

## Lecture F06 Mud:

- 1. Which came first, Biot-Savart for E&M or for Fluids?** (2 students)  
Not sure. Biot-Savart was first used for Fluids in the mid 1800's by Helmholtz.
- 2. Is there some sort of Gauss's Law for vortices to avoid doing the Biot-Savart integral?** (1 student)  
Nope. Gotta deal with it as is.
- 3. How is  $V_\theta = \Gamma/2\pi r$  for the straight 3-D vortex in the first example?** (1 student)  
I'm not sure what you mean. Carrying out the Biot-Savart integral on the straight 3-D vortex produced  $V_\theta = \Gamma/2\pi h$ , where  $h$  was the perpendicular distance from the vortex. This is the same as the 2-D result, except that  $r$  was replaced with  $h$  (following Anderson's notation).
- 4. If the circulation is greatest at the tips, is the lift greatest at the tips also?** (1 student)  
I think you're confusing the circulation  $\Gamma$  with the wake vortex strength  $\gamma = -d\Gamma/dy$ . The circulation  $\Gamma$  and hence  $L' = \rho V_\infty \Gamma$  both go to zero at the tips. In contrast,  $\gamma$  is typically maximum near the tips.
- 5. Confused about sign conventions for  $\Gamma$  and  $\gamma$ ?** (4 students)  
 $\Gamma$  on the wing is defined positive about the  $y$ -axis by righthand rule.  
 $\gamma$  in the wake is defined positive about the  $x$ -axis by righthand rule.
- 6. What would  $\gamma(y)$  for a wing with a winglet look like?** (1 student)  
First of all, the vortex sheet in this case is not planar, but is upturned on the edges, following the winglets. So  $\gamma$  has to be treated as a function of arc length  $s$  along the span – first along  $y$ , and then along  $z$  following the winglet. Qualitatively,  $\gamma(s)$  looks similar to that of a flat wing. The largest  $\gamma$  typically occurs near the winglet's tip. There may also be a “spike” in  $\gamma$  at the wing/winglet junction, depending how the wing/winglet system is designed.
- 7. In the PRS, if  $\Gamma$  is constant, why isn't  $d\Gamma/dy = 0$ ?** (1 student)  
 $\Gamma$  is not completely constant – it sharply drops to zero at the tip over a very small distance. So  $d\Gamma/dy = 0$  over most of the span, but it's large where  $\Gamma$  is sharply dropping to zero.
- 8. Are we finding the downwash at one point  $y_o$ , or over the whole span?** (1 student)  
When doing the integral to compute  $w$ , we hold  $y_o$  fixed. But this  $y_o$  is left as “ $y_o$ ” rather than a specific number, so the result is an expression in terms of  $y_o$ . We can then plug in a range of  $y_o$  values into the expression to create points for the  $w$  versus  $y_o$  plot.
- 9. How did you decide that  $dw = \gamma dy/4\pi(y_o - y)$ ?** (1 student)  
This is an application of the Biot-Savart law to the vortex filament consisting of a  $dy$ -wide strip of the wake, with circulation  $\gamma dy$ .

10. **What does the induced angle distribution tell me?** (1 student)

It will be used to compute the loading on the wing, and hence the lift and induced drag.

11. **Didn't understand PRS?** (3 students)

I'll go over it in recitation.

12. **No mud** (9 students)