

Solution Convergence

Recall for our triangular grid finite volume scheme, the basic iterative scheme looked like:

$$A_i \frac{U_i^{n+1} - U_i^n}{\Delta t} + \underbrace{\mathfrak{F}_{ab_i}^n + \mathfrak{F}_{bc_i}^n + \mathfrak{F}_{ca_i}^n}_{R_i^n \equiv \text{residual of cell}} = 0$$

Approximation of

$$\oint_{\partial \mathcal{C}_i} (\vec{F}_i + \vec{G}_j) \cdot \vec{n} ds$$

$$\Rightarrow U_i^{n+1} = U_i^n - \frac{\Delta t}{A_i} R_i^n$$

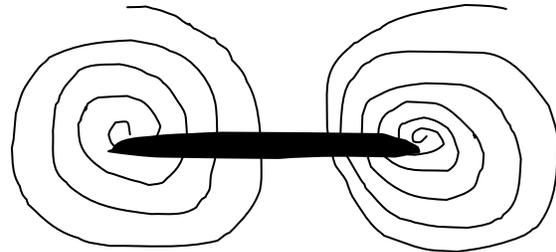
Update formula for cell i
to iteration $n+1$ from
iteration n

Suppose we are interested in the steady answer to our problem, i.e.
 $t = 0$

$$U^0 = U_\infty^0 = \begin{cases} \rho_\infty \\ \rho_\infty u_\infty \\ \rho_\infty v_\infty \\ \rho_\infty E_\infty \end{cases}$$



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We want



Initial guess of uniform flow

answer as $t \rightarrow \infty$
when $\frac{dU}{dt} = 0$
(steady-state)