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Space, Time, and Energy Landscapes Mechanobiology notes

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General tutorial session #5:

SPACE, TIME, AND ENERGY
LANDSCAPE IN MECHANOBIOLOGY

08 / 11 / 2006

Molecular forcesWinnuk Hwang

but first ☺

Funding opportunities at National Science FoundationJimmy Hsia

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- new opportunities . nano- and bio-mechanics and materials submission windows 09/01 - 10/01/2006 and 02/15 - 03/15/07
- newer opportunities . partnerships for international research & education due 10/30/2006 to support 14-17 projects, \$ 2.5M each.
- newest opportunities . East Asia and Pacific summer institutes for U.S. citizens for students in Australia, China, Japan, Korea, Taiwan . emerging frontiers in research and innovation (EFRI) crosscutting & disciplinary areas.
2006 was the program's first year : 16 proposals topics for 2007 solicitation : ⁽¹⁾autonomously reconfigurable engineered systems enabled by Cyberinfrastructure, ⁽²⁾cellular and biomolecular engineering

- Basic considerations

Generalized force as free energy gradient

$$\mathbf{f} = -\frac{\partial E}{\partial \mathbf{x}} \quad \text{or, in vector form} \quad \vec{F} = -\vec{\nabla} E$$

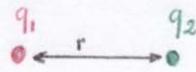
1. what is the radial dependence of \vec{F} , E ?and use V as potential energy (for E)2. what is the interaction range of \vec{F} ?3. " " " energy implied by \vec{F} ?

Types of intermolecular interactions :

- ① electrostatic (ES), ② Van der Waals / steric
- ③ hydrogen bonding, ④ hydrophobic

① electrostatic

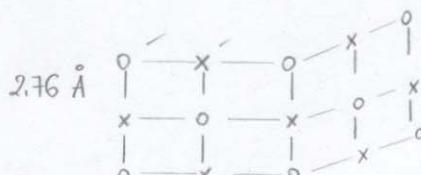
$$U_{ES}(r) = \frac{1}{4\pi\epsilon_0\epsilon_r} \frac{q_1 q_2}{r} \quad \text{with} \quad \epsilon_0 = 8.89 \times 10^{-12} \text{ C}^2/\text{J}\cdot\text{m}$$



$$\epsilon_r = \begin{cases} 1 & (\text{air}) \\ 80 & (\text{water}) \end{cases} \quad \text{dielectric constant}$$

Space, time and energy scales in mechanobiology - 2.

ex: sodium chloride NaCl



$$q_{\text{Na}} = -q_{\text{Cl}} = e = 1.6 \times 10^{-19} \text{ C}$$

$$U_{\text{NaCl}} = 120 \text{ kcal/mol}$$

thermal energy as energy ruler

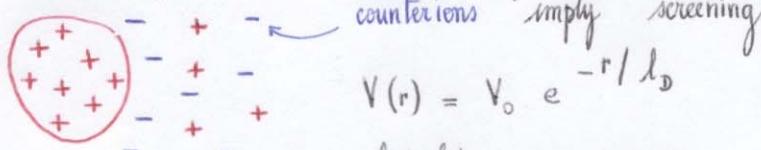
$$p(E) \propto \exp\left(-\frac{E}{k_B T}\right)$$

a salt NaCl crystal is stable
at room temperature

$\left\{ \begin{array}{l} \text{at } T = 300 \text{ K, } k_B T \approx 0.59 \text{ kcal/mol} \\ E \gg k_B T \text{ is unlikely while } E \ll k_B T \text{ is probable} \end{array} \right.$

but in water $U_{\text{NaCl}} = \frac{120}{80} = 1.5 \text{ kcal/mol} > k_B T \Rightarrow \text{salt dissolves}$

electrostatic screening: in an electrolyte solution where a charged group is buried



$$V(r) = V_0 e^{-r/l_D}$$

electrolyte $i = 1, 2, 3, \dots$

$\left\{ \begin{array}{l} \text{of bulk concentration } \rho_{\infty i} \\ \text{of valency } z_i \text{ (with } Z_{\text{Na}} = +1) \end{array} \right.$

the Debye length is $l_D = \frac{1}{\sqrt{\sum_i \rho_{\infty i} \frac{z_i^2 e^2}{\epsilon_0 \epsilon k_B T}}}$

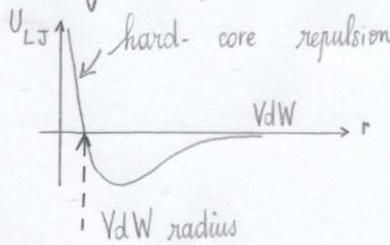
(no screening at high T from agitation!)

ex: $[\text{NaCl}] = 1 \text{ mM}$ $l_D = 9.6 \text{ nm}$ and in pure water at pH=7 (10^{-7} M)
 1 M $l_D = 3 \text{ \AA}$ $l_D = 960 \text{ nm} \sim 1 \mu\text{m}$

② Van der Waals / steric interactions

Lennard Jones potential

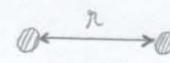
$$U_{\text{LJ}}(r) = A \left[\left(\frac{\sigma}{r}\right)^{12} - \left(\frac{\sigma}{r}\right)^6 \right]$$



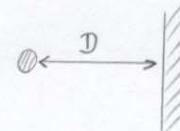
- * steric: strong, short-ranged
- VdW

VdW with surfaces

$$\text{VdW} \sim \frac{1}{r^6}$$



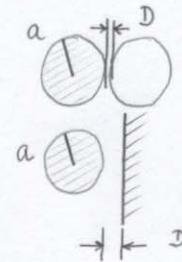
$$\text{VdW} \sim \frac{1}{D^3}$$



Space, time, and energy scales in mechanobiology - 3.

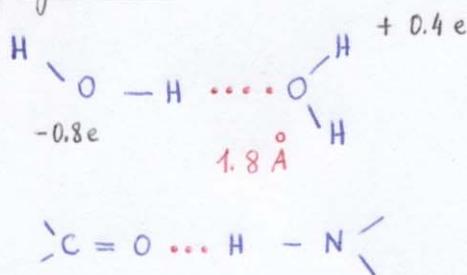
VdW with spheres

$$VdW \sim \frac{1}{D^3} \quad \text{if } a \gg D$$



VdW can matter at macroscopic scales, by walls.

③ Hydrogen bonds



short-ranged
directional

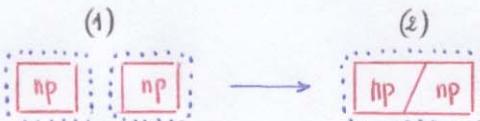
accounts for specificity of protein structure

Compare energies

$U_{H\text{-bond}}$	$\sim 3\text{-}9 \text{ kcal/mol}$
U_{VdW}	~ 0.24
$U_{ATP \text{ hydrolysis}}$	~ 14
$U_{\text{covalent bond}}$	> 100

④ hydrophobicity

: water around nonpolar molecules
forms a network of hydrogen bonds = "clathrate"



(2) entropically preferable because less order

hydrophobic interaction is attractive
entropic
long-ranged ($\sim 10 \text{ nm}$)

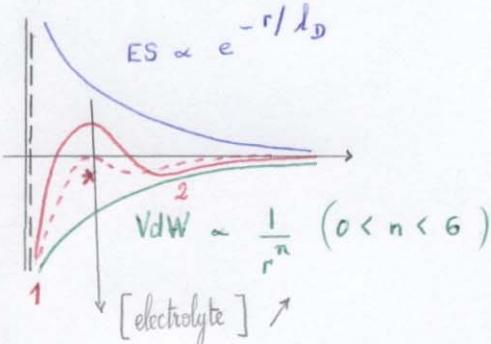
it is also { proportional to solvent-accessible surface area of nonpolar groups
= surface-tension driven γ

$$\gamma \sim 72 \text{ mJ/m}^2 \text{ (air)} \quad \text{or} \quad 50 \text{ mJ/m}^2 \text{ (H-carbons)}, \text{ relative to water}$$

$$\sim 80 \text{ cal/mol. \AA}^2 \text{ geometry-dependent}$$

DLVO

most interactions above are attractive, insensitive to electrolytes : VdW, H-bonds
but ES interaction is repulsive, and sensitive to electrolytes.



* critical coagulation concentration \rightarrow aggregation
1, 2 primary & secondary minima

Thermal forces and Brownian motion

Ju Wei

- add random variables: $y = x_1 + x_2 + \dots + x_N$
 $\bar{y} = \langle y \rangle \equiv E[y] = E[x_1] + E[x_2] + \dots + E[x_N]$
 $\text{var}[y] \equiv \langle (y - \langle y \rangle)^2 \rangle = \text{var}[x_1] + \dots + \text{var}[x_N]$
 $E[(y - E[y])^2] = N \text{ var}[x]$

from linearity of operator: $y = \frac{y}{N}$, $E[y] = \frac{E[y]}{N} = E[x]$
 average becomes more deterministic $\text{var}[y] = \frac{\text{var}[y]}{N^2} = \frac{N \text{ var}[x]}{N^2} \xrightarrow[N \rightarrow \infty]{\text{as more samples}} 0$

- x may be sampled by probability density

the central limit theorem states that, irrespective of the shape of x , y is Gaussian

$$\rho(y) \longrightarrow \frac{1}{\sqrt{2\pi N \sigma_x^2}} \exp\left(\frac{(y - N E[y])^2}{2 N \sigma_x^2}\right)$$

if you convolute 2 Gaussians, you get Gaussian \Rightarrow attractor shape

- diffusion equation (10): $\partial_t \rho = -\partial_x (-D \partial_x \rho) = D \partial_x^2 \rho$
 random walk motion of step $\pm a$

at $t=0$ initial conditions known \Rightarrow position = delta function δ

$$x(t) = 0 + \Delta x_1 + \dots + \Delta x_{t/\Delta t}$$

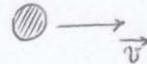
$$E[x(t)] = 0 \quad \text{on average}$$

but spread now $\text{var}[x(t)] = \frac{t}{\Delta t} \text{ var}[\Delta x^2] = \nu t a^2$ with $\frac{1}{\Delta t} = \nu$

$$\rho(x(t)) = \frac{1}{\sqrt{2\pi 2\nu t}} \cdot \exp\left(-\frac{x^2}{2 \cdot 2\nu t}\right) \quad \text{by identifying } D \equiv \frac{\nu a^2}{2}$$

parabolic kinetics

Green's function solution to diffusion equation.

- Brownian motion:  $F_{\text{drag}} = -6\pi r \eta v = -\lambda v = m \ddot{v}$

$$\text{if } v(0) = v_0, v(t) = v_0 e^{-\frac{\lambda t}{m}} \xrightarrow[t \rightarrow +\infty]{} 0$$

contradicts equipartition theorem $\langle \frac{mv^2}{2} \rangle = \frac{k_B T}{2}$ problematic!

Einstein : there is not only a dissipative force (drag) but also stimulative force (at microscopic scale).

$$m \ddot{v} = F_{\text{diss}} + F_{\text{stim.}} = \text{fluctuation} = -\lambda v + F_{\text{fluct.}}(t)$$

$$\langle F_{\text{fluct.}}(t) \rangle = 0$$

$$\langle F_{\text{fluct.}}(t) F_{\text{fluct.}}(t') \rangle = b(t-t') = B \delta(t-t') \quad \text{white noise}$$

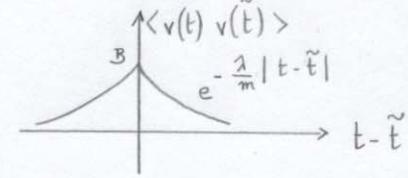
$$v(t) = \frac{1}{m} \int_{-\infty}^t dt' F_{\text{fluct.}}(t') \exp\left[-\frac{\lambda}{m}(t-t')\right] \quad \text{uncorrelated fluct.}$$

velocity correlation even if white noise : $\langle v(t) \tilde{v}(\tilde{t}) \rangle = (B/2m\lambda) e^{-\lambda/m|t-\tilde{t}|}$

$$[B] = \text{force}^2$$

the ratio between square of stimulative force and dissipative force is fixed ($\propto T$)

$$\frac{B}{2\lambda} = k_B T = \text{Einstein's relation}$$



- How do diffusion and Langevin equations match?

$$\langle x^2(t) \rangle = 2 \mathcal{D} t$$

$$\frac{d}{dt} \langle x(t) x(t) \rangle = 2 \mathcal{D} = 2 \langle x(t) v(t) \rangle$$

$$\text{or } \mathcal{D} = \int_0^t g(t') dt' : \text{fluctuation-dissipation theorem}$$

valid as $t \rightarrow +\infty$ observation time

$t \gg \frac{m}{\lambda}$ larger than molecular time scale
(or macroscopic times)

$$\mathcal{D} = \langle x(t) v(t) \rangle = \left\langle \int_0^t v(t') dt' \cdot v(t) \right\rangle$$

$$= \int_0^t \langle v(t) v(t') \rangle dt'$$

$$= \underbrace{\int_0^t \langle v(t') v(0) \rangle dt'}_{\equiv g(t')}$$

This fluctuation-dissipation theorem (Green-Kubo formula) has many implications :

- thermal conductivity
- semiconductor's electrical conductivity
- shear viscosity

transport properties \hookrightarrow equilibrium fluct.

- $\mathcal{D} = \lambda k_B T$ Einstein's relation (no mass)

Space, time, and energy scales in mechanobiology - 6

"Reactions", energy landscapes and kinetics

Pat Doyle

see Pat Doyle's handwritten notes.

Cellular sensing of force and geometry in rigidity responses:
protein unfolding by force

Michael Sheetz

- reverse system engineering approach: what components are responsible for cellular responses? capability to sense form, rigidity and respond is critical to biology rapid neuronal sensing is through ion channels, but longer-term responses are cytoskeleton-based transformation is described as the ability to respond to rigidity and grow

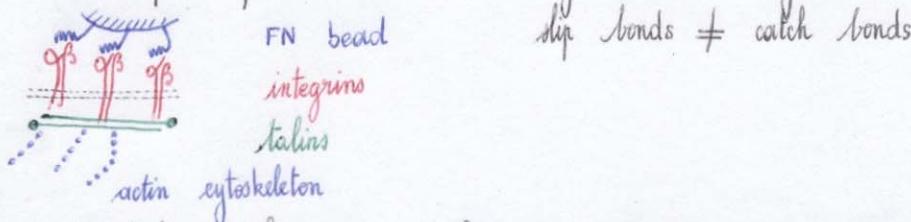
- sensing (geometry & rigidity / force) → transduction → response (Sheetz - Vogel Nat. Rev '06)

(ms - s) (s) (min, cycles)
force causes GFP-paxillin accumulation in RPTP α +/+ with fibronectin reinforcement response mediated by integrins

intracellular / extracellular communication ⇒ feedback and integrated response after a few cycles

- early response? and its role?

. spatial distribution of integrins is important for talin binding
timers of integrins ⇒ fibronectin strong attachment
2pN slip bond between integrins and cytoskeleton (through talins)



- . force-dependent reinforcement, where are involved C-Src, vinculin, RPTP α et al.
GFP-paxillin stretch-dependent binding to identify molecules necessary for reinforcement.
can the plasma membrane be removed and the cytoskeleton (CSK) alone show same? yes!
CSK-bound proteins after stretch: { FAK, p130 Cas , PKB/Akt, paxillin
not vinculin (some in vivo & in vitro)
reversible, ATP-independent, mechanical

- measure signaling downstream:
 - G protein activation by csk
 - Rap 1, not Ras, is activated by stretch
 - Src family kinase phosphorylation of p130 Cas if stretch
- Cas: force transducer since \textcircled{P} Cas correlates with stretch application
protein unfolding or protein distortion responsible for this transduction?
- stretch Cas SD itself? pull a latex surface to uniformly stretch the molecule
Cas SD phosphorylation requires stretch for c-Src, Fyn, and c-Abl (not Csk) ph.
unfolding of Cas SD appears to be sufficient and necessary for its phosphorylation
(SD = substrate domain of Cas)
- unfolded & phosphorylated Cas is at the periphery of cells (as assessed by Ab stain)
- titin domains unfold as expected for a force sensor ($\sim 200 \text{ pN}$ per unf. event)
hydrogen bonds critically important to dictate unfolding forces & properties
 \rightarrow graded force sensor in one single molecule: domains structure is key concept
(same with FN - Viola Vogel's work)