

## Problem S1 (Signals and Systems)

1. Consider the system of equations

$$\begin{aligned}x + y - 2z &= -1 \\x + 4y + 2z &= 5 \\x + y - z &= 0\end{aligned}$$

Solve for  $x$ ,  $y$ , and  $z$ , in three separate ways. The goal of part (1) is to practice solving systems of equations, so that when you get to part (2), you will have a fair basis of comparison.

- (a) Determine  $x$ ,  $y$ , and  $z$  using (symbolic) elimination of variables.
  - (b) Determine  $x$ ,  $y$ , and  $z$  by Gaussian reduction.
  - (c) Determine  $x$ ,  $y$ , and  $z$  using Cramer's rule.
2. Consider the system of equations

$$\begin{aligned}4x + 2y + 2z &= 7 \\3x + y + 2z &= 5 \\x + 3y - z &= 4\end{aligned}$$

Again, solve for  $x$ ,  $y$ , and  $z$ , in three separate ways. This time, please time each part (a), (b), (c) below.

- (a) Determine  $x$ ,  $y$ , and  $z$  using (symbolic) elimination of variables.
- (b) Determine  $x$ ,  $y$ , and  $z$  by Gaussian reduction.
- (c) Determine  $x$ ,  $y$ , and  $z$  using Cramer's rule.
- (d) How much time did each method take?
- (e) Which method do you prefer? When answering this question, think about how much time might be required for a larger system, say, one that is  $5 \times 5$ .