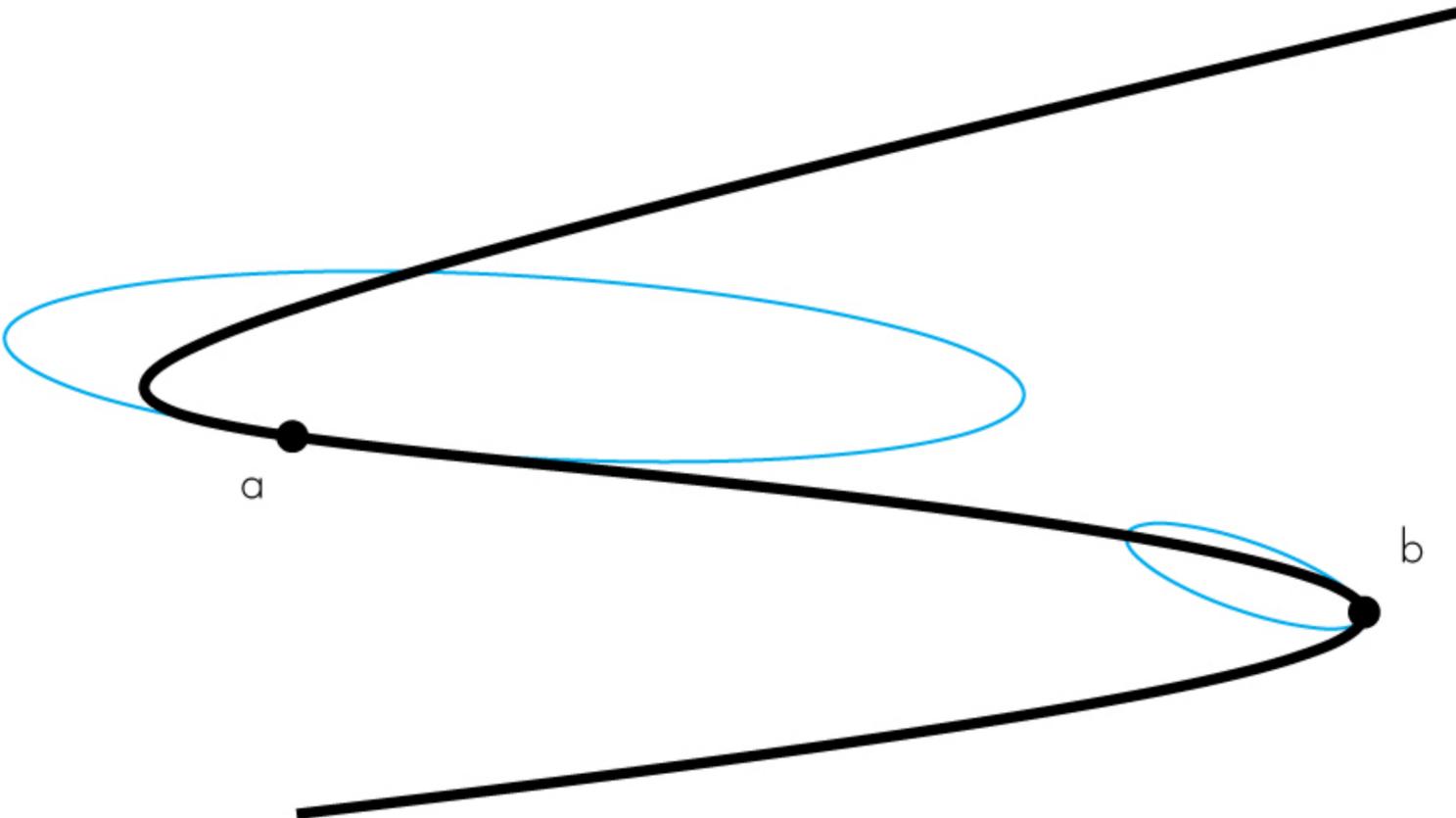
CONSTANT



VARIABLE

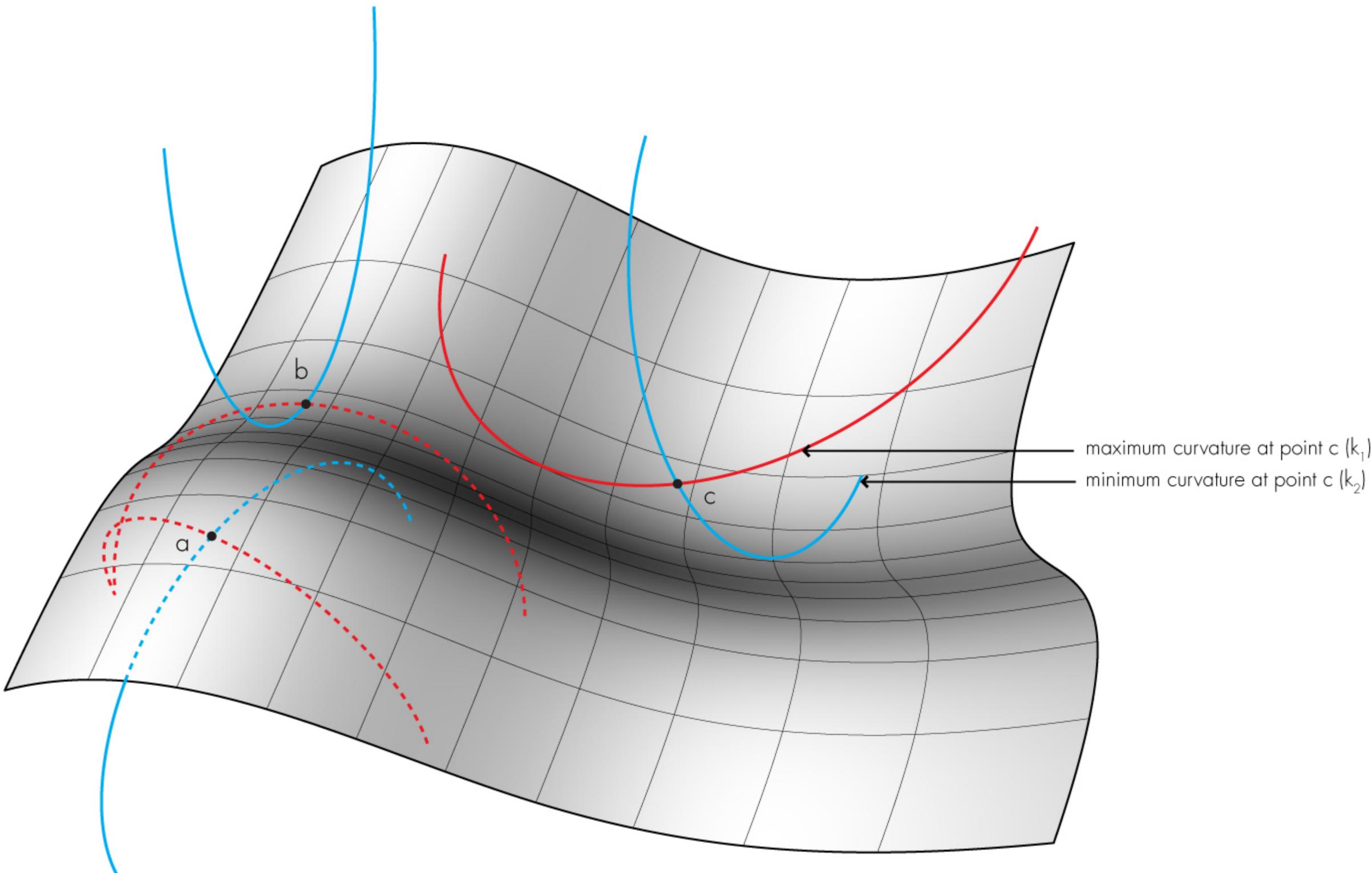
CURVATURE

curvature in space curves



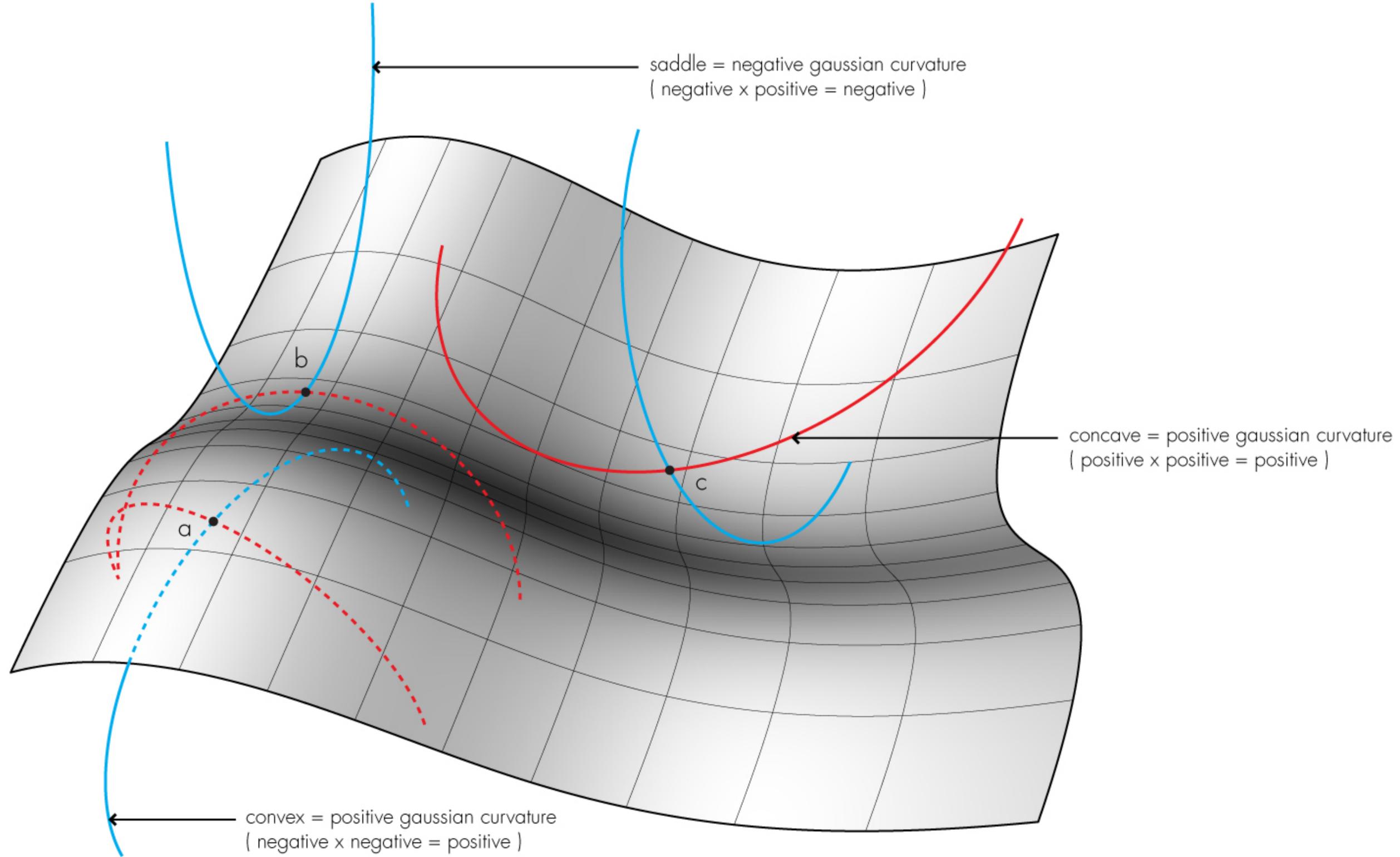
CURVATURE

principal curvature in surfaces (k_1, k_2)



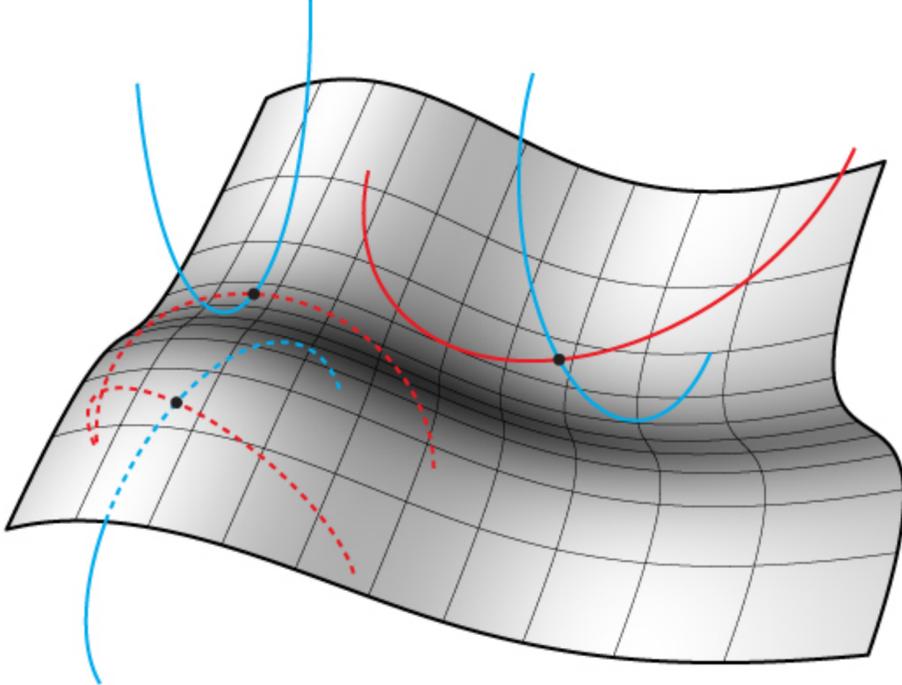
CURVATURE

gaussian curvature in surfaces ($K = k_1 \times k_2$)

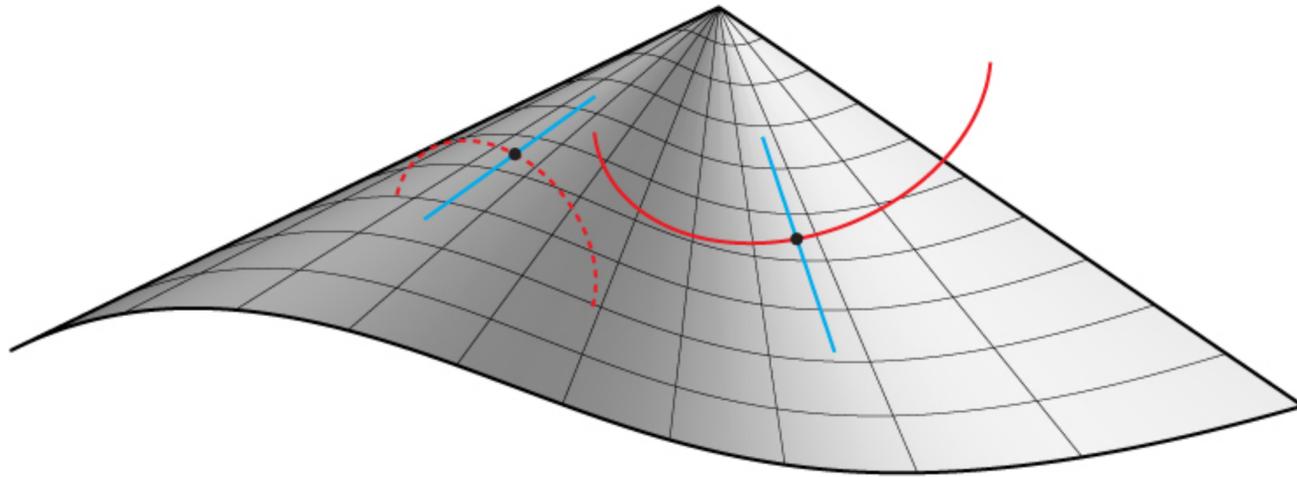


CURVATURE

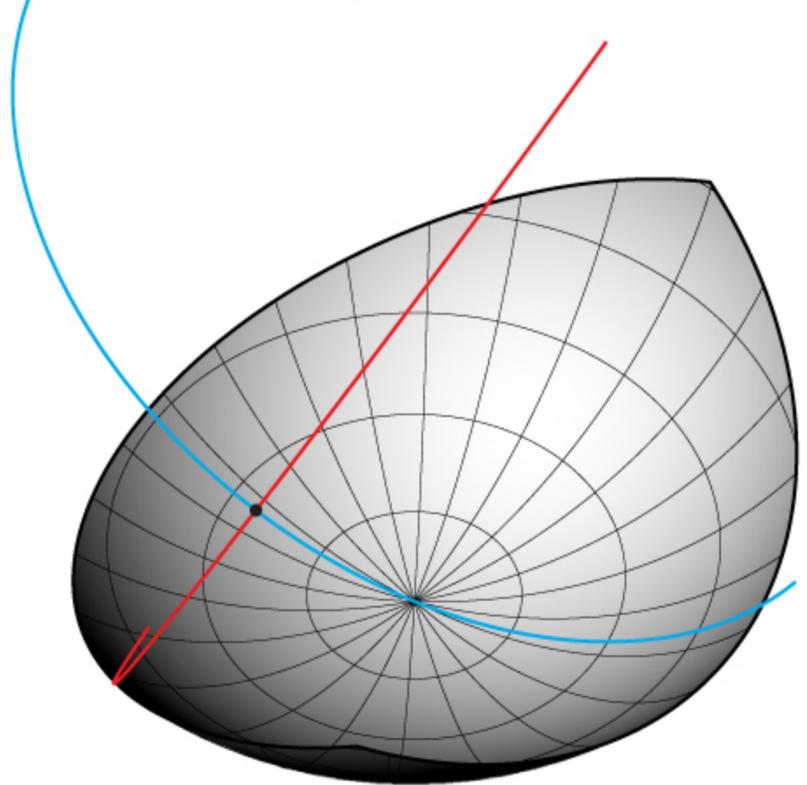
special cases and gaussian curvature



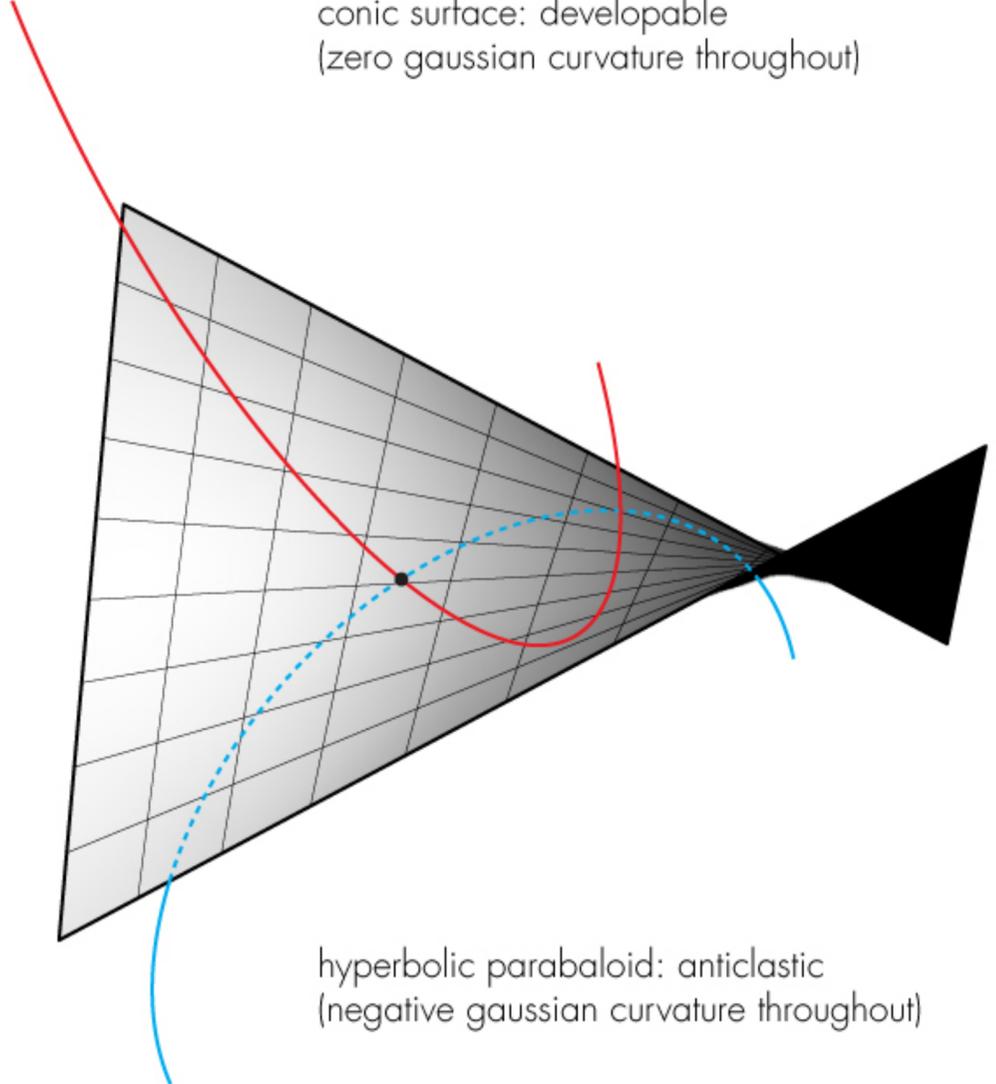
complex surface
(value of gaussian curvature changes)



conic surface: developable
(zero gaussian curvature throughout)



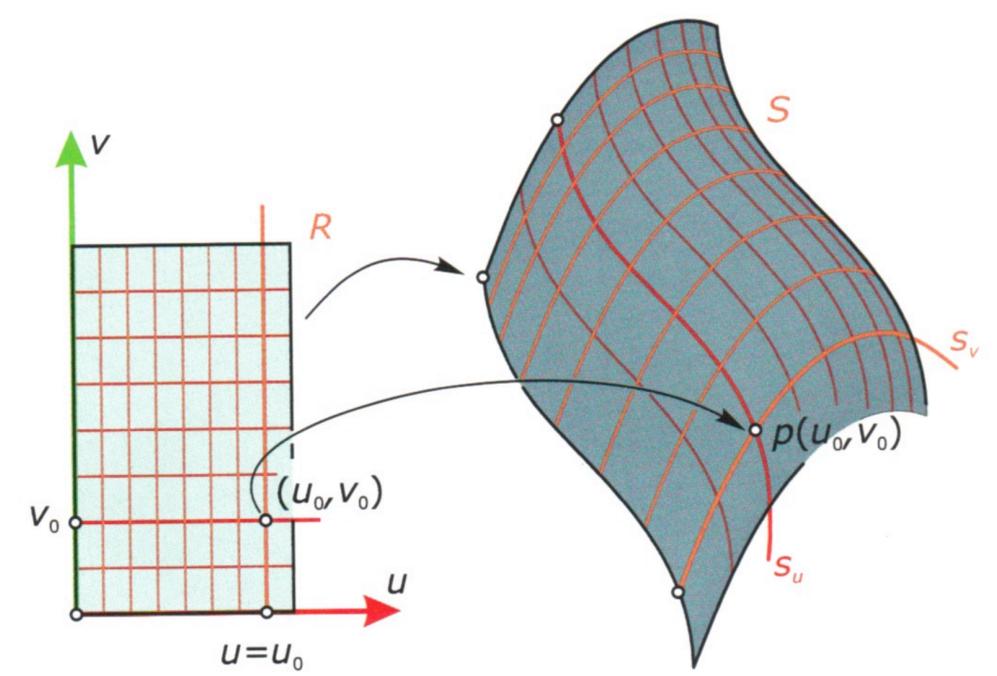
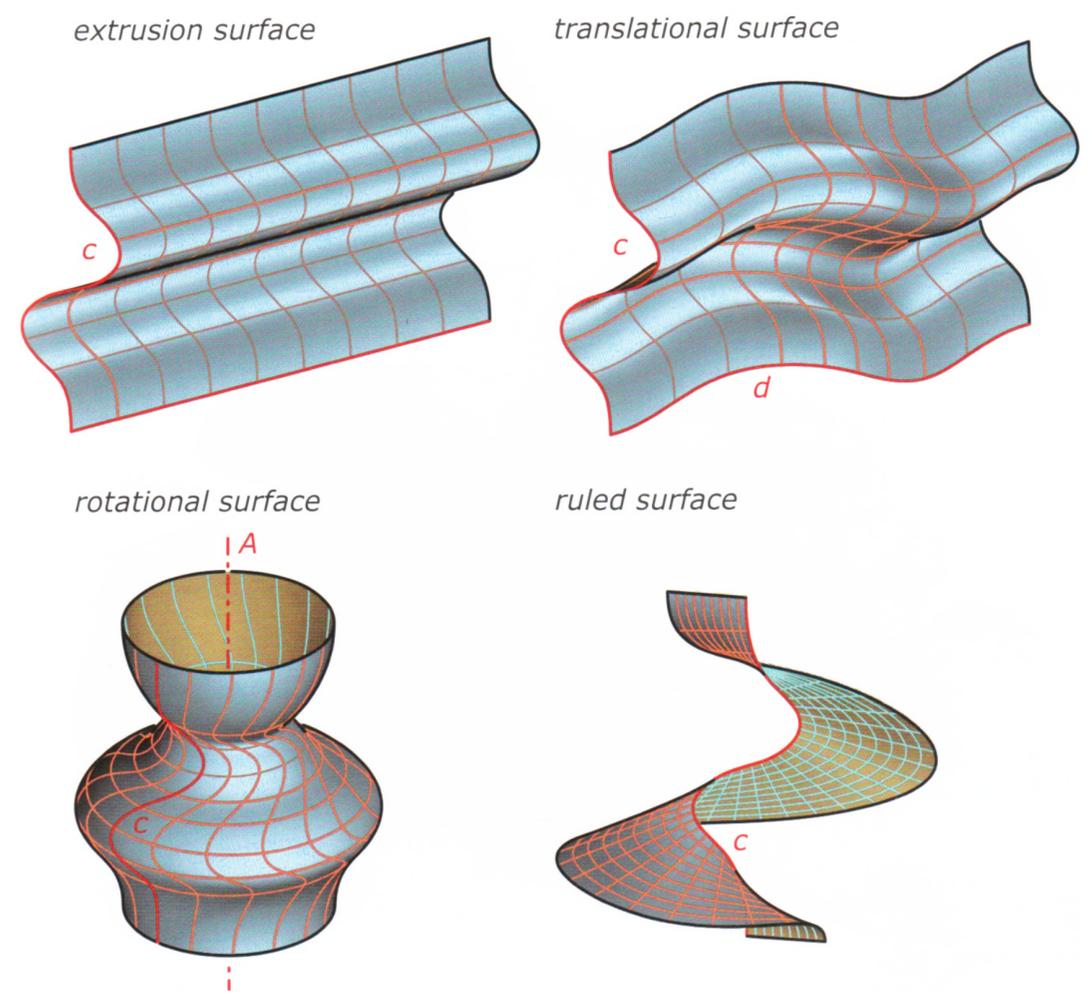
sphere: synclastic
(positive gaussian curvature throughout)



hyperbolic paraboloid: anticlastic
(negative gaussian curvature throughout)

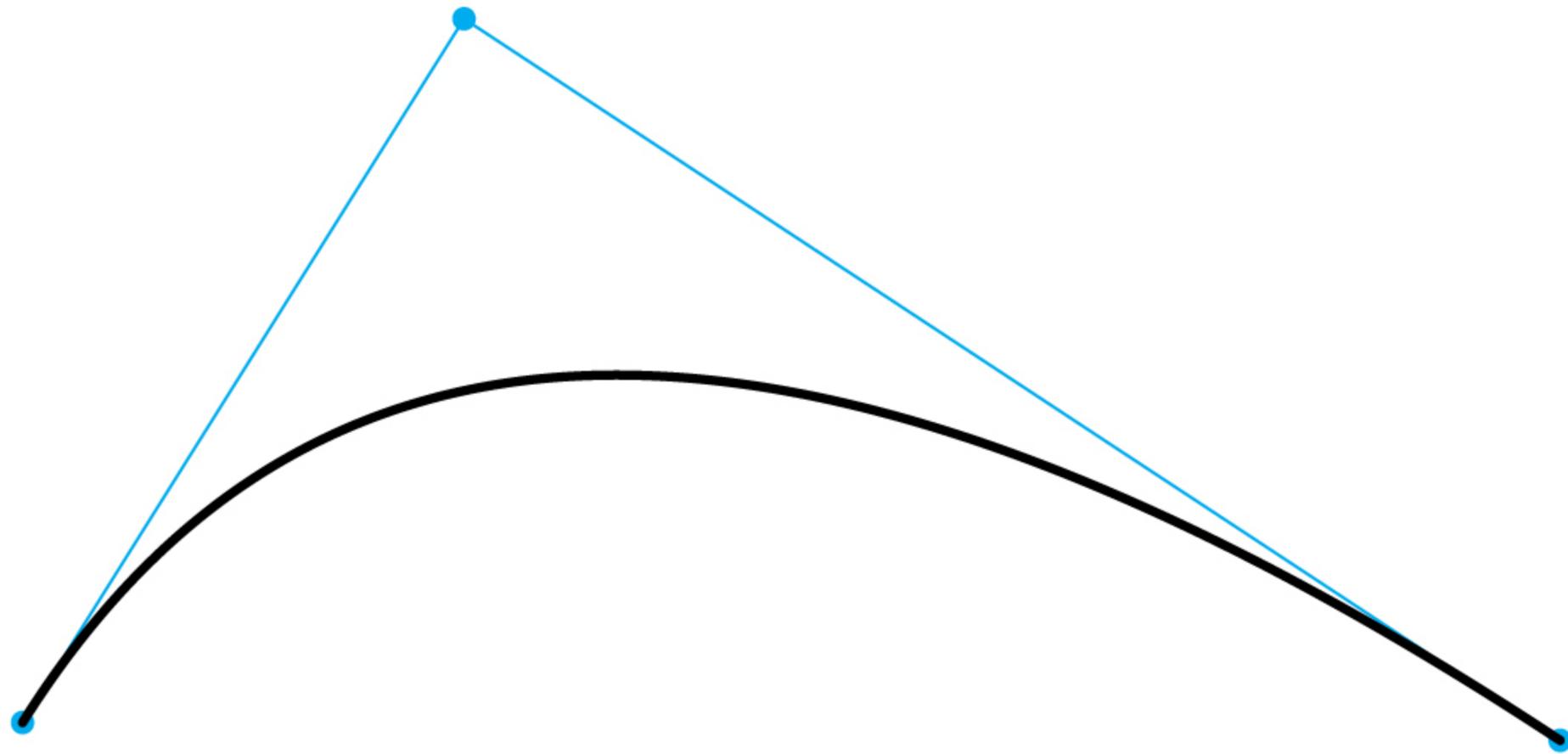
CURVATURE

curves + surfaces



CURVATURE

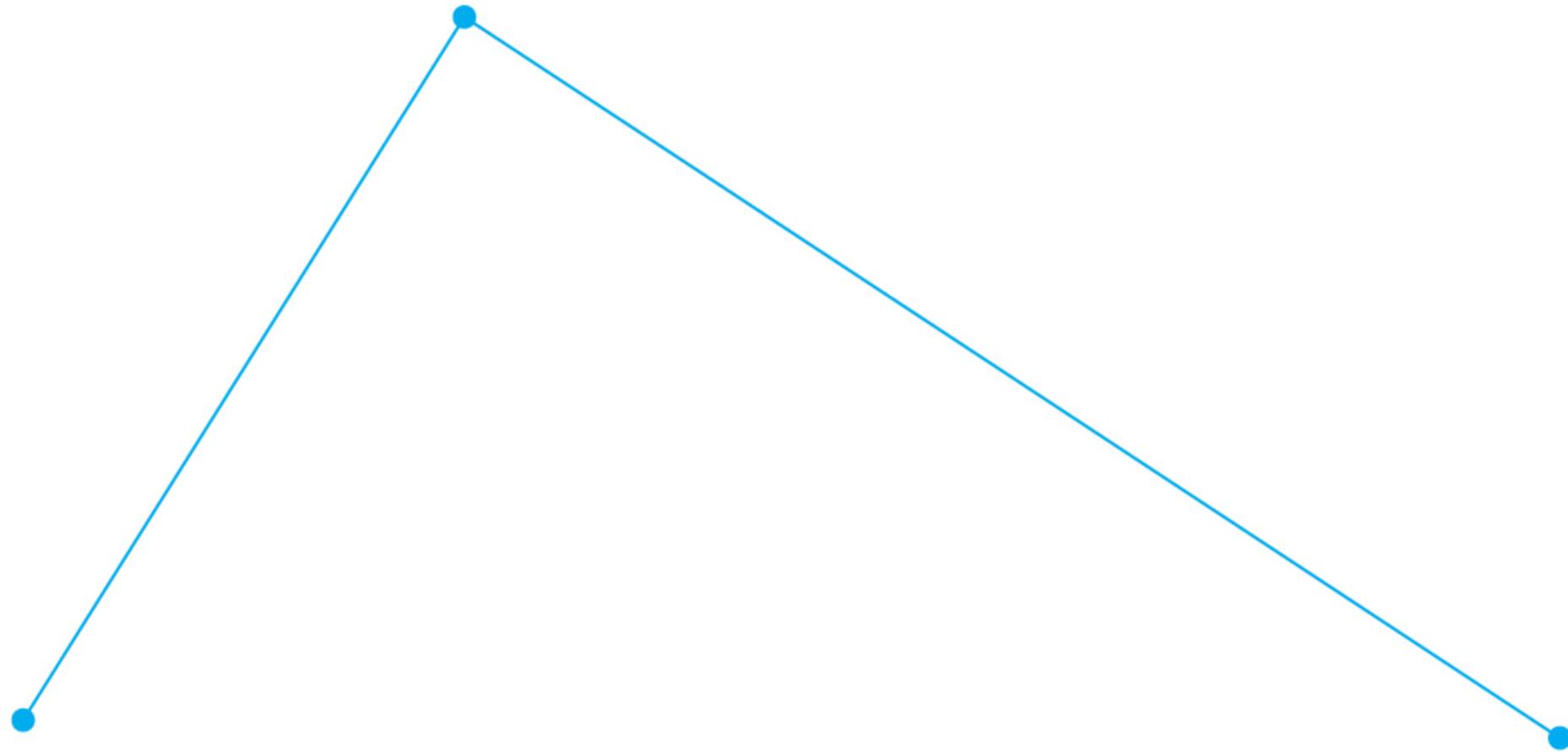
bezier curves and de castljam's algorithm



Bezier Curve with 3-Point control polygon

CURVATURE

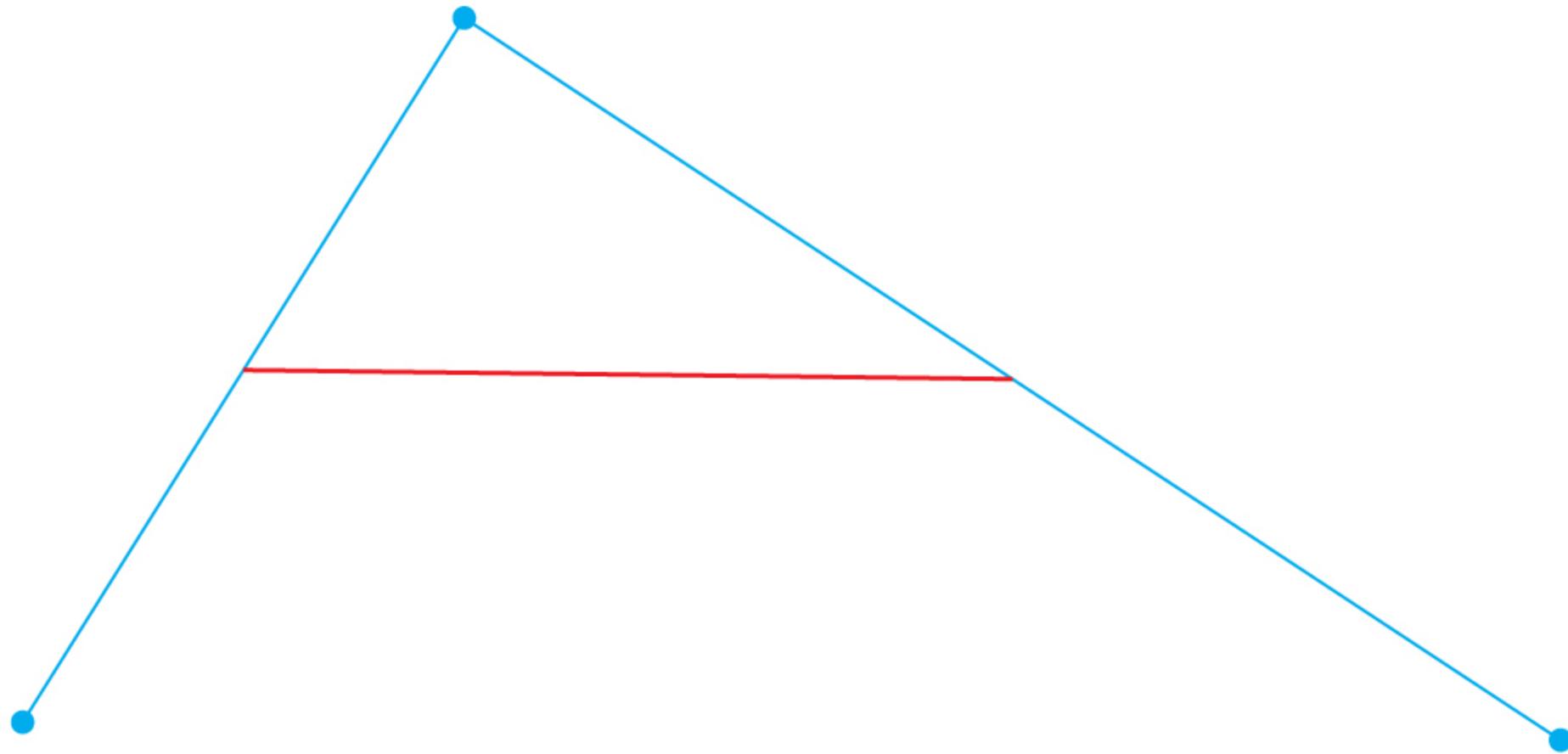
bezier curves and de castljam's algorithm



3-Point control polygon

CURVATURE

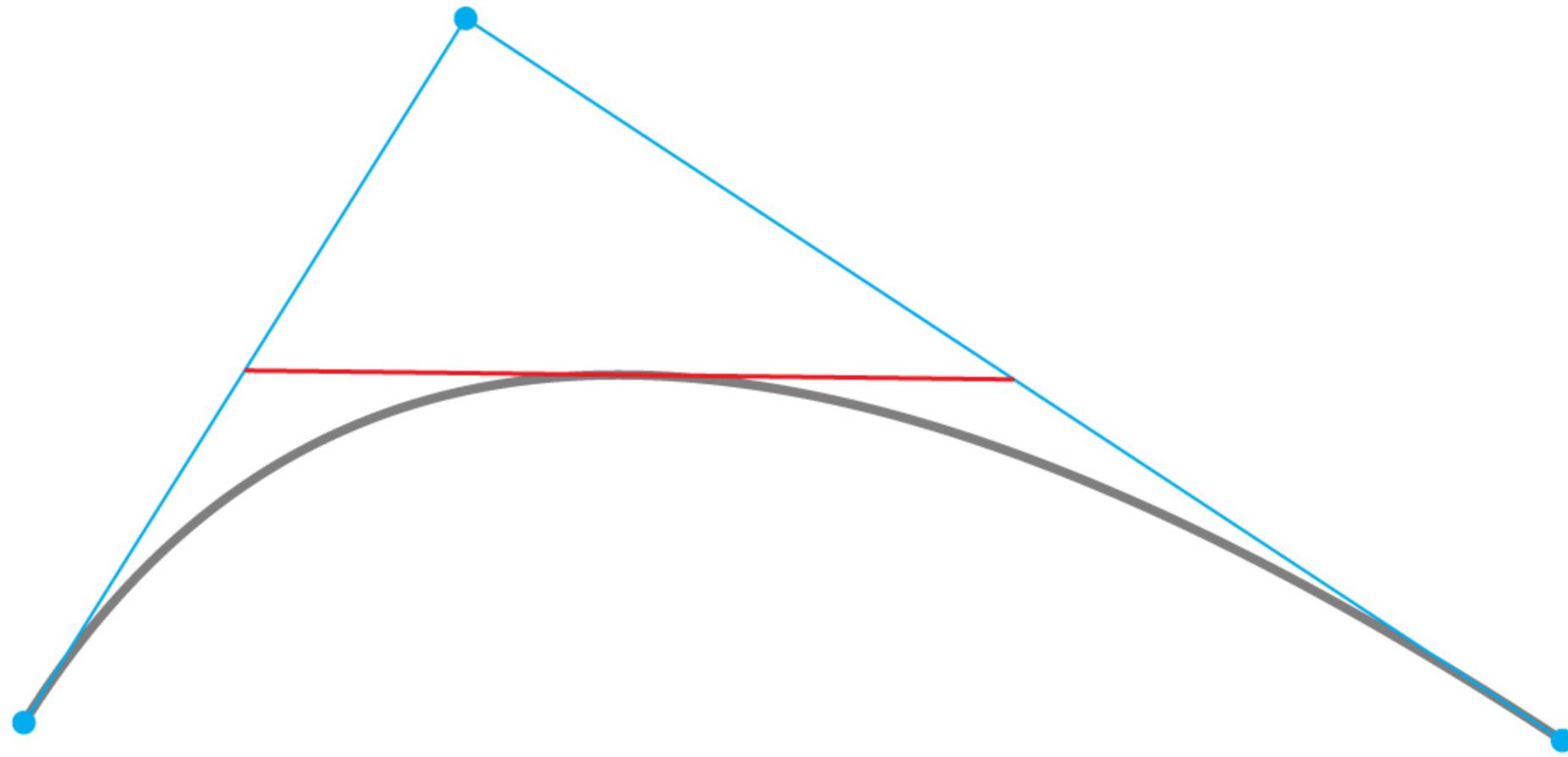
bezier curves and de castljam's algorithm



Line connecting mid-points of control polygon legs

CURVATURE

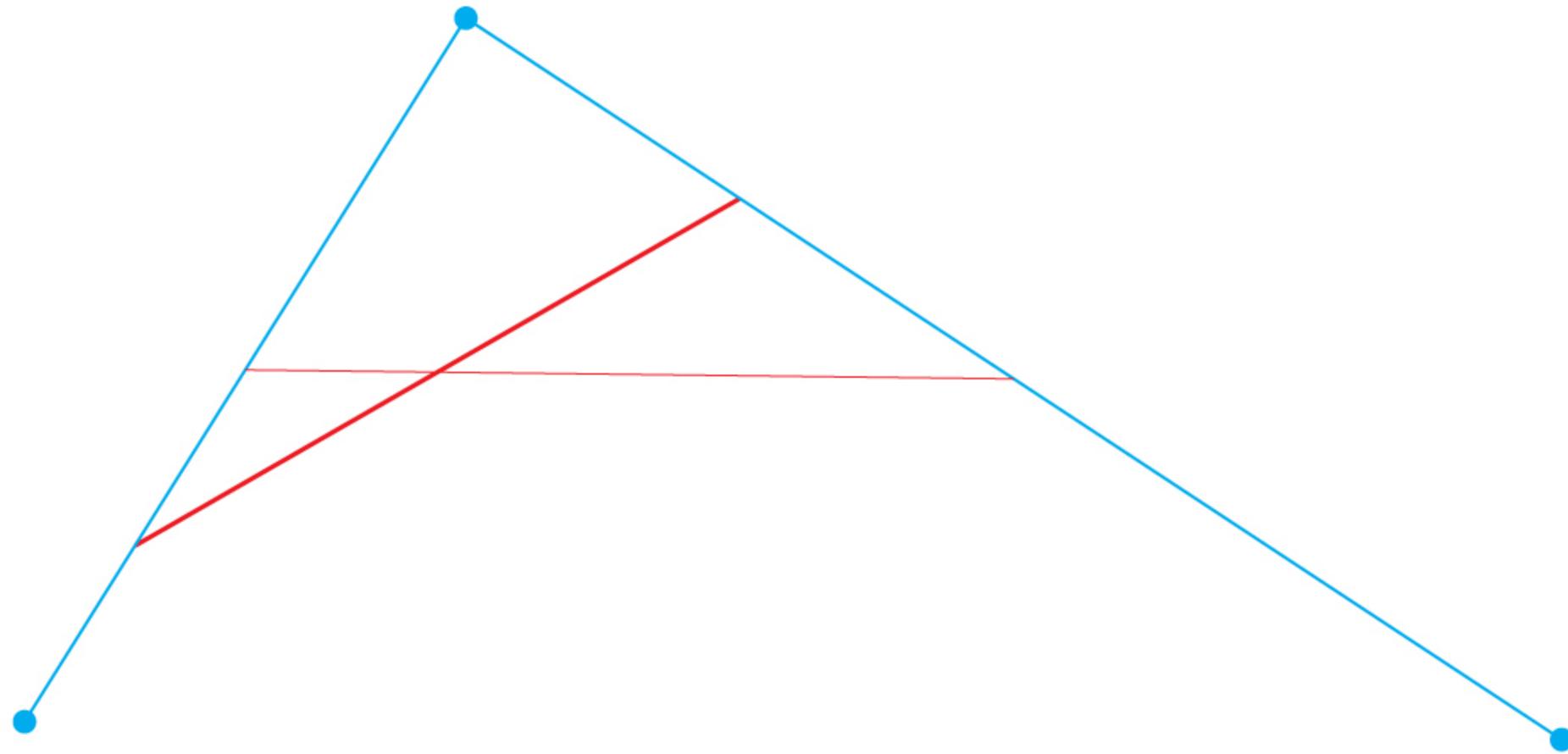
bezier curves and de castljam's algorithm



Bezier lies tangent to the mid-point of this line

CURVATURE

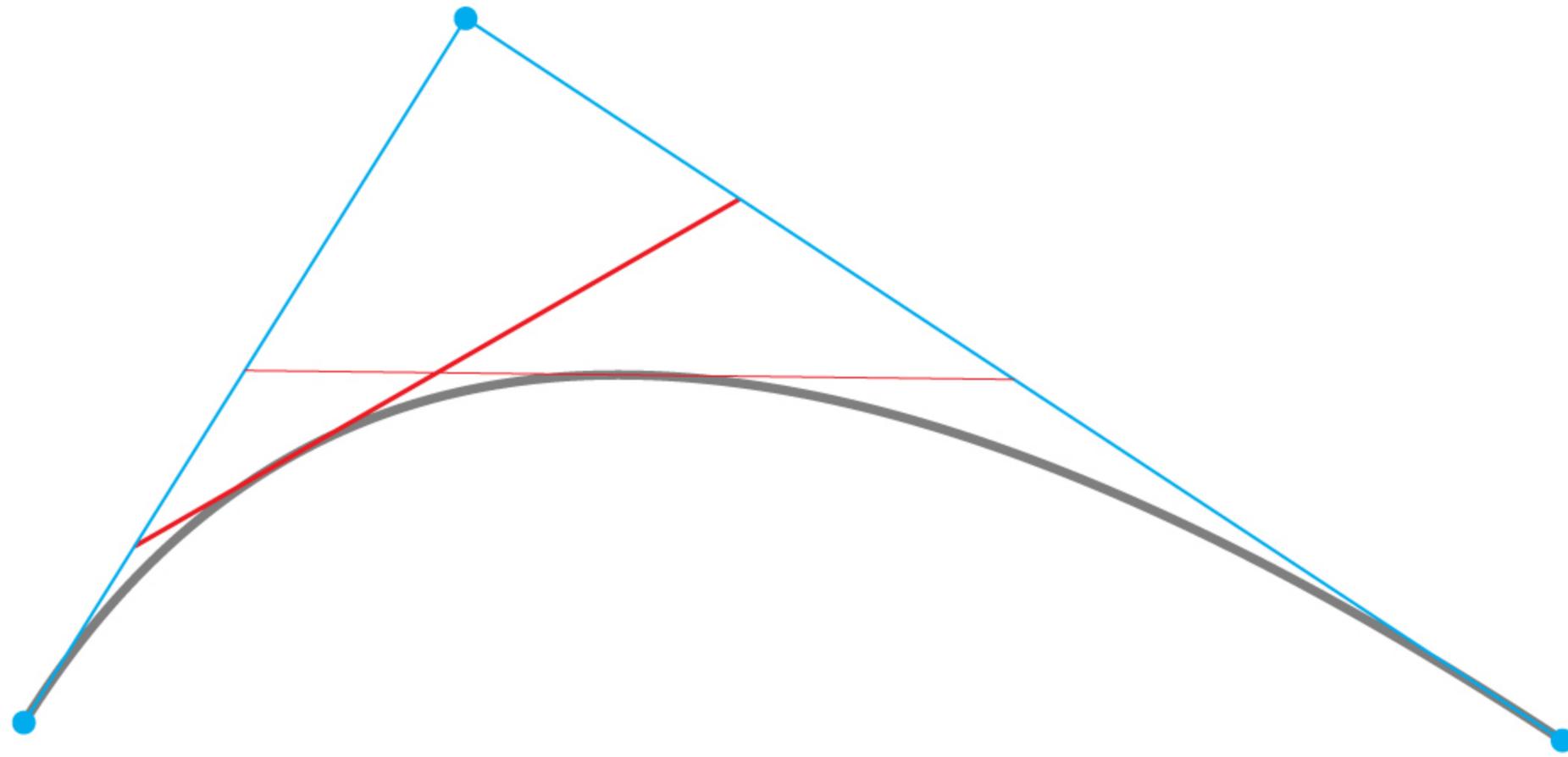
bezier curves and de castljam's algorithm



Line connecting quarter-points of control polygon legs

CURVATURE

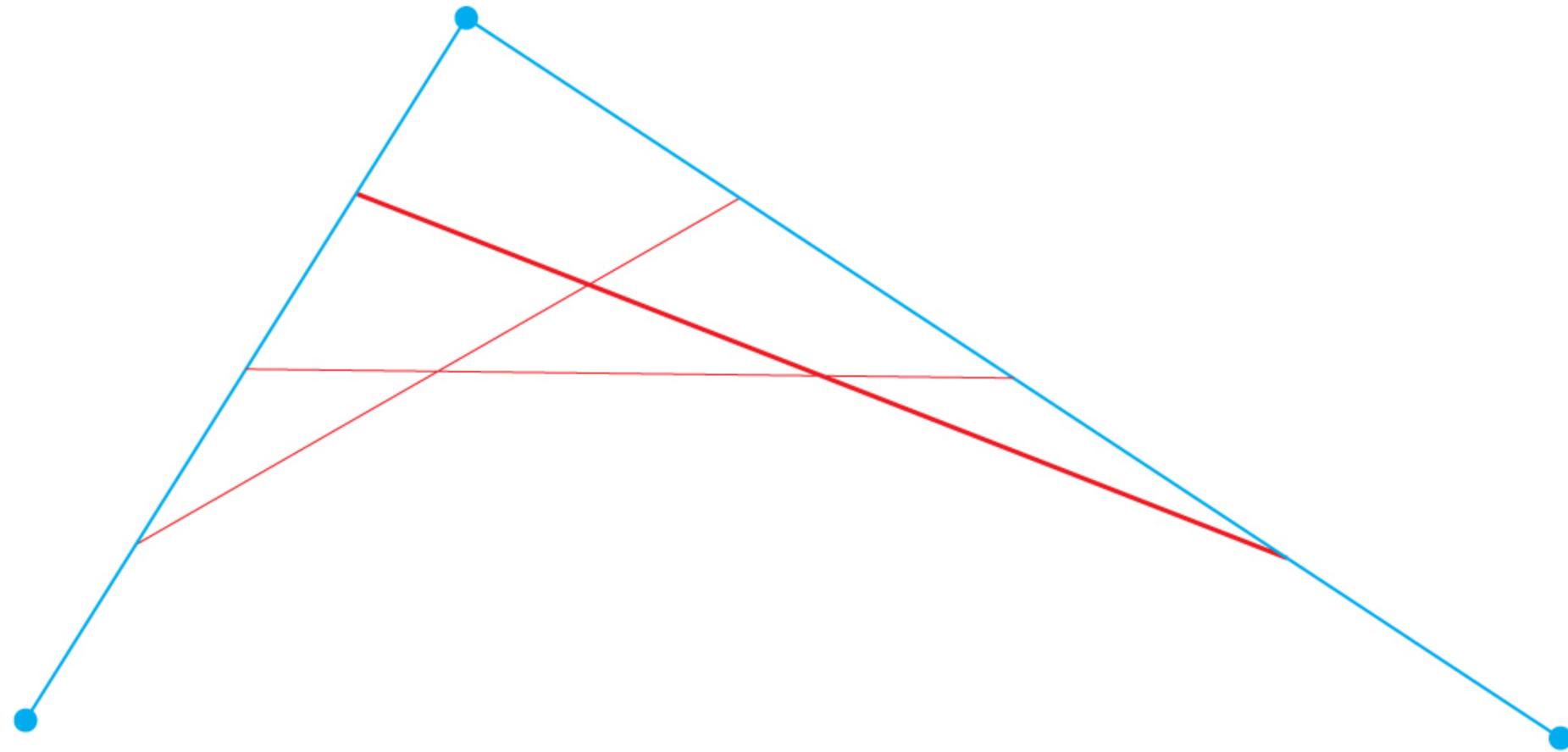
bezier curves and de castljam's algorithm



Bezier lies tangent to the quarter-point of this line

CURVATURE

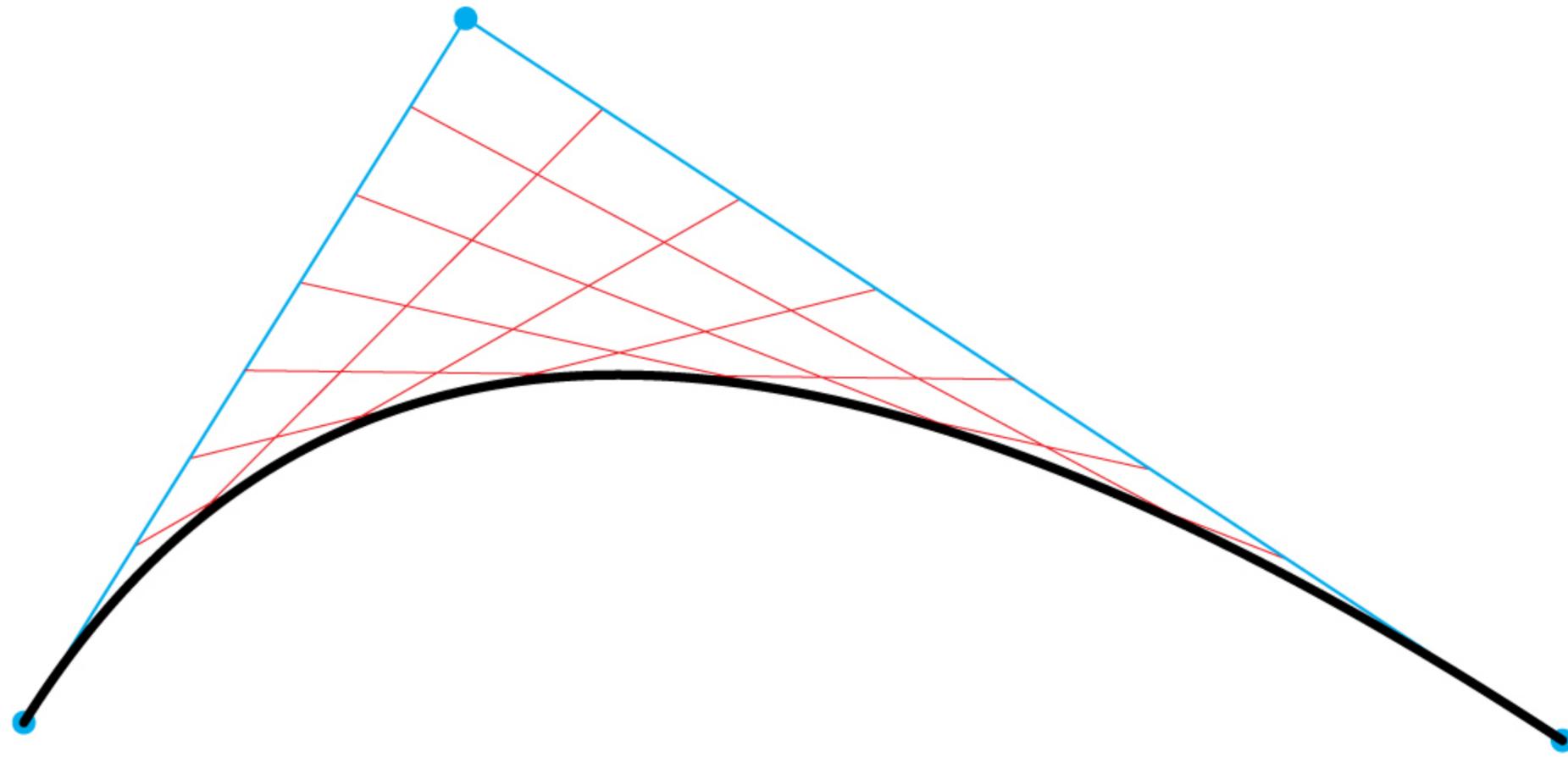
bezier curves and de castljam's algorithm



Line connecting three-quarter-points of control polygon legs

CURVATURE

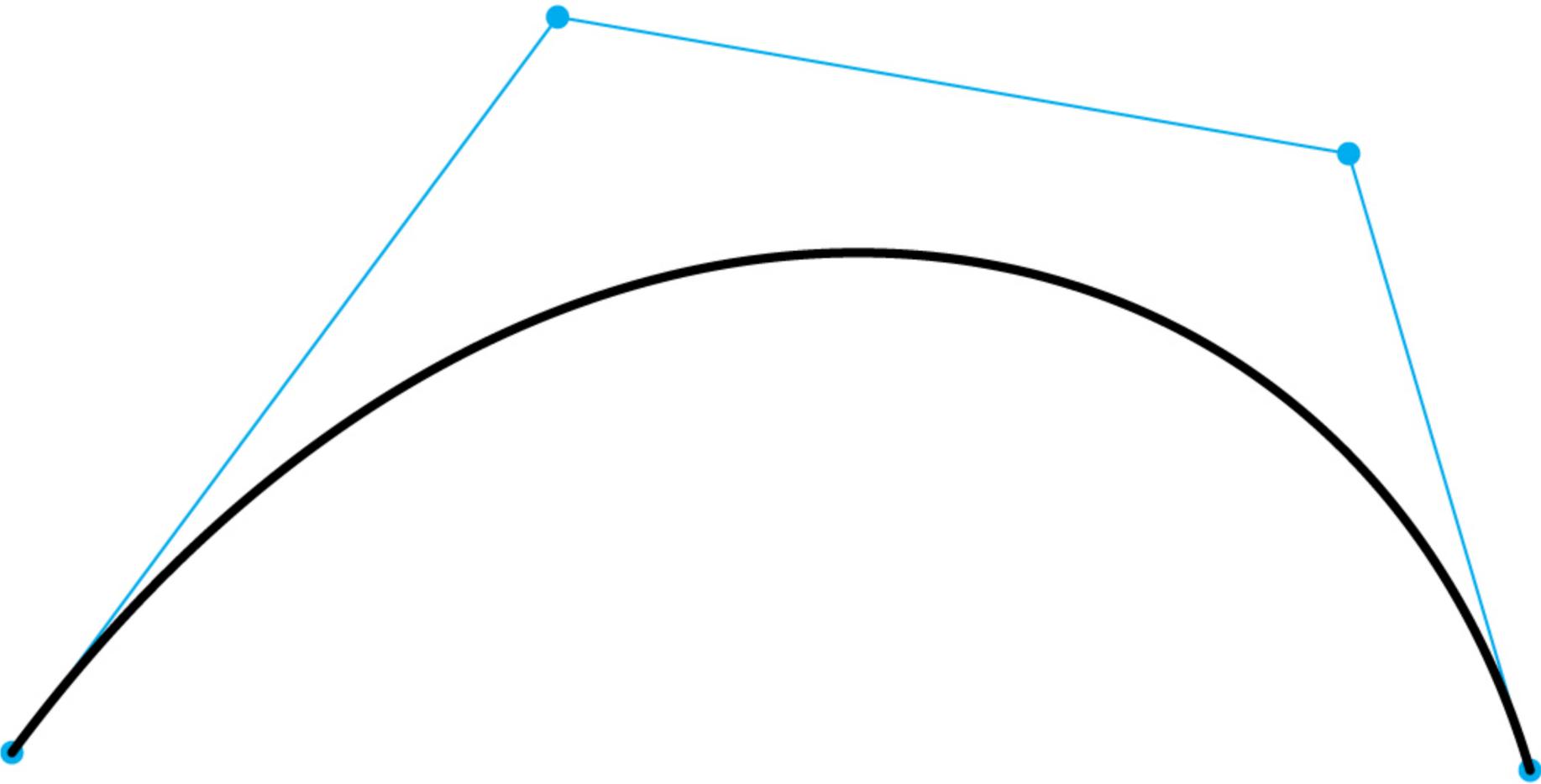
bezier curves and de castljam's algorithm



Bezier = Limit as N approaches infinity

CURVATURE

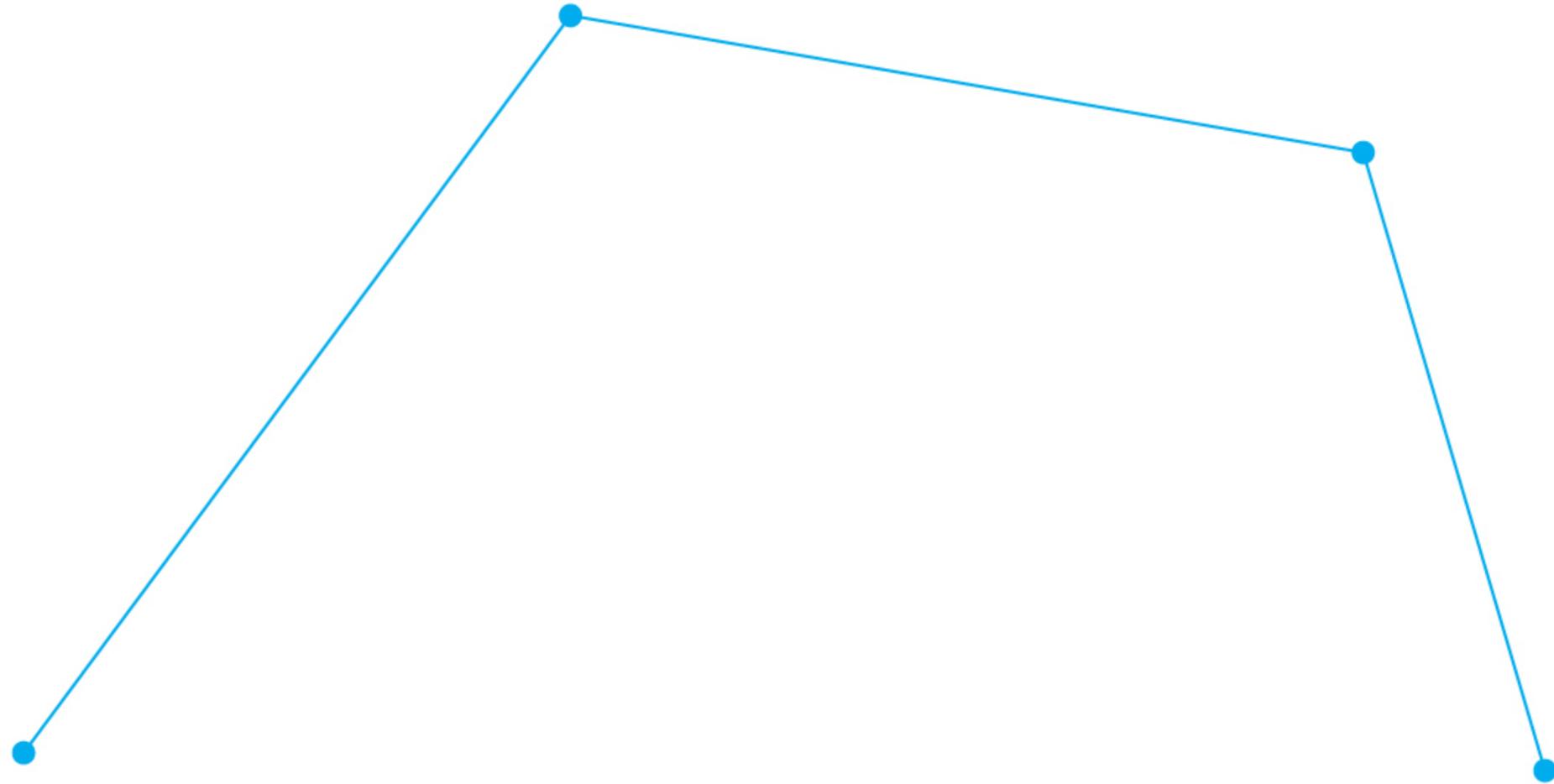
bezier curves and de castl'jau's algorithm



Bezier Curve with 4-point control polygon

CURVATURE

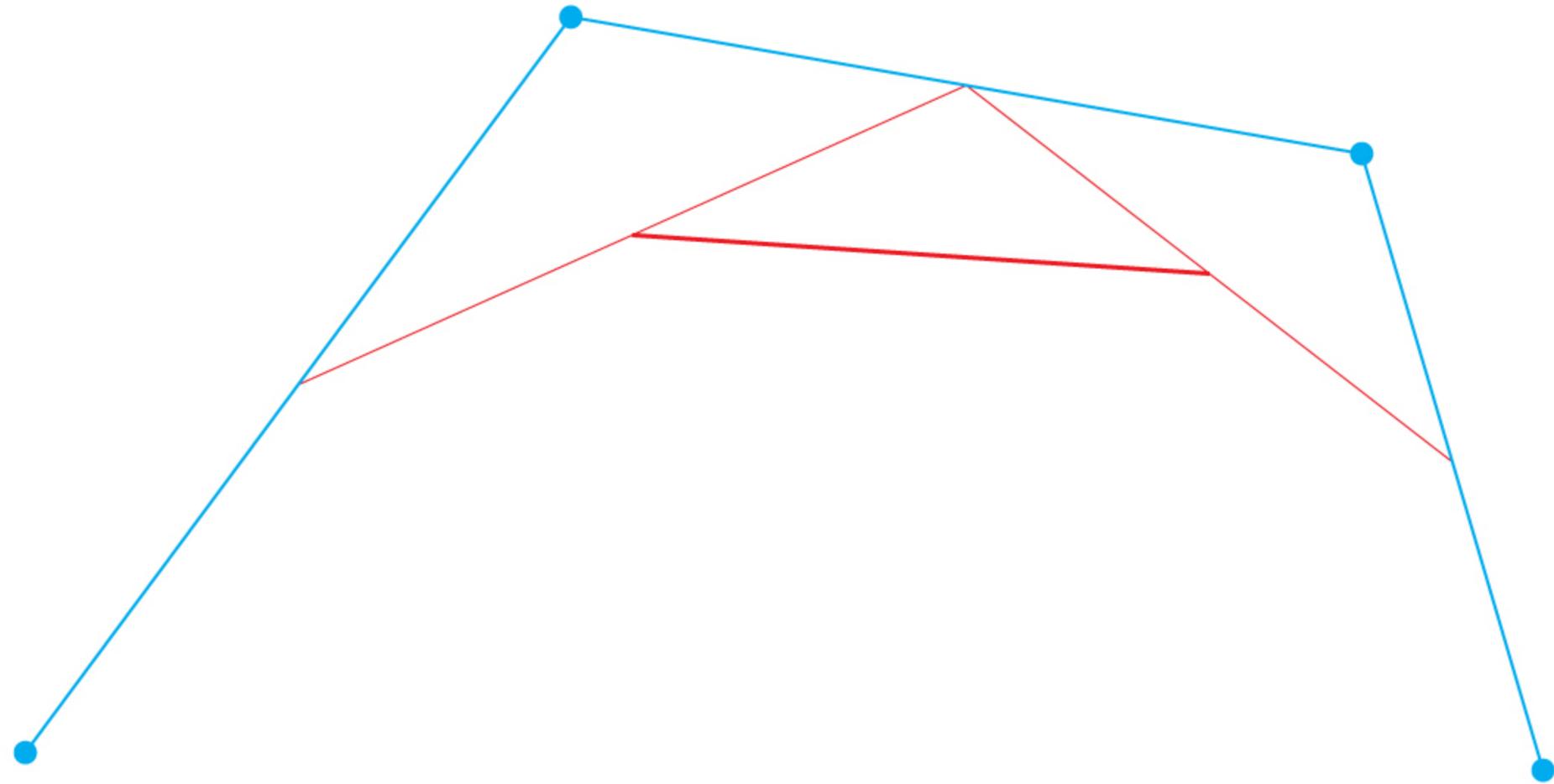
bezier curves and de castljam's algorithm



4-point control polygon

CURVATURE

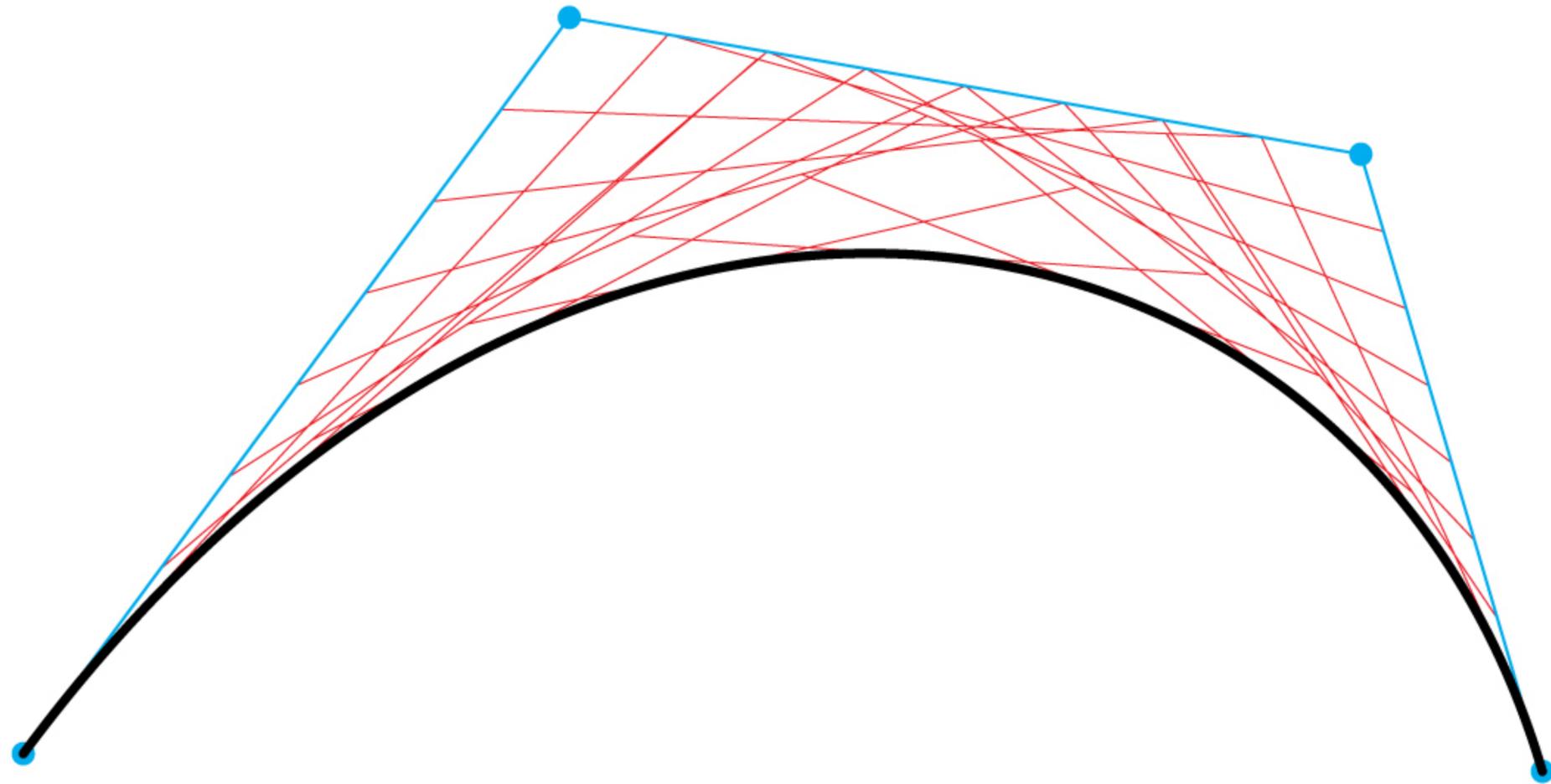
bezier curves and de castljam's algorithm



Line connecting mid-points of lines connecting mid-points of control polygon legs

CURVATURE

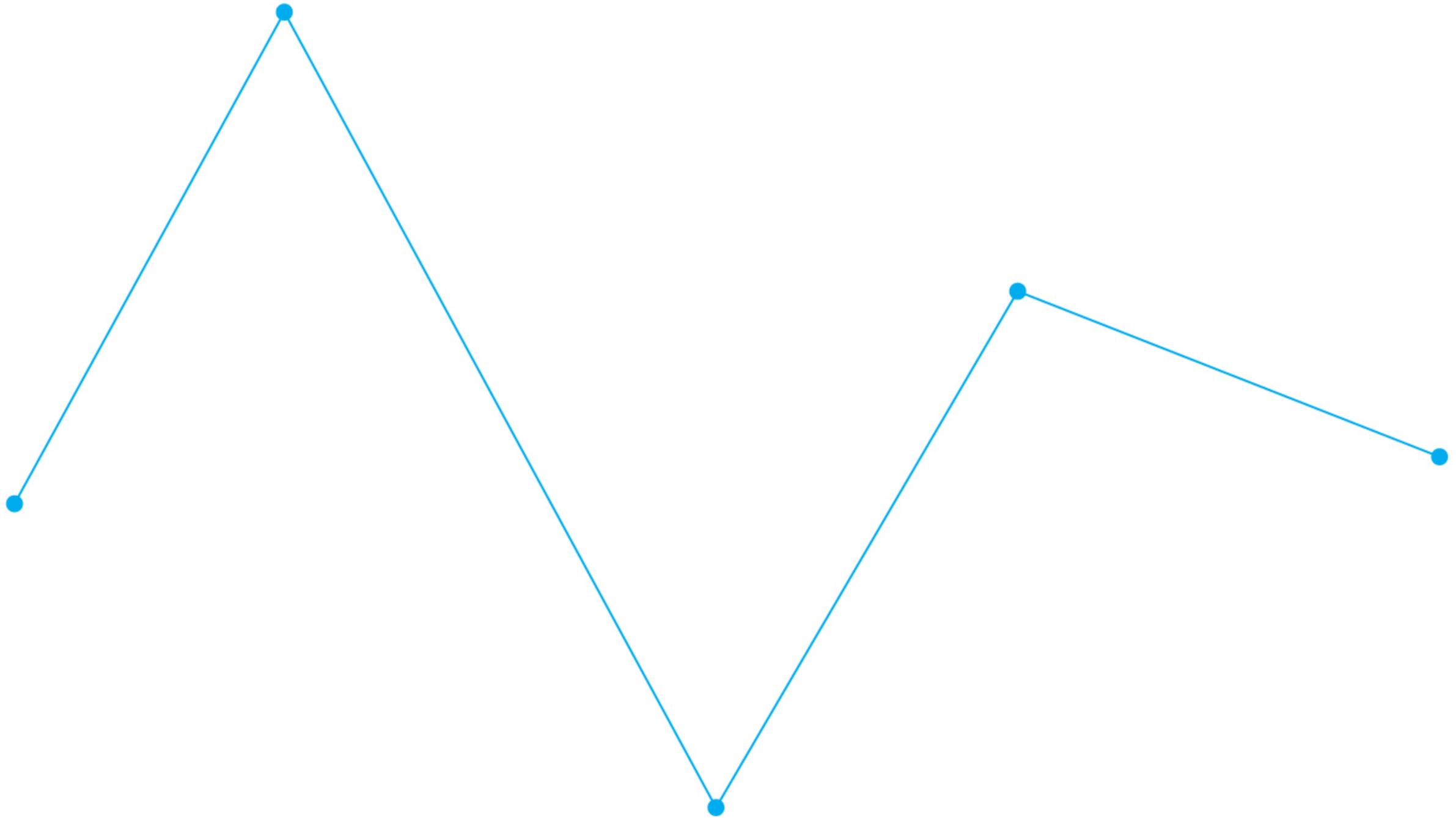
bezier curves and de castljam's algorithm



Bezier = Limit as N approaches infinity

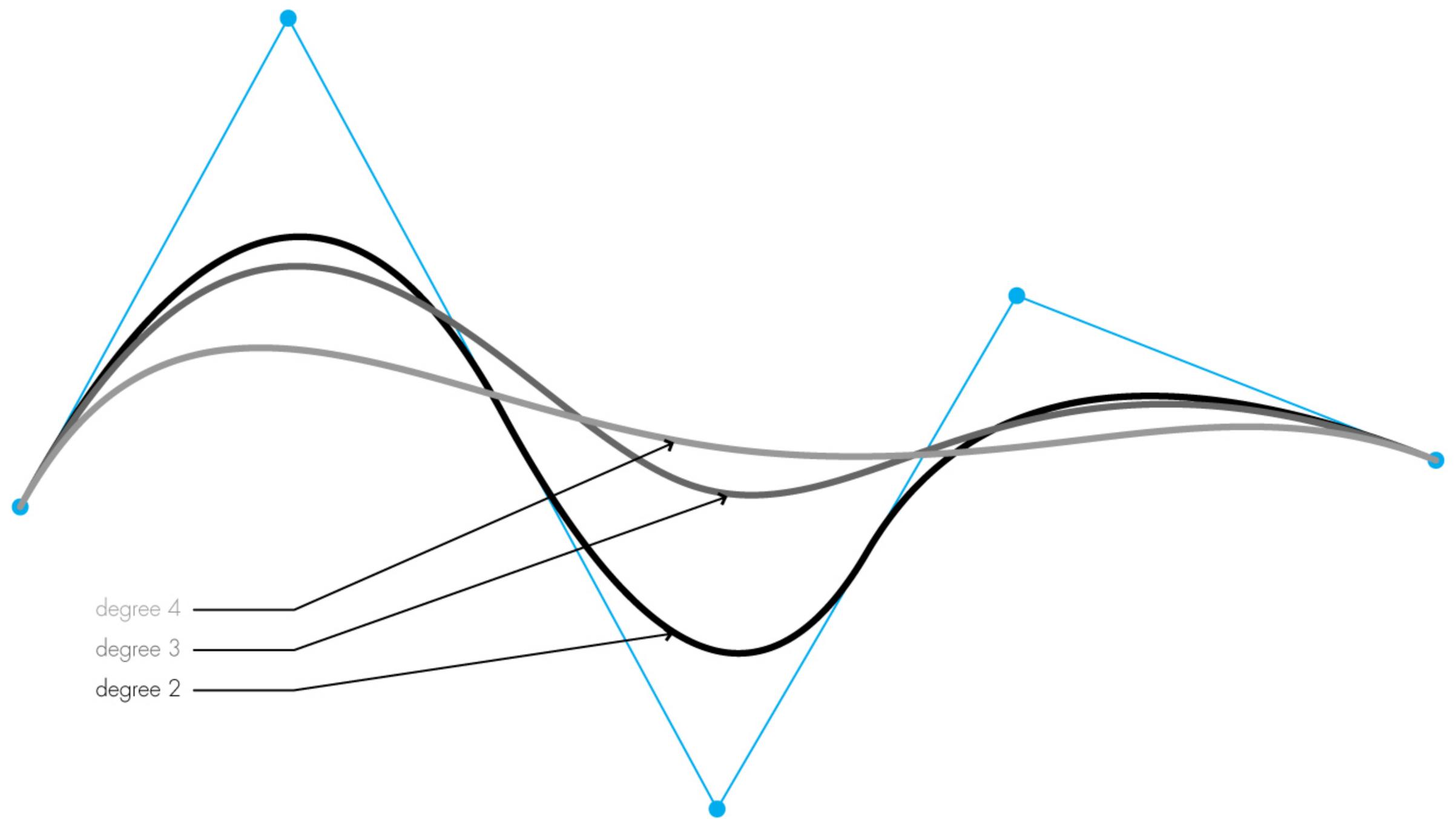
CURVATURE

nurbs: non-uniform rational b-spline



CURVATURE

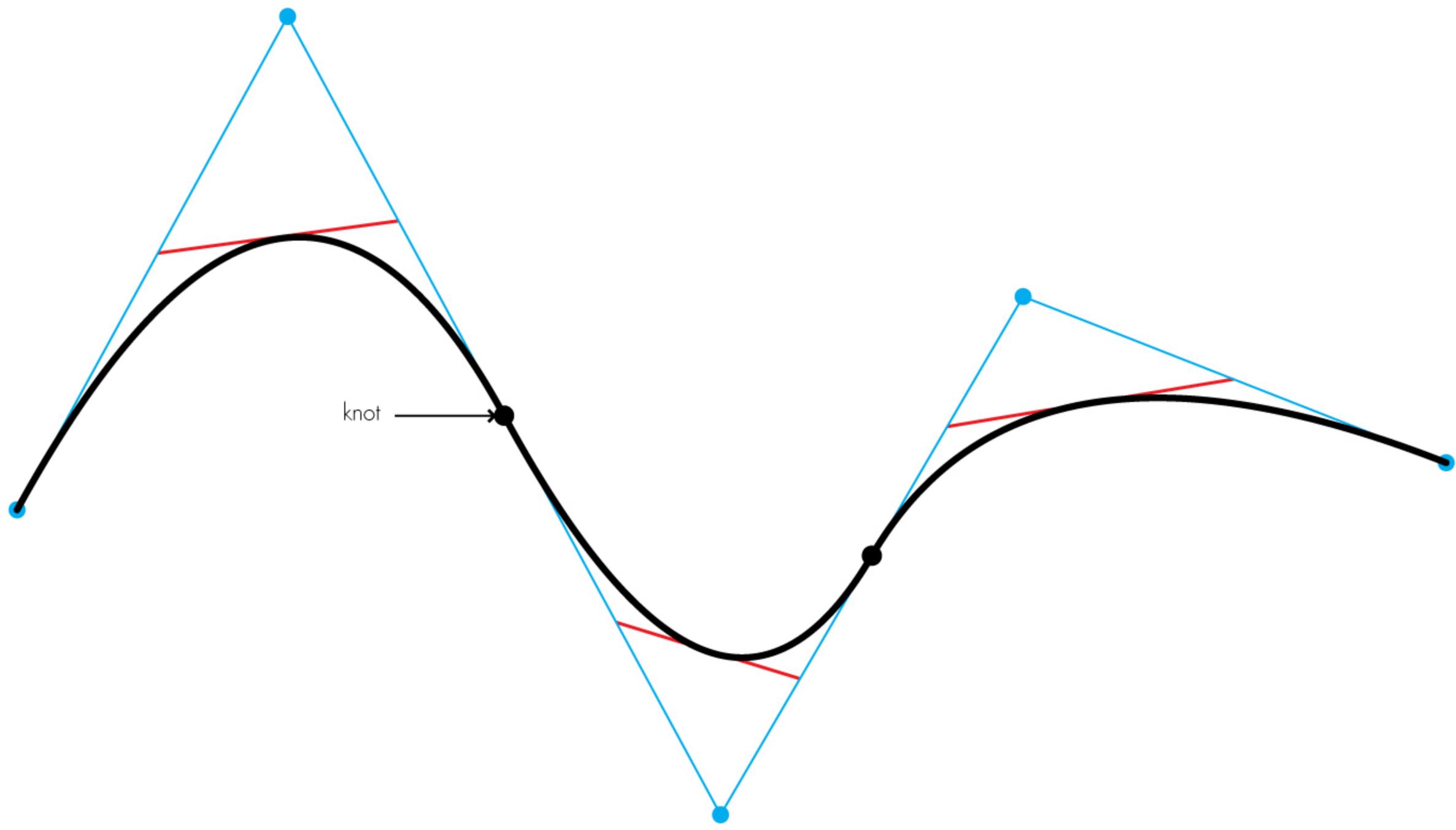
nurbs: non-uniform rational b-spline



degree 4
degree 3
degree 2

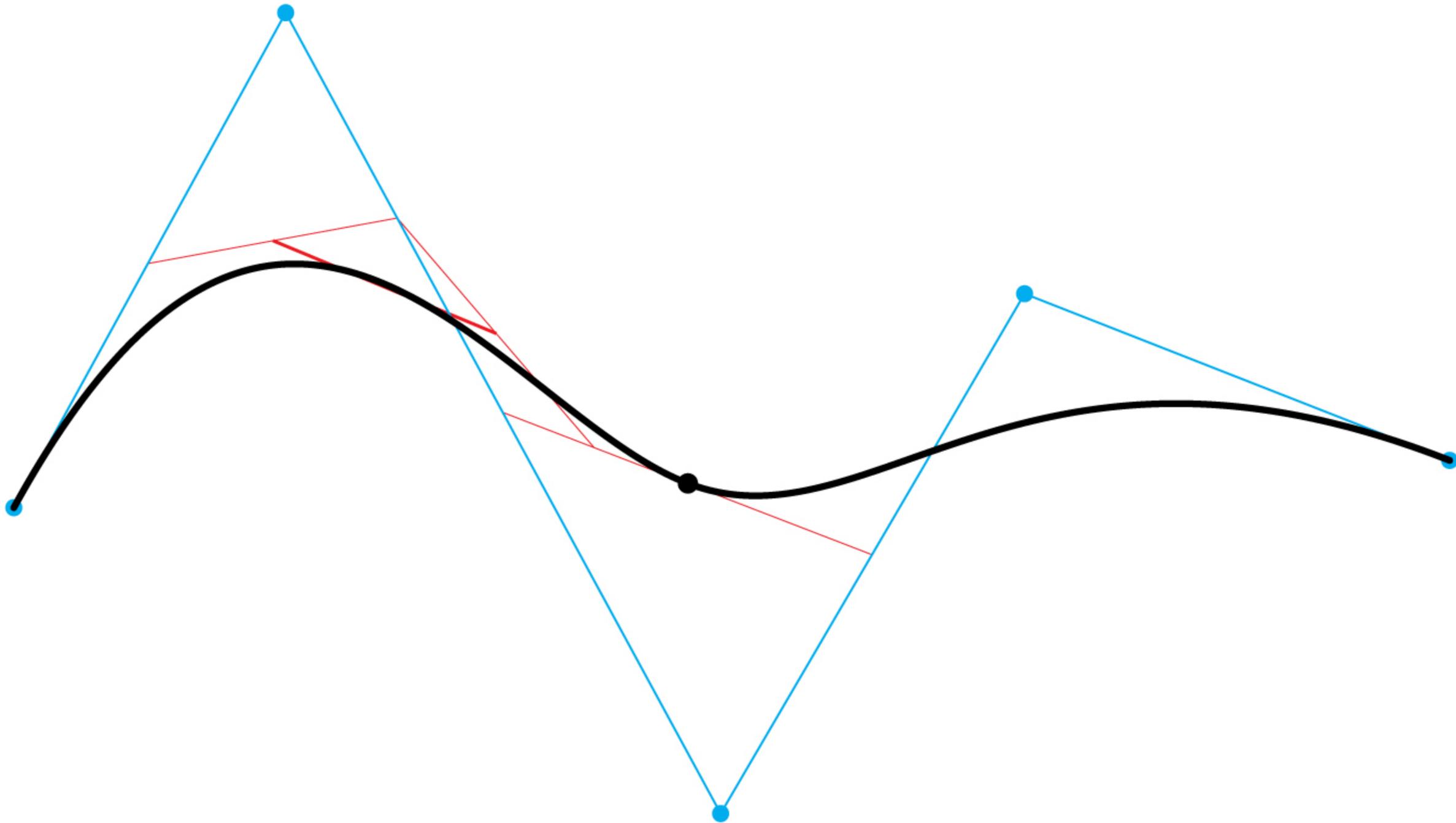
CURVATURE

nurbs: non-uniform rational b-spline



CURVATURE

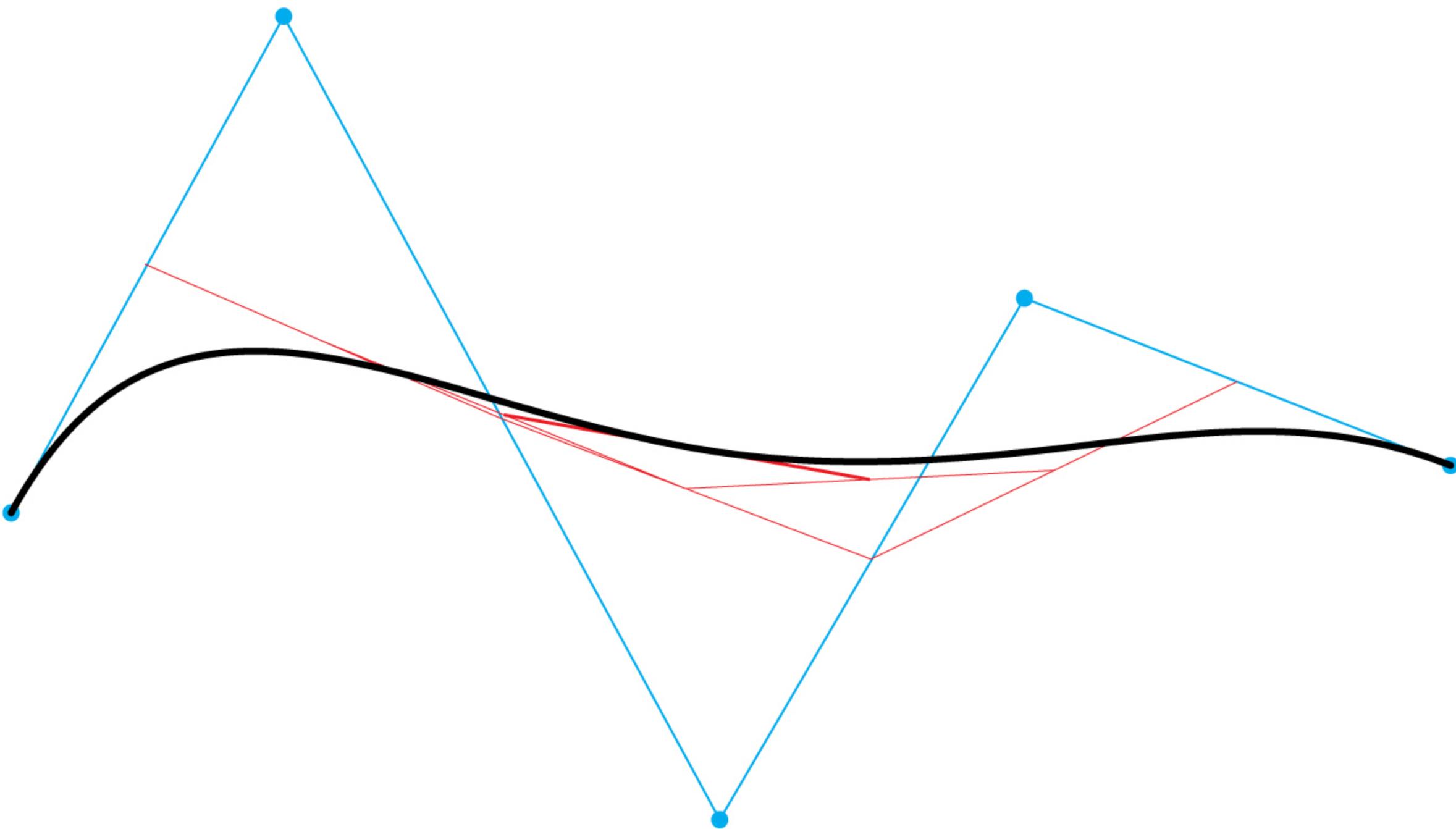
nurbs: non-uniform rational b-spline



Degree 3 Nurbs Curve (default)

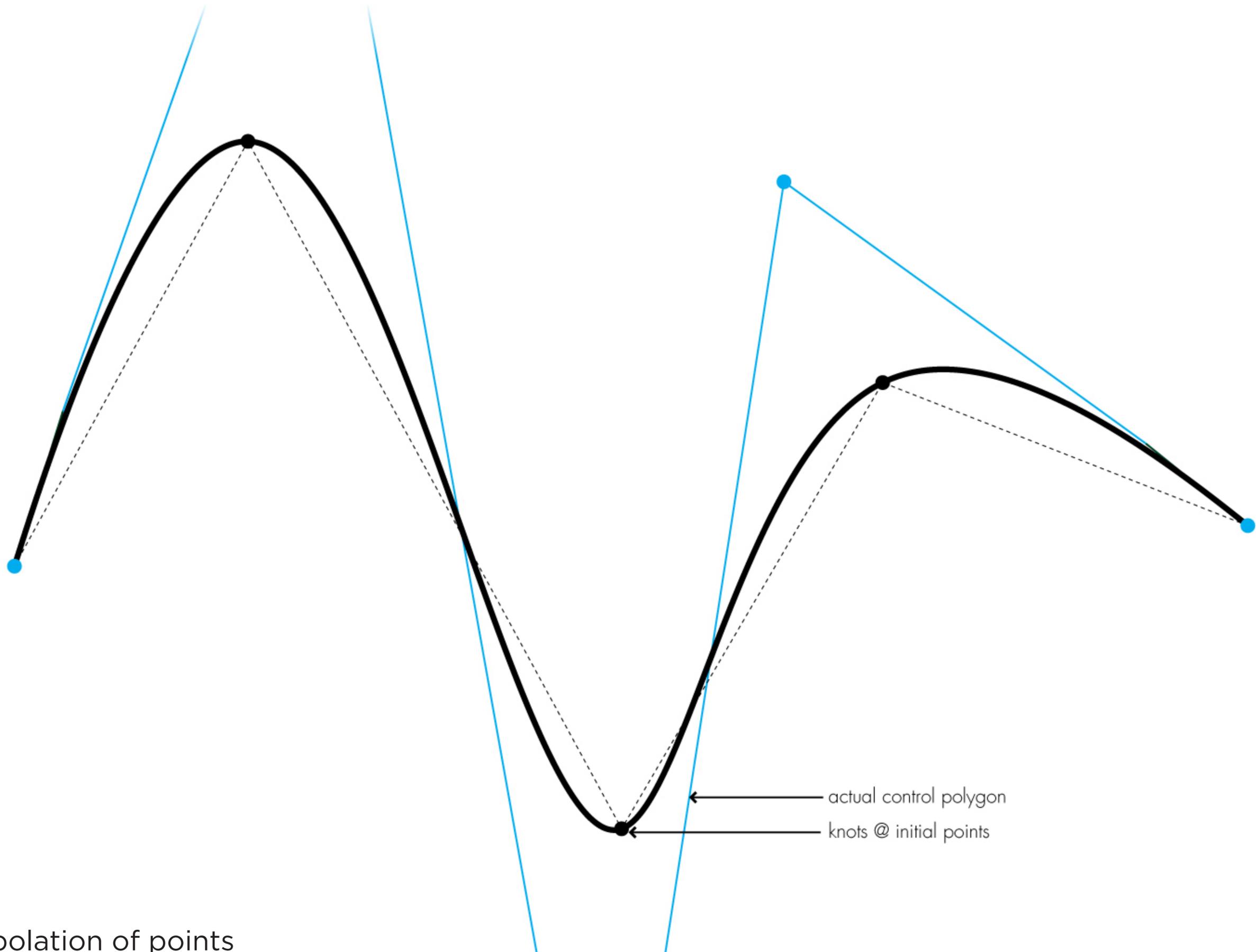
CURVATURE

nurbs: non-uniform rational b-spline



CURVATURE

nurbs: non-uniform rational b-spline



actual control polygon

knots @ initial points

Nurbs by Interpolation of points

**See also *Architectural Geometry*
for b-spline and subdivision
curve calculations**

Possible Resources

In Technique:

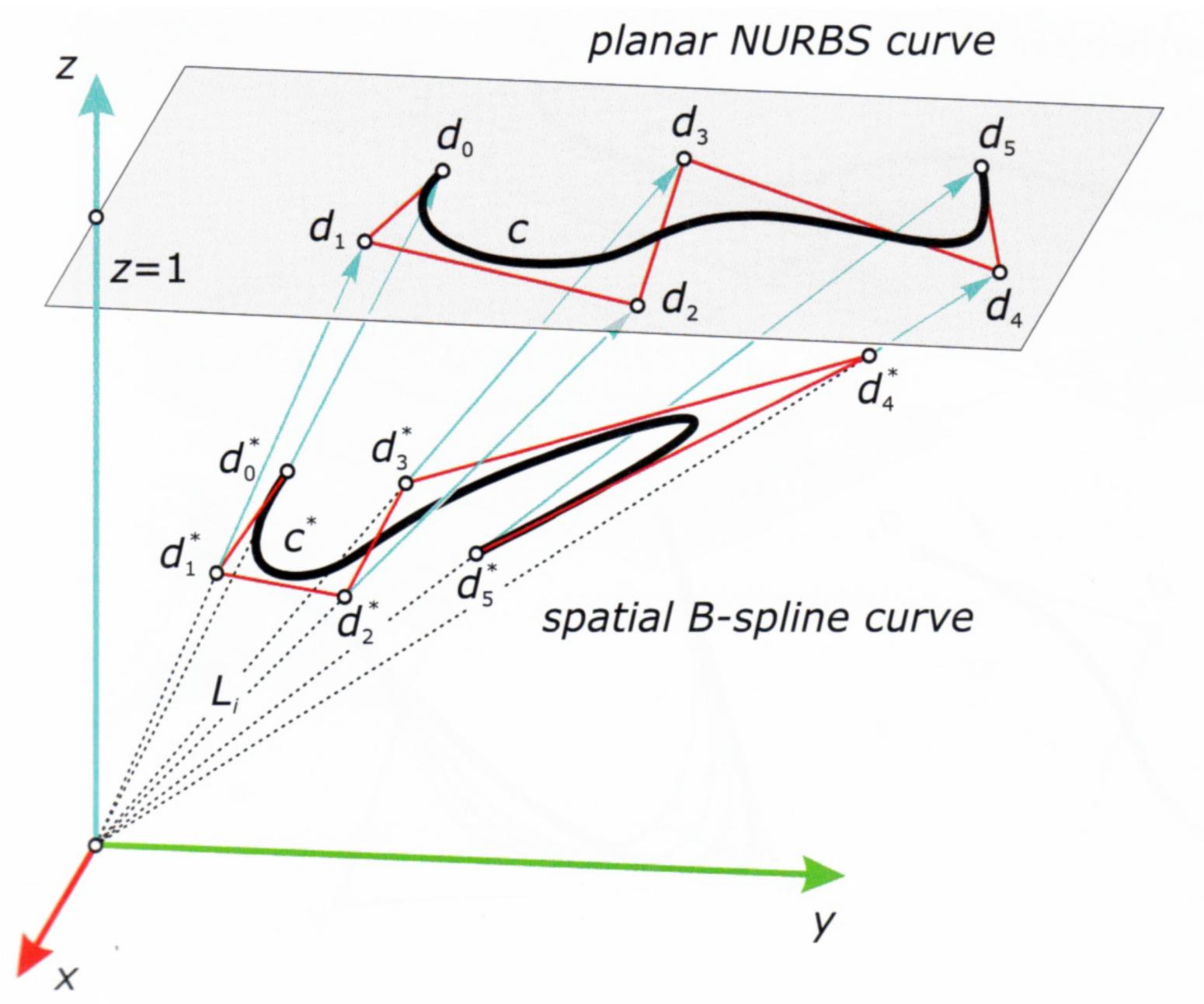
- Pottaman, Asperil, Hofer, Kilian: *Architectural Geometry* (Ch. 8)

In Discourse:

- Greg Lynn: *Animate Form* (introduction)
- Brandon Clifford: *In Defense of the Curve*

CURVATURE

nurbs: non-uniform rational b-spline



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4.105 Geometric Disciplines and Architecture Skills: Reciprocal Methodologies
Fall 2012

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