



Variability Simulation

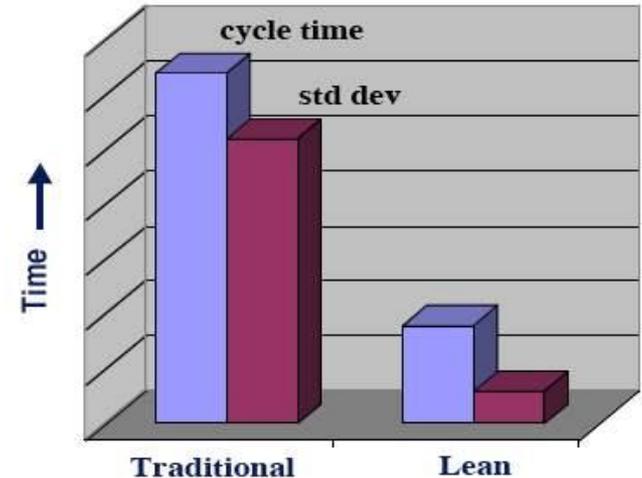
Learning Objectives

At the end of this module, you will be able to:

- **Discuss the impact that variability has on process performance**

The Impact of Variation

- **Variation impacts**
 - **Cycle time & throughput (Accounts Payable module)**
 - **Cost of Quality (Quality module)**
 - **Process capability (Six Sigma module)**
- **Reducing process variation is a key step in implementing lean practices**



Pre and post lean engineering drawing release data for major aircraft program

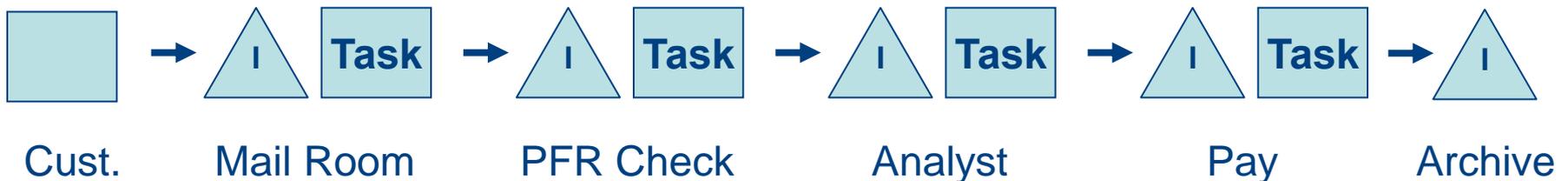
Source: Lockheed Martin Corporation

Learning About Variation

- **In this module, we will gain understanding about impact of variation through two simulations**
 - **Dice game will give experiential encounter**
 - **Computer simulation will rapidly show impact of process changes**
- **We' ll discover some important connections between variation and WIP, cycle time, throughput and utilization**
- **The Quality and Six Sigma Modules will introduce tools for controlling variation and its impact on process capability**

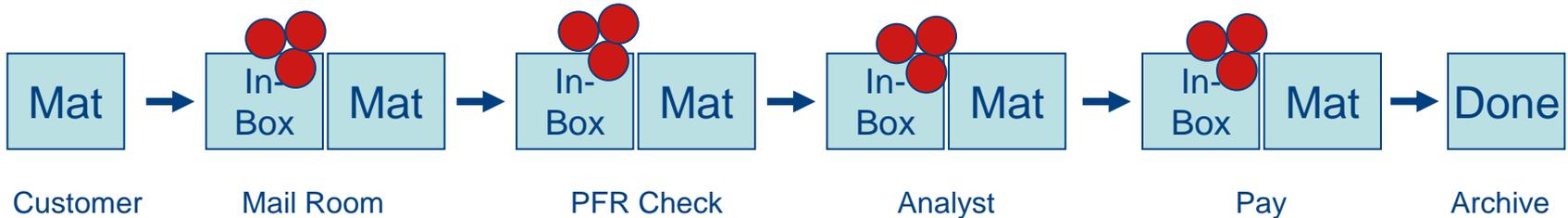
A “Perfect” System?

- Imagine a system that is perfectly balanced, has no rework, and has just enough capacity to meet customer demand
 - This module uses labels from the AP case study and/or the Clinic Lego® simulation, but this could be any system!
- The only imperfection we allow is variability in both input and process
- How will this system behave? Let’s find out...



Dice Game Setup

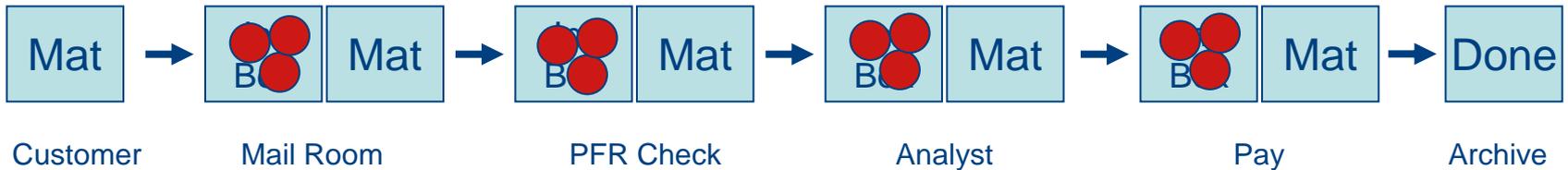
- 5-step system
- Mat with record sheet and 6-sided die at each station
- Middle 4 stations have inbox, with 3 chips per in-box



- **System processes chips**
(each time period, move a quantity of chips from one person to the next)
- **Roll of dice determines how many chips are moved**
- **CAN'T PASS MORE CHIPS THAN YOU HAVE IN YOUR "IN" BIN AT THE BEGINNING OF THE ROUND**
- **Let's work through one cycle**

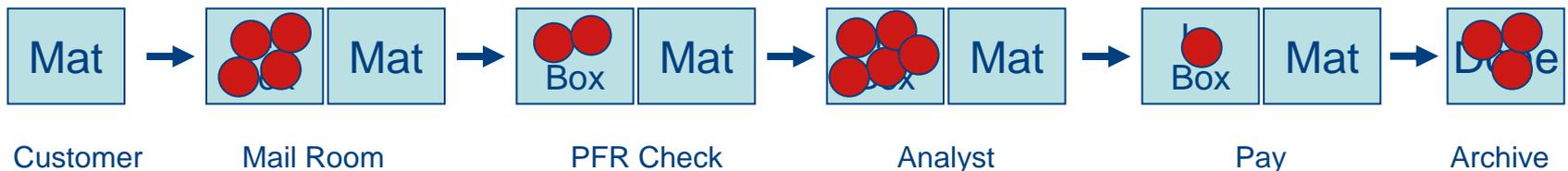
Example - Day1

Start of Day



Customer rolls a '3', passes 3 chips to Mail Room
 Mail Room rolls a '2', passes 2 chips to PFR Check
 PFR Check rolls a '5', passes 3 chips to Analyst
 Analyst rolls a '1', passes 1 chip to Pay
 Pay rolls a '6', passes 3 chips to the Archive

- **All these actions happen simultaneously**
- **Don't wait for other players to pass chips before you pick up yours**



End of Day

Accounting Example – Analyst

- Each round, record invoices completed and Work In Progress (WIP) level on your sheet
- From our example
 - Analyst at start of Day 1 had 3 WIP
 - Rolls a 1 and completes 1 invoice
 - Receives 3 invoices from PFR check and ends day with 5 WIP



DAY	Invoices Completed	WIP
		3
1	1	5
2		
3		
4		
5		
6		
7		
8		
9		
10		
11		
12		
13		
14		
15		
16		
17		
18		
19		
20		

A Total Invoices Completed	
B Invoices per day =A/20	
C Utilization =B/3.5	
D Ending WIP	
E Estimate cycle time =D/B	

Customer Worksheet

- Customer records new invoices from die roll
- Get Invoices Completed from Archive-Done
- Records total WIP by adding up all WIP or using mathematical shortcut below

Shortcut

Total WIP (new) = Total WIP (previous)
 + New Invoices
 - Invoices Complete

DAY	New Invoices Put Into the Process	Invoices Completed (Archive-Done)	Total WIP
			12
1	3	3	12
2			
3			
4			
5			
6			
7			
8			
9			
10			
11			
12			
13			
14			
15			
16			
17			
18			
19			
20			
A Totals			A1
B Invoices per day =A1/20			A2
C Utilization =B/3.5			
D Average WIP=A2/20			
E Average cycle time =D/B			

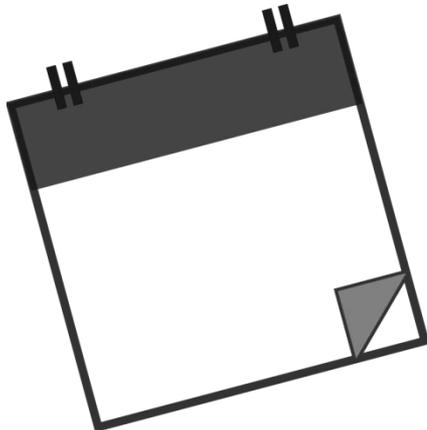
What *Should* happen?

- Consider 20 time periods, or “days”
- Each day, 3.5 chips are processed on average (the average of 1, 2, 3, 4, 5, 6)
- Intuitively, what *should* be the average throughput? Over 10 days? Over 20?
- What is the ideal flow (elapsed) time?

Let's find out what really happens...

Ready, Set, Play!

Day 20



Accounting

- **After 20 days, each person should add the appropriate columns to carry out the calculations at the bottom of their tally sheet**
- **The customer does slightly more complex calculations (use calculator if needed)**

Let's tabulate some results

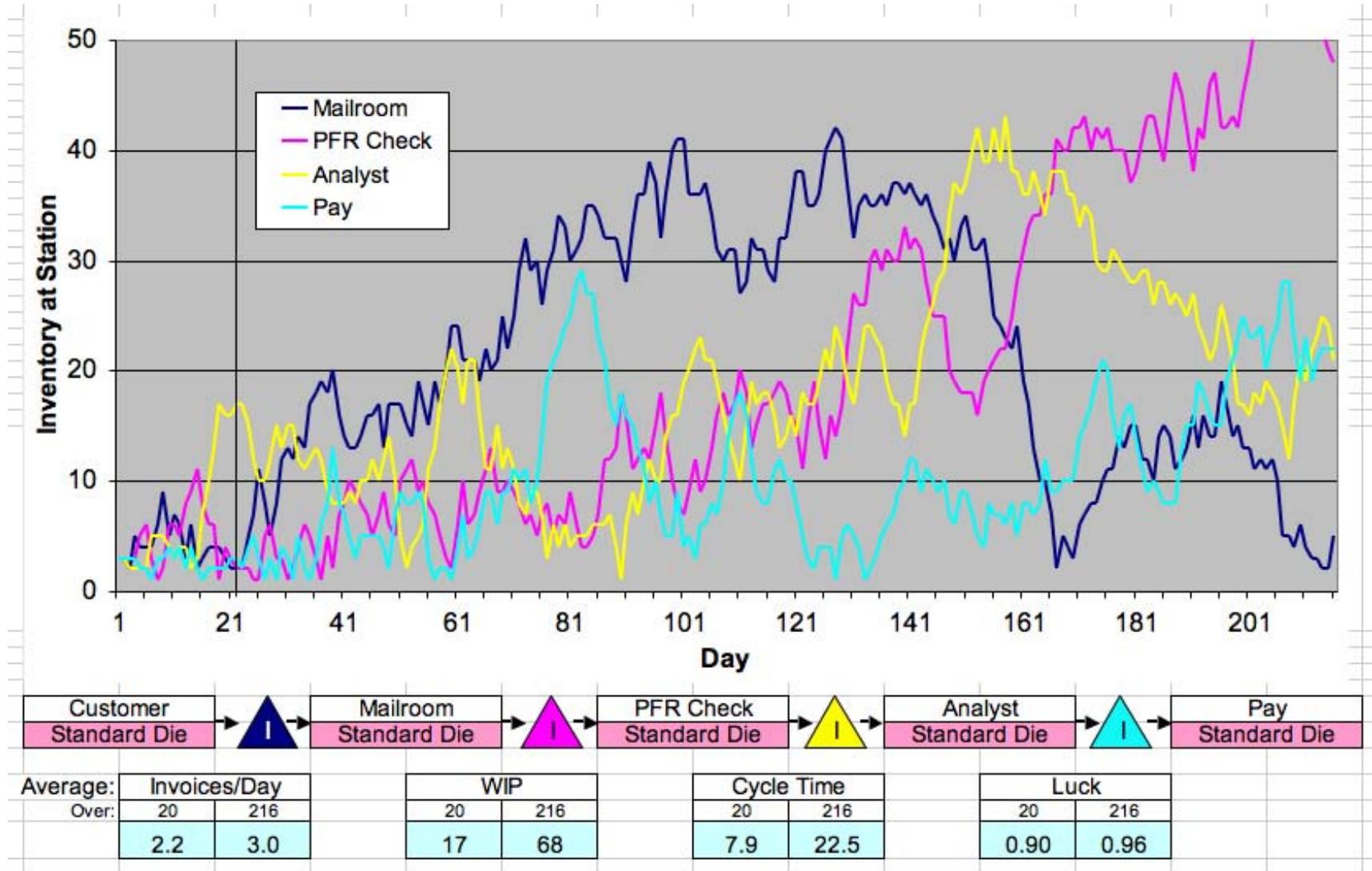
Questions

- **Why are fewer jobs processed than expected? Why is cycle time longer?**
 - **Statistical fluctuations**
 - Information that cannot be precisely predicted, varies from one instance to the next
 - **System dependencies**
 - Doing one task depends on having done another
 - Can't make up for lost capacity
- **How might the performance of this system be improved?**

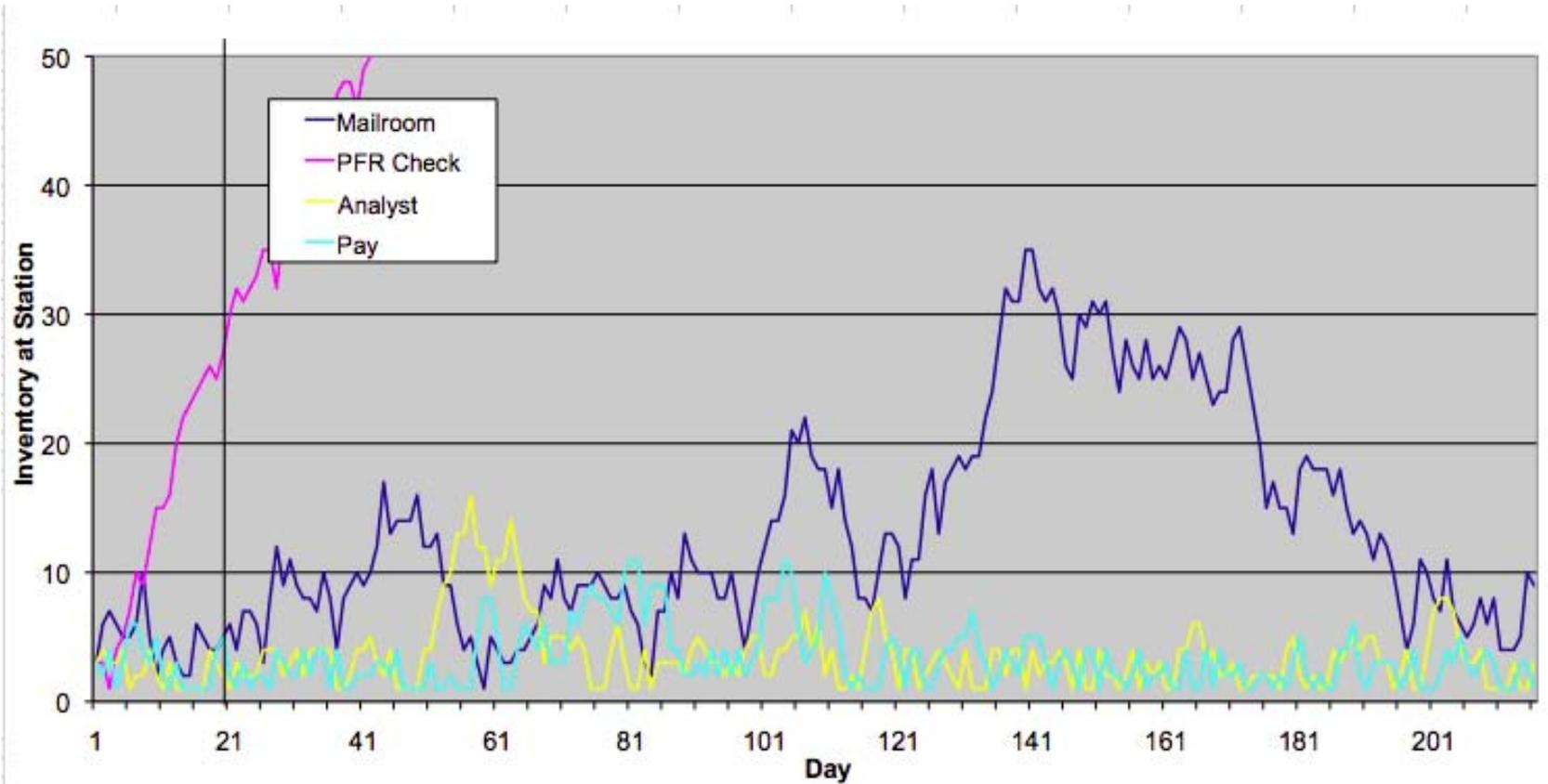
Computer Simulation

- **We can more rapidly gather experimental data with a computer simulation of the dice game**
- **We can easily change customer input and process step variation to see the impact.**
- **Look at the impact of input and process variability on cycle time after 20 and 216 days**

Spreadsheet Simulation

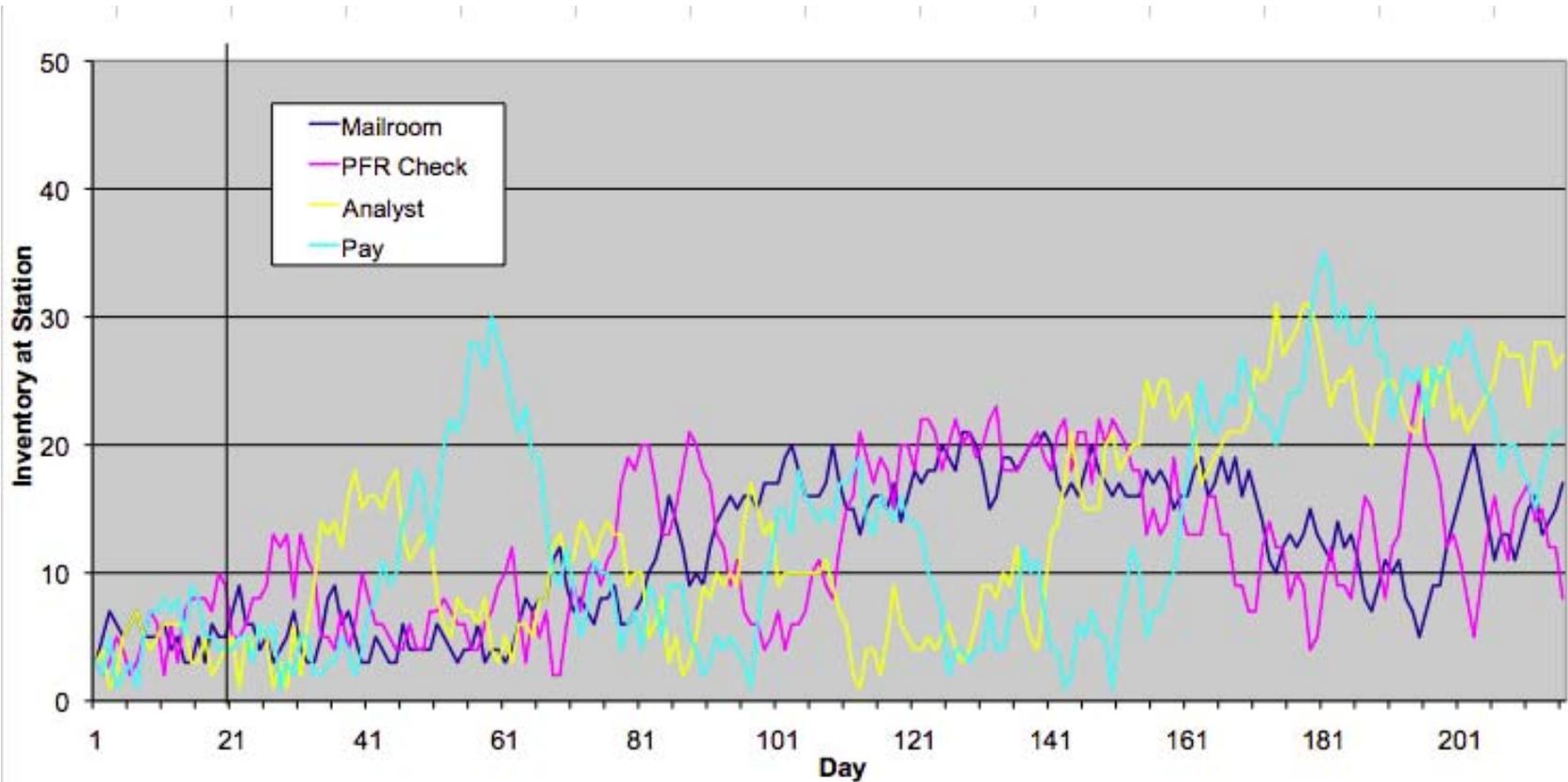


Bottleneck



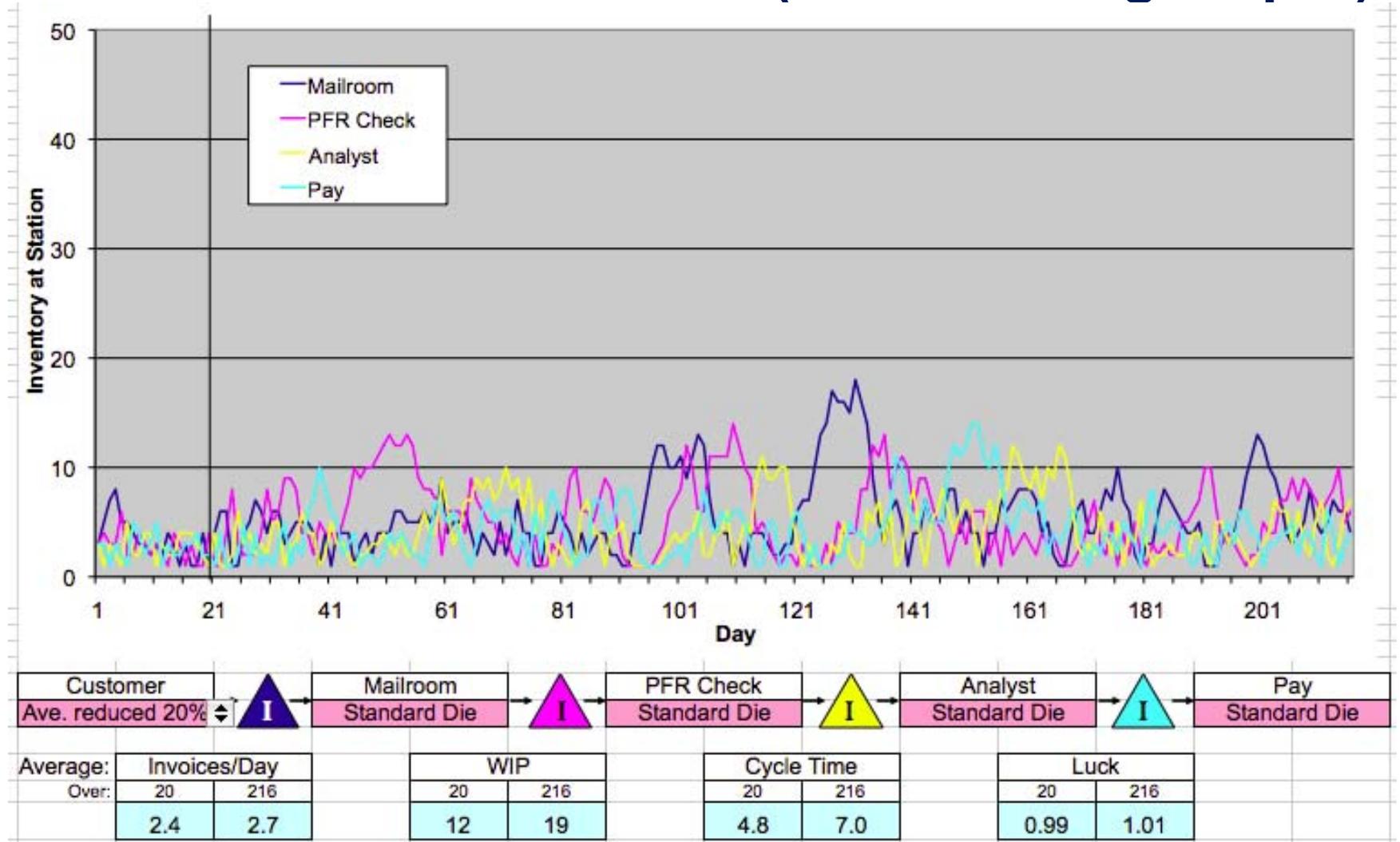
Customer	▲ I		Mailroom	▲ I	PFR Check	▲ I	Analyst	▲ I	Pay
Standard Die			Standard Die		Ave. reduced 30%		Standard Die		Standard Die
Average:	Invoices/Day		WIP		Cycle Time		Luck		
Over:	20	216	20	216	20	216	20	216	
	2.2	2.3	25	128	11.4	56.0	0.98	0.97	

Reduced Input Variation

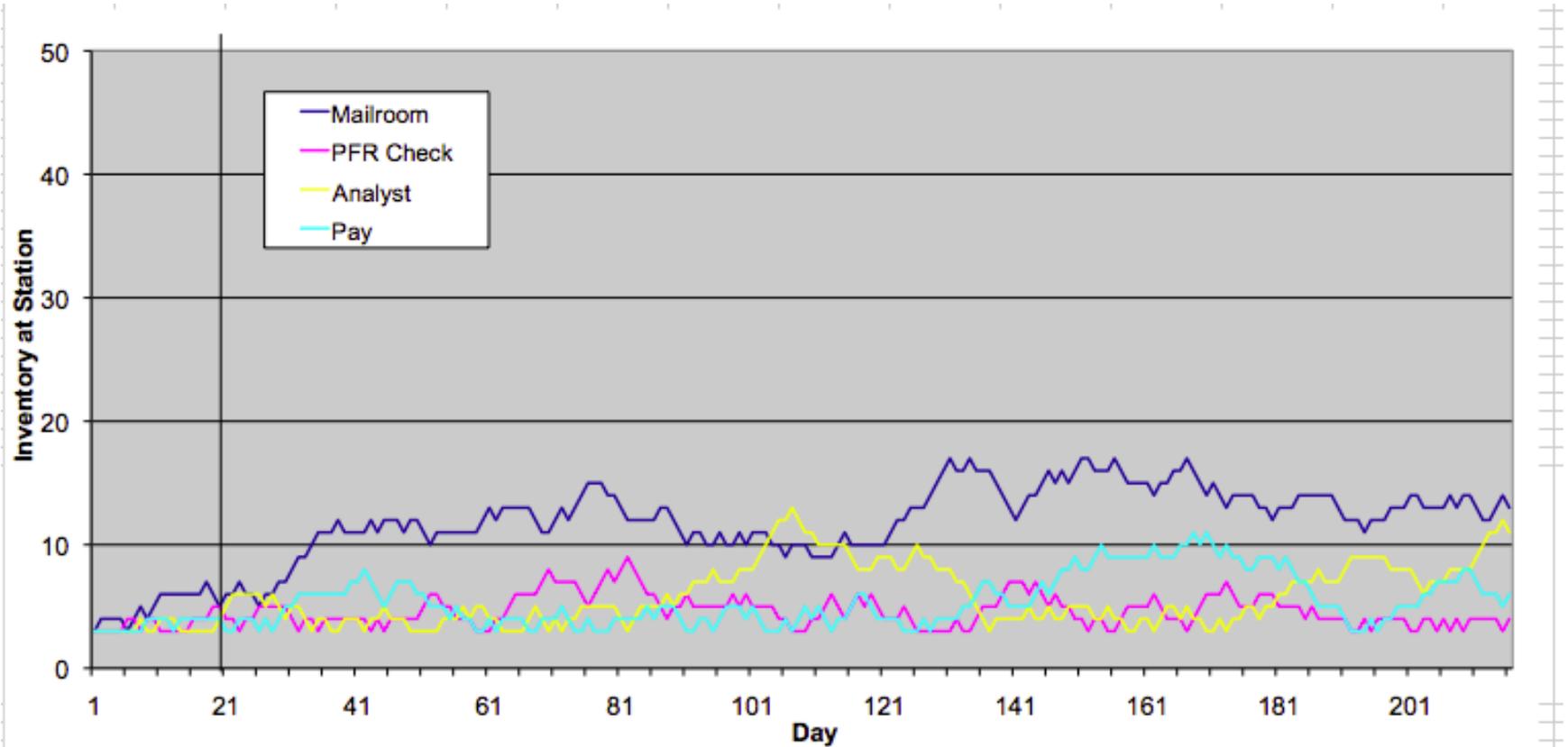


Customer	▲ I		Mailroom	▲ I	PFR Check	▲ I	Analyst	▲ I	Pay
Var. reduced 70%	↕		Standard Die		Standard Die		Standard Die		Standard Die
Average:	Invoices/Day		WIP		Cycle Time		Luck		
Over:	20	216	20	216	20	216	20	216	
	3.0	3.2	20	50	6.6	15.7	1.00	0.97	

Reduced Demand (lower average input)

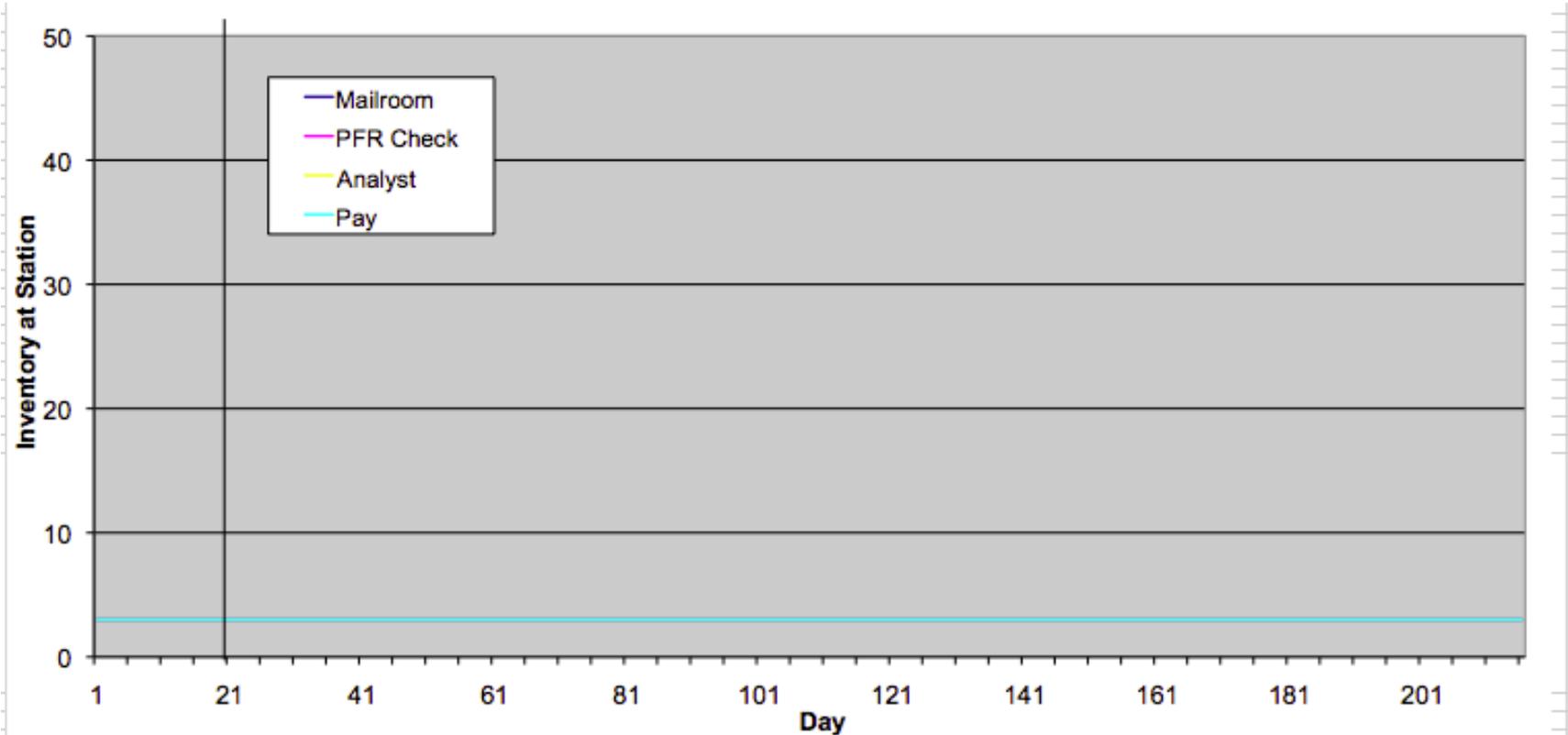


Reduced Total Variation



Customer	→ I	Mailroom	→ I	PFR Check	→ I	Analyst	→ I	Pay
Var. reduced 70%		Var. reduced 70%		Var. reduced 70%		Var. reduced 70%		Var. reduced 70%
Average:	Invoices/Day		WIP		Cycle Time		Luck	
Over:	20	216	20	216	20	216	20	216
	3.1	3.4	15	27	5.0	8.1	0.89	1.00

Constant Demand, Low Variation



Customer	→ I →		Mailroom	→ I →		PFR Check	→ I →		Analyst	→ I →		Pay
Constant (3)			Var. reduced 70%			Var. reduced 70%			Var. reduced 70%			Var. reduced 70%
Average:	Invoices/Day		WIP		Cycle Time		Luck					
Over:	20	216	20	216	20	216	20	216				
	3.0	3.0	12	12	4.0	4.0	1.01	1.00				

Queue Time

- Based on the equation for queue time,

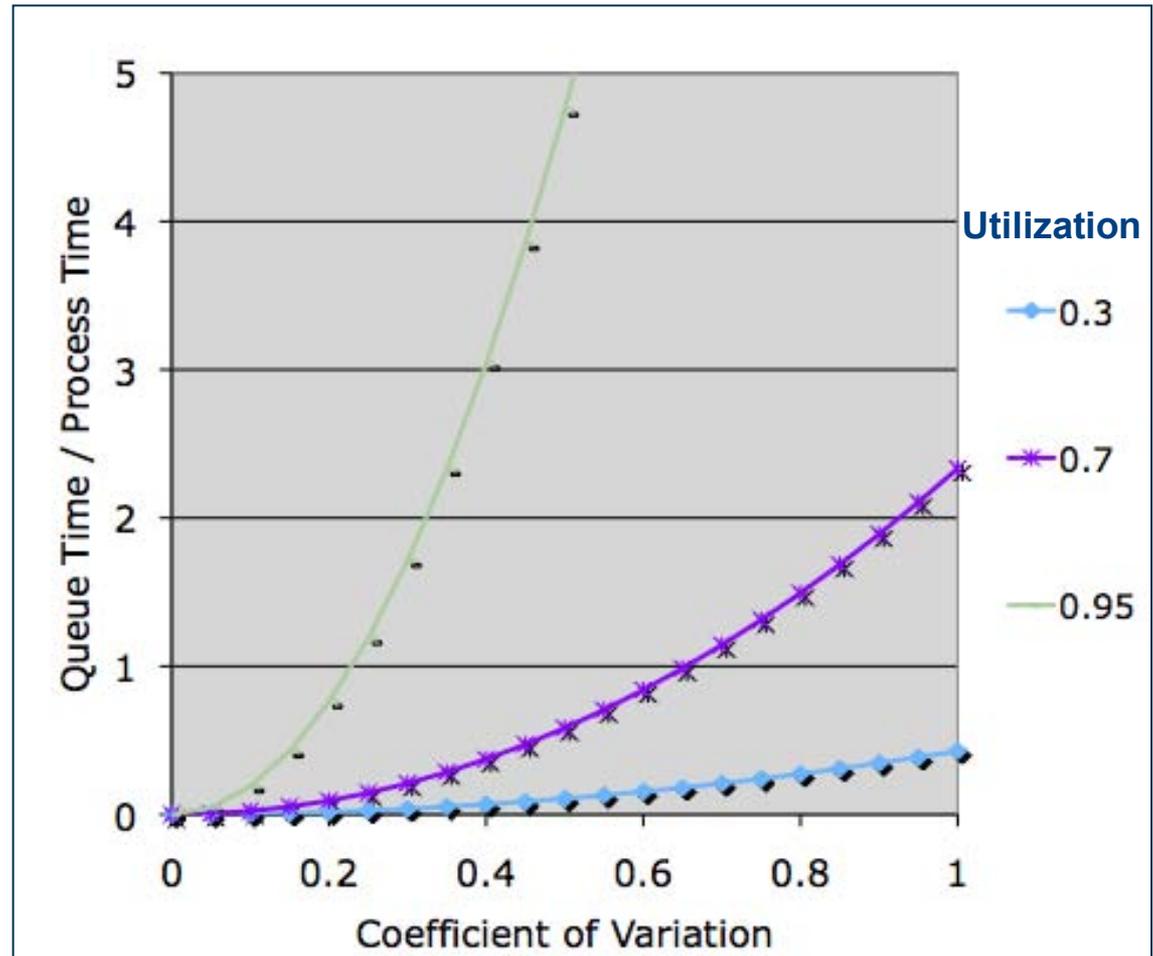
$$\text{Time_in_Queue} = \text{Activity_Time} * \left(\frac{\text{Utilization}}{1 - \text{Utilization}} \right) * \left(\frac{CV_a^2 + CV_p^2}{2} \right)$$

- CV_a is input variation
 - Which we may not control
- CV_p is process variation
 - Which we want to minimize
- Utilization is demand/capacity
 - Note to be “efficient” this should be 1...

Time_in_Queue = Wait time Activity_Time = Processing time

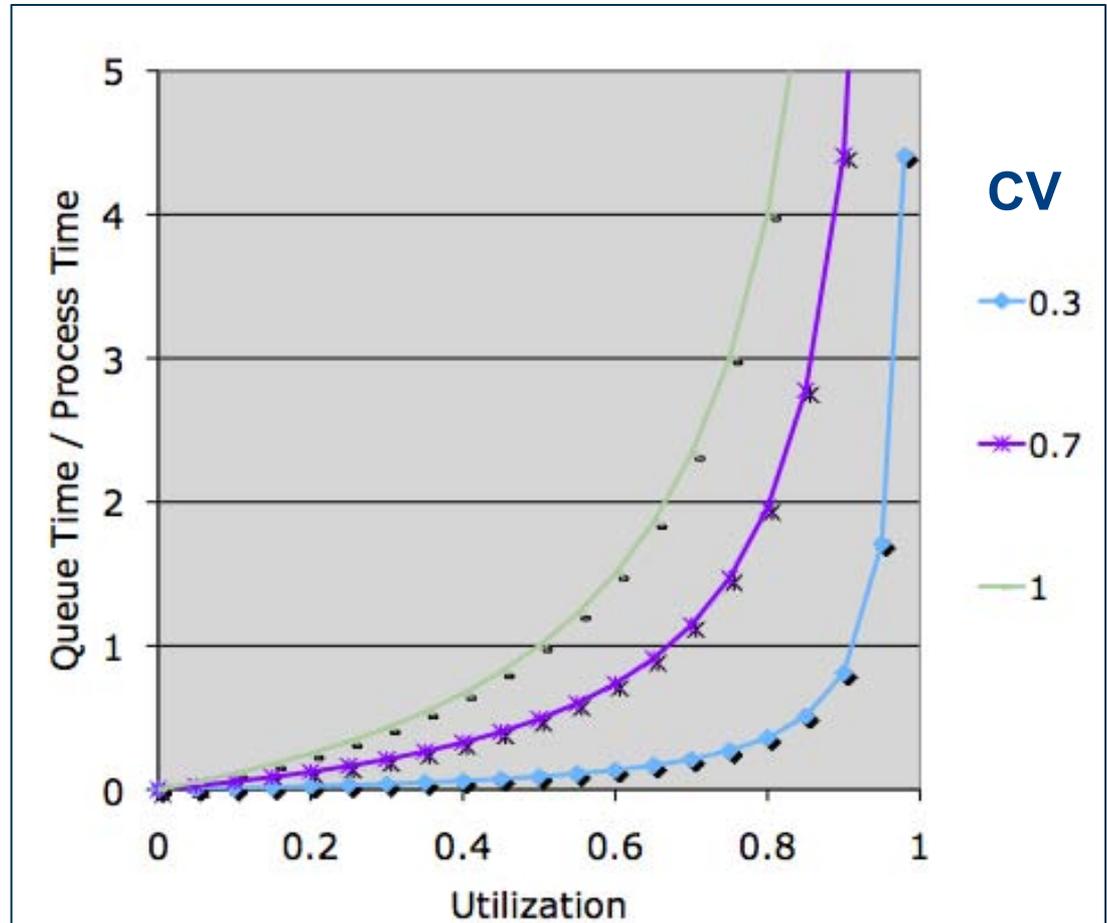
Controlling Variability

- Heroic reductions in variability required if utilization is high
- This is the motivation behind the 6-Sigma approach



Controlling Utilization (overburden)

- For any variation level, some level of utilization makes queue time explode
- This is *muri* and *mura* in action
- Often, slight easing makes a dramatic difference



Simulation: Summary

- **Simulated the system to examine behavior over a longer time period, more replications**
- **We made several improvements that demonstrate the power of a lean philosophy:**
 - **Reduced INPUT and PROCESS variability**
 - **Reduced average utilization of system slightly**
 - **Less variability and some “excess” capacity allowed response to customer need - Pull**
 - **Eliminating variability allowed straight-through flow to customer demand - Perfection**

Take Aways

- **Variability reduces expected process performance.**
- **Variability can occur in all processes across an enterprise, from manufacturing to engineering to administrative functions to patient care.**

Acknowledgements

Contributors

- **Ken Gilbert - University of Tennessee at Knoxville**
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- **Earll Murman – MIT**
- **Barrett Thomas – University of Iowa**

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