

# Activity Planning and Execution I: Operator-based Planning and Plan Graphs



Slides draw upon  
material from:  
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Univ Strathclyde

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16.410-13  
October 4<sup>th</sup>, 2010

## Assignments

- **Remember:**  
Problem Set #5: Constraint Satisfaction and Activity Planning,  
out Wed. Sep. 29<sup>th</sup>, due Wed, Oct. 6<sup>th</sup>, 2010.
- **Reading:**
  - Today: Advanced Planning [*AIMA*] Ch. 11;  
“GraphPlan,” by Blum & Furst.
  - Wednesday: Dechter, R., I. Meiri, J. Pearl, “Temporal  
Constraint Networks,” *Artificial Intelligence*, 49, pp.  
61-95, 1991 posted on Stellar.
- **Exam:**
  - Mid-Term - October 20<sup>th</sup>.

■ Brian Williams, Fall 10 ■

# Simple Spacecraft Problem

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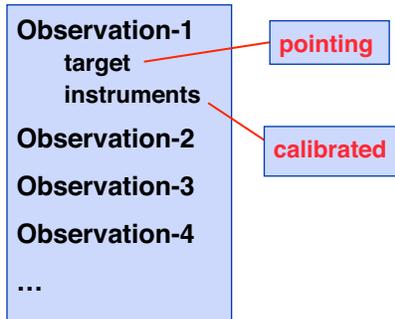


Image credit: NASA.

Propositions: Target Pointed To, Camera Calibrated?, Has Image?  
Operators: Calibrate, Turn to Y, and Take Image.

## Outline

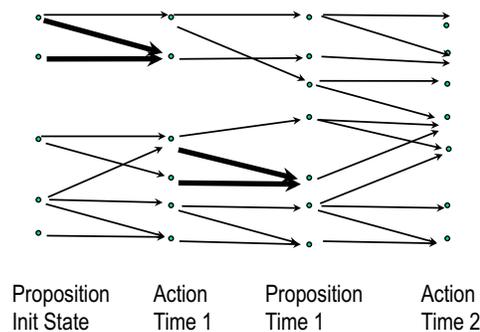
- Graph Plan
  - Problem Statement
  - Planning Graph Construction
  - Plan Extraction

# Graph Plan

- Developed in 1995 by Avrim Blum and Merrick Furst, at CMU.
- The Plan Graph compactly encodes all possible plans.
  - has been a key to scaling up to realistic problems.
- Plan Graph representation used for:
  - An encoding method for formulating planning as a CSP.
  - Relaxed planning as an admissible heuristic (state space search + A\*).
- Approach has been extended to reason with temporally extended actions, metric and non-atomic preconditions and effects.

## Approach: Graph Plan

1. Construct compact constraint encoding of state space from operators and the initial state.  
- *Planning Graph*
2. Generate plan by searching for a consistent subgraph that achieves the goals.



# Representing States

- State
  - A consistent conjunction of propositions (positive literals).
    - E.g., (and (cleanhands) (quiet) (dinner) (present) (noGarbage))
    - All unspecified propositions are false.
- Initial State
  - Problem state at time  $i = 0$ .
    - E.g., (and (cleanHands) (quiet)).
- Goal State
  - A partial state.
    - E.g., (and (noGarbage) (dinner) (present)).
  - A Plan moves a system from its initial state to a final state that extends the goal state.

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# Representing Operators

(:operator cook :precondition (cleanHands)  
:effect (dinner))

Note: STRIPS doesn't  
allow derived effects;  
you must be complete!

**Preconditions:** Propositions that must be true to apply the operator.

- A conjunction of propositions (no negated propositions).

**Effects:** Propositions that the operator changes, given that the preconditions are satisfied.

- A conjunction of propositions (called **adds**) and their negation (called **deletes**).

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## (Parameterized) Operator Schemata

- Instead of defining many operator instances:  
**pickup-A** and **pickup-B** and ...

- Define a schema:

```
(:operator pick-up
  :parameters ((?ob1 - block))
  :precondition (and (clear ?ob1)
                    (on-table ?ob1)
                    (arm-empty))
  :effect (and (not (clear ?ob1))
              (not (on-table ?ob1))
              (not (arm-empty))
              (holding ?ob1)))
```

## Example Problem: Dinner Date

Initial Conditions: (:init (cleanHands) (quiet))

Goal: (:goal (noGarbage) (dinner) (present))

Actions:

```
(:operator carry :precondition
  :effect (and (noGarbage) (not (cleanHands))))
```

```
(:operator dolly :precondition
  :effect (and (noGarbage) (not (quiet))))
```

```
(:operator cook :precondition (cleanHands)
  :effect (dinner))
```

```
(:operator wrap :precondition (quiet)
  :effect (present))
```

+ noops

Plan: (Cook, Wrap, Carry)

## Visualizing Actions

(:operator **cook** :precondition (cleanHands)  
:effect (dinner))

cleanHands  $\Rightarrow$  cook  $\Rightarrow$  dinner

(:operator **carry** :precondition  
:effect (and (noGarbage) (not (cleanHands))))

carry  $\Rightarrow$  noGarb  
carry  $\Rightarrow$  cleanH

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## Visualizing Actions

- **Persistence actions (No-ops)**

- Every literal has a no-op action, which maintains it from time  $i$  to  $i+1$ .

(:operator noop-P :precondition (P) :effect (P))

P  $\Rightarrow$  Noop-P  $\Rightarrow$  P

In Blum & Furst: (& lecture)

AIMA:

Only persist positive literals.

Persists negative literals as well.

either approach okay for PSet. <sup>12</sup>

## Operator Execution Semantics

If all propositions of *:precondition* appear in state *i*,  
Then create state *i+1* from *i*, by

- adding to *i*, all “add” propositions in *:effects*,
- removing from *i*, all “delete” propositions in *:effects*.

(:operator **cook** *:precondition* (cleanHands)  
*:effect* (dinner))

(cleanHands)  
(quiet)  $\Longrightarrow$  cook  $\Longrightarrow$  (cleanHands)  
(quiet)  
(dinner) 13

## Operator Execution Semantics

If all propositions of *:precondition* appear in state *i*,  
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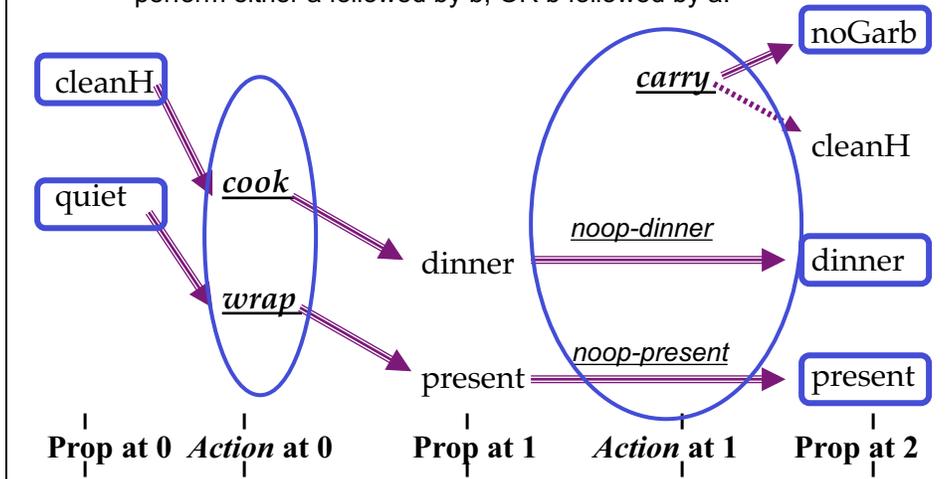
- adding to *i*, all “add” propositions in *:effects*,
- removing from *i*, all “delete” propositions in *:effects*.

(:operator **dolly** *:precondition*  
*:effect* (and (noGarbage) (not (quiet))))

(cleanHands)  
(quiet)  $\Longrightarrow$  dolly  $\Longrightarrow$  (cleanHands)  
(noGarbage) 14

## Representing Plans: $\langle \text{Actions}[i] \rangle$

- Sets of concurrent actions that are performed at each time [i]
  - Concurrent actions can be interleaved in any order.
    - ⇒ If actions a and b occur at time i, then it must be valid to perform either a followed by b, OR b followed by a.



## A Complete Consistent Plan

Given an initial state that holds at time 0, and goal propositions, a plan is a solution iff it is:

Complete:

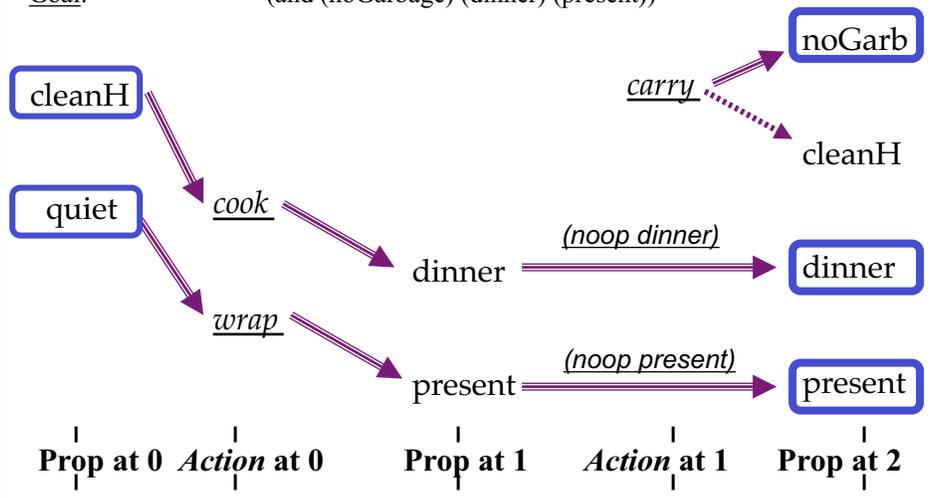
- The **goal propositions** all hold in the **final state**.
- The **preconditions** of every operator at time i, are **satisfied** by **propositions** at time i.

Consistent:

## Example of a Complete Plan

Initial Conditions: (and (cleanHands) (quiet))

Goal: (and (noGarbage) (dinner) (present))



## A Complete Consistent Plan

Given an initial state that holds at time 0, and goal propositions, a plan is a solution iff it is:

Complete:

- The goal propositions all hold in the final state.
- The preconditions of every operator at time  $i$ , are satisfied by propositions at time  $i$ .

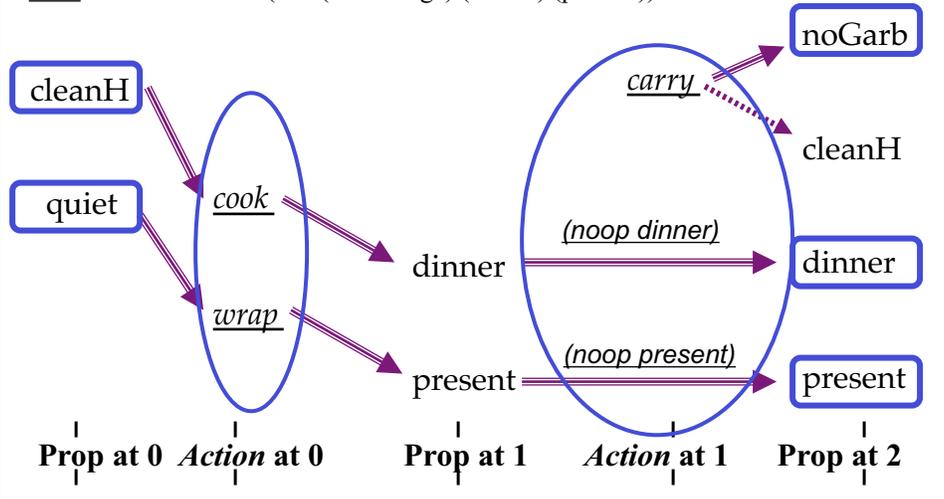
Consistent:

- The operators at any time  $i$  can be **executed in any order**, without one of these operators **undoing**:
  - the **preconditions** of another operator at time  $i$ .
  - the **effects** of another operator at time  $i$ .

## Example of a Complete Consistent Plan

Initial Conditions: (and (cleanHands) (quiet))

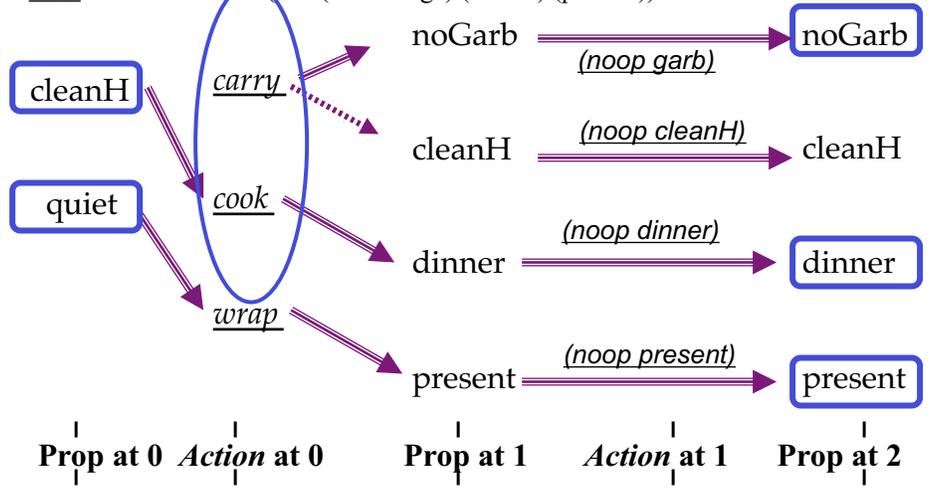
Goal: (and (noGarbage) (dinner) (present))



## Example of a Complete **Inconsistent** Plan

Initial Conditions: (and (cleanHands) (quiet))

Goal: (and (noGarbage) (dinner) (present))



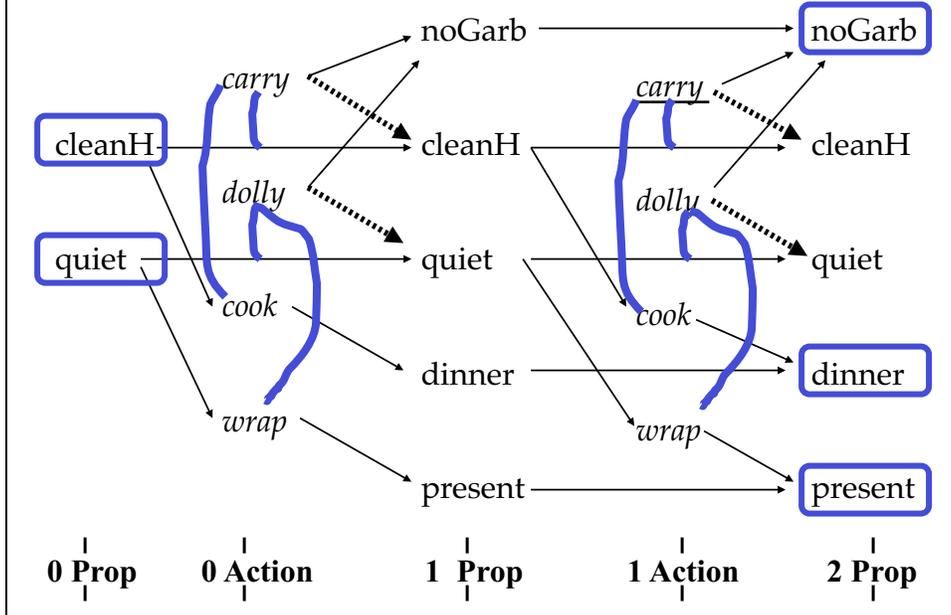
## Outline

- Graph Plan
  - Problem Statement
  - Planning Graph Construction
  - Plan Extraction

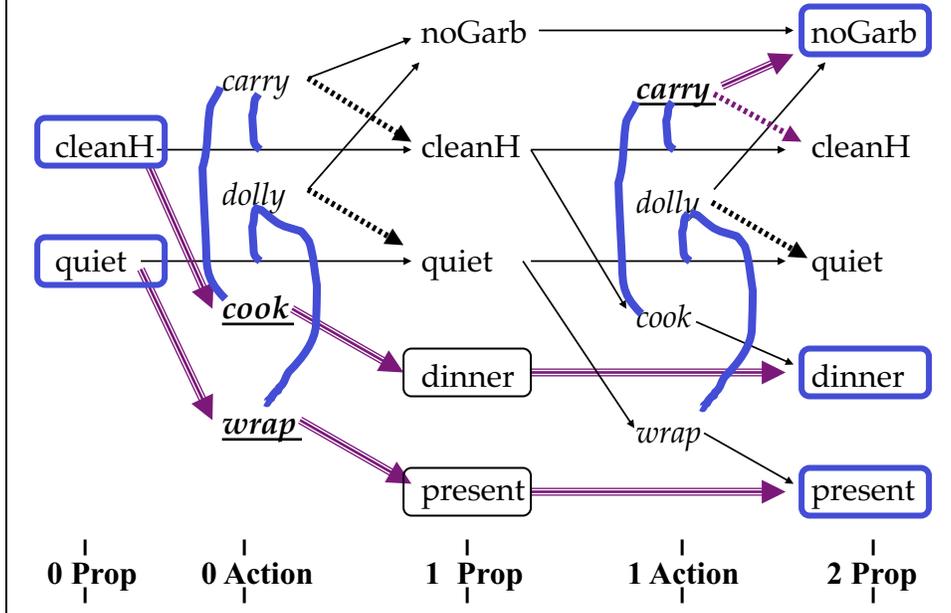
## Graph Plan Algorithm

- Phase 1 – Plan Graph Expansion
  - Graph **includes all plans** that are complete and consistent.
  - Graph prunes many infeasible plans.
- Phase 2 - Solution Extraction
  - Graph frames a kind of **constraint satisfaction problem** (CSP).
  - Extraction **selects** actions to perform at each time point, **by assigning variables** and by testing consistency.

## Example: Planning Graph and Solution



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## Graph Plan Algorithm

- Phase 1 – Plan Graph Expansion
  - Graph **includes all plans** that are complete and consistent.
  - Graph prunes many infeasible plans.
- Phase 2 - Solution Extraction
  - Graph frames a kind of **constraint satisfaction problem** (CSP).
  - Extraction **selects** actions to perform at each time point, **by assigning variables** and by testing consistency.
- Repeat Phases 1 and 2 for planning graphs with an increasing numbers of action layers.

## Planning Graphs Prune

### Initial state reachability:

Prunes partial states and actions at each time  $i$  that are not reachable from the initial state,

### Consistency:

Prunes pairs of propositions and actions that are mutually inconsistent at time  $I$ , and

### Goal state reachability:

plans that cannot reach the goals.

## Graph Properties

- Plan graphs are constructed in polynomial time and are of polynomial in size.
- Plan graphs do not eliminate all infeasible plans.
- ➔ Plan generation requires *focused* search.

## Constructing the Planning Graph... (Reachability)

- Initial proposition layer
  - Contains propositions that hold in the initial state.

## Example: Initial State, Layer 1

cleanH

quiet

0 Prop

0 Action

1 Prop

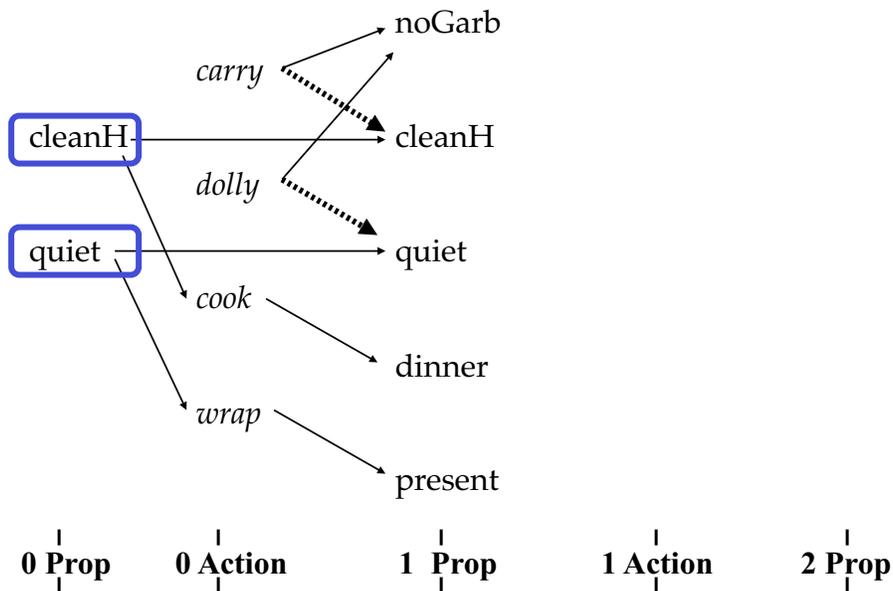
1 Action

2 Prop

## Constructing the Planning Graph... (Reachability)

- Initial proposition layer
  - Contains propositions that hold in the initial state.
- Action layer  $i$ 
  - If all of an action's preconditions appear in proposition layer  $i$ ,
  - Then add action to layer  $i$ .
- Proposition layer  $i+1$ 
  - For each action at layer  $i$ ,
  - Add all its effects at layer  $i+1$ .

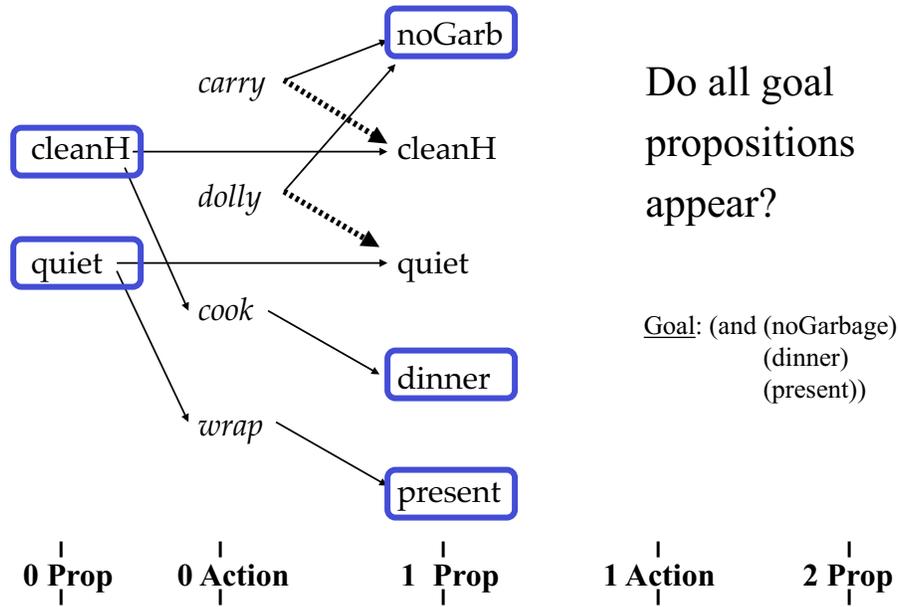
## Example: Add Actions and Effects



## Constructing the Planning Graph... (Reachability)

- Initial proposition layer
  - Contains propositions that hold in the initial state.
- Action layer  $i$ 
  - If all of an action's preconditions appear in proposition layer  $i$ ,
  - Then add action to layer  $i$ .
- Proposition layer  $i+1$ 
  - For each action at layer  $i$ ,
  - Add all its effects at layer  $i+1$ .
- Repeat adding layers until all goal propositions appear.

## Round 1: Stop at Proposition Layer 1?



## Constructing the Planning Graph... (Consistency)

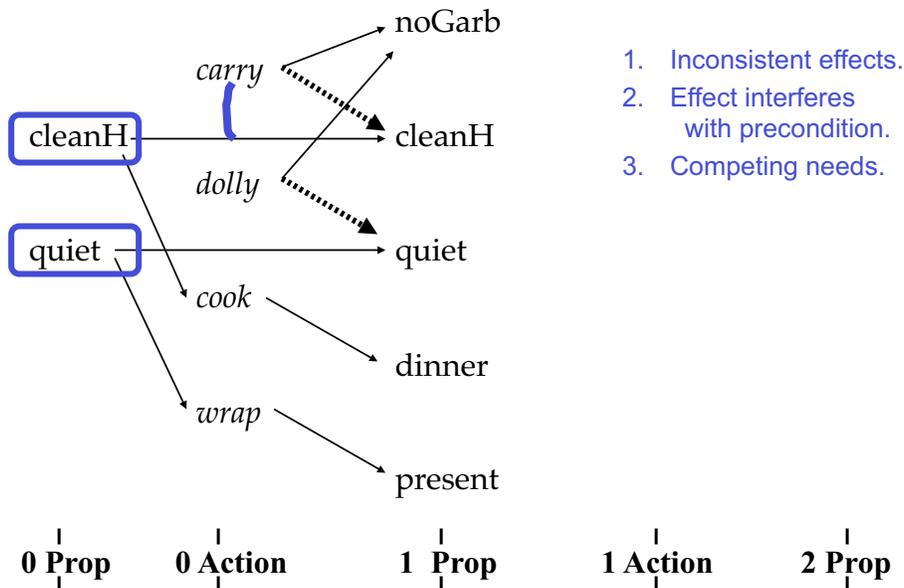
- Initial proposition layer
  - Contains propositions that hold in the initial state.
- Action layer  $i$ 
  - If action's preconditions appear **consistent** in  $i$  [**non-mutex**],
  - Then add action to layer  $i$ .
- Proposition layer  $i+1$ 
  - For each action at layer  $i$ ,
  - Add all its effects at layer  $i+1$ .
- Identify mutual exclusions
  - Between actions in layer  $i$ , and
  - Between propositions in layer  $i + 1$ .
- Repeat until all goal propositions appear **non-mutex**.

## Mutual Exclusion: Actions

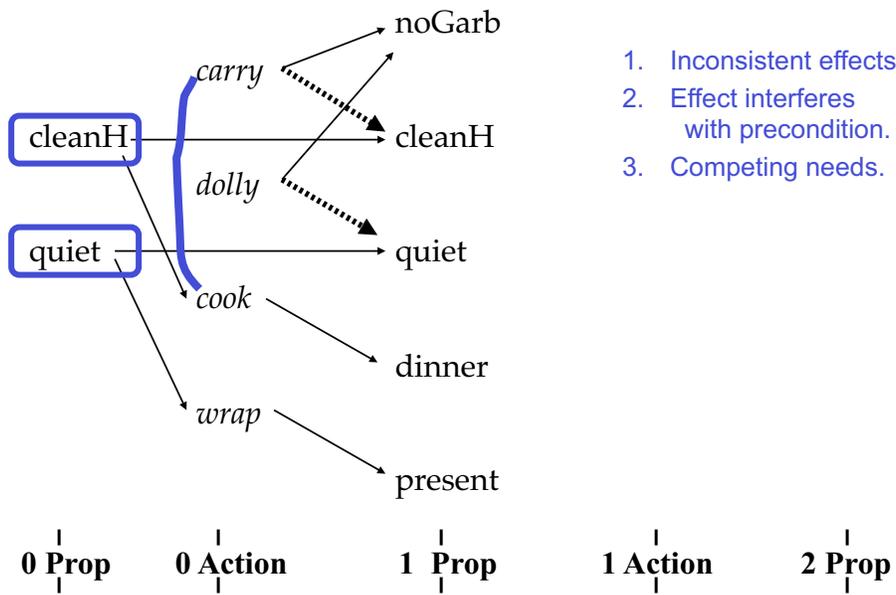
- Actions A,B are **mutually exclusive at level  $i$**  if no valid plan could consistently contain both at  $i$ :
  - They have inconsistent effects.
    - A **deletes** B's effects.
  - Effects interfere with preconditions.
    - A **deletes** B's preconditions, or
    - vice-versa.
  - Their preconditions compete for needs.
    - A and B have **inconsistent preconditions**.

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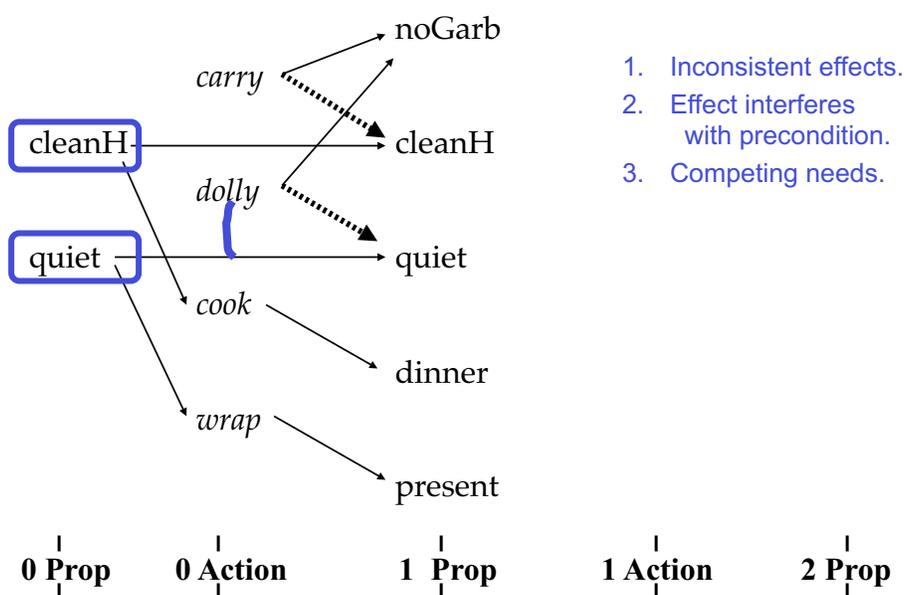
## Mutual Exclusion: Actions



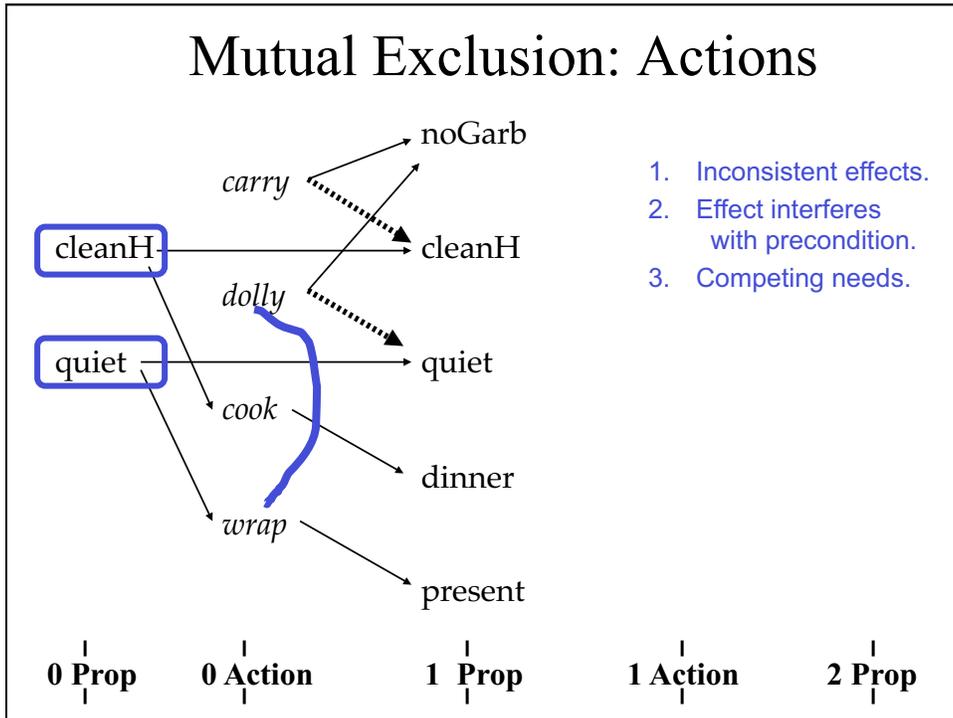
## Mutual Exclusion: Actions



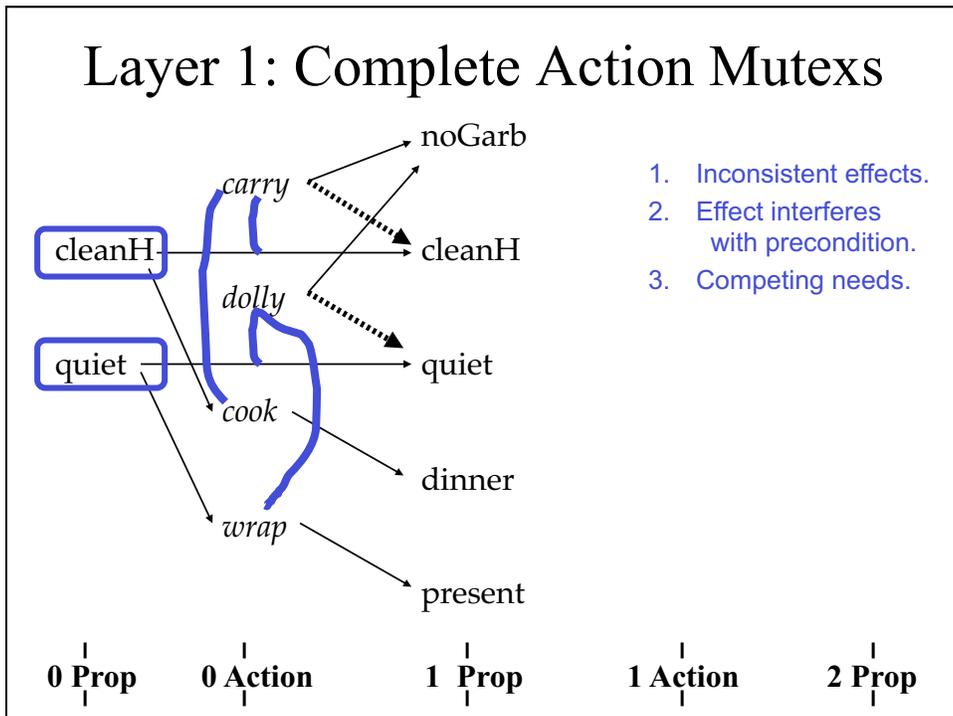
## Mutual Exclusion: Actions



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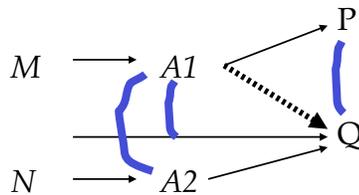
## Layer 1: Complete Action Mutexs



# Mutual Exclusion: Proposition Layer

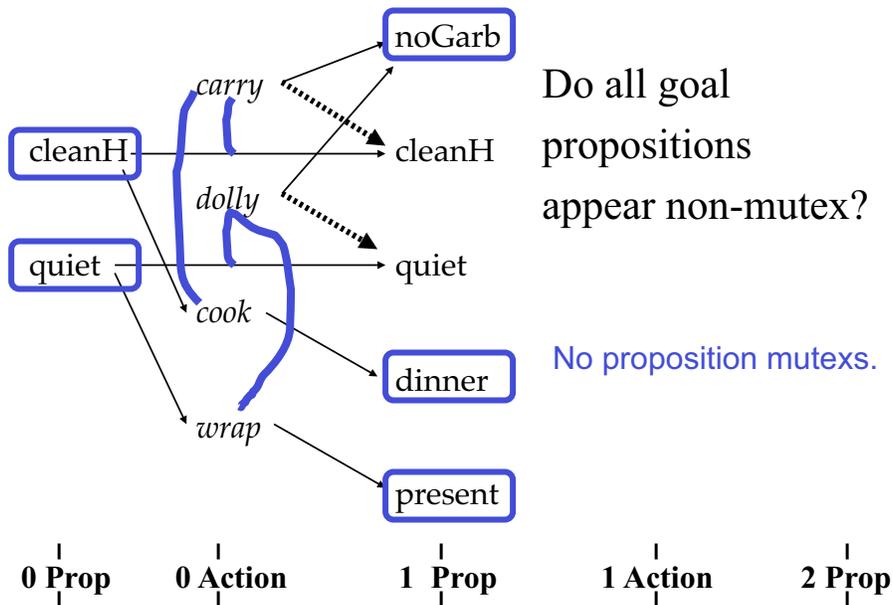
Propositions P,Q are *inconsistent at i*

- if **no valid plan** could possibly **contain both** at  $i$ ,
- ⇒ if at  $i$ , all ways to **achieve P** exclude each way to **achieve Q**.

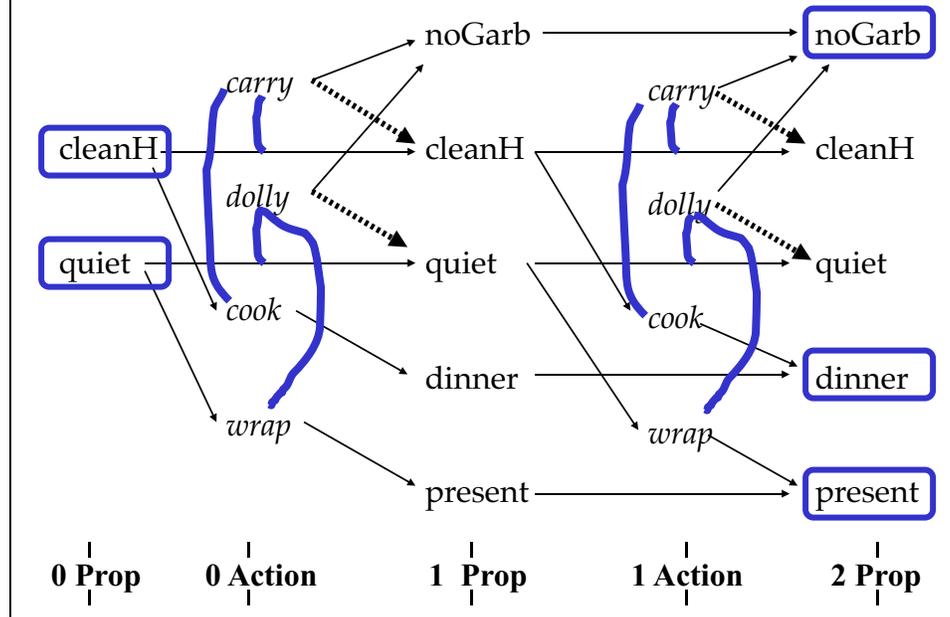


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# Layer 1: Add Proposition Mutexs



## Round 2: Extending The Planning Graph



## Outline

- Graph Plan
  - Problem Statement
  - Planning Graph Construction
  - Plan Extraction 

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