

# Definition of Stability

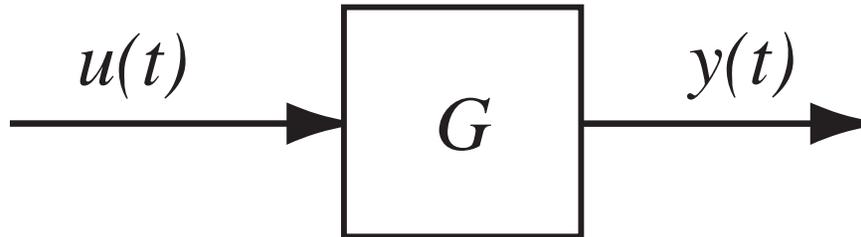
*Stability* is an important concept in linear systems — we all want to fly in airplanes with stable control systems! Although many of us have an intuitive feel for the idea of “stability,” we need a working definition that will allow us to classify systems as either stable or unstable.

Working with a partner, draft a definition of stability. The definition should be specific enough that you can test whether a system with impulse response  $g(t)$  (or equivalently, transfer function  $G(s)$ ) is stable or not.

Note: There are dozens, and maybe hundreds, of definitions of stability. There is no “wrong” answer!

When you are finished, press “1” on your PRS remote.

# Definition of Stability Solution



The LTI system  $G$  is Bounded Input / Bounded Output (BIBO) stable if every bounded input  $u(t)$  produces a bounded output  $y(t)$ .

Basically, this definition says that every “nice” input produces a “nice” output.

# BIBO Stability I

Consider the systems  $F$ ,  $G$ , and  $H$ , with impulse responses given by

$$f(t) = \sigma(t)e^{-2t}$$

$$g(t) = \sigma(t)$$

$$h(t) = \sigma(t)e^t$$

Which of the systems are BIBO stable?

1.  $F$ ,  $G$ , and  $H$
2.  $F$  and  $G$
3.  $F$  only
4.  $G$  and  $H$
5.  $H$  only
6. none of the above

# BIBO Stability I

Consider the systems  $F$ ,  $G$ , and  $H$ , with impulse responses given by

$$f(t) = \sigma(t)e^{-2t}$$

$$g(t) = \sigma(t)$$

$$h(t) = \sigma(t)e^t$$

Which of the systems are BIBO stable?

The correct answer is:

1.  $F$ ,  $G$ , and  $H$
2.  $F$  and  $G$
3. ♥  $F$  only
4.  $G$  and  $H$
5.  $H$  only
6. none of the above

# BIBO Stability II

Consider the system  $G$  with impulse response given by

$$g(t) = \frac{1}{1+t} \sigma(t)$$

Is the system  $G$  BIBO stable?

1. Yes
2. No
3. Don't know

# BIBO Stability II

Consider the system  $G$  with impulse response given by

$$g(t) = \frac{1}{1+t} \sigma(t)$$

Is the system  $G$  BIBO stable?

The correct answer is:

1. Yes
2.  No
3. Don't know

# BIBO Stability III

Consider the system  $G$  with impulse response given by

$$g(t) = \frac{1}{\sqrt{t}}\sigma(t)$$

Is the system  $G$  BIBO stable?

1. Yes
2. No
3. Don't know

# BIBO Stability III

Consider the system  $G$  with impulse response given by

$$g(t) = \frac{1}{\sqrt{t}}\sigma(t)$$

Is the system  $G$  BIBO stable?

The correct answer is:

1. Yes
2.  No
3. Don't know